

Prior Exam Questions

1. The function below is very important in probability and statistics. Write a user-defined function that takes as input parameters x , u , and s , returns the value of the function evaluated at these values. You can use the numpy function `numpy.exp()` to calculate the exponential.

$$P(x) = \frac{1}{\sqrt{2\pi}s^2} \exp\left(-\frac{(x-u)^2}{2s^2}\right)$$

Then, write the programming commands which call this function and plot it for x between -3 and 3 with $u=0$ and $s=1$ (for all values of x). Be sure to label your axes and show the plot.

2. Assume a function called *isprime* is available for you to use in a module called *ENGR102* which determines if a number is a prime number or not. The input parameter for *isprime* is a single integer and the output is either True or False. Write the Python program that would input two integers and then test only the odd numbers between and including these two numbers, to see if they are prime numbers or not using the *isprime* function. The output of your program should be a list of prime numbers found. If no prime numbers were found, then output should state that no prime numbers were found. Start your code with: from ENGR102 import isprime.
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3. Write a Python program that can be used to find the x,y coordinates of the local maxima and the minima points between $x = -3$ and $x=5$ for the polynomial $y = x^3 - 3x^2 - 5.5x + 25$. The output should be the coordinates for both the maxima and the minima.
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4. A text file named 'data.dat' is stored on a computer's hard drive. In a text editor the file displays:

```
# Created on November 15, 2018
# Time, Temperature, Windspeed
# (min), (deg F), (knots)
0, 33.47, 1.27
5, 32.59, 1.95
10, 33.62, 0.76
15, 33.79, 1.12
```

Write a program that reads the contents of this file, assigns the header lines to a variable that is a list of strings, and assigns the data to a variable that is a floating point np.array that contains all of the data in the file. (The data should be in a 4 x 3 array.) Write this code using standard file I/O commands; *do not use* any csv reader that you may know of in some Python package.

5. Write a function that will take as input a set of numbers, and which returns the mean and variance of the set of numbers. The input can be a list, tuple or numpy.array. For a set of numbers x_1, x_2, \dots, x_n , the mean is defined as shown below. Do NOT use the numpy functions `numpy.mean` and `numpy.var`; you must use a loop in your function.

$$m = \frac{1}{n} \sum_{i=1}^n x_i \qquad S^2 = \frac{1}{n} \sum_{i=1}^n (x_i - m)^2$$

6. Given two numpy arrays A and B, write the Python code to calculate $C = AB$ (matrix multiplication (not by-element)). Assume that the inner dimensions of A and B match.
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7. A *perfect number* is a positive integer >1 that is equal to the sum of its proper divisors. The smallest perfect number is 6 since the sum of the proper divisors for 6 (1, 2, and 3) equals 6. The integer 28 is also a perfect number since the divisors for 28 are 1, 2, 4, 7, and 14 and the sum of these numbers equals 28.

Write a function that takes as input a positive integer ≥ 1 , then determines the proper divisors of that integer, sums these divisors, and returns a True value if the number is a perfect number or a False value if it is not.

Assume that the program that calls this function verifies that the input is a positive integer ≥ 1 .

Recall that “The proper divisors of a positive integer N are those numbers, other than N itself, that divide N without remainder. For $N > 1$ they will always include 1, but for $N = 1$ there are no proper divisors. The proper divisors of 6 are 1, 2, and 3. The proper divisors of 100 are 1, 2, 4, 5, 10, 20, 25, and 50.”

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8. A text file named `item_cost.dat` is stored on a computer's hard drive. In a text editor the file displays the first few lines of the file (note that the first line contains a header).

Write a program that reads the contents of this file, determines the cheapest item and prints the information about that item and its cost to the screen using the following format:

The cheapest item is Item57. It costs \$1.05.

Write this code using standard file I/O commands; *do not use* any csv reader available in some Python package. You cannot use any built-in sorting functions. You should use a list (or more than one list), a loop (or more than one loop). You may assume that all costs are unique (no two items cost the same).

Item, Cost (\$)
Item1, 3.75
Item2, 3.50
Item3, 2.75
Item4, 4.50

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9. Explain what happens (what will be output) when the code below is executed. If the code generates an error, explain the cause of the error.

```
print(int('5.5'))
```

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10. Given the string `A='Aggie Engineers Rock And Are In High Demand By Industry'`. Write the Python code to prepare a list of the words in this string.

