

Image-to-Markup Generation with Coarse-to-Fine Attention

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Outline

- 1 Introduction: Image-to-Markup Generation
- 2 Dataset: IM2LATEX-100K
- 3 Model
- 4 Experiments
- 5 Conclusions & Future Work

Multimodal Generation

*Real text is not disembodied. It always appears in context... As soon as we begin to consider the generation of text in context, we immediately have to countenance issues of **typography** and **orthography** (for the written form) and **prosody** (for the spoken form)... This is perhaps most obvious in the case of systems that generate both text and graphics and attempt to combine these in sensible ways.*

Dale et al. [1998]

Image to Text

- Natural OCR [Shi et al., 2016, Lee and Osindero, 2016, Mishra et al., 2012, Wang et al., 2012]



cocacola

Image to Text

- Natural OCR [Shi et al., 2016, Lee and Osindero, 2016, Mishra et al., 2012, Wang et al., 2012]



cocacola

- Image Captioning [Xu et al., 2015, Karpathy and Fei-Fei, 2015, Vinyals et al., 2015]



A man in street
racer armor is
examining the tire
of another racers
motor bike

IM2LATEX-100K

$$A_0^3(\alpha' \rightarrow 0) = 2g_d \varepsilon_\lambda^{(1)} \varepsilon_\mu^{(2)} \varepsilon_\nu^{(3)} \left\{ \eta^{\lambda\mu} (p_1^\nu - p_2^\nu) + \eta^{\lambda\nu} (p_3^\mu - p_1^\mu) + \eta^{\mu\nu} (p_2^\lambda - p_3^\lambda) \right\}.$$

A_{0}^{3}(\alpha^{\prime}\rightarrow 0)=2\,g_{d}\,\varepsilon_{\lambda}^{(1)}\varepsilon_{\mu}^{(2)}\varepsilon_{\nu}^{(3)}\left\{\eta^{\lambda\mu}\,(p_1^{\nu}-p_2^{\nu})+\eta^{\lambda\nu}\,(p_3^{\mu}-p_1^{\mu})+\eta^{\mu\nu}\,\left(p_2^{\lambda}-p_3^{\lambda}\right)\right\}.

IM2LATEX-100K

$$\left\{ \begin{array}{l} \delta_\epsilon B \sim \epsilon F, \\ \delta_\epsilon F \sim \partial \epsilon + \epsilon B, \end{array} \right.$$

```
\left( \begin{array}{l} \delta_\epsilon B \sim \epsilon F, \\ \delta_\epsilon F \sim \partial \epsilon + \epsilon B, \end{array} \right).
```

IM2LATEX-100K

$$\int_{\mathcal{L}_{d-1}^d} f(H) d\nu_{d-1}(H) = c_3 \int_{\mathcal{L}_2^A} \int_{\mathcal{L}_{d-1}^L} f(H) [H, A]^2 d\nu_{d-1}^L(H) d\nu_2^A(L).$$

\int \limits_{\{\mathcal{L}_{d-1}^d\}} f(H) d\nu_{d-1}(H) = c_3 \int \limits_{\{\mathcal{L}_2^A\}} \int \limits_{\{\mathcal{L}_{d-1}^L\}} f(H) [H, A]^2 d\nu_{d-1}^L(H) d\nu_2^A(L).

IM2LATEX-100K

$$J = \begin{pmatrix} \alpha^t & \tilde{f}_2 \\ f_1 & \tilde{A} \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 0 & L \end{pmatrix} \begin{pmatrix} \alpha & \tilde{f}_1 \\ f_2 & A \end{pmatrix} = \begin{pmatrix} \tilde{f}_2 L f_2 & \tilde{f}_2 L A \\ \tilde{A} L f_2 & \tilde{A} L A \end{pmatrix}$$

```
J = \left( \begin{array}{cc} c & c \end{array} \right) \left( \begin{array}{cc} \alpha^t & \tilde{f}_2 \\ f_1 & \tilde{A} \end{array} \right) \left( \begin{array}{cc} 0 & 0 \\ 0 & L \end{array} \right) \left( \begin{array}{cc} \alpha & \tilde{f}_1 \\ f_2 & A \end{array} \right) = \left( \begin{array}{cc} \tilde{f}_2 L f_2 & \tilde{f}_2 L A \\ \tilde{A} L f_2 & \tilde{A} L A \end{array} \right)
```

IM2LATEX-100K

$$\lambda_{n,1}^{(2)} = \frac{\partial \overline{H}_0}{\partial q_{n,0}}, \lambda_{n,j_n}^{(2)} = \frac{\partial \overline{H}_0}{\partial q_{n,j_n-1}} - \mu_{n,j_n-1}, \quad j_n = 2, 3, \dots, m_n - 1.$$

```
\lambda_{n,1}^{(2)} = \frac{\partial \overline{H}_0}{\partial q_{n,0}}, \lambda_{n,j_n}^{(2)} = \frac{\partial \overline{H}_0}{\partial q_{n,j_n-1}} - \mu_{n,j_n-1}, \quad j_n = 2, 3, \dots, m_n - 1.
```

IM2LATEX-100K

$$(P_{ll'} - K_{ll'})\phi'(z_q)|\chi> = 0$$

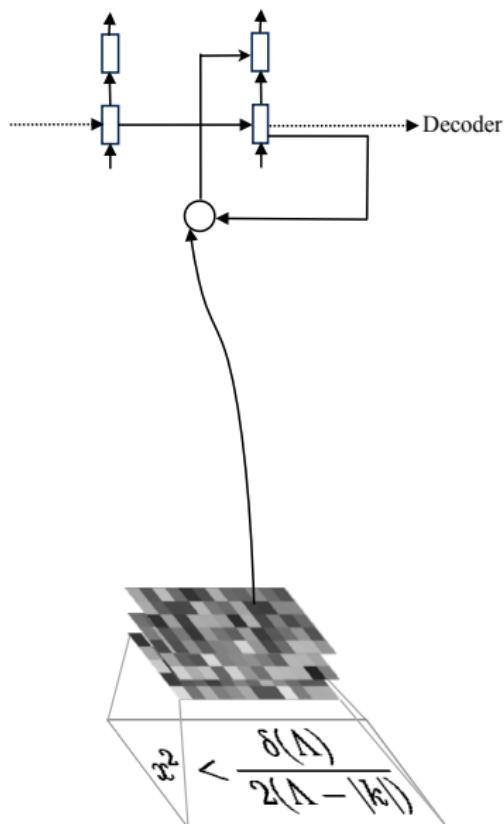
$$(P_{\{\Pi'\}} - K_{\{\Pi'\}})\phi'(z_{\{q\}})|\chi> = 0$$

IM2LATEX-100K

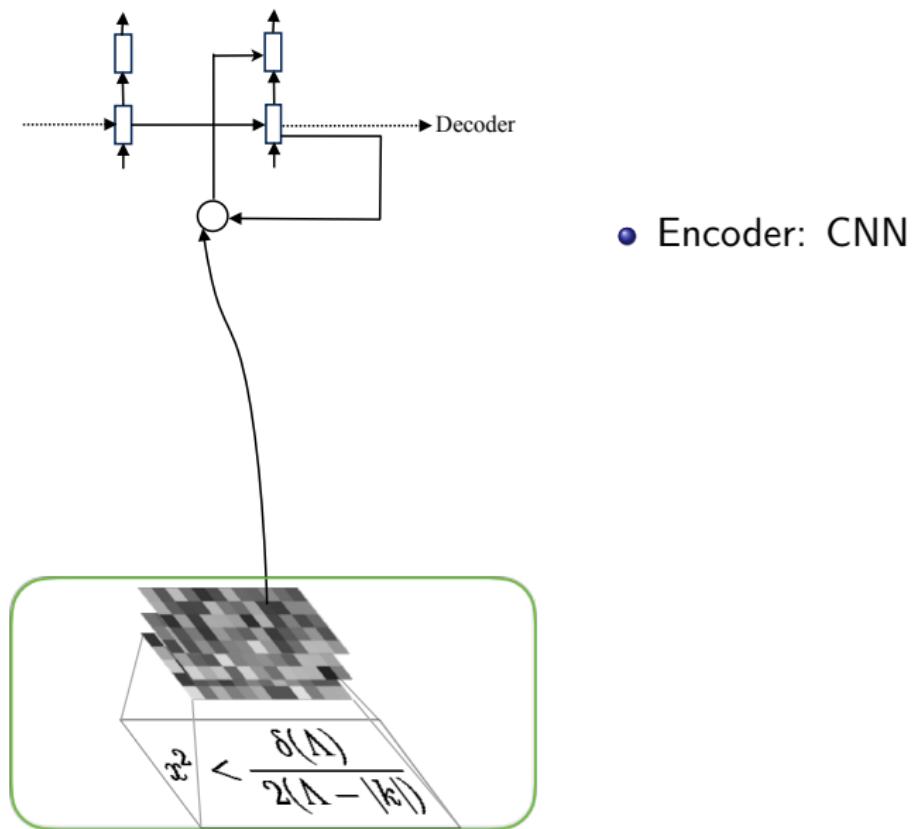
#	img size	median #char	min #char	max #char
103,556	1654×2339	98	38	997

