

School of Science
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Master Degree in Physics

Automatic Pipeline for the Identification of Ground Glass Opacities on CT Images of Patients Affected by COVID-19

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Abstract

Since the beginning of the 2020, COVID-19 has widely spread all over the world and its been declared a pandemic. CORona VIRus Disease 19 (COVID-19) is a respiratory infective disease caused by SARS-CoV2 virus. COVID-19 has widely spread all over the world since the beginning of 2020, and its been declared as pandemic by OMS. Chest CT scans of aptients affected by COVID-19 have shown consolidation and ground glass opacities, so becomes very important to segment and quantify these regions in order to understand the infection pathogenesis, help diagnosis and monitoring the recovery of healed patients.

In this theses I will propose an application of the color quantization as segmentation method for automatic identification of the infected regions in CT scans of COVID-19 affected patients.

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Introduction

Since the end of 2019, COVID-19 has widely spread all over the world. Up to now the gold standard for the identification of the pathology is the RT-PCR even if it is reported that its sensitivity might not be enough for COVID-19 identifications [2] and requires a lot of time to provide results.

Up to now the gold standard for the diagnosis of this disease are the reverse transcription-polymerase chain reaction (RT-PCR) and the gene sequencing of sputum, throat swab and lower respiratory tract secretion [9].

Many COVID-19 affected patients have shown ground glass opacities(GGO) and consolidation(CS) in chest CT, which are also made in relation with the stage of the disease [6]. As shown by [10], initial prospective analysis have shown that the 98% have bilateral patchy shadows or ground glass opacity (GGO) and consolidation(CS) in lung. Other study have have monitored the change on volume and shape of these features on healed patients [2] in order to monitoring their recovery. In Figure ?? are compared slices of an healthy control and a patient affected by COVID-19. We can clearly see the GGO and CS regions in the lung of the second one.

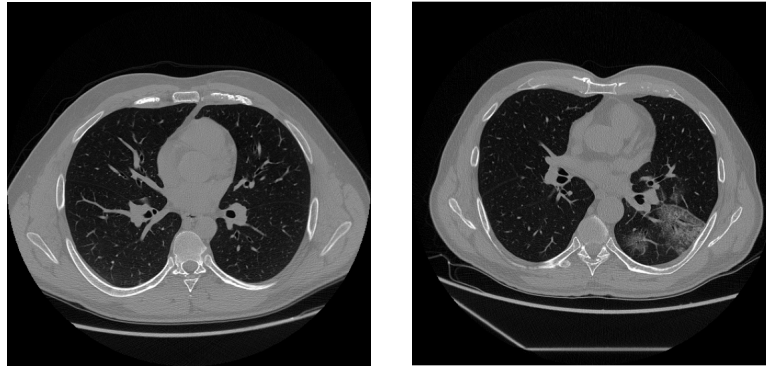


Figure 0.0.1: *CT scan of thorax for an healthy patient(left) and a COVID-19 affected one(right) in which we can observe a huge amount of GGO in the right lung*

GGO and CS are not exclusive of COVID-19, but may be also caused by pulmonary edema, bacterial infection, other viral infection or alveolar haemorrhage [11]. However the combination between CT scan information and other diagnostic techniques like the RT-PCR mentioned above, may help the diagnosis, the monitoring of the course of the disease and the checking of the recovery in healed patients. Since COVID-19 is a new disease, the study of these features in COVID-19 affected patients may help the understanding of the infection pathogenesis.

Austin in Glossary of terms for CT of the lungs [5] define the Ground Glass Opacities as *hazy increased attenuation of lung, with preservation of bronchial and vascular*

margins caused by partial filling of air spaces, interstitial thickening, partial collapse of alveoli, normal expiration, or increased capillary blood volume. For the reason given before, the identification of this kind of lesions in CT scans of lung is very important. Up to now the segmentation is made in a manual or semiautomatic way, which are time consuming and subjective, since involves the interaction with trained personnel. AN automatic and fast way for the identification of this features is desired.

In this thesis work I will present an automatic and fast pipeline for the identification of these kind of lesions. The pipeline was developed by using 83 chest CT scans of COVID-19 affected patients, kindly provided by Sant'Orsola hospital. Also scans from two public dataset (ZENODO [12], MOSMED [14]) where used as benchmark. The developed pipeline is completely unsupervised and its based on the color quantization, so the relation between the HU and the different linear attenuation coefficient of tissues is exploited. In order to takes into account other features, like the spatial extension of the lesion areas, or the different shape of the lung structure, a suitable color space was build.

The pipeline was implemented in python and to perform the different operations different image processing libraries where used : *SimpleITK*, *OpenCV* and *scikit-image*.

The time performance of the pipeline are verified on the DIFA servers and the segmentation accuracy on labels provided by the manual segmentation performed by and expert.

Chapter 1

Infection Identification Pipeline

In this chapter I will discuss the developed pipeline. In the first section I will describe the basic idea behind the pipeline, given some concept about the color quantization and discuss the main structure of the pipeline, by speaking about the aims and the problem managed by each block.

After that, in the second section, I will describe the actual pipeline implementation, by given some concept about the used frameworks and by describe in details the implementation of each block of the pipeline.

In the end, in the last section, I will speak about the routines used to optimize the several parameters involved.

1.1 Pipeline Description

As I've said before the aim of these thesis is the developing of a pipeline for the identification of GGO and CS areas in chest CT scans of COVID-19 affected patients. The pipeline aims to have the following characteristics:

- **Fully Automated:** to remove the dependency from an external operator, and so the subjectivity of the segmentation;
- **Fast:** in order to compete with certified software and to provides a segmentation in few minutes.

The pipeline is unsupervised, so doesn't requires to provide the expected outcomes, so the labels where used only for the quality check. During the pipeline developing we have to takes into account is that the infection regions may have different patients according to the stage of the disease or recovery, as we can see in Figure 1.1.1, and usually these patterns are spatially disconnected; so we have decided to use a pixel classification technique.

In the end the basic idea was to use the Color Quantization as medical imaging segmentation, which aims to identify the different type of tissue and lesions by grouping them by color similarity. In particular we aims to assign to each structure inside the lung a characteristic colors and label each voxel by identify it as belonging to the tissue with the most similar characteristic color. This approach is justified since exist a relation between the kind of tissue and the color used to display it in a CT scan, given by Hounsfield Unit.

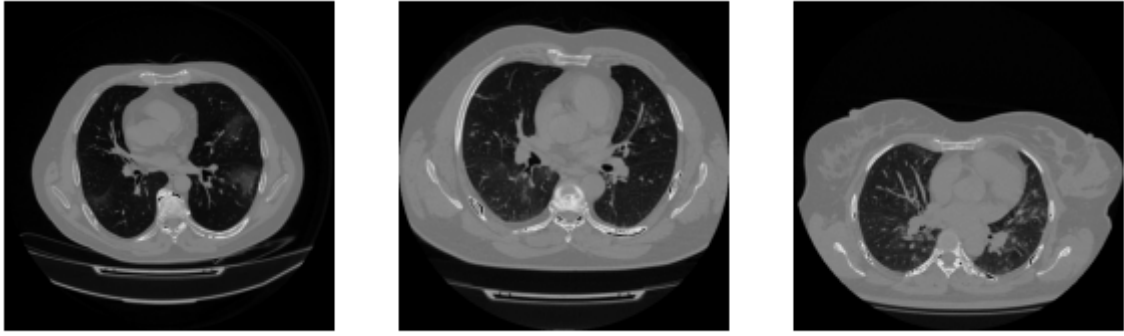


Figure 1.1.1: *Ground Glass Opacities of COVID-19 affected patients with different severity of the disease. From left to right this scans belong to CT-1, CT-2 and CT-4 category of MOSMED [14] dataset*

Since it is unlikely to find a structure with a single voxel extension, I've used the multi-channel characteristics of digital images to take into account also the neighbouring voxels.

