

$$1. \lim_{x \rightarrow 1} \frac{x^2 - 2x + 1}{x^2 + x - 2} = \lim_{x \rightarrow 1} \frac{(x-1)(x-1)}{(x-1)(x+2)} = \lim_{x \rightarrow 1} \frac{x-1}{x+2} = \frac{1-1}{1+2} = \frac{0}{3} = \boxed{0}$$

getting $\frac{0}{0}$

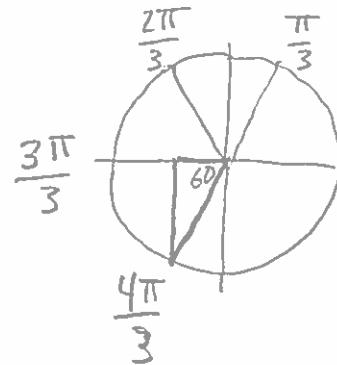
$$2. \lim_{x \rightarrow 4} \frac{\frac{1}{x} - \frac{1}{4}}{x-4} = \lim_{x \rightarrow 4} \frac{\frac{1}{x} - \frac{1}{4}}{x-4} \cdot \frac{4x}{4x} = \lim_{x \rightarrow 4} \frac{4-x}{(x-4)4x}$$

getting $\frac{0}{0}$

$$= \lim_{x \rightarrow 4} \frac{-(x/4)}{(x-4)4x}$$

$$= \lim_{x \rightarrow 4} \frac{-\frac{1}{4}}{4x} = -\frac{1}{4 \cdot 4} = -\frac{1}{16} = \boxed{-\frac{1}{16}}$$

$$3. \lim_{x \rightarrow 4\pi/3} \sin(x) = \sin\left(\frac{4\pi}{3}\right) = \boxed{-\frac{\sqrt{3}}{2}}$$



$$4. \lim_{x \rightarrow \pi} \frac{\cos^2(x) - 1}{\cos(x) + 1} = \lim_{x \rightarrow \pi} \frac{(\cos(x) + 1)(\cos(x) - 1)}{\cos(x) + 1} = \lim_{x \rightarrow \pi} (\cos(x) - 1)$$

getting $\frac{0}{0}$

$$= \cos(\pi) - 1$$

$$= -1 - 1$$

$$= \boxed{-2}$$

$$1. \lim_{x \rightarrow -5} \frac{x+5}{x^2 + 3x - 10} = \lim_{x \rightarrow -5} \frac{x+5}{(x+5)(x-2)} = \lim_{x \rightarrow -5} \frac{1}{x-2} = \frac{1}{-5-2}$$

↑ getting $\frac{0}{0}$

$$= \boxed{\frac{-1}{7}}$$

$$2. \lim_{h \rightarrow 0} \frac{\sqrt{5+h} - \sqrt{5}}{h} = \lim_{h \rightarrow 0} \frac{\sqrt{5+h} - \sqrt{5}}{h} \cdot \frac{\sqrt{5+h} + \sqrt{5}}{\sqrt{5+h} + \sqrt{5}}$$

↑ getting $\frac{0}{0}$

$$= \lim_{h \rightarrow 0} \frac{\sqrt{5+h}^2 - \sqrt{5}^2}{h(\sqrt{5+h} + \sqrt{5})} = \lim_{h \rightarrow 0} \frac{(5+h) - 5}{h(\sqrt{5+h} + \sqrt{5})} = \lim_{h \rightarrow 0} \frac{h}{h(\sqrt{5+h} + \sqrt{5})}$$

$$3. \lim_{x \rightarrow 5\pi/4} \sin(x) = \sin\left(\frac{5\pi}{4}\right)$$

= $\boxed{-\frac{\sqrt{2}}{2}}$

$$= \lim_{h \rightarrow 0} \frac{1}{\sqrt{5+h} + \sqrt{5}} = \frac{1}{\sqrt{5+0} + \sqrt{5}} = \boxed{\frac{1}{2\sqrt{5}}}$$

$$4. \lim_{x \rightarrow \pi/2} \frac{\sin(x) - 1}{2 - 2 \sin(x)} = \lim_{x \rightarrow \frac{\pi}{2}} \frac{\sin(x) - 1}{-2(\sin(x) - 1)} = \lim_{x \rightarrow \frac{\pi}{2}} \left(-\frac{1}{2}\right) = \boxed{-\frac{1}{2}}$$