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11. A schematic for converting Phone letters to digits mapping is shown in the image on the right. Write a Python program that prompts the user to enter a 10-character phone number in this format `XXX-XXXXXXX`. The program replaces the last seven alphabetic characters by their equivalent digits and displays the entered phone number in this format `XXX-XXX-XXXX`. For example, if `800-GOFEDX` is entered, the program displays `'800-GOFEDX` is equivalent to `800-463-3339`'. You may assume that the last seven characters are alphabetic characters from A – Z.



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12. Write a program that will input data (namely, the results for a recent ENGR 102 quiz) from the keyboard, save it to a file in the same directory where your python files are saved, and then print the average quiz grade to the screen. Your program should prompt the user for the name of the file to create, how many data entries there are, and then request the values be entered until the user entries are complete. Each entry includes a student's name and his/her score. Write this code using standard file I/O commands. Before the program terminates, print the average quiz grade to the screen with the appropriate format:

The average grade for this quiz is 78.2

When opened in a text editor, the output file should display the following (for example) and be nicely formatted (note the header line and the alignment of columns):

Name	Score
Tom	85
Jim	96.5
Helen	92
Sam	89.5
Tina	97

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13. An Armstrong number is a positive 3 digit integer, where the sum of the cubes of its digits is equal to the integer itself. For example, 371 is an Armstrong number as $(3**3) + (7**3) + (1**3) = 371$

Write a function called *Armstrong_number* that takes as input two positive 3 digit integers and returns a list or array or tuple containing all the Armstrong numbers between and including these two integers, and a True or False Boolean variable, True meaning an Armstrong value was found in the range. Assume that the code in the calling function is set to ensure that the second integer input to the function is greater than the first and that both values for x are in the range $100 \leq x \leq 999$.

14. A text file named '*peanut.dat*' of unknown length is stored on a computer's hard drive. In a text editor the file displays the first few lines of the file (note that the first line contains a header):

Number	MajorDia	MinorDia
1	17.61	5.46
2	16.47	5.46
3	18.08	6.12

Write a program that reads the contents of this file. Then for each peanut number, output to the screen the peanut number, Major Diameter, Minor Diameter and the diameter ratio in a formatted and ordered output, with headings, and the correct number of decimal places such as shown below for the first 3 peanuts:

number	MajorDia	MinorDia	Ratio
1	17.61	5.46	3.23
2	16.47	5.46	3.02
3	18.08	6.12	2.95

Write this code using standard file I/O commands; *do not use* any Python module csv reader. Use formatted outputs, reporting values to 2 decimal places; you may not use the round() function.

15. Write a program that will repeatedly ask the user to input a student's redheadedness and age. The program will continue to ask for input until a negative age value is entered, meaning that the user is done inputting data. The program should determine the number of redheaded students and their minimum and maximum ages, and the number of non-redheaded students and their minimum and maximum ages. The results should be written to a new file using the name '*Student_Data_23Fa.txt*'. The file, when is opened in a text editor, should look like this:

Gender	Number of Students	Minimum Age	Maximum Age
Redheaded	32	17	24
Not Red	57	17	26

Note the required header line, data spacing, and column alignment

16. The Taylor series to approximate the cos (x) for all values of x, is defined as

$$\cos x = \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n)!} x^{2n}$$

Write a function called *Tay_term* that inputs a value of *n* and returns the value of the series for only that value of *n*, as shown in the formula above. For example, if a value of *n*=3 was transferred to the

function, and *x* = 0.5, *Tay_term* would return the value for $\frac{(-1)^3}{(2*3)!} x^{(2*3)}$ for *x*=0.5. The main

program operates by first designating x as a global variable, then asking the user to input a value of x . To calculate the value for cosine of x using this series, the function *Tay_term* is repeatedly called with each increment of n , the values for each term are summed, until the value of the absolute value of the current term returned by the function is less than 0.00001. The output should display the results such as

