

```
In [ ]: import numpy as np
import pandas as pd
pd.set_option("display.precision", 4)

from modules.helpers import parseMatrixRows, parseMatrixColumns, parseMatrixIndexes
from modules.plot import highlightNotZero, plotSchema

from modules.model import BarProps
from modules.model import Point, Bar
from modules.matrices import LoadMatrix, BarMatrices, modelMatrix
from modules.internalForces import *
```

Vstupy

```
In [ ]: crossSection = {"width": 200, "height": 300}
material = "C30/37"
barProps = BarProps(material, crossSection)
print(f'E = {barProps.E} kPa \nI = {barProps.I} m-4\nA = {barProps.A} m2')
```

```
E = 33000000.0 kPa
I = 0.0004499999999999993 m-4
A = 0.06 m2
```

Definovanie bodov

```
In [ ]: p1 = Point(0,0, "bod 1", [0,1,2])
p2 = Point(0,5, "bod 2", [3,4,5])
p3 = Point(5,5, "bod 3", [6,7,8])
p4 = Point(5,2, "bod 4", [9,10,11])
p1.stiff #votknutie v bode 1
p4.hinge #klbova podpera v bode 4
print(f'p1 = {p1}\n p2 = {p2}\n p3 = {p3}\n p4 = {p4}')
```

```
p1 = Point(x=0, y=0, name='bod 1', codeNumbers=[0, 1, 2], dof=[0, 0, 0])
p2 = Point(x=0, y=5, name='bod 2', codeNumbers=[3, 4, 5], dof=[1, 1, 1])
p3 = Point(x=5, y=5, name='bod 3', codeNumbers=[6, 7, 8], dof=[1, 1, 1])
p4 = Point(x=5, y=2, name='bod 4', codeNumbers=[9, 10, 11], dof=[0, 0, 1])
```

Definovanie prútov

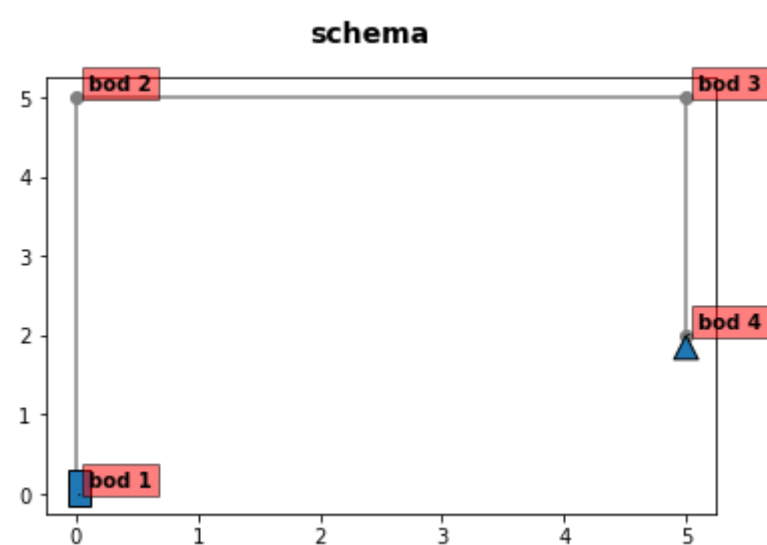
```
In [ ]: bar12 = Bar(p1, p2)
bar23 = Bar(p2, p3)
bar34 = Bar(p3, p4)
print(f'bar12 = {bar12.len} m \nbar23 = {bar23.len} m\nbar34 = {bar34.len} m')
```

```
bar12 = 5.0 m
bar23 = 5.0 m
bar34 = 3.0 m
```