- Originally developed for OpenAI requests for research
- LaTeX sources of arXiv papers on high energy physics from 2003 KDD cup [Gehrke et al., 2003]
- Extracted with regular expressions
- Rendered in a vanilla LaTeX environment

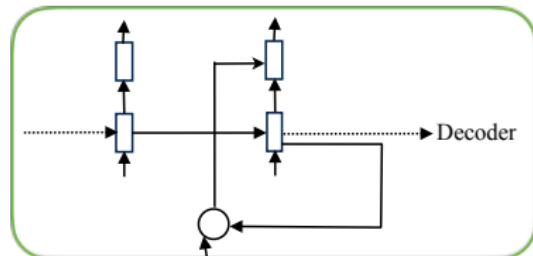
Attention-based Image Captioning (Xu et al. 2015)



Attention-based Image Captioning (Xu et al. 2015)



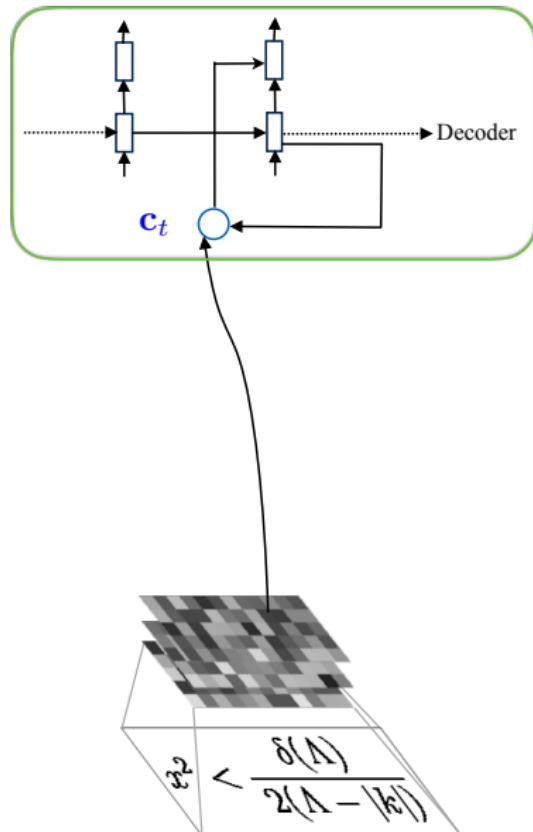
Attention-based Image Captioning (Xu et al. 2015)



- Encoder: CNN
- Decoder: RNN with attention

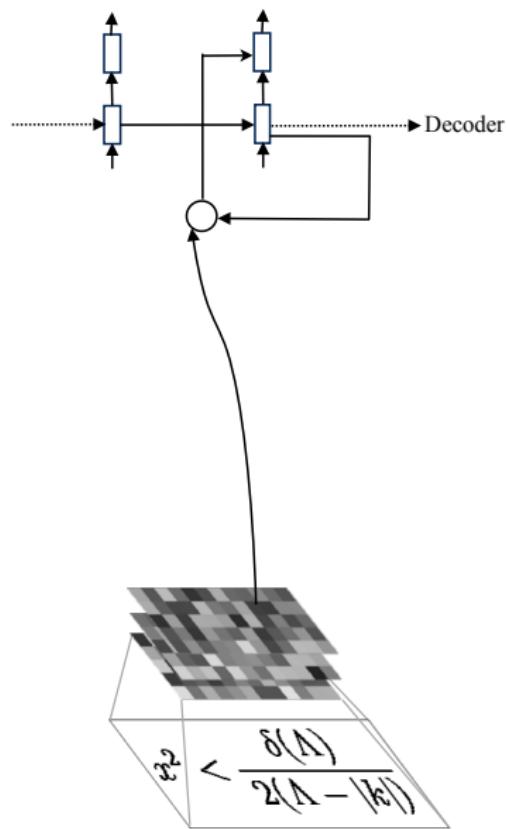
$$z^2 < \frac{\delta(\Lambda)}{2(\Lambda - |k|)}$$

Attention-based Image Captioning (Xu et al. 2015)



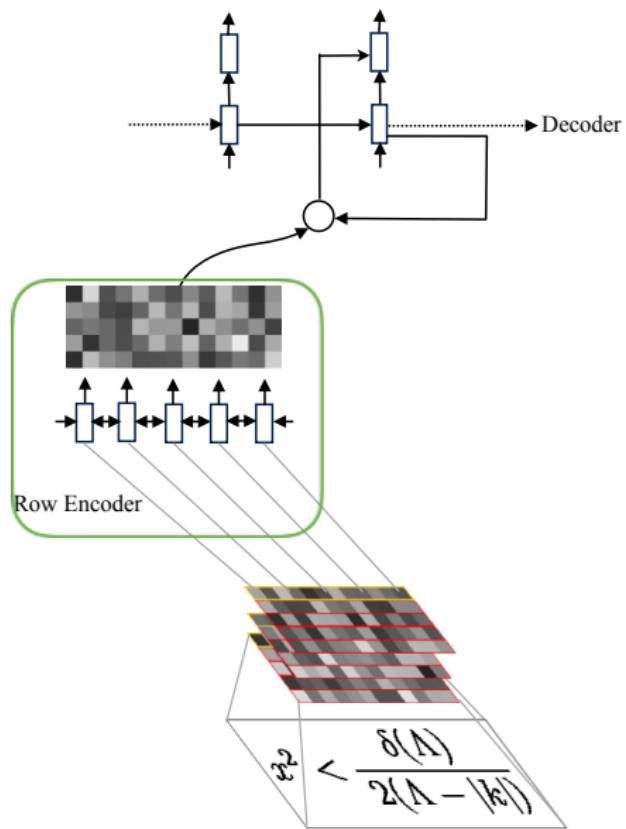
- Encoder: CNN
- Decoder: RNN with attention

Attention-based Image Captioning (Xu et al. 2015)



- Encoder: CNN
- Decoder: RNN with attention
- Objective: maximize log-likelihood

Model Extensions



- Row Encoder: RNN over each row of feature map
- Parameters shared across rows
- Row embeddings to initialize RNN

Attention

```
r = { \frac{\sqrt{Q} - \{ 3 \}}{ } }
```

$$r = \frac{\sqrt{Q_3}}{l} \sin\left(\frac{l}{\sqrt{Q_3}} u\right),$$

Attention

```
r = { \frac{ \sqrt{Q} - \{ 3 \} }{ } }
```

$$r = \frac{\sqrt{Q_3}}{l} \sin\left(\frac{l}{\sqrt{Q_3}} u\right),$$

Attention

$$r = \left\{ \frac{\sqrt{Q_3} - \sqrt{3}}{l} \right\} \sin \left(\frac{l}{\sqrt{Q_3}} u \right),$$

Coarse-to-Fine Attention

$$r = \frac{\sqrt{Q_3}}{l} \sin\left(\frac{l}{\sqrt{Q_3}} u\right),$$

Coarse-to-Fine Attention

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Coarse-to-Fine Attention

```
r = \frac{\sqrt{Q}}{l} \{ \dots \}
```

$$r = \frac{\sqrt{Q_3}}{l} \sin\left(\frac{l}{\sqrt{Q_3}} u\right),$$

Coarse-to-Fine Attention

```
r = \frac{\sqrt{Q}}{\sqrt{3}} \{
```

$$r = \frac{\sqrt{Q_3}}{l} \sin\left(\frac{l}{\sqrt{Q_3}} u\right),$$

Coarse-to-Fine Attention

```
r = \frac{\sqrt{Q}}{\sqrt{3}} \{
```

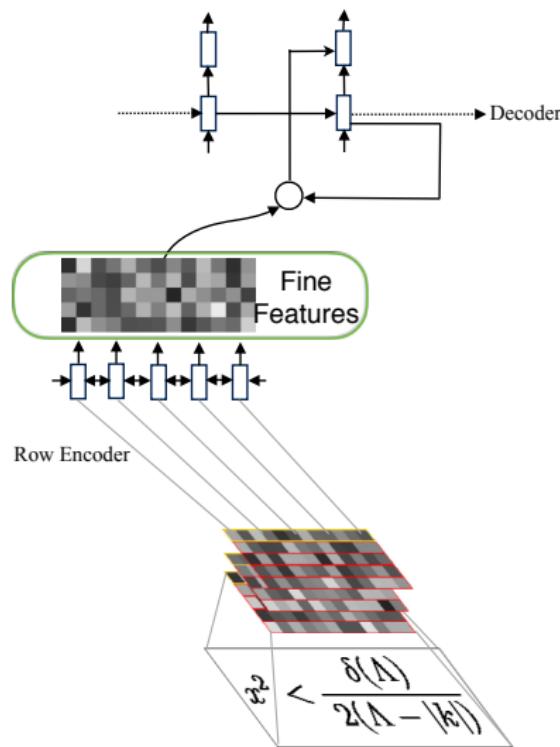
$$r = \frac{\sqrt{Q_3}}{1} \sin \left(\frac{l}{\sqrt{Q_3}} u \right),$$



