.1. Find the global extrema of the function $f(x) = \frac{x}{2} + \cos(x)$ on the closed interval $\left[0, \frac{\pi}{2}\right]$.

$$f'(x) = \frac{1}{2} - \sin(x) = 0$$

$$\sin(x) = \frac{1}{2}$$

$$f(o) = \frac{0}{2} + \cos(o) = 1$$

$$f\left(\frac{T}{6}\right) = \frac{T1/6}{2} + \cos\left(\frac{T}{6}\right) = \frac{T}{12} + \frac{\sqrt{3}}{2} = \frac{T1 + 6\sqrt{3}}{12} \approx \frac{3.1 + 6.1.7}{12} = \frac{13.3}{2} > 1$$

$$f\left(\frac{T}{2}\right) = \frac{T1/2}{2} + \cos\left(\frac{T}{2}\right) = \frac{T}{4} \approx \frac{3.14}{4} \approx 0.78$$

finds a global max of
$$f(\frac{\pi}{6}) = \frac{\pi + 6\sqrt{3}}{12}$$
 at $X = \frac{\pi}{6}$

f has a global min of
$$f(\overline{z}) = \overline{x}$$
 at $x = \overline{z}$

2. Find the global extrema of the function $f(x) = 8\sqrt{x} - x$ on the open interval (0, 25).

$$f(x) = 8x^{1/2} - x$$

$$f(x) = 8, \frac{1}{2}x^{-\frac{1}{2}} = \frac{4}{\sqrt{x}} - 1 = 0$$

$$\frac{4}{1}$$
 = 1

$$\frac{1}{4} = \sqrt{x}$$

$$\frac{4}{1} = \sqrt{x}$$
 $\frac{4}{1} = \sqrt{x}$
 $\frac{4}$

$$f'(x) = -2x^{-\frac{3}{2}} = \frac{-2}{\sqrt{x^3}}$$

$$f''(16) = -\frac{2}{\sqrt{16}3} = -\frac{2}{43} < 0 \leftarrow \text{So local max at } x = 16$$

If has a global max of
$$f(16)=16$$
 at $X=16$
No a lobal min.

1. Find the global extrema of the function $f(x) = \sin(x) - \frac{x}{2}$ on the closed interval $\left[0, \frac{\pi}{2}\right]$.

$$f(x) = \cos(x) - \frac{1}{z} = 0$$

$$Cos(x) = \frac{1}{2}$$

$$f(0) = \sin(0) - \frac{0}{2} = 0 - 0 = 0$$

$$f(\frac{\pi}{3}) = \sin(\frac{\pi}{3}) - \frac{\pi}{3} = \frac{\sqrt{3}}{2} - \frac{\pi}{6} = \frac{3\sqrt{3} - \pi}{6} = \frac{3\sqrt{13} - \pi}{6} = \frac{3\sqrt{13} - \pi}{6} = \frac{3\sqrt{13} - \pi}{6} = \frac{3}{3} = 0.3$$

$$f(\frac{\pi}{2}) = \sin(\frac{\pi}{2}) - \frac{\pi/2}{3} = 1 - \frac{\pi}{4} = \frac{4-\pi}{4} \approx \frac{4-3.1}{4} = \frac{0.9}{4} \approx 0.22$$

f has a global min of
$$f(0) = 0$$
 at $x = 0$

f has a global max of $f(\frac{17}{3}) = \frac{3\sqrt{3}-17}{3}$ at $x = \frac{17}{3}$

2. Find the global extrema of the function $f(x) = x - 2\sqrt{x}$ on the open interval (0,9).

$$f(x) = x - 2x^{1/2}$$

$$f(x) = 1 - 2 \cdot \frac{1}{2} \times \frac{1}{2} = 1 - \frac{1}{\sqrt{x}} = 0$$

$$I = \frac{1}{\sqrt{x}}$$

$$\sqrt{x} = 1$$

$$\sqrt{x} = 1$$

critical point

$$f'(x) = \frac{1}{2} \times \frac{-3}{2} = \frac{1}{2\sqrt{x^3}}$$

$$f''(x) = \frac{1}{2\sqrt{1}} = \frac{1}{2} > 0$$
, so local min. at $x=1$