Definovanie síl

```
In [ ]: F = 10 #kN
Q = 5 #kN/m
load_bar12 = Load(Q = Q, bar=bar12)
load_bar23 = Load(F = F, F_position=0.5, bar=bar23)
load_bar34 = Load(Q=0, F=0, bar=bar34)
```

```
In [ ]: plotSchema([p1,p2,p3,p4])
```



```
In [ ]: def barSolution(bar, barProps, load):
    # print bar geometry
    [lx, ly] = bar.l_xy
    alfa = bar.angle
    print(f'bar properties \nalfa = {alfa} deg')
    print(f'lx = {lx}\nly = {ly}')
```

print stiffness matrix

```

bar_matrices = BarMatrices(barProps, bar)
A0 = bar_matrices.rotation
B0 = bar_matrices.transmission
k = bar_matrices.gss_stiffness
k = parseMatrixIndexes(k, bar.codeNumbers)
print('-----')
print(
    f'stiffness matrix \n{k}\n rotation matrix \n{A0}\n transmission matrix \n{B0}')

# calculate primary internal forces
IntF = InternalForces_primary(load, bar)

# print Load vector
FA_l = LoadMatrix.lss(0, IntF.Va, IntF.Ma)
FB_l = LoadMatrix.lss(0, IntF.Vb, IntF.Mb)
FA_g = LoadMatrix.gss(FA_l, A0.T)
FB_g = LoadMatrix.gss(FB_l, A0.T)

F = LoadMatrix.super(FA_g, FB_g)
F = parseMatrixRows(F, bar.codeNumbers)
print('-----')
print(f'load vector \n{F}')

toReturn = {
    "bar" : bar,
    "barProps": barProps,
    "lx" : lx,
    "ly" : ly,
    "alfa" : alfa,
    "A0" : A0,
    "B0" : B0,
    "k" : k,
    "F" : F,
    "FA_g" : FA_g,
    "FB_g" : FB_g,
}
return toReturn

```

Riešenie na prúte 1-2

```
In [ ]: bar12_Solution = barSolution(bar12, barProps, load_bar12)
```

```

bar properties
alfa = -90.0 deg
lx = 0
ly = -5
-----
stiffness matrix
      0      1      2      3      4      5
0  1.4256e+03 -2.4161e-11  3.5640e+03 -1.4256e+03  2.4161e-11  3.5640e+03
1 -2.4161e-11  3.9600e+05  2.1823e-13  2.4161e-11 -3.9600e+05 -1.2102e-10
2  3.5640e+03  2.1823e-13  1.1880e+04 -3.5640e+03 -2.1823e-13  5.9400e+03
3 -1.4256e+03  2.4161e-11 -3.5640e+03  1.4256e+03 -2.4161e-11 -3.5640e+03
4  2.4161e-11 -3.9600e+05 -2.1823e-13 -2.4161e-11  3.9600e+05  1.2102e-10
5  3.5640e+03 -1.2102e-10  5.9400e+03 -3.5640e+03  1.2102e-10  1.1880e+04
rotation matrix
      0      1  2
0  6.1232e-17 -1.0000e+00  0
1  1.0000e+00  6.1232e-17  0
2  0.0000e+00  0.0000e+00  1
transmission matrix
  0  1  2
0 -1  0  0
1  0 -1  0
2  5  0 -1
-----
load vector
      0
0 -1.2500e+01
1 -7.6540e-16
2 -1.0417e+01
3 -1.2500e+01
4 -7.6540e-16
5  1.0417e+01

```

Riešenie na prúte 2-3

```
In [ ]: bar23_Solution = barSolution(bar23, barProps, load_bar23)
```

```

bar properties
alfa = 0.0 deg
lx = 5
ly = 0
-----
stiffness matrix
      3      4      5      6      7      8
3  396000.0      0.0      0.0 -396000.0      0.0      0.0
4      0.0  1425.6  3564.0      0.0 -1425.6  3564.0
5      0.0  3564.0  11880.0      0.0 -3564.0  5940.0
6 -396000.0      0.0      0.0  396000.0      0.0      0.0
7      0.0 -1425.6 -3564.0      0.0  1425.6 -3564.0
8      0.0  3564.0  5940.0      0.0 -3564.0  11880.0
rotation matrix
  0  1  2

```

```
0 1.0 0.0 0
1 -0.0 1.0 0
2 0.0 0.0 1
transmission matrix
0 1 2
0 -1 0 0
1 0 -1 0
2 0 5 -1
-----
load vector
0
3 0.00
4 -5.00
5 -6.25
6 0.00
7 -5.00
8 6.25
```

