Comp 411

Principles of Programming Languages

Lecture 6

Implementing Syntactic Interpreters

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A Syntactic Evaluator

Can we translate our syntactic reduction rules into a program?

```
; an illegal program can return an AST
;; AST \rightarrow V \subseteq AST
(define eval
  (lambda (M) ; M is an AST
   (cond
                       ; case split on form of M
     ((var? M) M)
                                       ; M is a free var (stuck!)
     ((or (const? M) (proc? M)) M) ; M is a value
     ((add? M)
                                ; M has form (+1r)
       (const-add (eval (add-left M)) (eval (add-right M))))
                                        ; M has form (N1 N2)
     (else
       (apply (eval (app-rator M)) (eval (app-rand M))))))
;; A⇒B A → B
(define apply (lambda (a-proc a-value)
 (cond
   ((not (proc? A-proc)) ; ill-formed app
     (make-app a-proc a-value)) ; return stuck state
   (else
                                 ; return reduced, substituted body
     (eval
       (subst a-value (proc-param a-proc)(proc-body a-proc)))))))
```



Coding Substitution

```
;; V Sym R \rightarrow R Blindly substitutes v for x in M (ignoring capture)
(define subst
  (lambda (v x M))
    (cond
      [(var? M) (cond [(equal? (var-name M) x) v] [else M])]
      [(const? M) M]
      [(proc? M))
        (cond [(equal? x (proc-param M)) M]
              [else (make-proc (proc-param M)
                       (subst v x (proc-body M)))])]
      [(add? M) (make-add (subst v x (add-left M))
                          (subst v x (add-right M)))]
      [else ;; M is (N1 N2)
        (make-app (subst v x (app-rator M))
                  (subst v x (app-rand M)))])))
```

Is **subst** safe? No! It is oblivious to free variables in M. Does it work in context?

Almost; it fails in some cases for illegal programs. Not all programs with free variables are detected.

Exercise: Revise **subst** so that it is safe. Note that blind substitution works as long as our top-level M is well-formed and contains no free variables. Why?



Comments on Syntactic Interpreter

We still need to define const-add. What does const-add do on non-const values? The key property of this evaluator is that it only manipulates (abstract) syntax. It specifies the meaning of LC by mechanically transforming the syntactic representation of a program. This approach only assigns a satisfactory meaning to complete LC programs, not to subtrees of complete programs. Counter-example:

$$((lambda (x) (+ x y)) 7)$$

If **const-add** mirrored syntactic evaluation, then it would return the abstract syntax tree for (+ 7 y) which is an irreducible "stuck" state—not a value—and the correct choice if we are strictly implementing syntactic evaluation. A more attractive alternative that is an elaboration of syntactic interpretation is to generate a run-time error because y is not a value. In a context where y is bound to (the abstract syntax tree for) 5, it returns (the abstract syntax tree for) 12; which is not (the abstract syntax tree for) (+ 7 y) or a run-time error. From a mathematical perspective, The meaning of sub-expressions should be defined so that meaning [...] is compositional, *i.e.*

$$[\![\ (\textbf{c} \ \textbf{M}_{\!1} \ ... \ \textbf{M}_{\!k} \) \,]\!] = [\![\ \textbf{c} \]\!] \ (\ [\![\ \textbf{M}_{\!1} \]\!], \ \ldots \ , [\![\ \textbf{M}_{\!k} \]\!])$$

Syntactic interpretation utterly fails in this regard because it cannot cope with free variables.



Can We Make Syntactic Evaluation Compositional?

Since syntactic evaluation does not assign meaning to components of abstract syntax trees, it technically cannot satisfy the compositionality criterion. The use of "stuck states" is a cute formal trick but fails the compositionality test (which is not considered an important issue according to current fashion). But we can partially patch syntactic evaluation by transforming a "stuck state" result to a corresponding error element (as determined by our compositional meaning).

So the stuck state result (+ 7 y) would be converted to the error element corresponding to an "unbound variable". Similarly, the stuck state (/ 7 0) might be converted to a "division by zero" error element.

We would also have to modify our syntactic evaluator to abort the computation when a sub-computation generates an error element and return that error element as the result.

This patched interpreter is still not compositional because no meanings can be assigned to subexpressions with free variables other than error elements but free variables within expressions are not necessarily errors. In the evaluation process, some free variables are replaced by values before they are evaluated.

Toward Semantic Interpretation

From a software engineering perspective, what is wrong with our syntactic interpreter? How fast is **subst**? How can we do better?

Avoid unnecessary substitutions by keeping a table of bindings, which we will call an environment.

```
;; Binding = (make-Binding Sym V) ; Note: Sym not Var [coding detail]
;; Env = (listOf Binding)
;; R Env \rightarrow V
(define eval
 (lambda (M env)
   (cond
     ((var? M) (lookup (var-name M) env)) ((or (const? M) (proc? M)) M)
     ((add? M); M has form '(+ 1 r)' in LC syntax
       (const-add (eval (add-left M) env) (eval (add-right M) env)))
     (else
               ; M has form '(N1 N2)' in LC syntax
       (apply (eval (app-rator M) env) (eval (app-rand M) env) env)))))
;; Proc V Env → V
(define apply
  (lambda (a-proc a-value env)
    (eval (proc-body a-proc) (cons ((proc-param a-proc) a-value) env)))
```



More Readable Notation for Lambda Expressions

 In essentially all functional languages for software development, there is alternate special notation for

- This alternate notation is literally an abbreviation for the explicit lambda form
- For this alternate notation, the beta-reduction rule has the form

```
(let [(x \ V)] \ M) \Rightarrow M[x := V] Call-by-value (let [(x \ N)] \ M) \Rightarrow M[x := N] Call-by-name
```



Gotcha's in Naive Semantic Interpretation

• What if a-proc contains free variables (which can happen in legal programs)? Do we always get the right answer (as defined by syntactic interpretation)? Illustration:

- What goes wrong? Should a lambda-expression really evaluate to itself? This is the most serious and most common blunder in writing interpreters.
- Think about how you might fix the problem. Hint: what information is missing in **env** when **a-proc** is evaluated? Remember, you want the same result as if you were performing syntactic interpretation.

