Dynamical Decoupling of Nitrogen-Vacancy Electron Spins in Diamond and Nanodiamond

Defense of the Bachelor thesis by Richard Kullmann

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Motivation

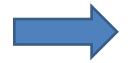
- magnetic field imaging: idea of single spins as sensors on the nanoscale
- quantum system used for this purpose ideally meets these criteria:
 - stable
 - controllable
 - can be easily prepared and read out

Motivation

- NV center meets these conditions
- High sensitivity requires long coherence times



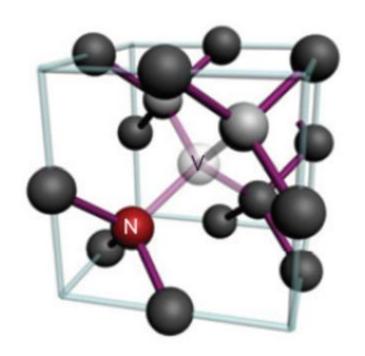
NV spin has to be decoupled from unwanted interactions with the environment



Dynamical decoupling techniques

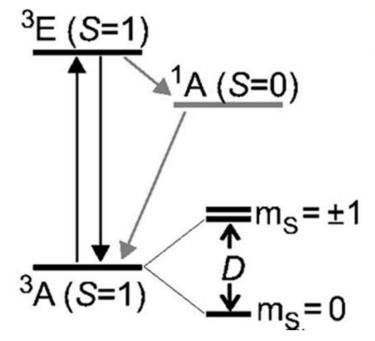
NV center

- Vacancy (V) next to substitutional nitrogen (N) atom in diamond lattice
- optically stable
- long coherence times even at room temperature
- single photon fluorescence



NV center

- description with 3 level system
- GS m_s =0 and m_s =±1 separated by D=2.87 GHz
- relaxation ES→GS: luminescence with ZPL at 637nm
- highest fluorescence at m_s=0
- optical initialization
- NV Hamiltonian:



$$H = DS_z^2 + g\mu_B \vec{S}\vec{B} + A_{\parallel}S_z I_z + A_{\perp}(S_x I_x + S_y I_y) + H_E$$

Rabi oscillations

single electronic spin (2 level system) in B-field
→ Zeeman splitting:

$$\hat{H}_Z = -\gamma_S \hat{S} \hat{B} = -\frac{\gamma_S \hbar B_z}{2} \hat{\sigma}_z = \frac{\hbar}{2} \omega_B \hat{\sigma}_z$$

adding oscillating field

$$\hat{B} = B_1(\hat{x}\cos\omega t - \hat{y}\sin\omega t)$$

$$\rightarrow \hat{H}_B = -\gamma \frac{\hbar}{2} \left(B_1(\cos \omega t \hat{\sigma}_x - \sin \omega t \hat{\sigma}_y) \right)$$

Rabi oscillations

total Hamiltonian:

$$\hat{H} = \frac{\hbar}{2} \begin{pmatrix} \omega_B & -\omega_1 e^{i\omega t} \\ -\omega_1 e^{-i\omega t} & -\omega_B \end{pmatrix}$$

• for $\omega_1 << \omega_B$, perturbation theory yields:

$$P_{1\to 0}(t) = \frac{\omega_1^2}{(\omega - \omega_{10})^2 + \omega_1^2} \sin^2\left(\frac{\sqrt{(\omega - \omega_{10})^2 + \omega_1^2}}{2}t\right)$$

Rabi's formula

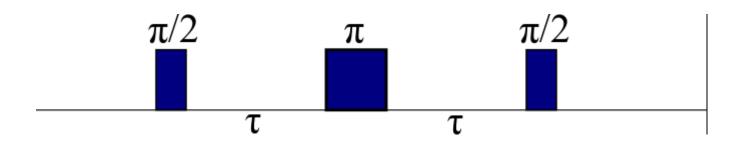
• in resonance: $\omega = \omega_{10} \rightarrow P_{1\to 0}(t) = \sin^2\left(\frac{\omega_1 t}{2}\right)$

Bloch sphere

Image of rotations on bloch sphere

Dynamical Decoupling sequences

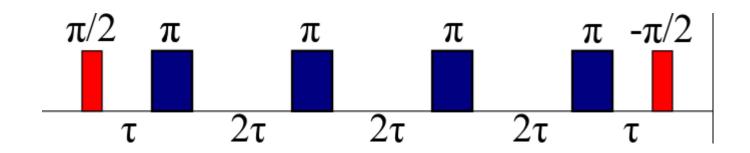
- Hahn Echo
 - 1st spin echo experiment
 - Measurement of T₂



Dynamical Decoupling sequences

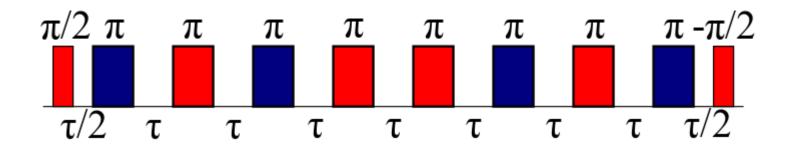
CPMG

- multiple π rotations around single axis
- higher decoupling efficiency than Hahn Echo



Dynamical Decoupling sequences

- XY
 - CPMG pulse spacing
 - $-\pi$ rotations around 2 axes \rightarrow 3D decoupling



Spectral decomposition

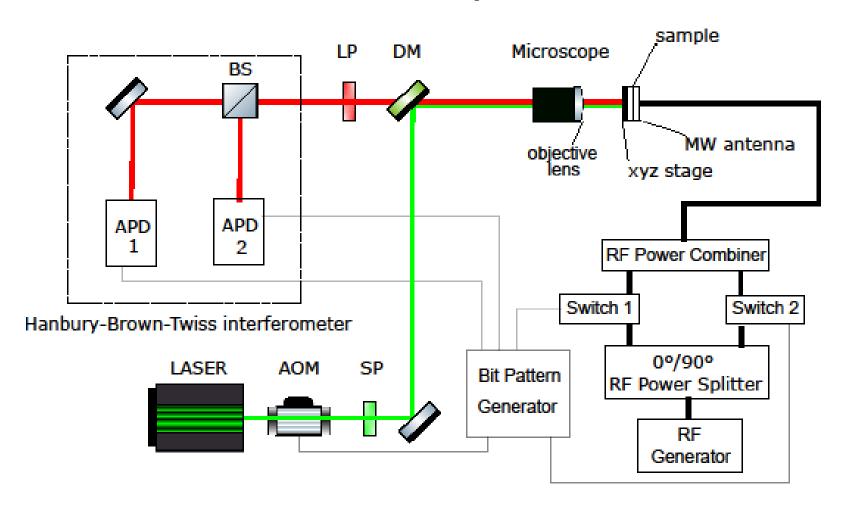
In general: loss of coherence obeys C(t)=e^{-X(t)}
with

$$\chi(t) = \frac{1}{\pi} \int_0^\infty d\omega S(\omega) \frac{F(\omega t)}{\omega^2}$$

 $S(\omega)$: spectral density function

 $F(\omega t)$: filter function

Setup



Measurements

Conclusion and Outlook

- successful implementation of DD protocols
- CPMG: improvement of factor 50 in nanodiamond and 200 in bulk \rightarrow 60 µs
- CPMG outperforms XY
- Spectral density in good agreement with other experiments
- error sources: BPG (pulse errors), MW splitter, AOM
- future
 - better time and phase control
 - Implementation of other decoupling protocols