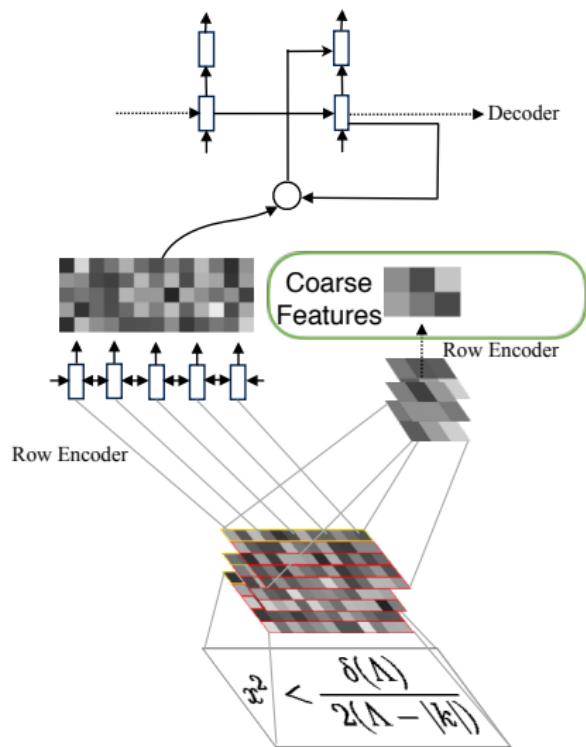
Coarse-to-Fine Attention

$$r = \frac{\sqrt{Q_3}}{l} \sin\left(\frac{l}{\sqrt{Q_3}} u\right),$$

Coarse-to-Fine Attention

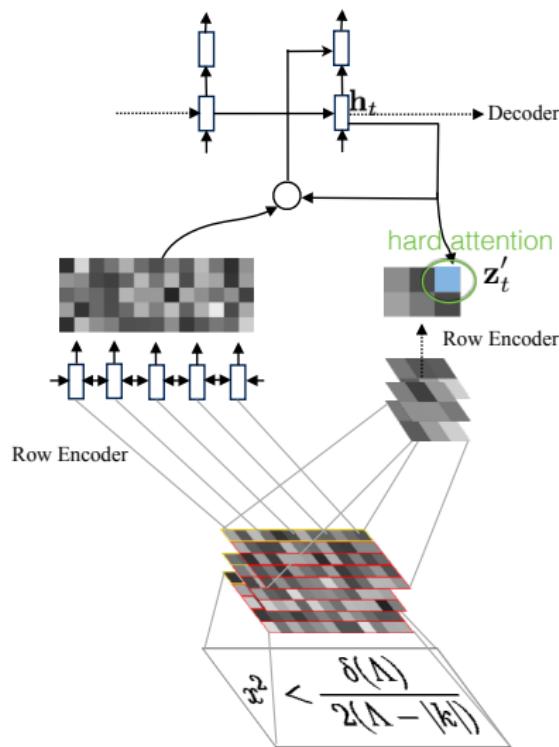


Coarse-to-Fine Attention



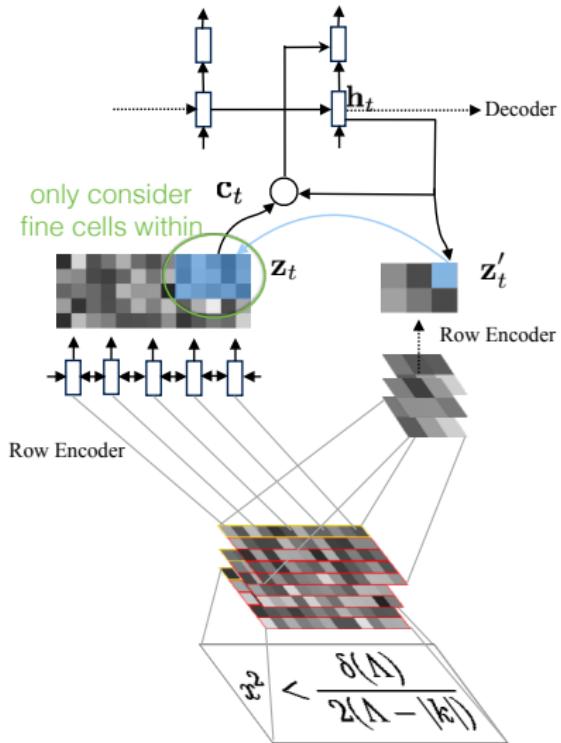
$$z^2 < \frac{\delta(\Lambda)}{2(\Lambda - |k|)}$$

Coarse-to-Fine Attention



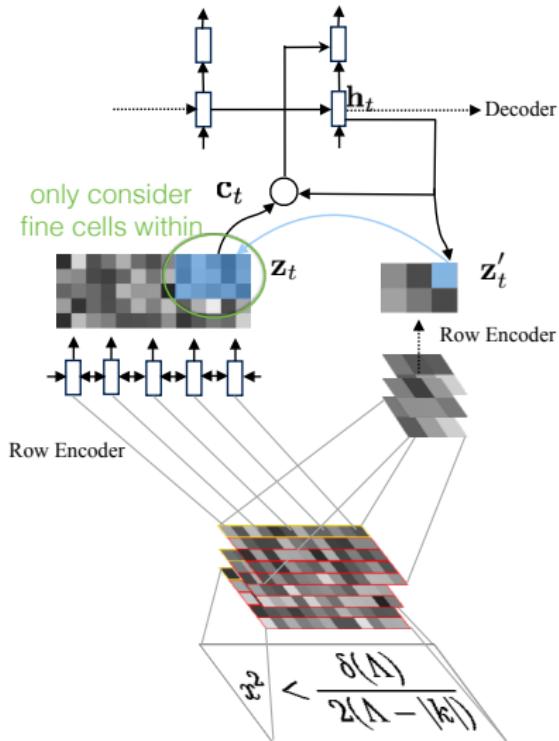
$$z^2 < \frac{\delta(\Lambda)}{2(\Lambda - |k|)}$$

Coarse-to-Fine Attention



$$p(z_t) = \sum_{z'_t} p(z'_t) p(z_t | z'_t)$$

Coarse-to-Fine Attention



$$p(z_t) = \sum_{z'_t} p(z'_t)p(z_t|z'_t)$$

Coarse-to-Fine Variants

- REINFORCE: hard attention [Xu et al., 2015] to select a **single** coarse cell, the presented model
- SPARSEMAX: use sparse activation function Sparsemax [Martins and Astudillo, 2016] instead of Softmax to select **multiple** coarse cells

Experiment Details

- Tokenization & Normalization:

