EA 2020/2021 Theory exercises

Exercise 1 Show by induction:

```
a) 1^2 + 2^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}
```

b) For any $n \geq 7$, we have that $n! > 3^n$

Exercise 2 Show that the following recursive algorithm computes correctly the factorial of a number. Assume that $n \ge 0$.

```
Function F(n)

if n = 0 then

s = 1

else

s = n \cdot F(n - 1)

return s
```

Exercise 3 Show that the following insertion sort algorithm is able to sort a list A of n numbers in nondecreasing order.

```
Function IS(n, A)

if n \ge 2 then

IS(n-1, A)

i = n-1

while i \ge 1 and A[n] < A[i] do

i = i-1

i = i+1

p = A[n]

j = n-1

while j \ge i do

A[j+1] = A[j]

j = j-1

A[i] = p
```

Exercise 4 Do a tail-recursive version of the following algorithm

```
Function S(n)

if n = 1 then

return n

else

return n + S(n-1)
```

Exercise 5 Read the problem B - A new chess game in EA2021_ProblemasAula in Mooshak. Consider a recursive approach to solve it.