↑

$$\frac{\sin\left(\frac{\pi}{2}\right) - 1}{2 - 2 \sin\left(\frac{\pi}{2}\right)} = \frac{1-1}{2-2} = \frac{0}{0}$$

$$1. \lim_{x \rightarrow 1} \frac{x^2 - 1}{x^2 + x - 2} = \lim_{x \rightarrow 1} \frac{(x-1)(x+1)}{(x-1)(x+2)} = \lim_{x \rightarrow 1} \frac{x+1}{x+2} = \frac{1+1}{1+2} = \boxed{\frac{2}{3}}$$

↑
getting $\frac{0}{0}$

$$2. \lim_{h \rightarrow 0} \frac{\frac{1}{5+h} - \frac{1}{5}}{h} = \lim_{h \rightarrow 0} \frac{\frac{1}{5+h} - \frac{1}{5}}{h} \frac{5(5+h)}{5(5+h)}$$

↑
getting $\frac{0}{0}$

$$= \lim_{h \rightarrow 0} \frac{5 - (5+h)}{h 5 (5+h)}$$

$$= \lim_{h \rightarrow 0} \frac{-h}{h 5 (5+h)} = \lim_{h \rightarrow 0} \frac{-1}{5(5+h)}$$

$$= \frac{-1}{5(5+0)} = \boxed{\frac{-1}{25}}$$

$$3. \lim_{x \rightarrow \pi/3} \sin(x) = \sin\left(\frac{\pi}{3}\right) = \boxed{\frac{\sqrt{3}}{2}}$$

$$4. \lim_{x \rightarrow \pi} \frac{\cos(x) + 1}{\cos^2(x) - 1} = \lim_{x \rightarrow \pi} \frac{\cos(x) + 1}{(\cos(x) - 1)(\cos(x) + 1)} = \lim_{x \rightarrow \pi} \frac{1}{\cos(x) - 1}$$

↑
getting $\frac{0}{0}$

$$= \frac{1}{\cos(\pi) - 1} = \frac{1}{-1 - 1} = \boxed{-\frac{1}{2}}$$

$$1. \lim_{x \rightarrow 2} \frac{x^2 - 4}{x^2 + 3x - 10} = \lim_{x \rightarrow 2} \frac{(x-2)(x+2)}{(x-2)(x+5)} = \lim_{x \rightarrow 2} \frac{x+2}{x+5} = \frac{2+2}{2+5} = \boxed{\frac{4}{7}}$$

getting $\frac{0}{0}$

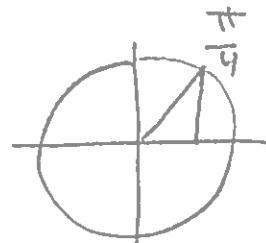
$$2. \lim_{x \rightarrow 3} \frac{\sqrt{x} - \sqrt{3}}{x - 3} = \lim_{x \rightarrow 3} \frac{\sqrt{x} - \sqrt{3}}{x - 3} = \lim_{x \rightarrow 3} \frac{\sqrt{x} - \sqrt{3}}{x - 3} \cdot \frac{\sqrt{x} + \sqrt{3}}{\sqrt{x} + \sqrt{3}}$$

$$= \lim_{x \rightarrow 3} \frac{\sqrt{x}^2 + \sqrt{x}\sqrt{3} - \sqrt{x}\sqrt{3} - \sqrt{3}^2}{(x-3)(\sqrt{x} + \sqrt{3})}$$

$$= \lim_{x \rightarrow 3} \frac{x - 3}{(x-3)(\sqrt{x} + \sqrt{3})}$$

$$= \lim_{x \rightarrow 3} \frac{1}{\sqrt{x} + \sqrt{3}} = \frac{1}{\sqrt{3} + \sqrt{3}} = \boxed{\frac{1}{2\sqrt{3}}}$$

$$3. \lim_{x \rightarrow \pi/4} \sin(x) = \sin\left(\frac{\pi}{4}\right) = \boxed{\frac{\sqrt{2}}{2}}$$



$$4. \lim_{x \rightarrow \pi/2} \frac{x - x \sin(x)}{\sin(x) - 1} = \lim_{x \rightarrow \frac{\pi}{2}} \frac{x(1 - \sin(x))}{\sin(x) - 1} = \lim_{x \rightarrow \frac{\pi}{2}} \frac{-x(\sin(x) - 1)}{\sin(x) - 1}$$

$$= \lim_{x \rightarrow \frac{\pi}{2}} (-x) = \boxed{-\frac{\pi}{2}}$$