Performance indices of an G/G/c queue

A web server receives jobs according to a Poisson process of rate λ = 10 j/s. The duration of each job is distributed according to an Hyper-Exponential distribution, of rate μ_1 = 50 j/s and μ_2 = 5 j/s and μ_1 = 0.8 .

Compute:

- 1. The utilization of the system
- 2. The (exact) average response time
- 3. The (exact) average number of jobs in the system

After a year, the traffic increases and stabilizes: now it can be considered distributed according to a 5 stages Erlang distribution, with λ = 240 j/s. To support this new scenario, two extra web servers are added, together with a load-balancer that holds request in a single queue, and dispatches them to the first available server. Assuming the time required by the load balancer to be negligible (i.e., the system can be modelled with a G/G/3 queue),

Compute:

- 1. The average utilization of the system
- 2. The approximate average response time
- 3. The approximate average number of jobs in the system