In this section I will describe how color quantization works for image segmentation, how the color space was built in order to incorporate also neighbouring information and the final structure of the segmentation pipeline.

1.1.1 Color Quantization for Medical Image Segmentation

Color quantization is the process of reducing the number of colors in a digital image. The main objective of quantization process is that significant information should be preserved while reducing the number of colors in an image, in other word quantization process shouldn't cause significant information loss in the image. Color quantization, accepted as a pre-processing application, is used to reduce the number of colors in images with minimum distortion such that the reproduced image should be very close to the original image visually, as in Figure ??.

Color quantization play an important role in many filed of applications such as segmentation, compression, color texture analysis, watermarking, text localization/detection, non photorealistic rendering and content-based retrieval [15].

In this work I've applied this technique to segment CT scans of patients affected by COVID-19. Use this technique as medical image segmentation implies that each different tissue is assigned to a particular color (properly it is a range of colors since the image is affected by noise and also the tissue may not have the same density in each point) so must exist a relationship between the kind of tissue and the color used to represent it. For CT scan which are in gray scale, each color is represented by a single value given by the Hounsfield Units (HU) : voxels colors are proportional to HU, which are defined as a linear transformation of the linear attenuation coefficient (μ). HU normalize the μ of a particular tissue according to a reference one, usually water (μ_{H_2O}), ss we can see in equation 1.1 :

$$HU = k \times \frac{\mu - \mu_{H_2O}}{\mu_{H_2O}} \quad (1.1)$$



Figure 1.1.2: *Color quantized RGB image. We observe the original image, a 16 color image which look similar to the original one, a 8 colors image and 4 colors image*

Where μ_{H_2O} is the linear attenuation coefficient of the water, μ is the linear attenuation coefficient of the tissue in the voxel and k is a multiplicative constant, which can be 1000 or 1024 depending on the manufacturer of the CT scan. In the end each color results proportional to the linear attenuation coefficient, different from each tissue, so exist a relation between the GL and the tissue type that makes this techniques available.

Color quantization and the properties of digital images allow us to consider also other properties of the image besides the single voxel intensity. This purpose can be achieved by building a suitable color space:

In digital image processing, images are represented with a 3D tensor, in which the first two dimensions represent the height and width of the image and the last one the number of channels. Gray scale images requires only one channel, so each pixel has a numeric values whose range may change according to the image format. On the other hand color images requires 3 channels, and the value of each channel represent the level of the primary color stored in this particular channel, so each color is represented by 3 different values, according to Young model.

In this work the different channel are used to takes in account different properties, exploited by the application of different filters. This allow us to consider also neighbouring pixels, that is really suitable for the segmentation since the lesions areas involves many closest voxel, not only a single one. We have also used this features to discriminate between and other lung regions like bronchi by exploit spatial information.

Once we have build the color space, we have to found the characteristic color of each tissue under study, which is represented by a centroids in the color space. In order to perform this task and achieve the centroid estimation a simple kmeans

clustering was used, since it provides a suitable segmentation with good time performances and it is efficiently implemented for multi-channel images in OpenCV [7]. Kmeans clustering requires a prior knowledge about the number of cluster, which in our case is given by the anatomical structure of the lung, so each cluster will correspond to a different anatomical structure.

Once we have estimated the centroids for each tissue, we use that for the actual segmentation, by assign each voxel to the cluster of the closest centroids: in this way the estimation step, that we will call "train", needs to be performed only once, so can be time expansive since is not involved in the actual segmentation.

1.1.2 Pipeline Structure

In this section I will discuss the general structure of the pipeline, more details about the actual implementation will be given in the next chapter. To perform the color quantization I've to find the characteristic color(centroids in the color space) of each tissue and use these colors for the actual segmentation, so the pipeline will be divided int two main steps. Before each of these steps we need a preliminary phase that aim to isolate the lung regions in order to exclude the extra lung areas and reduce the false positives. In the end the pipeline structure is divided in three main blocks as we can see in Figure ?? :

- **Pre-Processing and lung extraction:** Preliminary step, involves registration of HU and isolation of lung regions;
- **Training :** estimation of the centroids, is performed only ones;
- **Labeling :** assignment of each voxel to the cluster of the closest centroids, it is the actual segmentation.

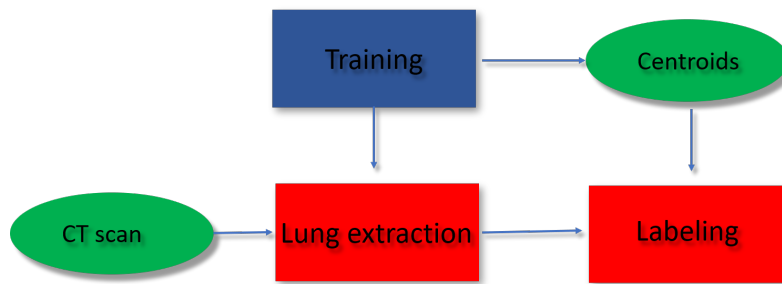


Figure 1.1.3: Flow chart of the main structure of the developed pipeline. The training process, which allows the estimation of the centroids, is performed only one time.

Pre Processing and Lung Extraction

This preliminary step is performed before both training and labeling.

First of all performs a registration of the HU on a common space, in order to overcomes the issues that may raise from the different padding values and multiplicative constant for HU computation(equation 1.1) used by the different manufacturer of

the CT scans.

This process is followed by a segmentation of the lung regions, which allows to remove all the extra lung regions avoiding the formation of false positives. During this process a particular attention was paid on the removal of the main bronchial structures, which can interfere with the actual segmentation, and the preservation of the lung regions which are the ones in which we are interested in.

Training

This step involves the estimation of the centroids for each tissue. To achieve this purpose we have chosen to perform a clustering by using the kmeans algorithm. We have to take into account that the kmeans clustering requires an homogeneous representation for each cluster. As we will see we have to manage this problem. One way to overcome this issue is to select several CT scans, which may be time consuming, or we can carefully select only one scan which provides an homogeneous representation of each cluster, as I've done in this work.

In summary, the implementation of this step involves the building of the multi-channel image, which allows us to take into account also the neighbouring information, the managing of the over represented clusters and the actual centroids estimation.

Labeling

This step involves the actual segmentation. The script which performs it requires as inputs the CT scans after the lung extraction, and the previously estimated centroids. This block of the pipeline simply assigns each voxel to the cluster corresponding to the nearest centroids and selects only the one corresponding to GGO and CS. In this way we are performing a pixel classification by assigning regions to a particular labels according only to intensities information, without exploiting spatial information: this allows us to group on the same cluster objects that are spatially disconnected as often happens in medical imaging field.

The distance between voxel color and each centroid is defined as euclidean distance :

$$d(x_j, c_i) = \sqrt{(x_j - c_i)^2}$$

Where x_j is the color vector for the j th voxel and c_i is the i th centroid.

To summarize, once the centroids are estimated, the segmentation pipeline will result in 2 main steps : **lung extraction** and **labeling**, as shown in Figure ?? in which we can observe the flowchart of each step with an image that shows the partial results.

1.2 Pipeline Implementation

In this chapter I will describe in details the actual pipeline implementation. First of all I will briefly describe the used framework for the actual implementation. After that I will describe step by step each block of the pipeline, describing how each task is achieved.

