

Find the derivatives of the given functions.

1. $f(x) = 2x^{10} + 4x^5 + 20x + \sqrt{2}$

$$f'(x) = \boxed{20x^9 + 20x^4 + 20}$$

2. $g(x) = \frac{1}{2x^3} + 2 = \frac{1}{2}x^{-3} + 2$

$$g'(x) = -\frac{3}{2}x^{-3-1} + 0 = -\frac{3}{2}x^{-4} = \boxed{\frac{-3}{2x^4}}$$

3. $y = \frac{1}{x} = x^{-1}$

$$y' = -x^{-1-1} = \boxed{\frac{-1}{x^2}}$$

4. $g(x) = \sqrt[5]{x^2} = x^{\frac{2}{5}}$

$$g'(x) = \frac{2}{5}x^{\frac{2}{5}-1} = \frac{2}{5}x^{-\frac{3}{5}} = \frac{2}{5x^{3/5}} = \boxed{\frac{2}{5\sqrt[5]{x^3}}}$$

5. $h(x) = \frac{1}{\sqrt{x}} = x^{-1/2}$

$$h'(x) = -\frac{1}{2}x^{-\frac{1}{2}-1} = -\frac{1}{2}x^{-\frac{3}{2}} = \boxed{\frac{-1}{2\sqrt{x}^3}}$$

Find the derivatives of the given functions.

$$1. \quad f(x) = \frac{x^4}{4} - \pi x^3 - x + 6 = \frac{1}{4} x^4 - \pi x^3 - x + 6$$

$$f'(x) = \frac{4}{4} x^3 - 3\pi x^2 - 1 = \boxed{x^3 - 3\pi x^2 - 1}$$

$$2. \quad y = \frac{5x^3}{3} = \frac{5}{3} x^3$$

$$y' = \frac{15}{3} x^2 = \boxed{5x^2}$$

$$3. \quad f(x) = \frac{10}{x} + \frac{x}{10} = 10x^{-1} + \frac{1}{10} x$$

$$f'(x) = 10(-1)x^{-1-1} + \frac{1}{10} = \boxed{\frac{1}{10} - \frac{10}{x^2}}$$

$$4. \quad g(x) = \frac{1}{\sqrt[3]{x^2}} = x^{-\frac{2}{3}}$$

$$g'(x) = -\frac{2}{3} x^{-\frac{2}{3}-1} = -\frac{2}{3} x^{-\frac{5}{3}} = \frac{-2}{3 x^{5/3}} = \boxed{\frac{-2}{3 \sqrt[3]{x^5}}}$$

$$5. \quad h(x) = \sqrt{2x} = \sqrt{2} \sqrt{x} = \sqrt{2} x^{\frac{1}{2}}$$

$$h'(x) = \sqrt{2} \frac{1}{2} x^{-\frac{1}{2}} = \boxed{\frac{\sqrt{2}}{2 \sqrt{x}}}$$