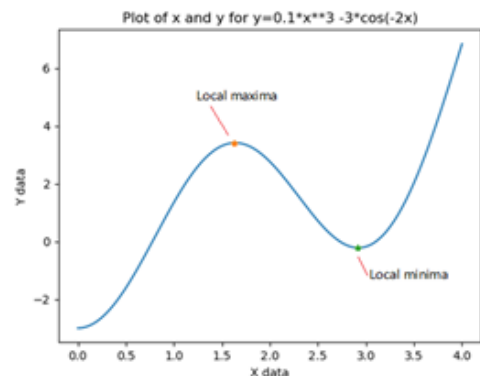
The cosine of 0.50 is 0.8776

Note: factorial() is a function available in the math module

17. Write a Python program that can be used to graph the following equation for x between $x=0$ and $x=4$. Be certain to include a sufficient number of values of x so that a smooth curve can be obtained with your plot. Include a graph title and labels for the x and y axes.

$$y = 0.1x^3 - 3\cos(-2x)$$

Next write a function that is to be called by your program to find the local maxima and minima points. Your function should import your, lists, arrays, or tuple of both the x and y data points and return the coordinates of the local maxima and minima. Plot the maxima/minima points on the graph and output/print the x,y coordinates for these two data points.



Additional Practice Problems:

As with any practice problems, these may or may not be similar to exam problems. However, working through these exercises should improve your program problem-solving, and assist you in doing well on the exam. I suggest first attempting these problems with no computer, calculator, cell-phone or other notes nearby. Once you've done what you can, then start utilizing other tools.

PRACTICE PROBLEM 01:

The Maclaurin series expansion for $\frac{1}{1-x}$ on an interval from $-1 < x < 1$ is as follows:

$$\frac{1}{1-x} = \sum_{n=0}^{\infty} x^n = 1 + x + x^2 + x^3 + x^4 + \dots + x^n$$

Write Python code which asks for input of a value of x on the interval $-1 < x < 1$, and which computes an approximation to $\frac{1}{1-x}$ using the series expansion summation. The summation should be continued until the term to be added to the summation is less than 10^{-6} in absolute value. Hint: Note that each term in the series is x raised to a power, including the 1 and x terms: $x^0 = 1$ and $x^1 = x$

PRACTICE PROBLEM 02:

Write a Python program that takes as inputs 5 integers. The program should check to see if any of the 5 are duplicates of another (i.e., check whether any of the integers were entered more than once). If, after all inputs are entered, a duplicate is found, the program should print "Duplicates", otherwise it should print "All Unique"

PRACTICE PROBLEM 03:

Write a program that will ask a user to enter names and ages of people, stopping when an age of 0 is entered (and not processing that person). The program should collect this information, and then output the average age, the name of the oldest person, and the name of the youngest person. Assume no two people have the same age.

PRACTICE PROBLEM 04:

Write a program that will ask the user to input two integers and calculate the sum of numbers between them that are multiples of 4. Exit the program if the user provides invalid input. Implement a loop to compute the partial sum. Do not use lists, tuples, arrays.

PRACTICE PROBLEM 05:

Write the Python code that is needed to print the numbers between 1 and 50 that are not divisible by 2 or by 3.

PRACTICE PROBLEM 06:

The function

$$P(x) = \frac{1}{\sqrt{2\pi s^2}} \exp \exp \left(-\frac{(x-u)^2}{2s^2} \right)$$

is very important in probability and statistics. Write a user-defined function that takes as input parameters x , u , and s , returns the value of the function evaluated at these values. You can use the numpy function `numpy.exp()` to calculate the exponential.

Then, write the programming commands which call this function and plot it for x between -3 and 3 with $u = 0$ and $s = 1$ (for all values of x). Be sure to label your axes and show the plot.

PRACTICE PROBLEM 07:

Other than answering that the Top-Down process starts at the top and the Bottom-Up process starts at the bottom, describe the differences in the approach to programming, using the Top-Down Design Process and the Bottom-Up Design process. List 2 advantages of each design process.

PRACTICE PROBLEM 08:

Assume a function called `isprime` is available for you to use in a module called `ENGR102` which determines if a number is a prime number or not. The input parameter for `isprime` is a single integer and the output is either `True` or `False`. Write the Python program that would input two integers and then test only the odd numbers between and including these two numbers, to see if they are prime numbers or not using the `isprime` function. The output of your program should be a list of prime numbers found. If no prime numbers were found, then output should state that no prime numbers were found. Start your code with: `from ENGR102 import isprime`.