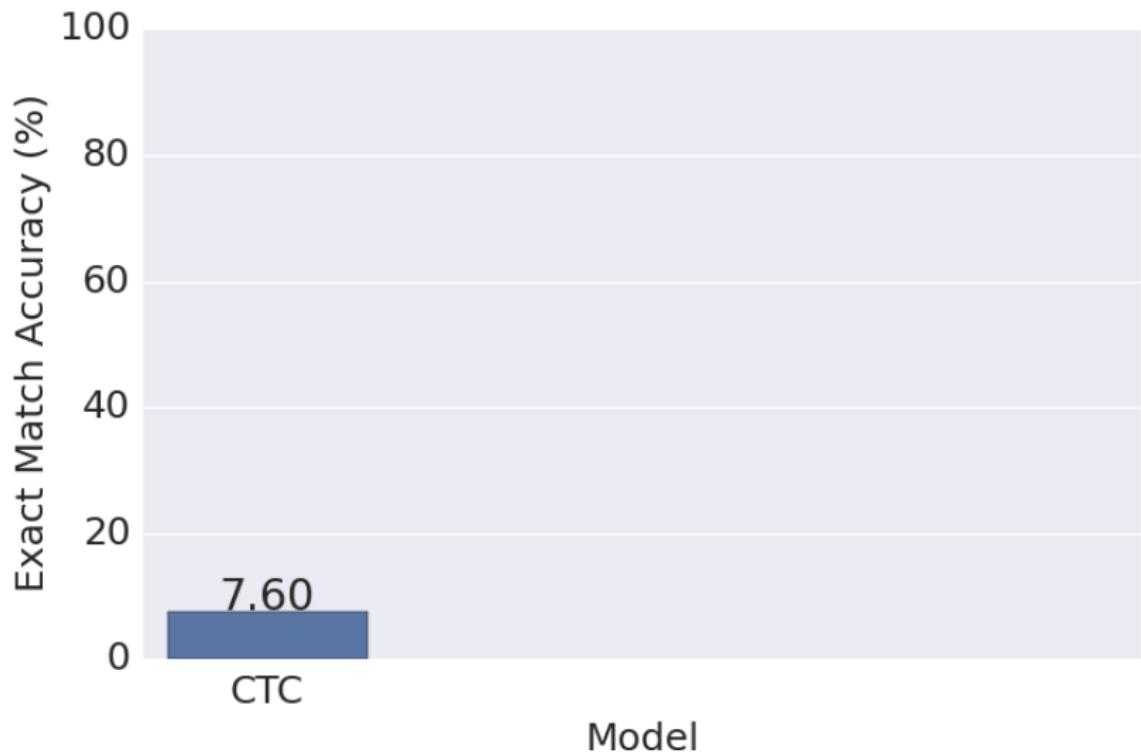
$P_{\{11'\}}^1 - K^2_{\{11\}}$



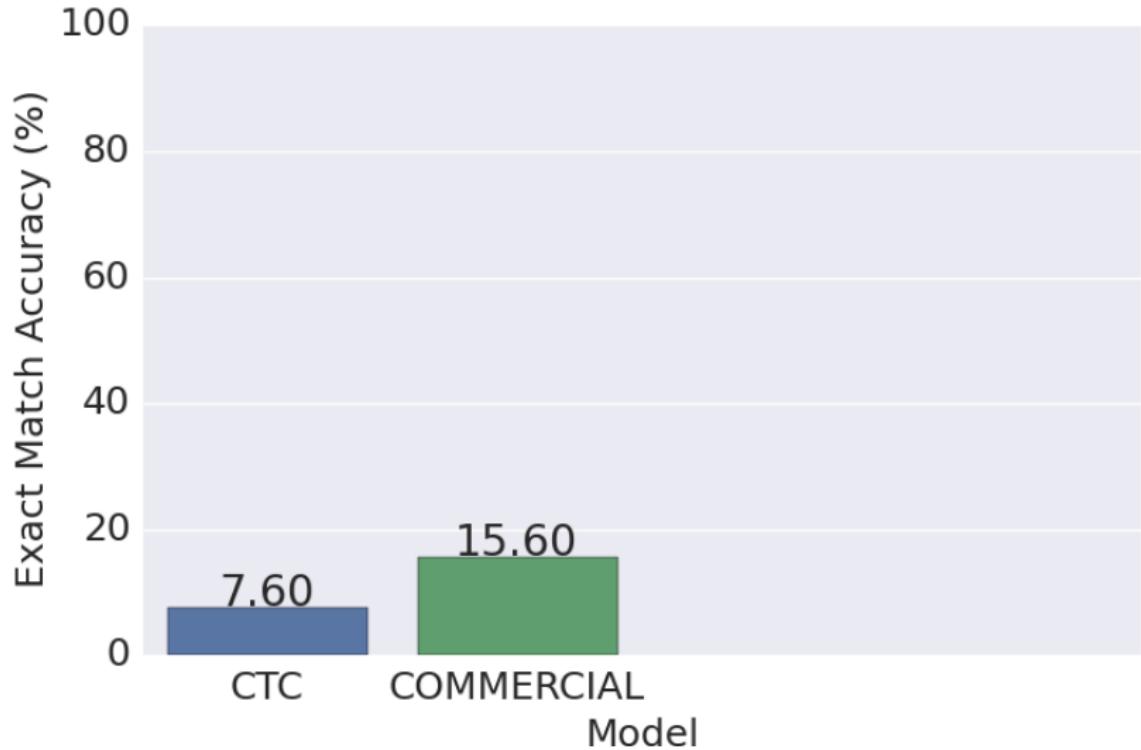
$P_{\{11'\}}^1 - K^2_{\{11\}}$

- Evaluation: exact image match accuracy (rendered prediction versus original image)
- Implementation: Torch [Collobert et al., 2011], based on OpenNMT [Klein et al., 2017]