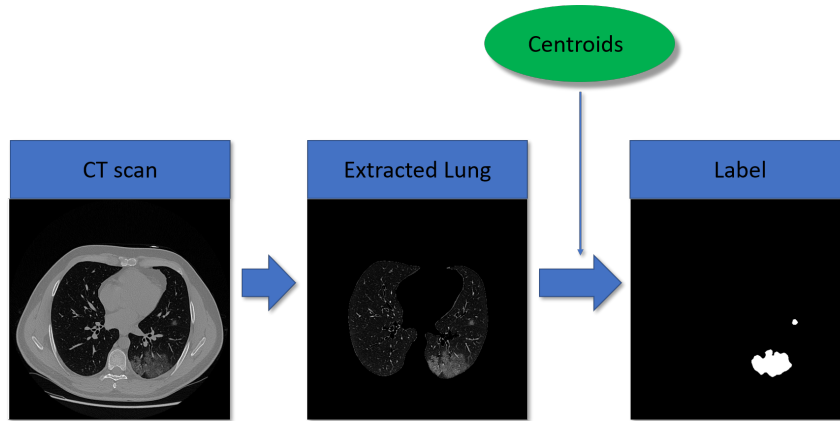


Figure 1.1.4: *Actual segmentation step, from left to right we can see the input image stack, the isolated lung regions and the final label. To performed the labeling a set of pre-computed centroids was used.*

The whole pipeline was implemented by using python, which is an high level object oriented programming language and to perform the necessary image processing operations, the managing of input and output images, and the other operation I've mainly used OpenCV [7] and SimpleITK.

Since python is an high level language, it allows an easy and fast implementation of the code, on the other hand working with optimized image processing libraries written in C++ allows to prevent the lack of performances.

The whole code is open source and available on github [8] and the pipeline installation is automatically tested on both Windows and Linux by using AppveyorCI and TravisCI. The installation is managed by setup.py, which provides also the full list of dependencies. The code documentation was generated by using sphinx and its available at To automatize the segmentation on multiple CT scans are provided bash and powershell script and, even if the centroids are already estimated, a training script is provided, in order to allow the user to estimate its own set.

The whole pipeline is organized into three scripts, which performs the main tasks:

- lung_extraction
- train
- labeling

The usage of SimpleITK to manage input and output file, allows the compatibility with medical image formats and the preservation of the spatial information.

1.2.1 Frameworks

In order to perform all the necessary image processing operations both involving 2D and 3D filters, to perform the color quantization and to manage the input and output medical image format, I've used mainly two libraries for image processing and computer vision. Both of the libraries has been written on C++ but has multi language support. I've performed all the 2D image processing operations like median blurring or filter application by using OpenCV [7]. For the managing of medical

image formats, ensuring the preservation of voxel spatial information, and for the 3D operations, I've used SimpleITK. To perform all the image filtering that aren't implemented in OpenCV like entropy calculation or percentile filter application I've used also scikit-image, which provides a large set of image processing tools.

OpenCV

OpenCV, acronym for Open Source Computer Vision, is an open source computer vision and machine learning software library. OpenCV was built to provide a common infrastructure for computer vision applications and to accelerate the use of machine perception in the commercial products. I've used the tools from this library to perform all the processing that involves the single image and, most important, to perform the color quantization, since the kmeans implementation offered by the library allows to cluster multi channel images in an efficient way.

This library is implemented in C++, however bindings are available for python, Java and MATLAB/OCTAVE. This library can use also hardware acceleration like Integrated Performance Primitives, and also CUDA and OpenGL based GPU interfaces are available.

SimpleITK

SimpleITK is a simplified programming interface to the algorithms and data structures of the Insight Toolkit (ITK) that support many programming languages. The library provides a simplified interface to use Insight Tool Kit (ITK) library. Insight Tool Kit (ITK) is an open source library which provides an extensive suite of tools for image analysis, developed since 1999 by US National Library of Medicine of the National Institutes of Health. This library provides tool useful to works also with N-dimensional images. This library provides a powerful tools for the reading and writing of the image. Since ITK, and so SimpleITK, consider the image like spatial object and not like arrays of values, it store also information about voxel spacing, size and origins, provided as well as the array, this makes us able to work only with the array by using numpy or OpenCV, by preserving the spatial information of the image. This library allow also to process the whole image volume, allowing 3D operations, which are used into many steps of the pipeline.

1.2.2 scikit-image

scikit-image [18] is an image processing library that implements algorithms and utilities for use in research, education and industry applications. scikit-image implements a rich collection of image processing functions implemented in python. The implemented filters are used when a corresponding implementation in OpenCV was not available. In particular the functions to compute the hessian filter and the percentile filter are extended to the whole stack of images. This library, like OpenCV, consider the image as an array, so doesn't use the spatial information about voxels.

1.2.3 Lung Extraction

Lung extraction is the first step of the pipeline that is performed by homonymus script. As input the CT scan to process in each format supported by SimpleITK and will provide as output the isolated lung regions as default in '.nii' format.

To achievement of the lung extraction involves 3 main steps:

1. **Pre-Processing** : Which register the HU in a common space, crop the outliers, and de-noise the image;
2. **Thresholding and reconstruction** : Which is the actual segmentation, that takes care to preserve all the intra-lung regions except for the main bronchial structures.
3. **Selection of lung** : allows the exclusion of all the extra-lung organs like intestine.

Pre-processing

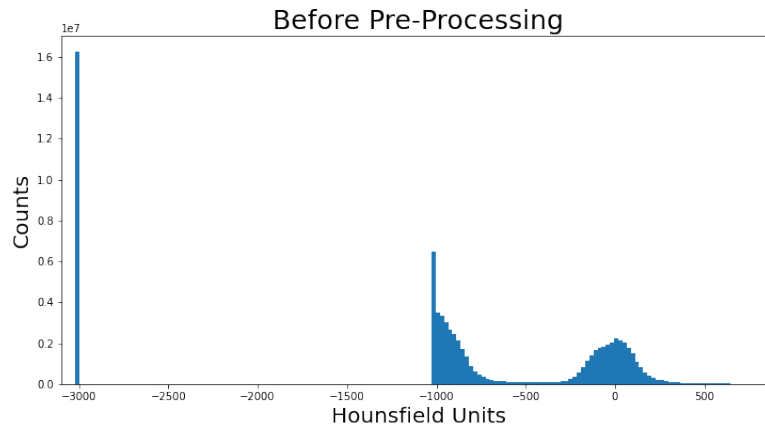
As I've said before, the k constant in the HU definition (equation 1.1) may change according to the scan manufacturer or scan model. Moreover, during the scan acquisition, all the regions outside the CT tube aren't sampled, so to obtain a square $N \times N$ image for each slice some padding values are added, which different values according to the scan manufacturer: for instance in the CT scan in Figure ??(a) the padding value is $-3000HU$ and the air value is -1024 . The first thing to do is to make the padding value and the air value equal for each scan considered and shift them to 0, because for the de-noising operation we need to work with unsigned int 16-bit gray scale image.

May also happen that some Hu are out of range, that because some patients may have metallic prosthesis that make the so called *metallic artifacts*. However we haven't to worry about this kind of artifacts because they will involve only body regions and not the lung ones, and so are removed during this step. In Figure ??(b) we can observe the histogram of the same scan after this pre-processing step, it is clear that both the padding and air values are set equal and shifted to zero, making positives all the other units.

