

Console Output:

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run:
Please give number of elements to be inserted : 5000000
Checking...
Binary search tree skipped due to large size.
AVL search tree: 1006 milliseconds.
Red-Black search tree: 1040 milliseconds.
Splay search tree: 828 milliseconds.
Sorting: 129 milliseconds.
AVL search tree: 1264 milliseconds.
RBT search tree: 2814 milliseconds.
BUILD SUCCESSFUL (total time: 9 seconds)
```

Theoretical Points:

AVL and Red-Black Trees are very similar, although share some key differences. The height of an AVL Tree is max around $1.4\log(n)$, while a Red-Black Tree has a max height of $2\log(n)$. On insertion, an AVL Tree may need $O(\log(n))$ operations, as it may need to rebalance the Tree. Counter to this, a Red-Black Tree will give $O(1)$. This relates that the AVL Tree is usually faster on searching, but slower on insertion.

For a Splay Tree, the search may be $O(n)$ if the elements are inserted in order. This case causes a Splay tree to be slower than most AVL and Red-Black Trees, as the inputs will usually be random. The benefits come from the self-adjusting aspect of the Splay Tree.

Experimental Points:

Although most results are very close, there is still some divergence. The Red-Black Tree has a worse run time in general compared to the AVL tree in both insertion and searching. Although the Red-Black tree has better theoretical insertion, when given a large and random set of data, it must do a lot of rebalancing that the AVL tree may not need to do. The Splay tree was the fastest as the inOrder function helps it insert everything in order.