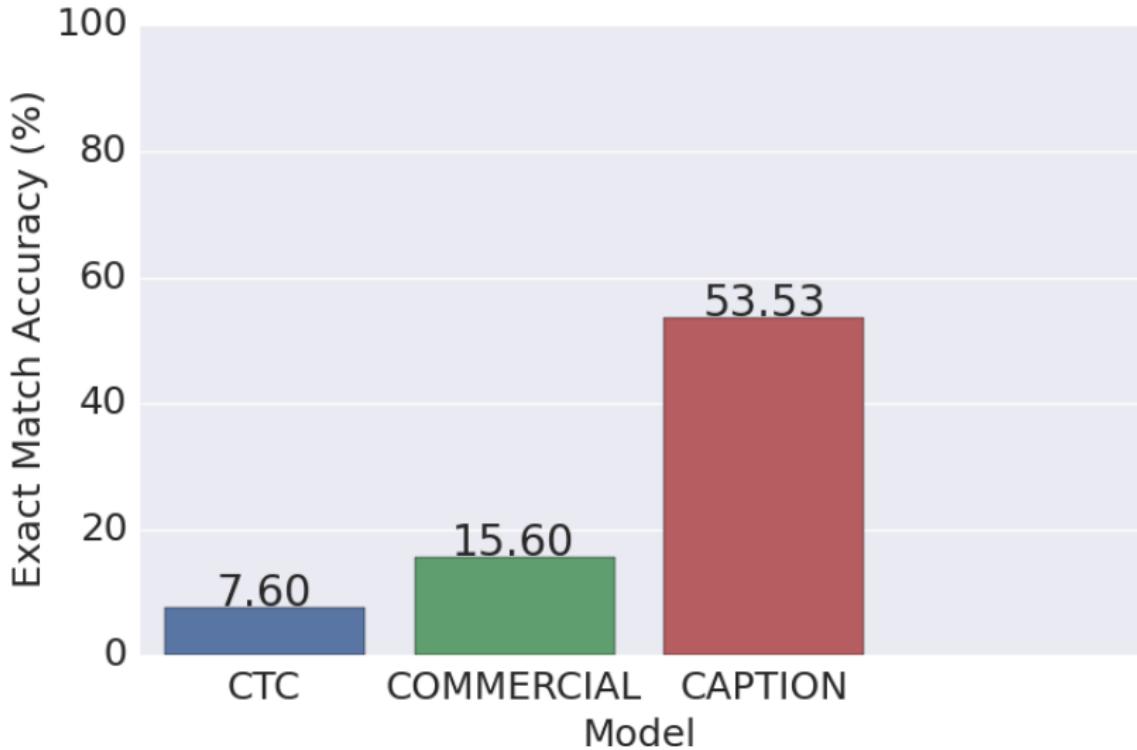
Baseline Results



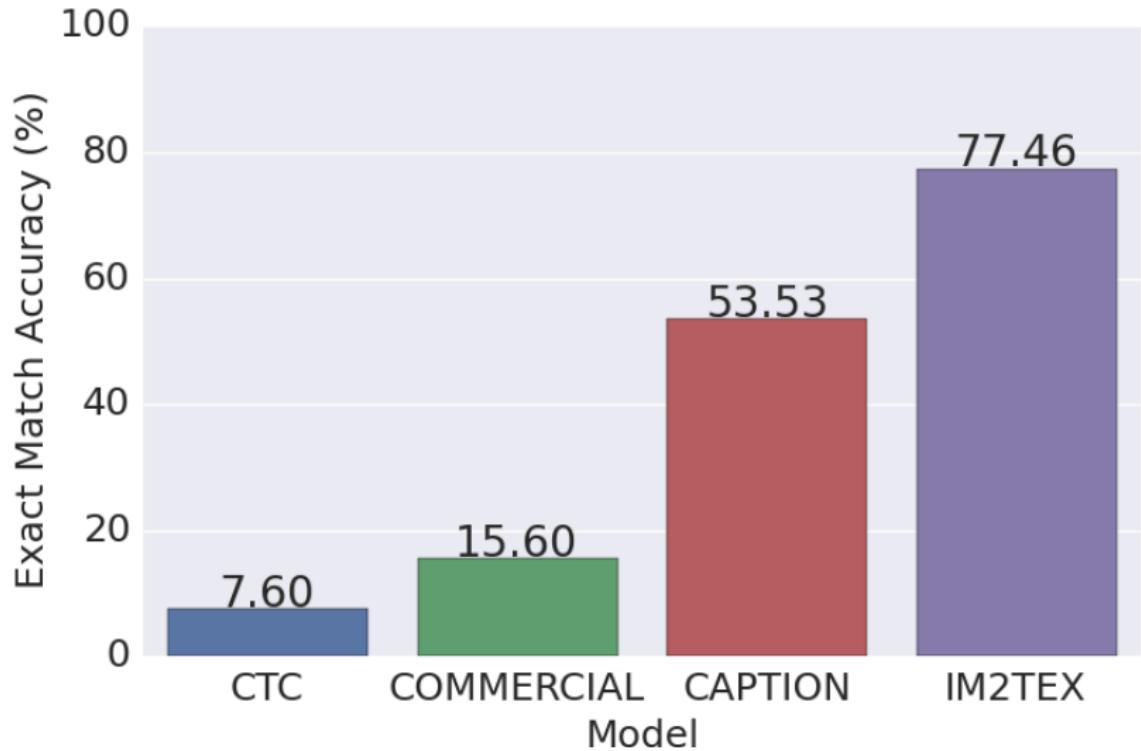
Baseline Results



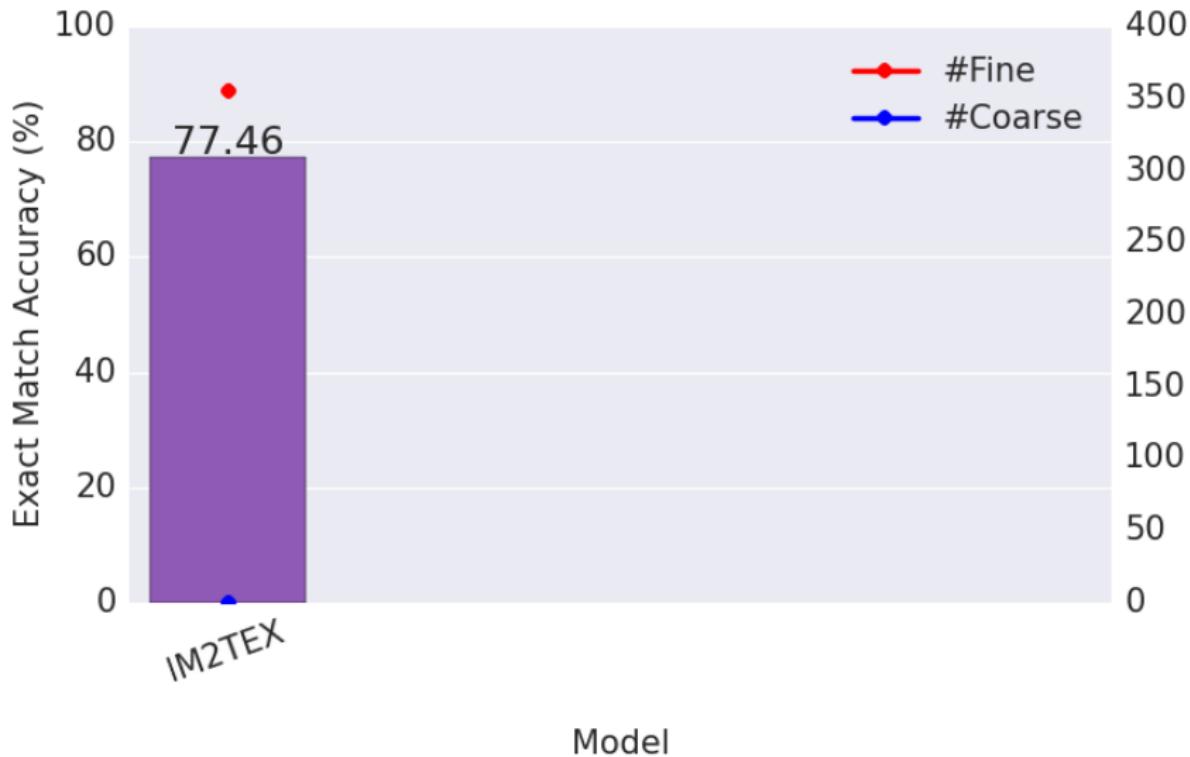
Baseline Results



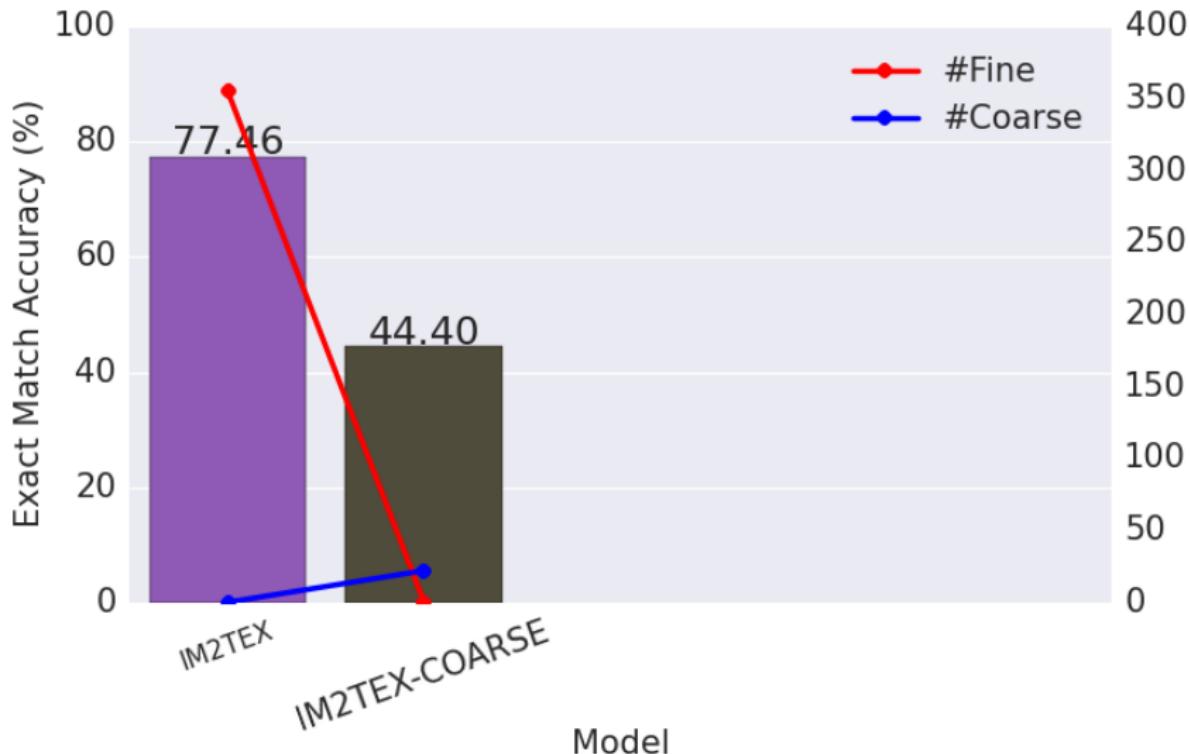
Baseline Results



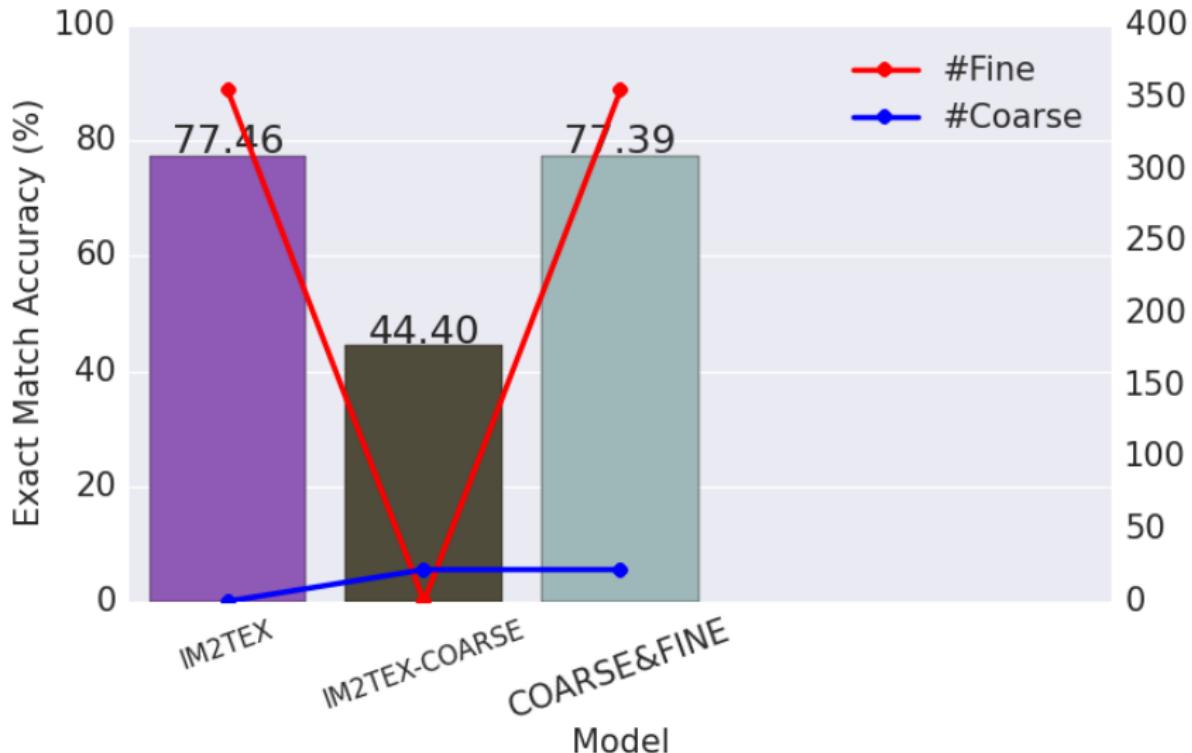
Main Results



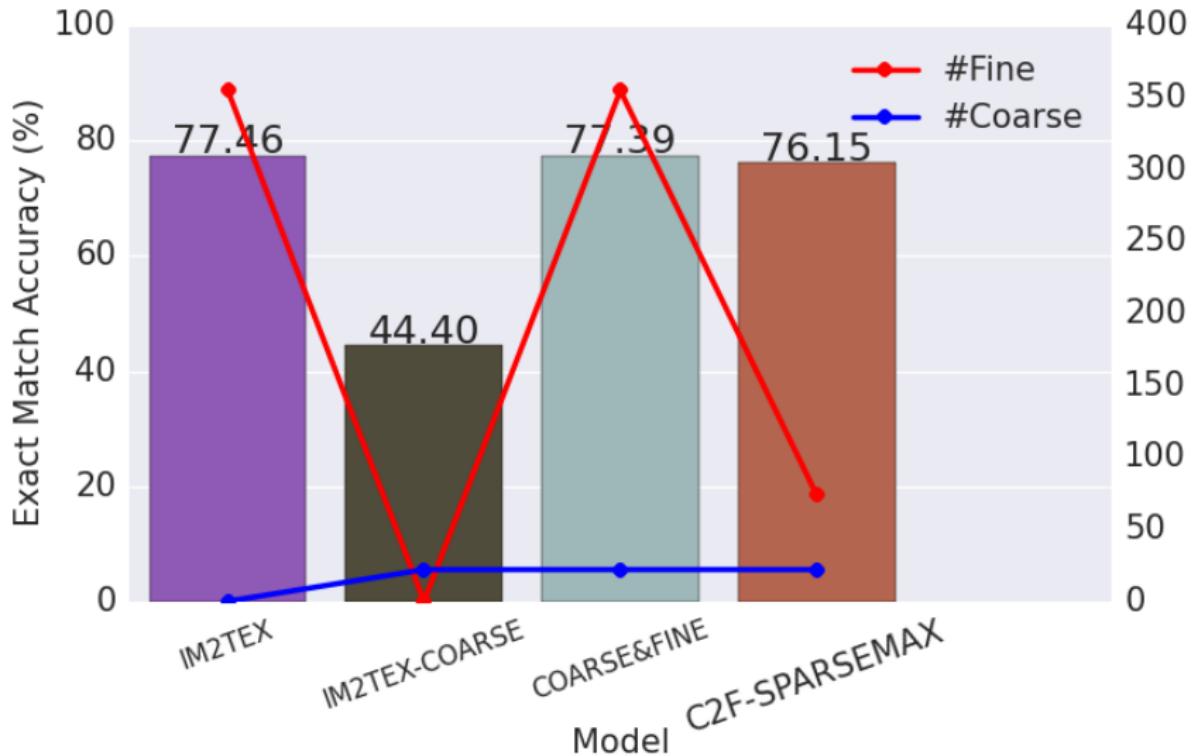
Main Results



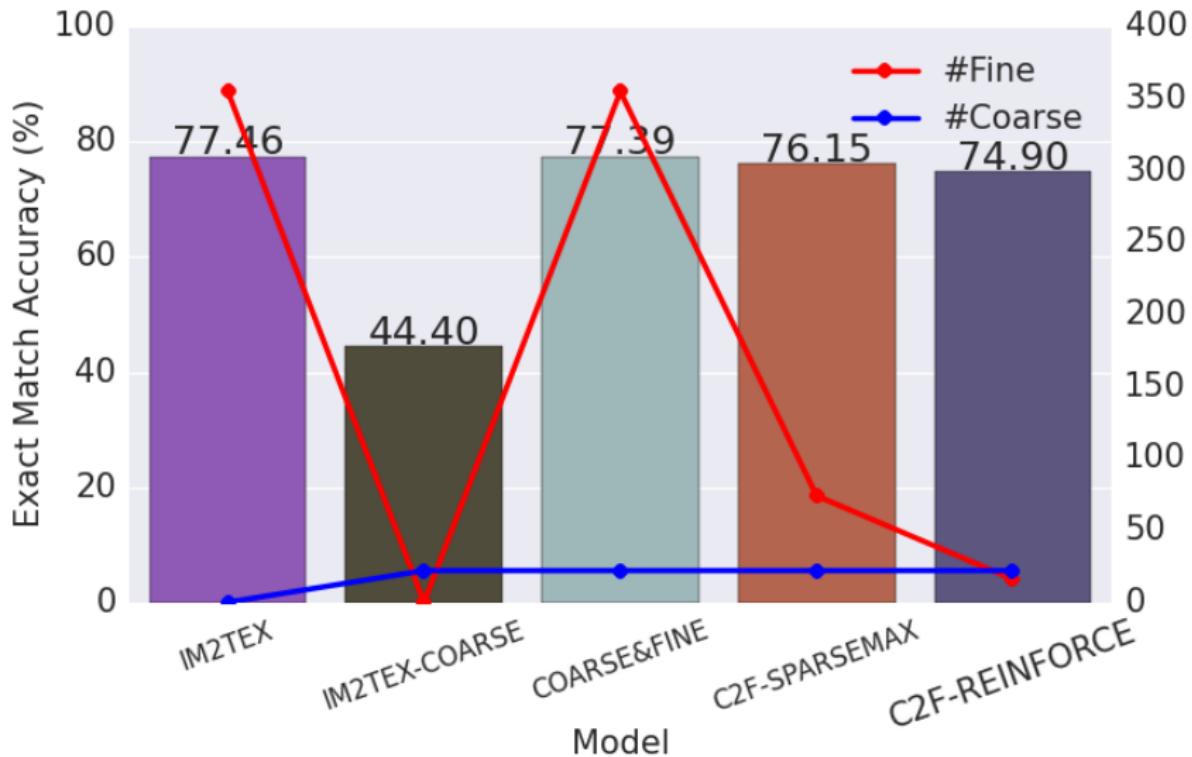
Main Results



Main Results



Main Results



Qualitative Results

$$Z = \sum_{\text{spins}} \prod_{\text{cubes}} W(a|e, f, g|b, c, d|h),$$

$$\{\Psi \circ \mu, f\} = (\overline{X}_i f) (Y^i \Psi) \circ \mu,$$

$$U_n(\theta, \phi) = \begin{pmatrix} \cos(\theta/2) & -e^{-in\phi} \sin(\theta/2) \\ \sin(\theta/2) e^{in\phi} & \cos(\theta/2) \end{pmatrix}$$

$$\sin \frac{\pi \alpha' s}{2} + \sin \frac{\pi \alpha' t}{2} + \sin \frac{\pi \alpha' u}{2} = -\frac{\pi^3}{16} \alpha'^3 stu + o(\alpha'^5),$$

$$Y(T, U) = \int_{\mathcal{F}} \frac{d^2 \tau}{\Im \tau} \Gamma_{2,2}(T, U) \left(-6 \left[\bar{\Omega}_2 - \frac{1}{8\pi \Im \tau} \right] \frac{\bar{\Omega}}{\bar{\eta}^{24}} - \frac{\bar{j}}{8} + 126 \right) ,$$

Handwritten Formulas

- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)