Riešenie na prúte 3-4

```
In [ ]: bar34_Solution = barSolution(bar34, barProps, load_bar34)
```

```
bar properties
alfa = 90.0 deg
lx = 0
ly = 3
-----
stiffness matrix
6 7 8 9 10 11
6 6.6000e+03 4.0009e-11 -9.9000e+03 -6.6000e+03 -4.0009e-11 -9.9000e+03
7 4.0009e-11 6.6000e+05 6.0620e-13 -4.0009e-11 -6.6000e+05 -1.2063e-10
8 -9.9000e+03 6.0620e-13 1.9800e+04 9.9000e+03 -6.0620e-13 9.9000e+03
9 -6.6000e+03 -4.0009e-11 9.9000e+03 6.6000e+03 4.0009e-11 9.9000e+03
10 -4.0009e-11 -6.6000e+05 -6.0620e-13 4.0009e-11 6.6000e+05 1.2063e-10
11 -9.9000e+03 -1.2063e-10 9.9000e+03 9.9000e+03 1.2063e-10 1.9800e+04
rotation matrix
0 1 2
0 6.1232e-17 1.0000e+00 0
1 -1.0000e+00 6.1232e-17 0
2 0.0000e+00 0.0000e+00 1
transmission matrix
0 1 2
0 -1 0 0
1 0 -1 0
2 -3 0 -1
-----
load vector
0
6 0.0
7 0.0
8 0.0
9 0.0
10 0.0
11 0.0
```

```
In [ ]: k1 = bar12_Solution['k']
k2 = bar23_Solution['k']
k3 = bar34_Solution['k']
```

```
In [ ]: modelMatrix = modelMatrix([k1,k2,k3])
modelMatrix.style\
.format('{:.2e}')\
.applymap(highlightNotZero)
```

Out []:

	0	1	2	3	4	5	6	7	8	9	10	11
0	1.43e+03	-2.42e-11	3.56e+03	-1.43e+03	2.42e-11	3.56e+03	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00
1	-2.42e-11	3.96e+05	2.18e-13	2.42e-11	-3.96e+05	-1.21e-10	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00
2	3.56e+03	2.18e-13	1.19e+04	-3.56e+03	-2.18e-13	5.94e+03	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00
3	-1.43e+03	2.42e-11	-3.56e+03	3.97e+05	-2.42e-11	-3.56e+03	-3.96e+05	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00
4	2.42e-11	-3.96e+05	-2.18e-13	-2.42e-11	3.97e+05	3.56e+03	0.00e+00	-1.43e+03	3.56e+03	0.00e+00	0.00e+00	0.00e+00
5	3.56e+03	-1.21e-10	5.94e+03	-3.56e+03	3.56e+03	2.38e+04	0.00e+00	-3.56e+03	5.94e+03	0.00e+00	0.00e+00	0.00e+00
6	0.00e+00	0.00e+00	0.00e+00	-3.96e+05	0.00e+00	0.00e+00	4.03e+05	4.00e-11	-9.90e+03	-6.60e+03	-4.00e-11	-9.90e+03
7	0.00e+00	0.00e+00	0.00e+00	0.00e+00	-1.43e+03	-3.56e+03	4.00e-11	6.61e+05	-3.56e+03	-4.00e-11	-6.60e+05	-1.21e-10
8	0.00e+00	0.00e+00	0.00e+00	0.00e+00	3.56e+03	5.94e+03	-9.90e+03	-3.56e+03	3.17e+04	9.90e+03	-6.06e-13	9.90e+03
9	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	-6.60e+03	-4.00e-11	9.90e+03	6.60e+03	4.00e-11	9.90e+03
10	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	-4.00e-11	-6.60e+05	-6.06e-13	4.00e-11	6.60e+05	1.21e-10
11	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	0.00e+00	-9.90e+03	-1.21e-10	9.90e+03	9.90e+03	1.21e-10	1.98e+04

```
In [ ]: def boundaryConditionsVector(points: list) -> list:
dofList=[]
for point in points:
dofList.append(point.dof)
return pd.DataFrame(np.array(dofList).flatten())
```

```
def boundaryConditionsFilter(bc_vector, cond):
    bc = np.array(bc_vector).flatten()
    df = pd.DataFrame(bc)
    return df[df[0]==cond].index.values.astype(int)

def loadVector(F1,F2,F3):
    x = F1.add(F2,fill_value=0)
    return x.add(F3,fill_value=0)
```

```
In [ ]: F1 = bar12_Solution['F']
        F2 = bar23_Solution['F']
        F3 = bar34_Solution['F']
```