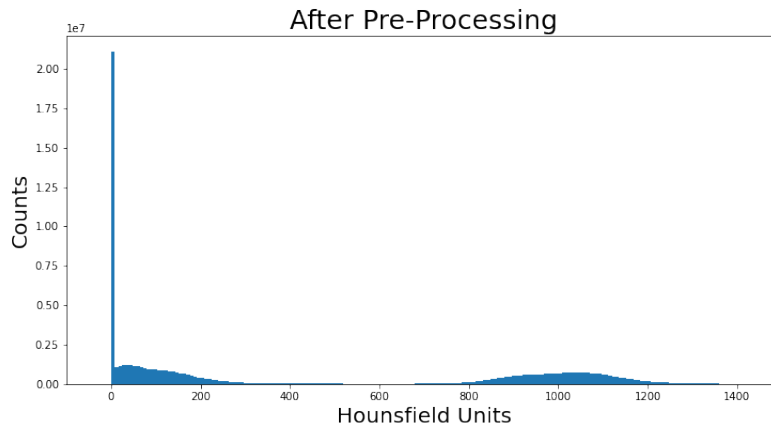
Before starting the actual lung segmentation, we need to perform a de-noising operations, which allow us to increase the differences between the GL of the body regions, and to sharp the edges. According to the procedure described in [1], I've used the bit plane slices. This approach allows to use the way in which each numerical values is stored in the computer by converting each values with its binary representation, this allows us to construct an image in which each voxel intensity is given only by the bits representing the regions multiplied by their significance.

In Figure ?? are displayed the images for each bit. As we can see all the bits from the 1st to the 11th doesn't carry any useful information but only noise, on the other and the bits from the 12th to the 16th aren't used in the image representation. In the end the de-noised image is constructed by using only the 9th, 10th and 11th bits times their significance that is defined as $significance = 2^{bit}$. In this way we have constructed an image in which the noise is highly reduced and the different regions are well separated.

After these procedures the scan is ready for the actual lung segmentation.



(a) Histogram of a CT scan before registration



(b) Histogram of a CT scan after the registration

Figure 1.2.1: *Histogram of voxel values before and after the pre-processing. We can observe that before the pre processing there are some HU out of range, which are the values used to fill the regions outside the tube, and the air value is around -1000 HU according to HU definition. After the rescaling we can observe that all the values are non-negatives.*

Thresholding and reconstruction

For the actual lung segmentation we have found that the most suitable technique is simply a global fixed threshold, since now the GL of the different body regions are well separated. This allow us to include all the intra-lung regions including the GGO, which are usually dropped if an adaptive threshold, like otsu, is performed. However after this process also extra lung regions, like intestine are segmented as lung. This is the reason why we need the last step to select only the lung.

Lung Selection

In Figure ??(a), I've reported a 3D reconstruction of the selected regions after the second step. As we can see the intestine is selected with the lung, which are connected by trachea and bronchi.

On the other end the intestine is disconnected from the lung regions, since are

structures anatomically disconnected. So we can use this characteristics to select only the lung. To perform this step I've used a suitable function from SimpleITK, which allow us to found the connected components by considering the whole image tensor, this means that we are able to found the connected components by considering all the 3 dimensions. At the end of the process, the components with the higher volume is the one corresponding to the lung and trachea regions, so we can simply select this component to achieve a correct selection of lung, as we see in Figure ??(b).

Motion Artifact Removal

Once we have found a mask for the lung, we have to manage the motion artifacts. This artifacts are related to cardiac or respiratory motion, and interfere with the identification of infection areas, since they are identified like ground glass regions. In this step we remove this kind of artifacts in order to reduce the number of false positives.

As we can see in Figure 1.2.4 this kind of artifacts are usually located near lung or heart regions and have an elongated form. The application of an hybrid hessian filter allow us to compute the contiguous edges, and in this way we are able to create a mask for the lung regions. However this method is not precise and can remove also interesting lung regions, so after that a reconstruction process is performed.

In this way a lung mask is created and its applied to the pre-process image. The results will be saved in '.nii' format, which allows to preserve the spatial information about the voxel.

1.2.4 Training

This step consist in the estimation of the centroids of the color space. May be really time consuming, but it is performed only once, so during the actual segmentation the corresponding script isn't run.

To achieved the estimation of centroids, a kmeans clustering of the multichannel images of several CT scan from different patients is performed. Since to achieve a correct estimation a huge amount of scan must be provided, this task is time consuming and computational expansive, however is performed only once and isn't directly involved in the actual segmentation, so doesn't affect the segmentation time. The achievement of this task involves two main steps :

1. **Preparation of images** : involves the building of the multi channel images, and the registration in a common space;
2. **Clustering** : Actual clustering, involves also the managing of the background problem.

Preparation of Images

This step involves the preparation of images, with the building of the multi channel image that incorporates neighbouring and edges informations as well as the registration in a common space and the managing of an allocation memory problem.

As I've said the multichannel image is build to incorporate more information during the clustering. We have found that a 4 channel image will provides good segmentation results. The 4 channel of the image are built as follows :

- Pure image;
- Median Blurred;
- Local Percentile filtered
- Maximum eigenvalues map

In Figure ?? I've displayed the 4 different channel of the image. Each channel allow us to consider different information:

The pure image will provides information about the tissue displayed in the single voxel; The median blurred image and the percentile filtered, allow us to consider also information about the tissue surrounding each particular voxel, since lesions usually involves several group of voxels.

In the end the maximum eigenvalues map allow us to consider also shape information. A source of error was the bronchial structures and the motion artifacts. Usually this features have a thin and elongated shape, in contrast with the lesion areas which are less thin or less elongated. Elongated structures presents na eigenvalues higher than the other. pn the other hand rounded structure presents eigenvalues more or less equal. This map allow us to discriminate between actual lesion regions and bronchial structures and motion artifacts. In this way we are able to reduce the false positives caused by this kind of artifacts.

The first step consist into the construction of the multichannel image of for each input series, after that all the images are shuffled and divided into several sub-samples. The creation of several sub-samples is made since the creation of a single, huge array with several images is not always possible, since requires a huge quantity of memory to be allocated, so we have chose to divide all the images into several sub-samples and cluster them independently, after that a clustering on the estimated centroids is performed.

Clustering

This step consist into the performing of the kmeans clustering for the centroids estimation. To perform this task I've used the OpenCV algorithm, which provides an optimized implementation of the algorithm for multi channel images. A first clustering is applied on each sub-sample, resulting in a set of centroids for each one of them. On this set is applied a second clustering, which provides the actual centroids. In both of the clustering, the initial centroids set is initialized by using the kmeans ++ algorithm, which allows to improve speed and accuracy of the clustering algorithm [4]. During this task we have to manage some issues. As we can see from Figure ?? the number of voxel with $GL = 0$ is several order of magnitude higher than for other GL . As prior we know that these voxels belonging from background, so this cluster is over represented. Since kmeans cluster requires an homogeneous representation for each cluster, this may raise problem during the centroids estimation. In order to overcome this issue we have simply removed this voxels from the clustering.

An other problem may be the estimation of the correct number of clusters. Kmeans clustering requires a prior knowledge on the number of clusters which is a crucial choice. In our case the anatomical knowledge about the lung may help, since we can consider one cluster for each anatomical structure. In the end we have found that 3 clusters are an optimal choice, and the considered structures are the following:

- Lung Parenchima;
- Ground Glass Opacities and consolidation;
- Bronchi;

We don't need a cluster to represent the background, since as I' ve said before the corresponding voxel aren't takes into account during the clustering. In the end a set of centroids for each subsamples was estimated and a second clustering was performed, to found the optimal centroids. This process takes a lot of time, but once we have estimated the optimal centroid set, we haven't to repeat it.

