1. Use a limit definition of the derivative to find the derivative of the function $f(x) = \frac{1}{x+1}$.

$$f(x) = \lim_{Z \to x} \frac{f(z) - f(x)}{z - x} = \lim_{Z \to x} \frac{1}{z - x}$$

$$=\lim_{z\to 2}\frac{1}{z+1}\frac{1}{x+1},\frac{(z+1)(x+1)}{(z+1)(x+1)}$$

$$=\lim_{Z\to\infty}\frac{(\chi+1)-(Z+1)}{(Z-\chi)(Z+1)(\chi+1)}=\lim_{Z\to\infty}\frac{-(Z-\chi)}{(Z-\chi)(Z+1)(\chi+1)}$$

$$= \lim_{Z \to \chi} \frac{-1}{(Z+1)(\chi+1)} = \frac{-1}{(\chi+1)(\chi+1)} = \frac{-1}{(\chi+1)^2}$$

Therefore:
$$f(x) = \frac{-1}{(x+1)^2}$$

Alternatively: $f(x+h) - f(x) = \lim_{h \to 0} \frac{x+h+1}{h} = \frac{x+1}{h}$

$$= \lim_{h \to 0} \frac{\frac{1}{x+h+1} - \frac{1}{x+1}}{h} \cdot \frac{(x+h+1)(x+1)}{(x+h+1)(x+1)}$$

$$=\lim_{h\to 0}\frac{(x+1)-(x+h+1)}{h(x+h+1)(x+h)}=\lim_{h\to 0}\frac{-h}{h(x+h+1)(x+h)}$$

$$= \lim_{h \to 0} \frac{-1}{(x+h+1)(x+h)} = \frac{-1}{(x+o+1)(x+1)} = \frac{-1}{(x+1)^2}$$

Therefore: $f(x) = \frac{-1}{(x+1)^2}$

1. Use a limit definition of the derivative to find the derivative of the function $f(x) = \sqrt{x+1}$.

$$f(x) = \lim_{Z \to x} \frac{f(z) - f(x)}{Z - x} = \lim_{Z \to x} \frac{\sqrt{Z+1} - \sqrt{x+1}}{Z - x}$$

$$= \lim_{Z \to x} \frac{\sqrt{Z+1} - \sqrt{x+1}}{Z - x} \cdot \frac{\sqrt{Z+1} + \sqrt{x+1}}{\sqrt{Z+1} + \sqrt{x+1}}$$

$$= \lim_{Z \to x} \frac{\sqrt{Z+1} + \sqrt{x+1} - \sqrt{x+1}\sqrt{Z+1} - \sqrt{x+1}}{(Z-x)(\sqrt{Z+1} + \sqrt{x+1})}$$

$$= \lim_{Z \to x} \frac{Z+1 - (x+1)}{(Z-x)(\sqrt{Z+1} + \sqrt{x+1})} = \lim_{Z \to x} \frac{(Z-x)(Z+1+\sqrt{x+1})}{(Z-x)(Z+1+\sqrt{x+1})}$$

$$= \lim_{Z \to x} \frac{1}{(Z-x)(Z+1+\sqrt{x+1})} = \frac{1}{(Z-x)(Z+1+\sqrt{x+1})}$$

Therefore: $f'(x) = \frac{1}{2\sqrt{x+1}}$

Alternatively: $f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} \frac{\sqrt{x+h+1} - \sqrt{x+1}}{h}$ $= \lim_{h \to 0} \frac{\sqrt{x+h+1} - \sqrt{x+1}}{h} \cdot \frac{\sqrt{x+h+1} + \sqrt{x+1}}{\sqrt{x+h+1} + \sqrt{x+1}}$

$$=\lim_{h\to 0}\frac{(x+h+1)-(x+1)}{h(\sqrt{x+h+1}+\sqrt{x+1})}=\lim_{h\to 0}\frac{h}{h(\sqrt{x+h+1}+\sqrt{x+1})}$$

$$=\lim_{h\to 0}\frac{1}{\sqrt{x+h+1}+\sqrt{x+1}}=\overline{(x+o+1+\sqrt{x+1})}=\overline{(x+o+1+\sqrt{x+1})}$$