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Handwritten Formulas

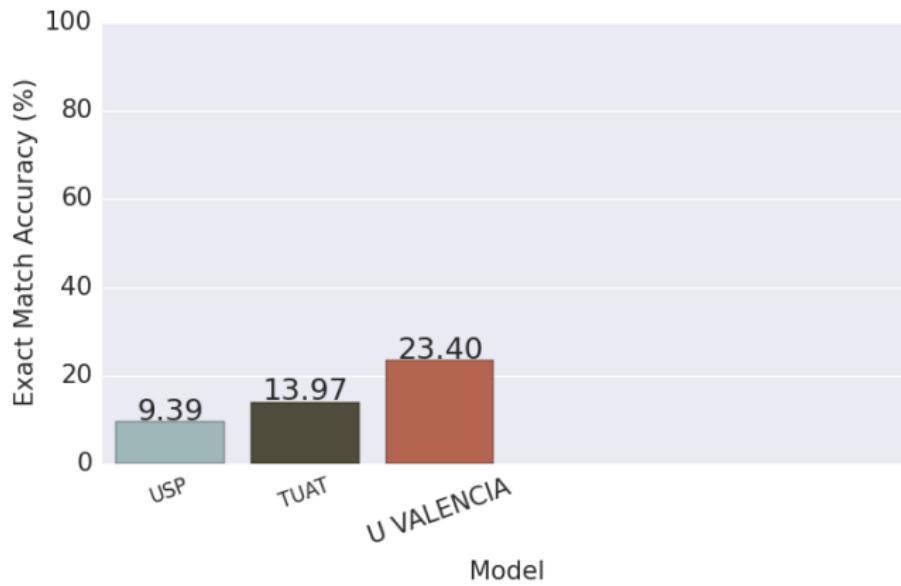
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$A_0^3(\alpha' \rightarrow 0) = 2g_d \epsilon_{\lambda}^{(1)} \epsilon_A^{(2)} \epsilon_{\gamma}^{(3)} \{ \eta^{\lambda\mu} (p_1^\nu - p_2^\nu) + \eta^{\lambda\nu} (p_3^\mu - p_1^\mu) + \eta^{\mu\nu} (p_2^\lambda - p_3^\lambda) \}$ $(A_{-0})^3(\alpha' \rightarrow 0) = 2g_d \{ \eta^{\lambda\mu} (\eta^{\nu\rho} (p_1^\nu - p_2^\nu) + \eta^{\lambda\rho} (p_3^\mu - p_1^\mu) + \eta^{\mu\rho} (p_2^\lambda - p_3^\lambda)) - \eta^{\lambda\mu} \eta^{\nu\rho} (p_1^\nu - p_2^\nu) - \eta^{\lambda\rho} \eta^{\mu\nu} (p_3^\mu - p_1^\mu) - \eta^{\mu\rho} \eta^{\nu\lambda} (p_2^\lambda - p_3^\lambda) \}$	$\begin{cases} \epsilon_B \sim \epsilon F, \\ \epsilon_F \sim \partial \epsilon + \epsilon B, \end{cases}$ $\left(\begin{array}{c cc} \delta & \delta \epsilon & \epsilon \delta \\ \hline \epsilon & \epsilon \delta & \delta \epsilon \end{array} \right)$
$\int_{L_{d-1}}^L f(H) d\nu_{d-1}(H) = c_3 \int_{\Lambda}^A \int_{X_{d-1}^L} f(H, A)^2 d\nu_{d-1}^L(H) d\nu_2^A(L)$ $\lim_{d \rightarrow \infty} \lim_{n \rightarrow \infty} \int_{\Lambda}^A \int_{X_{d-1}^L} f(H, A)^2 d\nu_{d-1}^L(H) d\nu_2^A(L) = c_3 \int_{\Lambda}^A \int_{X_{d-1}^L} f(H, A)^2 d\nu_{d-1}^L(H) d\nu_2^A(L)$	$J = \begin{pmatrix} \alpha & f_2 \\ f_1 & \tilde{A} \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \alpha & f_1 \\ f_2 & A \end{pmatrix} = \begin{pmatrix} f_2 L f_2 & f_2 L A \\ \tilde{A} L f_2 & \tilde{A} L A \end{pmatrix}$ $J = \begin{pmatrix} \alpha & f_2 \\ f_1 & \tilde{A} \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \alpha & f_1 \\ f_2 & A \end{pmatrix} = \begin{pmatrix} f_2 L f_2 & f_2 L A \\ \tilde{A} L f_2 & \tilde{A} L A \end{pmatrix}$
$\lambda_{n,1}^{(2)} = \frac{\partial \bar{H}_0}{\partial q_{n,0}}, \quad \lambda_{n,j_n}^{(2)} = \frac{\partial \bar{H}_0}{\partial q_{n,j_n-1}} - \mu_{n,j_n-1}, \quad j_n = 2, 3, \dots, m_n - 1.$ $\lambda_{n,1}^{(2)} = \frac{\partial \bar{H}_0}{\partial q_{n,0}}, \quad \lambda_{n,j_n}^{(2)} = \frac{\partial \bar{H}_0}{\partial q_{n,j_n-1}} - \mu_{n,j_n-1}, \quad j_n = 2, 3, \dots, m_n - 1.$	$(P_{ij} - K_{ij}) \phi'(z_q) x \geq c$ $(P_{ij} - K_{ij}) \phi'(z_q) x \geq c$ $(P_{ij} - K_{ij}) \phi'(z_q) x \geq c$

Handwritten Formulas

- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)

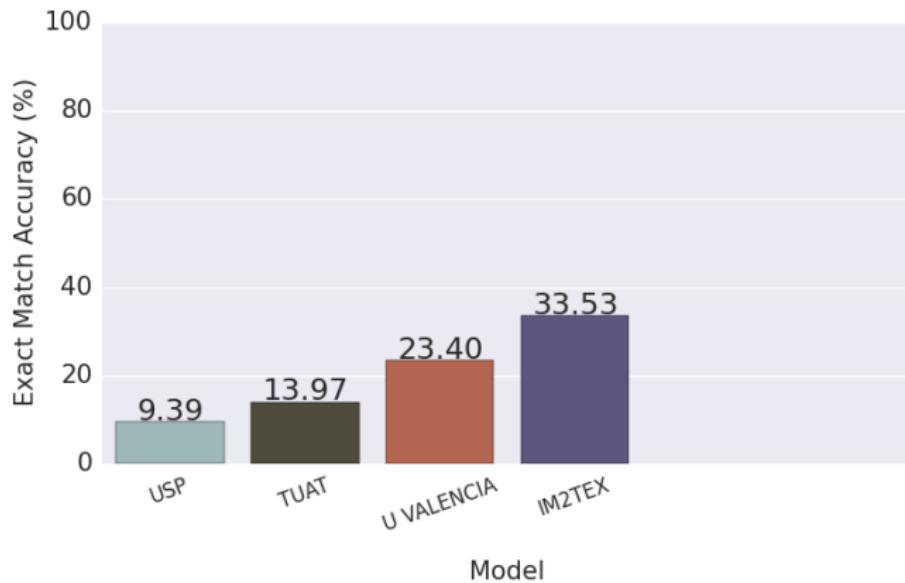
CROHME 13



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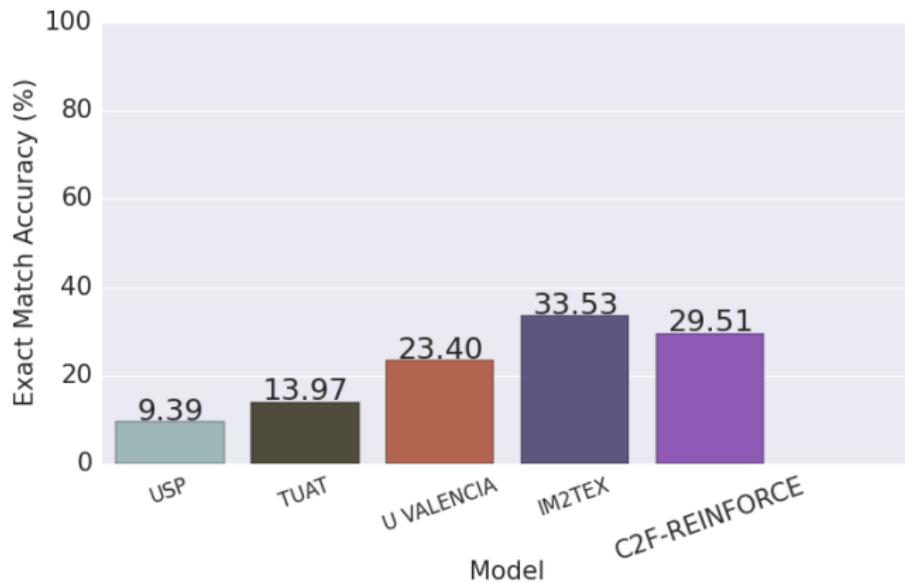
CROHME 13



Handwritten Formulas

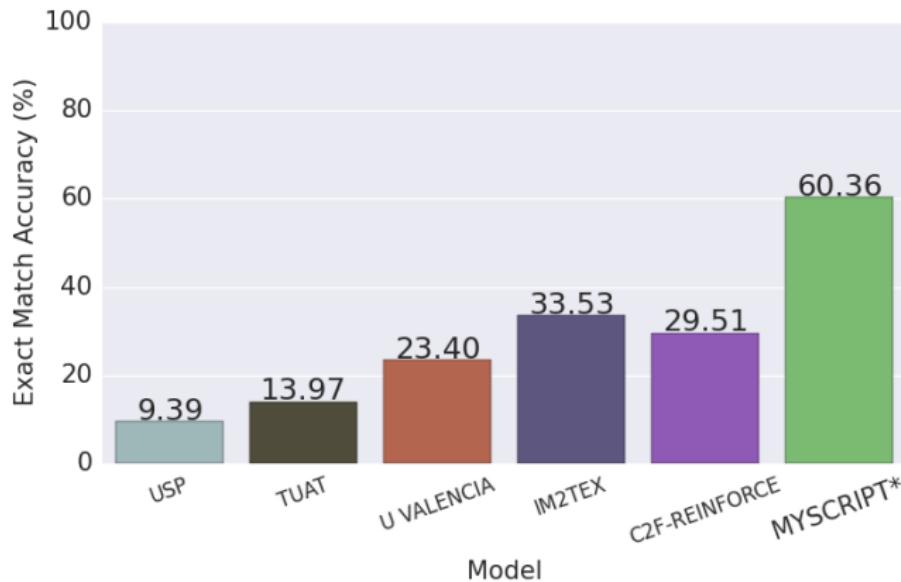
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CROHME 13