The pseudocode of this script is reported in algorithm ??

Algorithm 1: Pseudo-code for the training script

```

Function shuffle_and_split(images, numberofsubsamples):
    | images←shuffle(images)
    | output←split(images, number of subsamples )
    | return output
End Function
Function kmeans_on_subsamples(subsamples, numberofcentroids):
    | centroids <- []
    | foreach Sub ∈ subsamples do
    | | center←kmeans(sub, number of centroids)
    | | centroids←append(center)
    | end
    | return centroids
End Function
Data: CT scans with Extracted lung
Result: Centroid matrix
foreach scan ∈ input_scans do
    | read the scan
    | sample←image_array
end
sample← build_multichannel(sample)
subsamples←shuffle_and_split(sample, number of subsamples)
centroid_vector←kmeans_on_subsamples(subsamples, n_centroids)
centroid←kmeans_clustering(centroid_vector, n_centroids)

```

1.2.5 Labeling

This is the last step of the pipeline, which involves the actual segmentation. This task is performed by simply assign each voxel to the cluster corresponding to the

nearest centroids, in this way an hard segmentation is achieved.

The script takes as input the CT scan after the lung extraction and build the multichannel image as described before. after that will assign each voxel to the cluster of nearest centroids, which is the centroids that minimize the distance :

$$cluster = \arg \min_S \sum_{i=1}^k \sum_S \|x - \mu_i\| \quad (1.2)$$

where x is the color vector of the voxel and μ is the i th centroid. During this process the background is automatically assigned to the 0 label, since we know as a prior that its value is 0.

To summarize the process, the pseudocode of the script is reported in algorithm ?? I've tested this algorithm on three different dataset, the results are described in the next chapter.

Algorithm 2: Pseudo-code for the labeling script

Function imlabeling(*image*, *centroids*):

foreach $c \in centroids$ **do**

 | distances $\leftarrow \|image - c\|^2$

end

 labels $\leftarrow \arg \min (distances)$

return labels

End Function

Data: CT scan to label, centroids

Result: GGO label

image \leftarrow build_multi_channel

labels \leftarrow imlabeling(image, centroids)

ggo \leftarrow labels = GGO label

1.3 Optimization of Parameters

During each step of the pipeline we have to set different parameters, like the kernel size for median and std filter, as well as the number of centroids to use fro the actual segmentation. In this section I will birefly describe how each one of these parameters was optimized, in order to obtain the best segmentation.

1.3.1 Estimation of the Number of Clusters

The designed algorithm for the centroids estimation is the kmeans clustering that requires a prior knowledge about the number of clusters to use. This is very important since a bad chose of the number of cluster will badly affect the whole segmentation results. In order to chose the proper number of clusters, I've consider two different source of information: the anatomical knowledge about the lung and the internal variability of the lung.

From anatomical knowledge about the lung, we can derive 3 clusters, corresponding to:

- Lung Parenchima;
- Ground Glass Opacity
- Alveolar structure.

Notice that the background of the image isn't considered as a cluster since it is removed from the segmentation for the reasons explained before.

In order to verify that this number of clusters is the best number of clusters, I've considered the internal cluster variability and build the elbow curve.

Clustering techniques try to group the data in different clusters in order to maximize the difference between points in different clusters and to maximize the similarity within each cluster. If the number of cluster is too low, the similarity within each cluster is low; when a proper number of cluster is chose the similarity is high and if we chose too much cluster, the similarity doesn't change too much.

As a measure of the difference within clusters I've used the sum of squared error, equation 1.3.

$$SSE = \sum (x_i - c_j)^2 \quad (1.3)$$

In order to estimate the best number of cluster, the basic idea was to repeat the segmentation several times with different number of clusters, compute the difference within the clusters and compute the sum of square() as a measure of the difference between clusters. After that the so called *elbow curve* was build, as plotted in Figure ??.

We can notice that the SSE decrease by increasing the number of clusters and it will be 0 when we chose as number of cluster equal to the number of points. So we are looking at a number of clusters which provides also a small SSE. The elbow is the point from which SSE start to decrease becaunse of the increasing of number of clusters.

In this case the elbbow corresponds to 3 clusters.

Notice that this process is heuristic and will provide a benchmark about the number of cluster chosen by prior knowledge.

1.3.2 Kernel Size Optimization

During the building of the multi channel image, we have to compute different image features, that requires the setting of different parameters. To properly set these parameters I've build a routine to estimate the best values.

To build this routine I've used the tools given by scikit-optimize library. The idea behind the optimization process is very simple but requires some ground truth labels. I've simply generates many set of parameters, train the centroids with this set and label some images, after that I've compute the according of this labels with ground truth ones. After that I've simply chose the set of paramenter which guarantees the best according with the references. The whole procedure is sketched in Figure ??

This process allows to optimize the parameters in order to obtain the best results as possible. As reference labels I've used the one provided by the public datasets ZENODO and MOSMED. This optimization allows to achieve a better segmentation, but isn't necessary and doesn't interfere to the actual centroids estimation, keeping the techniques unsupervised.

Algorithm 3: Parameter Optimization Algorithm

Data: Test scans, Ground Truth
 old_iou \leftarrow 0
 best_parameters \leftarrow *None*
do
 parameters \leftarrow generates set of parameters
 labels \leftarrow segmentation(parameters)
 iou \leftarrow IoU(labels, ground_truth)
 if iou > old_iou **then**
 | best_paramenters \leftarrow parameters
 end
 old_iou \leftarrow iou
while iter < max_iter

