

Polinómios

Método de HORNER  
ou dos parêntesis  
encadeados

função polinomial

$y = P_m(x)$

$a = [a_0 | a_1 | a_2 | \dots | a_i | \dots | a_m]$

CASOS

1.  $m=0 \rightarrow P_0(x) = a_0$  (4)

$\# + = \# * = 0$

$y = a_0$   
 $y = P_0(x)$

2.  $m=1 \rightarrow P_1(x) = a_0 + a_1 x$  (5)

$\# + = \# * = 1$

$y = a_0 + a_1 x$   
 $y = P_1(x)$

Quantos  $+$  e  $*$  estão associados a (1)?

3.  $m=2$

$P_2(x) = a_0 + a_1 x + a_2 x^2$  (6)

$\# + = 2$   
 $\# * = 3$

$P_2(x) = a_2 * x * x + a_1 * x + a_0$  (7)

$P_2(x) = (a_2 x + a_1) x + a_0$  (8)

$\# + = 2$   
 $\# * = 2$

4.  $m=3$

$P_3(x) = a_0 + a_1 x + a_2 x^2 + a_3 x^3$  (10)

$\# + = 3$   
 $\# * = 6$

$y = P_2(x)$   
Parábola  
 $y = ax^2 + bx + c$

$$P_3(u) = a_3 \times \underline{u} \times \underline{u} \times \underline{u} + a_2 \times \underline{u} \times \underline{u} + a_1 \times \underline{u} + a_0$$

$$P_3(u) = ((a_3 u + a_2)u + a_1)u + a_0 \quad (11)$$

$$\begin{cases} \# + = 3 \\ \# * = 3 \end{cases}$$

$$\triangleright \boxed{4. \quad m=3}$$

$$P_3(u) = a_3 u^3 + a_2 u^2 + a_1 u + a_0 \quad (10)$$

$$\begin{cases} \# + = 3 \\ \# * = 6 \end{cases}$$

Case  $m$

$$P_m(u) = a_m u^m + a_{m-1} u^{m-1} + \dots + a_2 u^2 + a_1 u + a_0 \quad (u)$$

$$\begin{cases} \# + = m \\ \# * = (?) \end{cases}$$

$$\# * = \sum \{1, 2, 3, \dots, m-1, m\} \quad (u)$$

$$S_m = \frac{1+m}{2} \times m$$

$$P = \left(\frac{1}{2} + \frac{m}{2}\right) \times m$$

$$= \frac{m}{2} + \frac{m^2}{2}$$

$$= O(m^2)$$

$$2-1=1$$

$$3-2=1$$

$$4-3=1$$

$$\vdots$$

$$\vdots$$

$$n-(n-1)=1$$

or Progression arithmetic

$$P_n(x) = ((a_n x + a_{n-1})x + a_{n-2})x + \dots + a_2)x + a_1)x + a_0 \quad (13)$$

$\# + = M$   
 $\# * = M$

$a = [a_0 \ a_1 \ \dots \ a_n]$

Algoritmo Método de HORNER.  
 Input:  $a, n$   
 output:  $P$

$n \leftarrow \text{length}(a)$   
 $P \leftarrow a(\text{end})$

Para  $i = n-1$  até  $1$   
 $P \leftarrow P \cdot x + a(i)$   
 Fim Para

$y = x^2$   
 $y = P_2(x)$   
 $P_2(x) = x^2$

$x = -1 \quad x = 0 \quad x = 1$

$P_2(x) = 0 + 0x + 1x^2$

$a = [0 \ 0 \ 1]$   
 $n = 2$

$S_n = \frac{1+n}{2} \times M$   
 $P = \left(\frac{1}{2} + \frac{M}{2}\right) \times M$   
 $= \frac{M}{2} + \frac{M^2}{2}$   
 $= O(M^2)$

$2-1=1$   
 $3-2=1$   
 $4-3=1$   
 $\vdots$   
 $n-(n-1)=1$

$n=1$

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```
MHorner.m  Interface01MHorner.mlx  +
1  function P = MHorner(a,x)
2  %UNTITLED4 Summary of this function goes here
3  % Detailed explanation goes here
4  n = length(a);
5  P = a(end);
6  for i=n-1:-1:1
7      P = P.*x+a(i);
8  end
9  end
```