PRACTICE PROBLEM 09:

What does the following python code output?

```
def myfunc(x):  
    a = 1  
    print(x)  
  
a = 5  
myfunc(a)  
print(a)
```

PRACTICE PROBLEM 10:

Write a function that will take as input a set of numbers, and which returns the mean and variance of the set of numbers. The input can be a list, tuple or `numpy.array`. For a set of numbers x_1, x_2, \dots, x_n , the mean is defined as $m = \frac{1}{n} \sum_{i=1}^n x_i$ and the variance is defined as $S^2 = \frac{1}{n} \sum_{i=1}^n (x_i - m)^2$. DO NOT use the numpy functions `numpy.mean` and `numpy.var`; you must use a loop in your function.

PRACTICE PROBLEM 11:

A text file named 'data.dat' is stored on a computer's hard drive. In a text editor the file displays:

```
# Created on November 5, 2023  
# Time, Temperature, Windspeed  
# (min), (deg F), (knots)  
0, 33.47, 1.27  
5, 32.59, 1.95  
10, 33.62, 0.76  
15, 33.79, 1.12
```

Write a program that reads the contents of this file, assigns the header lines to a variable that is a list of strings, and assigns the data to a variable that is a floating point `np.array` that contains all of the data in the file. (The data

should be in an n x 3 array.) Write this code using standard file I/O commands; do not use any csv reader that you may know of in some Python package.

PRACTICE PROBLEM 12:

What is the output of the following python program?

```
data = [[[1, 2], [3, 4]], [[5, 6], [7, 8]]]
print(data[1][0][0])
```

PRACTICE PROBLEM 13:

Write a program that takes in coefficients for a polynomial equation and prints the complete equation. Write a function that takes the derivative of any polynomial equation and call that function to take the derivative of the inputted polynomial equation and print out the derivative.

PRACTICE PROBLEM 14:

Write a program that intakes an arbitrary number of patients' names and signs/symptoms; including blood pressure, pulse, respiratory rate, and blood glucose. Have the information assigned to the patient's name in a Python dictionary. Then print out the patient's information when the user types in that person's name to a prompt.

PRACTICE PROBLEM 15:

Create a program that will open up a file named 'grades.txt' and then find and print the average score, the maximum score and the minimum score. Each grade will be on a new line in the file. Do not use a .csv reader for this problem.

PRACTICE PROBLEM 16:

Create a function(numcondition()) which asks user two integer values, and returns true if both add up and multiply to more than 10 and 20 respectively, and false if neither of these conditions are satisfied. If one is satisfied, it returns which condition is satisfied. use test cases and docstring.

PRACTICE PROBLEM 17:

Write a function in python that asks for the ideal mass of products in a chemical reaction and then for the actual mass produced. The function should then return the percent yield of the chemical reaction. Then write another function that will take the return of the first function and add it to a .txt file. Each time the function is run, the next percent yield should be documented on another line.

PRACTICE PROBLEM 18:

Create a program that makes two warriors fight each other. Each warrior should have a critical strike chance, an armor stat (that reduces damage taken proportionally), an attack range (minimum and maximum of possible damage to deal), an evasion stat, and a health stat that are all given by user input. Print the number of rounds (each round being an attack from one of the warriors) and the health of each warrior and the damage dealt after each round. (This program should use arrays, loops, and external libraries.)

EXAMPLE PROBLEM 19:

A vending machine will return the fewest number of coins possible as change. Take as input the amount of change required, and provide as output how many of each type of coin will be dispensed. Assume only dollar coins, quarters, dimes, nickels and pennies are available.

EXAMPLE PROBLEM 20:

Define a function that takes a word and counts the number of consonants & vowels. Use this function to perform the same action for each word in a sentence inputted by a user. (Treat "y" as a consonant, unless you want a challenge.)

EXAMPLE PROBLEM 21:

Write a function to insert a number to an ordered list (assume it goes from small to big) so that the list still goes from small to big. Return the updated list. Do not use a "sort" method