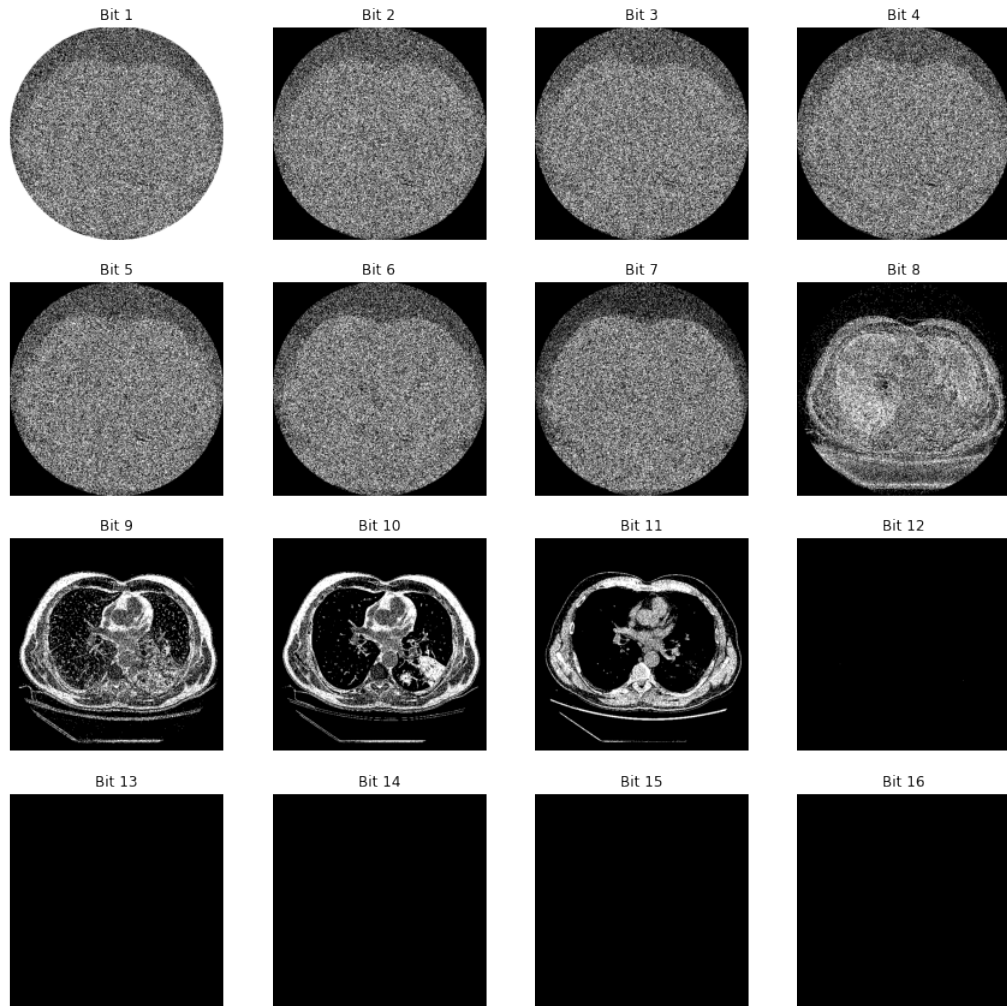


Figure 1.2.2: *Images corresponding to each one of the 16 bits. The image from the 1st to the 8th bit carry only noise, and the images from the 12th to the 16th, doesn't contains any information. The de noised image is composed of the 9th, 10th, and 11th bits times their significance.*

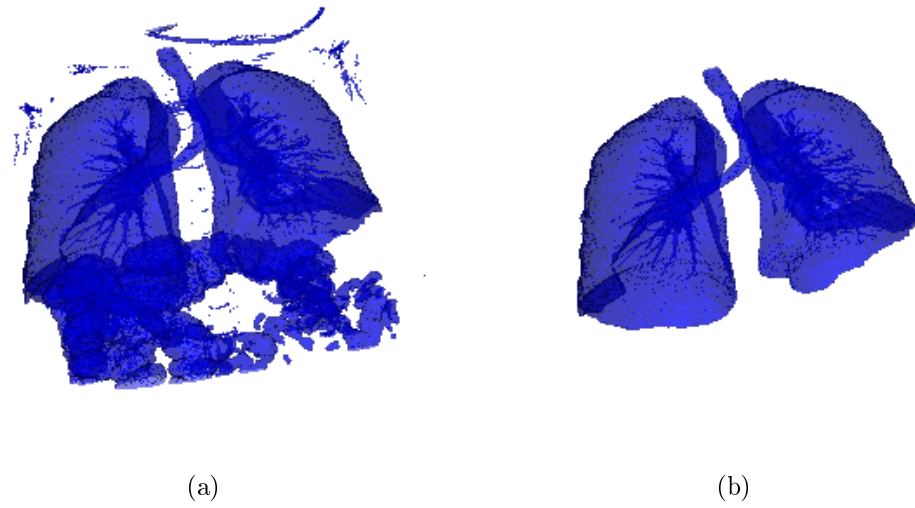


Figure 1.2.3: *3D rendering of the selected lung structure. In figure (a) we can see the volume selected after the threshold. It possible to see that also the intestine is selected along with extra lung regions. In figure (b) the selected volume after the connected components. We can observe how all the extra lung regions are correctly removed.*



Figure 1.2.4: *From left to right the image with motion artifacts, the created mask and the image after the removal*

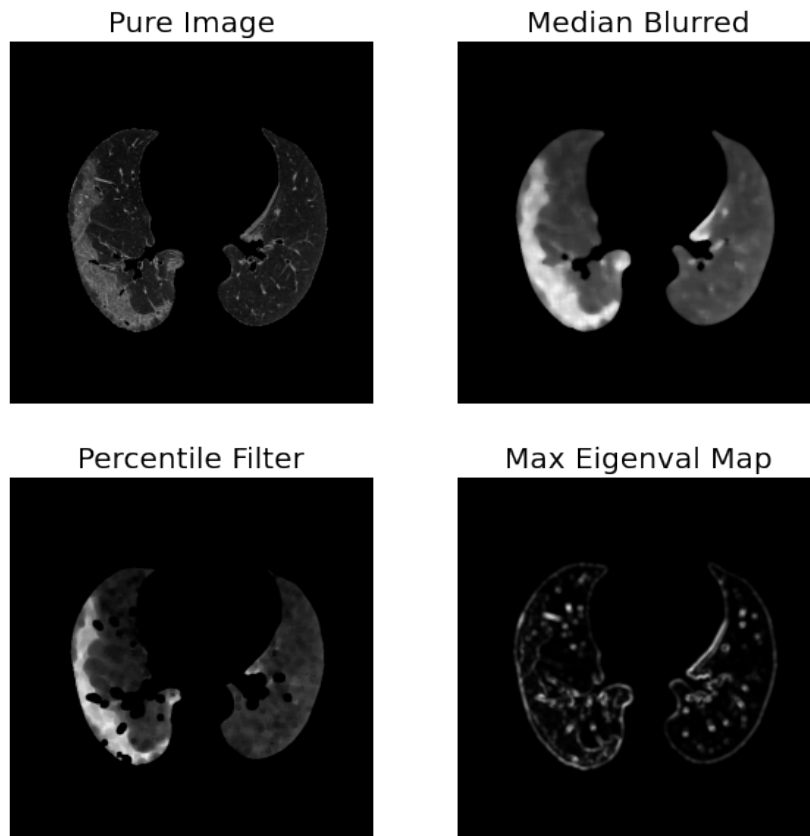


Figure 1.2.5: Image used for each dimension of the color space from left to right and from top to bottom we have the pure image, the median blurred image, the maximum eigenvalues map and the percentile filtered.

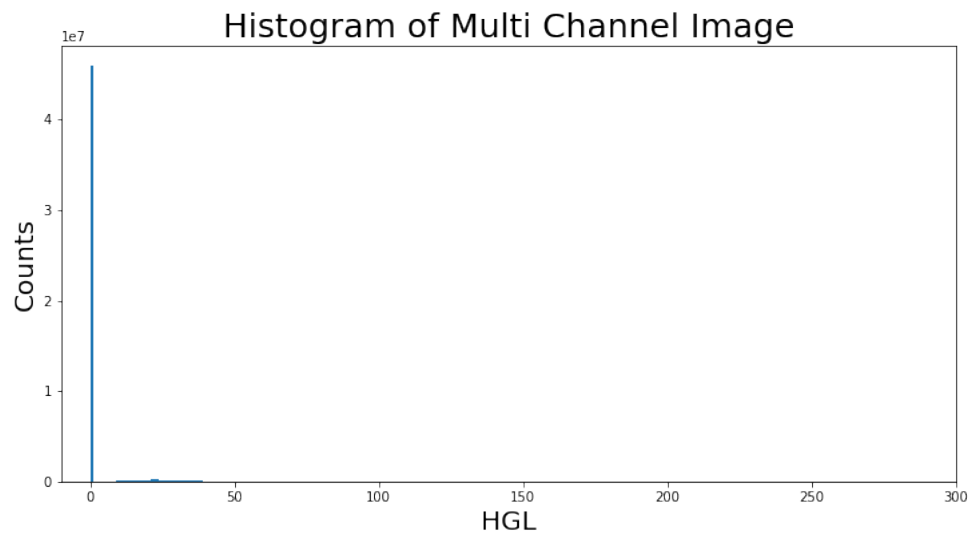


Figure 1.2.6: *Histogram of the multichannel image to cluster, we can clearly see the overrepresented cluster at 0 GL*

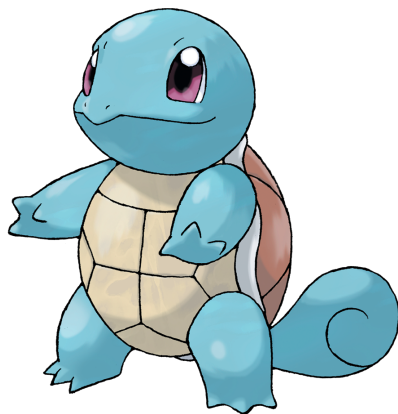


Figure 1.3.1: *Elbow curve*

Chapter 2

Results

In this chapter I will discuss the results of the segmentation. The pipeline was mainly tested on the samples kindly provided by Sant’Orsola hospital, even if also some test on MOSMED and ZENODO was made. The results involves both timing and quality of the segmentation. The centroids used for the segmentation where trained over the 83 CT scans provided by Sant’Orsola and were used for segment all the scans.

