§10.2 Contraved Monotonic Seguences Definitions: A sequence & an 3 = a, az, az, ... is 1) Increasing if an+1 > an 2) Decreasing if antican (3) Non decreasing if an i ≥ an ... 4 Monincreusing if anti \ an \ \ (5) Monotonic if its non increasing or non decreasing (i.e. $a_{n+1} \geq a_n$ or $a_{n+1} \leq a_n$ for all n.) Examples increasing increasing in monotonic monotonic { 1 } a decreasing nonincreasing monotonic Testing a sequence { an } = {f(n)} for monotinicity nonincreasing non decreasing anti = an $a_{n+1} \leq a_n$ anti-an <0 anti-an ≥0 only $\frac{a_{n+1}}{a_n} \geq 0$ if an > 0 $\frac{a_{n+1}}{a_n} \leq 0$

f(n) <0

f(m) > 0

Ex
$$\left\{1-\frac{1}{n}\right\}_{n=1}^{\infty}$$

A $a_{n+1}-a_n=\left(1-\frac{1}{n+1}\right)-\left(1-\frac{1}{n}\right)=\frac{11}{n-1}>0$ Increasing

B) $f(n)=\frac{1}{n^2}>0$ Increasing

Definitions A sequence $\left\{a_n\right\}_{n=1}^{\infty}$

Theorem M sequence $\left\{a_n\right\}_{n=1}^{\infty}$

Theorem M sequence $\left\{a_n\right\}_{n=1}^{\infty}$

Theorem M sequence $\left\{a_n\right\}_{n=1}^{\infty}$

Theorem M sequence decreases and is bounded below by $\left\{a_n\right\}_{n=1}^{\infty}$

Thus the sequence decreases and is bounded above by $\left\{a_n\right\}_{n=1}^{\infty}$

Thus the sequence decreases and is bounded above by $\left\{a_n\right\}_{n=1}^{\infty}$

Theorem by $\left\{a_n\right\}_{n=1}^{\infty}$

So the seguence converges!