Handwritten Formulas

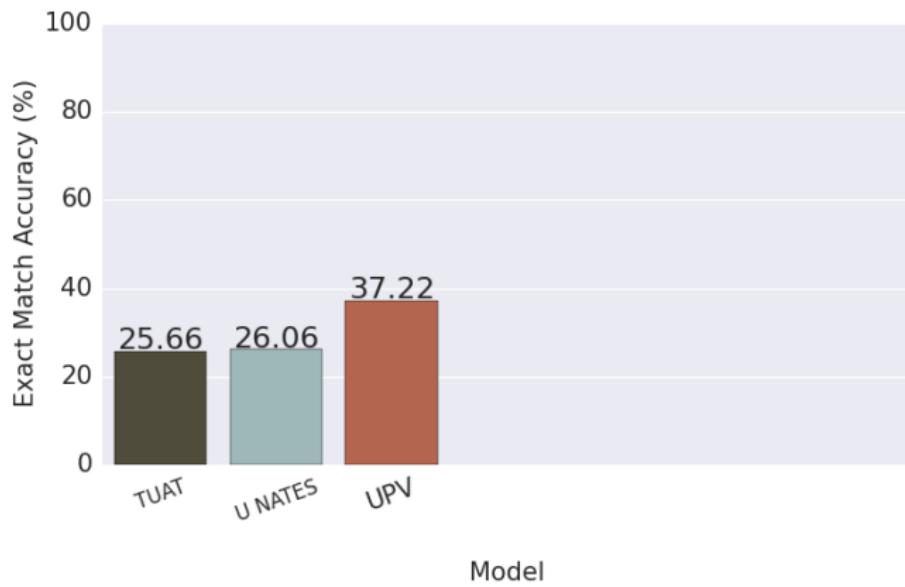
- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)
CROHME 13 (*uses private in-domain handwritten training data)



Handwritten Formulas

- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)

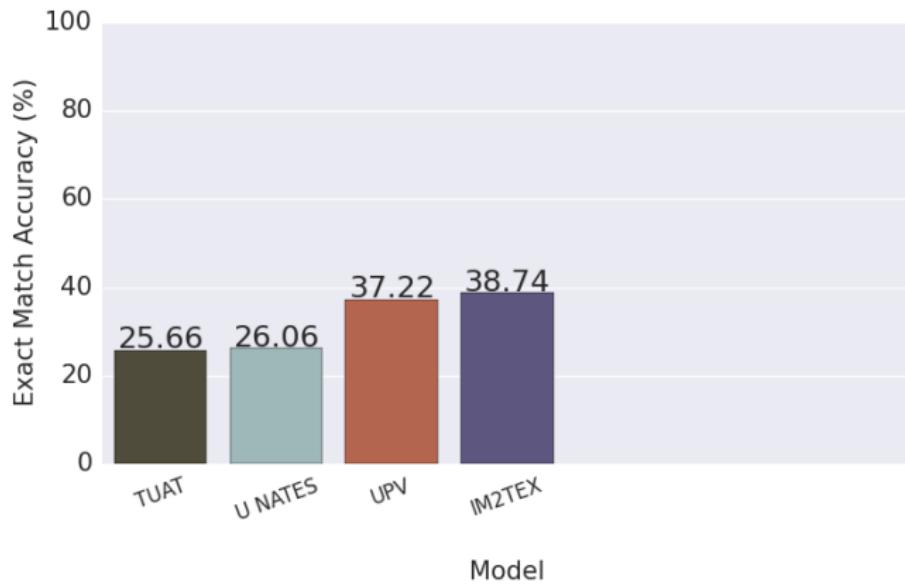
CROHME 14



Handwritten Formulas

- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)

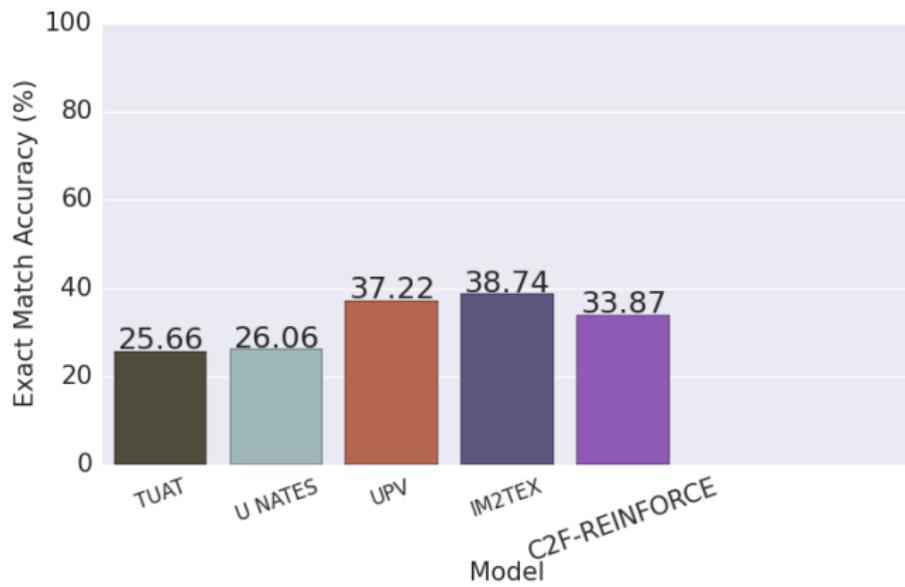
CROHME 14



Handwritten Formulas

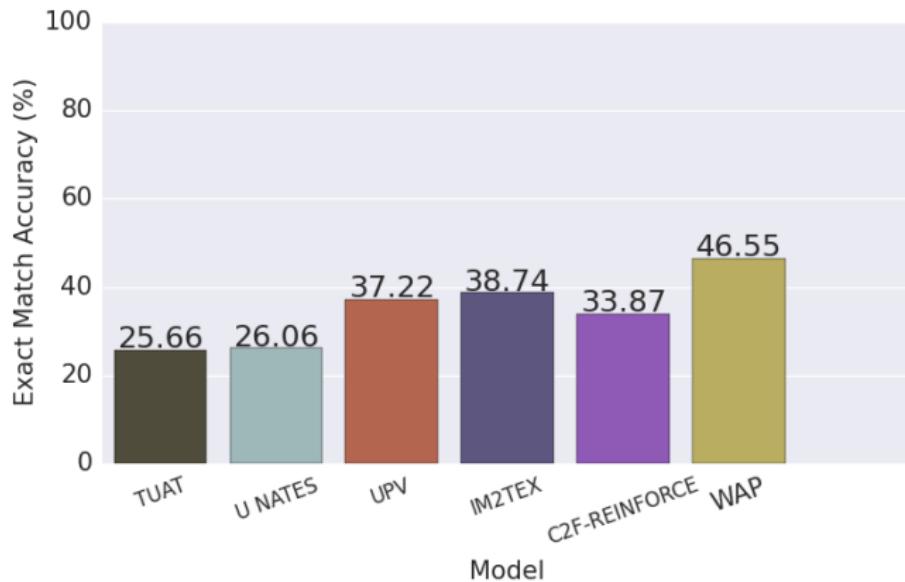
- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)

CROHME 14



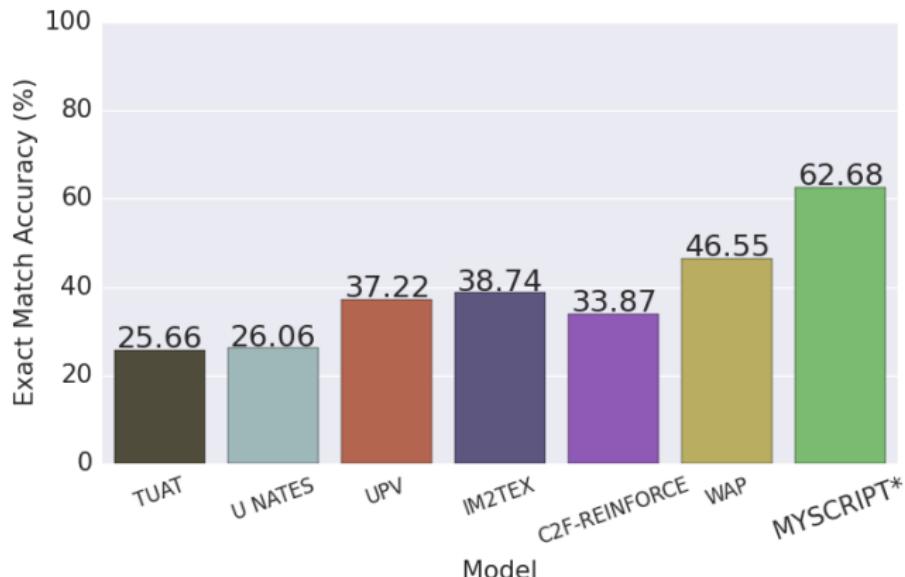
Handwritten Formulas

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- Finetune and evaluate on CROHME 13 and 14 (8K training set)
CROHME 14 (WAP: Zhang et al. [2017])



Handwritten Formulas

- Synthetic handwritten formulas by using handwritten characters [Kirsch, 2010] as font, used for pretraining
- Finetune and evaluate on CROHME 13 and 14 (8K training set)
CROHME 14 (*uses private in-domain handwritten training data)



Conclusions & Future Work

- The constructed dataset IM2LATEX-100K is rich structured and challenging
- A case study of multi-modal document recognition/generation
- Coarse-to-fine attention can be applied to other tasks

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Q & A

- More visualizations:

<http://lstm.seas.harvard.edu/latex/>

- Source code (part of OpenNMT):

<http://opennmt.net/OpenNMT/applications/>