I’ve also used the some healthy scan patient to ensure that no lesion areas are identified.

As reference I’ve used some manual segmentation performed by expert radiologist. To match the grund truth and the label under test I’ve used as metrics the intersection over union(IoU).

2.1 DataSet Description

This section is dedicated to the description of the dataset used for the developing and test of the pipeline. The description includes general image characteristics and some metadata. If within the dataset are provided also some ground truth manual segmented labels, also the segmentation modes are described.

2.1.1 Sant’Orsola

Sant’Orsola data was the ones mainly considered in this work. The consist into 83 anonymized CT scans from 83 different patients affected by COVID-19, manually labeled by interns; and 5 healthy control. This dataset was used to train the model by the centroids estimation and also to verify the time performances of the pipeline vs the one of a certified software. The series are distributed as follows:

Property	Value
Number of Scans	83
Distribution by sex(M/F/O)	66.3/33.7/0
Distribution by age(min/median/max)	35/60/89

2.1.2 MOSMED

MosMed is a dataset which contains 1110 anonymized CT scan of human lung from both patients affected by COVID-19 in several stages for the disease, and healthy controls. A small subset of this scans is labeled. The scans are obtained between 1st March and 25th of April 2020 by different Russian hospital. This dataset is born with educational and AI developing purpose. The studies are divided into 5 categories, from healthy patients to the most severe cases. Each scan of the dataset is saved in *.nifti* format and during the conversion from the original dicom series only 1 image every 10 was preserved. The resulting dataset have the following characteristics:

Property	value
Number of Scans	1110
Distribution by sex(M/F/O)	42/56/2
Distribution by age(min/median/max)	18/47/87
Number of studies in each category	254/648/125/45/2

As I've said before, the CT scans are divided into 5 categories, depending on the percentage of the involved lung parenchima :

Class	Description
CT-0	Normal lung tissues
CT-1	presence of GGO, lung parenchima involved less than 25%
CT-2	GGO, involvement of lung parenchima in 25 – 50%
CT-3	GGO and consolidation, involvement of lung parenchima in 50 – 75%
CT-4	GGO, consolidation and reticular changes, lung parenchima involved more than 75%

Of these five categories only 50 annotations are available, mostly involves only the patients of CT-1 group, which is the only one used for the performances checking, since is the only one with the annotations. Scans have been annotated by the experts of Research and Practical Clinical Center for Diagnostics and Telemedicine Technologies of the Moscow Health Care Department.

2.1.3 ZENODO

This dataset consists into 20 CT scans of patients affected by COVID-19, labeled by two expert radiologist and verified by an expert radiologist. The anatomic structures labeled are the left and right lung and the infections regions. Each file is in *.nii* format and no metadata was available.

Unfortunately only half of the scans are in HU, the remaining are in 8-bit gray scale, which is not suitable to verify the pipeline since it requires as input an image in HU.

2.2 Time Performances

An important point of the developed pipeline is that it must provide results in a small amount of time. In this section I will discuss the time performances. The

timing was performed by taking into account each dataset and the number of slices in each scans, Since for this work I've to segment several scans (over 100) I've used some script that allows to perform the two main step of the pipeline separately. So in the end I've computed the time for the lung extraction step and the labeling separately for each dataset. In case of the Sant'Orsola Data, I've also match the time of this pipeline with the one of one certified medical segmentation software. The results are displayed in table

2.3 Accuracy Comparison

In order to check the performances of the pipeline, I've performed a comparison between the areas estimated by the pipeline itself and the one belonging from the manual segmentation. In order to match the labels and found how much they are according, I've used the Intersection over Union metrics, also known as Jaccard score. The intersection over union is a very suitable metrics in this case, mostly because allows to overcome the issue of the over-represented background:

Since the number of voxel of the non-GGO is several order of magnitude higher than the GGO ones, metrics like Pixel Accuracy will fails. IoU encodes the shape properties of the objects under comparison, e.g. the widths, heights and locations of two bounding boxes, into the region property and then calculates a normalized measure that focuses on their areas (or volumes); in this way the IoU is invariant to the scale of the considered problem. The Intersection over Union is defined as follows:

$$IoU = \frac{\|A \cap B\|}{\|A \cup B\|}$$

Where $A, B \in S \subseteq \mathbb{R}$ are, in our case, the estimated labels and the ground truth.

An other test that was made was to segment scans from healthy patients and check that no GGO was detected. This kind of test was made on the 5 healthy patients from Sant'Orsola and on the $CT - 0$ group of MOSMED dataset.

Healthy Control

MOSMED

ZENODO

Sant'Orsola

Chapter 3

Review on Image Segmentation techniques

Image segmentation consist in the partitionng of an image into non overlapping, consistnt regions that are homogeneous respect to some characteristics such as intensity or texture [16]. Nowadays several non-invasive medical imaging techniques are available, such as Computed Tomography(CT), Magnetic Resonance Imaging (MRI) or X-Ray imaging,. that provides a map of the subject anatomy. Image segmentation plays a crucial role in many medical-imaging applications by automating or facilitatong the delineation of anatomical structures and other regions of interest [16]. Manual segmentation is possible, but is time consuming and subject to operator variability; making the results difficult to reproduce [19], so automatic or semi-automatic methods are preferable.

A major difficulty of medical image segmentation is the high variability in medical images. First and foremost, the human anatomy itself shows major modes of variation. Furthermore many different modalities (X-ray, CT, MRI, etc.) are used to create medical images [17].

The results of segmentation can be used to perform feature extraction, that provides fundamental information about organs or lesion volumes, cell counting, etc. If the patient perform several analysis during time, image segmentation is a useful tool to monitor the evolution of particular lesions or tumors during, for example, a therapy.

This chapter contains a brief introduction on medical digital images and a brief review on the image segmentation techniques shuch as clustering or thresholding.

3.1 Review on Image Segmentation Methods

During the years, several segmentation methods have been developed based on a lot of different approaches These metods can be categorized in several way, for example we can divide them into *supervised* or *unsupervised* if they requires or not a set of training data, or can be classified according to the used information type, like *Pixel classification methods*, which use only information about pixel intensity, or *Boundary following* methods, which use edge information, etc. In this section I will provide a brief review on the main segmentation methods, organized in the same way as in [16] that divides the methods in 8 categories:

1. Thresholding,

2. Region growing,
3. Classifiers,
4. Clustering,
5. Markov Random Fields models,
6. Artificial Neural Networks,
7. Deformable Models,
8. Atlas guided approaches.

3.1.1 Thresholding

Thresholding approach is very simple and basically segments a scalar image by creating a binary partitioning of image intensities [16]. It can be applied on an image to distinguish regions with contrasting intensities and thus differentiate between tissue regions represented within the image [19]. Figure ?? show an histogram of a scalar image with two classes, threshold based approach attempts to determine an intensity value, called *threshold* which separate the desired classes [16]. So to achieve the segmentation we can group all the pixels with intensity higher than the threshold in one class and all the remaining in the other class.



Figure 3.1.1: *Caption*

The threshold value is usually setting by visual assesment, but can also be automatized by algorithm like otsu one.

Sometimes may happen that more than two classes are present in the image, so we can set more than one threshold values in order to achieve this multiclass segmentation, also in this case there are algorithms to automatized this process, like an extension of the previous one called *multi otsu threshold*.

This is a simple but very effective approach to segment images when different structures have an high contrast in intensities. Threshold doesn't takes into account the spatial characteristic of the image, so it is sensitive to noise and intensity inhomogeneities, that corrupt the image histogram of the image and making difficult the separation [16]. To overcome these difficulties several variation of thresholding have been proposed based on local intensities and connectivity.

Threshold is usually used as initial step in sequency of image processing operations, followed by other segmentation technique that improve the segmentation quality. Since threshold use only intensity information, can be considered a pixel classification technique.

3.1.2 Region Growing Approach

Region growing approach allows to extract connected regions from an image. This algorithm start at seed location in the image(usually manually selected) and check the adjacent pixels against a predefined homogeneity criterion [19], based on intensity, and/or edges. If the pixels met the criterion, they are added to the region. A continuos application of the rule allow the region to grow.

Like thresholding, region growing is used in combination with other image segmentation operations, and usually allows the delineation of small and simple structures such as tumor and lesions [16].

Regions growing can also be sensitive to noise so extracted regions may have holes or even become disconnected. May also happen that separate rion becomes connected due to partial volume effect.

When we use this approach we have to consider that for each region we want to segment a seed must be planted. There are some algorithm, related to region growing, that does not require a seed point, like split and merge one. Split and merge operates in a recursive fashion. The first step is to check the pixel intensity homogeneity, if they are not homogeneous, the region is splitted into two equal sized sub-regions. This step leads to an oversegmentation, so a merging step is performed, which merge together adjacent regions with similar intensities [19].



Figure 3.1.2: *Caption*

3.1.3 Classifiers Approach

Classifiers approaches use statistical pattern recognition techniques to segment images by using a mixture model that assume each pixels belonging to one of a known set of classes [19]. To assign each pixel to the corresponding classes, use the so called *feature space*, which is the space of any function of the image like intensity. An example of 1D feature space is image histogram.

The feature of each pixel form a pattern that is classified by assign a probability measure for the inclusion of each pixel in each class [19].

This approach assume a prior knowledge about the total number in the image and the probability of occurence of each class. Generally this quantity aren't known, so we need a set of training data to usa as reference.

There are different techninques wich use this approach:

- **k-Nearest Neighborhood** : each pixel is classified in the same class as the training data with the closest intensity;
- **Maximum likelihood or Bayesian** : Assume that pixel intensities are independent samples from a mixture of probability distributions and the classification is obtained by assign each pixel to the class with the highest posterior probability.

This approach requires a structure to segment with distinct and quantifiable features. It is computationally efficient and can be applied to multichannel images. This approach doesn't consider a spatial modelling and need a manual interaction to obtain the training data that must be several since the use of the same training set for a large number of scans can lead to biased results.

3.1.4 Clustering

Clustering approach is similar to classifiers one but in an unsupervised fashion, so doesn't require a training dataset. Clustering iteratively alternate between segmenting the image and characterizing the properties of each class. In this way we can say that clustering approach train itself by using the data available information. We can identify 3 main clustering algorithms:

- **k-means clustering:** that iteratively compute a mean intensity for each class and segmentats the image by classifying each pixel in the class with the closest mean;
- **Fuzzy C-means:** this algorithm generalize the K-means clustering in order to achieve soft- segmentation;
- **Expectation Maximization:** use the same clustering principle as k-means by assuming that the pixel follows a Gaussian mixture model. It iterates between posterior probability and compute the the Maximul Likelihood estimates for the means, covariances and mixing coefficients of the mixture model.

This approach doesn't requires training data, but suffer to an high sensitivity to the initial parameters and do not incorporates spatial model, so it is a pixel classification technique [16].

3.1.5 Markov Random Field

Markov Random Field(MRF) is not a proper segmentation method but its a statistical model that's used within segmentation methods that model the spatial interaction between neighbouring pixels. It's often incorporated in clustering algorithms such as K-means with a Bayesian prior probability.

This model is used because most pixels belong to the same class as their neighbouring pixels, this means that any anatomical structure that consist of only one pixel has a very low probability of occourring [16].

A difficulty of this model is that it is very sensitive to the parameters that controls the strenght of the spatial interactions. An other MRF disavvantage is that requires computationally intensive algorithms. However, despite these disadvantages, MRF are widely used to model segmentation classes and intensity inhomogeneities [16].

3.1.6 Artificial Neural Networks

Artificial Neural Networks are formed by using artificial neurons derived from physiological models [19]. Neural Networks are made by nodes that simulate a biological learning. Each node of the network it is able to perform an elementary operation.

3.1.7 Deformable Model

Deformable Model use an artificial, closed, contour/surface able to expand or contract over time and conforme to a specific image feature [19]. This approach is physically motivated model-based thechnique for the detection of region boundaries [16].

The curve/surface is placed near the desidered boundary and it is deformed by the action of internal and external forces that act iteratively. The external forces are usually derived from the image.

This approach has the capability to directly generate closed parametric curves or surfaces from images and an also incorporate smootness constraint that providesrobustness to noise and spurioous edges.

However this approach requires a manual interaction to place the appropriate set of parameters.

kmeans clustering

In this appendix I will describe the kmeans clustering algorithm, which is the one used for the computation of the centroids set, which corresponds to the characteristic color of each lung structure we wish to segment.

Kmeans clustering is a clustering technique. Clustering technique are unsupervised classification technique which aims to divide data into non overlapping groups such that the data belonging to one group is similar to each other, but they are very distinct from data existing in the other groups [3] [13].

Since clustering techniques are unsupervised, aims to cluster by evaluating similarities and dissimilarities of intrinsic characteristics between clusters [13], so no expected outcomes is given during method of learning [3].

Kmeans clustering seek to assign each point to a particular cluster in a way that minimize the average square distance between points in the same cluster [4]. A vector representing the mean is used to describe each cluster, so this technique is described as a centroid model [13]. Each point is assigned to the cluster with the nearest mean.

Given an integer k and a set of n data points from \mathbb{R}^d , the kmeans clustering seek to find k centers that minimize a potential function given by the sum of squares:

$$\Phi = \sum_{x \in S} \min \|x - c\|^2 \quad (3.1)$$

Where $S \subset \mathbb{R}^d$ is a set of points. In this work \mathbb{R}^d is the colors space and S is the space of color of each voxel.

The steps of the algorithm are the following:

1. Select the value of k as initial centroids
2. Form k cluster by allocating every point to its most nearest centroid
3. Recalculate the centroid for each cluster until the centroid does not change.

Arthur and Vassilvitskii [4] have pointed that this algorithm is not accurate and can produce arbitrarily bad clusters. So they have developed a popular algorithm, the "kmeans++" which improves the clustering accuracy by made an accurate choice of the initial cluster centers.

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