Vektor zaťaženia

```
In [ ]: loadVector = loadVector(F1,F2,F3)
        loadVector
```

Out []:

	0
0	-1.2500e+01
1	-7.6540e-16
2	-1.0417e+01
3	-1.2500e+01
4	-5.0000e+00
5	4.1667e+00
6	0.0000e+00
7	-5.0000e+00
8	6.2500e+00
9	0.0000e+00
10	0.0000e+00
11	0.0000e+00

```
In [ ]: bc_vector = boundaryConditionsVector([p1,p2,p3,p4])
        bc_0 = boundaryConditionsFilter(bc_vector, 0)
        loadVector.drop(bc_0, inplace=True)
        loadVector
```

Out []:

	0
3	-12.5000
4	-5.0000
5	4.1667
6	0.0000
7	-5.0000
8	6.2500
11	0.0000

Matica tuhosti

```
In [ ]: bc_1 = boundaryConditionsFilter(bc_vector, 1)
        copyModelMatrix = modelMatrix.copy()
        copyModelMatrix.drop(bc_0, inplace=True)
        filteredModelMatrix = copyModelMatrix[bc_1]
        parseMatrixIndexes(filteredModelMatrix.copy(), ["u[2]", "v[2]", "fi[2]","u[3]", "v[3]", "fi[3]","fi[4]"])
```

Out []:

	u[2]	v[2]	fi[2]	u[3]	v[3]	fi[3]	fi[4]
u[2]	3.9743e+05	-2.4161e-11	-3564.0	-3.9600e+05	0.0000e+00	0.0	0.0000e+00
v[2]	-2.4161e-11	3.9743e+05	3564.0	0.0000e+00	-1.4256e+03	3564.0	0.0000e+00
fi[2]	-3.5640e+03	3.5640e+03	23760.0	0.0000e+00	-3.5640e+03	5940.0	0.0000e+00
u[3]	-3.9600e+05	0.0000e+00	0.0	4.0260e+05	4.0009e-11	-9900.0	-9.9000e+03
v[3]	0.0000e+00	-1.4256e+03	-3564.0	4.0009e-11	6.6143e+05	-3564.0	-1.2063e-10
fi[3]	0.0000e+00	3.5640e+03	5940.0	-9.9000e+03	-3.5640e+03	31680.0	9.9000e+03
fi[4]	0.0000e+00	0.0000e+00	0.0	-9.9000e+03	-1.2063e-10	9900.0	1.9800e+04

```
In [ ]: def nodeDisplacements(modelMatrix):
        inv = pd.DataFrame(np.linalg.inv(modelMatrix.values), modelMatrix.columns, modelMatrix.index)
```

```
return inv.dot(loadVector)*-1
```

Deformácie

```
In [ ]: displacements = nodeDisplacements(filteredModelMatrix)
        parseMatrixRows(displacements.copy(), ["u[2]", "v[2]", "fi[2]", "u[3]", "v[3]", "fi[3]", "fi[4]"])
```

```
Out[ ]:      0
u[2]  5.8585e-03
v[2]  1.3700e-06
fi[2]  5.2184e-04
u[3]  5.8433e-03
v[3]  1.4330e-05
fi[3]  7.3404e-04
fi[4]  2.5546e-03
```

```
In [ ]: def modelDisplacements(displacements):
        return pd.DataFrame(np.zeros((12, 1))).add(displacements, fill_value=0)
```

```
In [ ]: modelDisplacements = modelDisplacements(displacements)
        rows = ["u[1]", "v[1]", "fi[1]", "u[2]", "v[2]", "fi[2]", "u[3]", "v[3]", "fi[3]", "u[4]", "v[4]", "fi[4]"]
        parseMatrixRows(modelDisplacements.copy(), rows)
```

```
Out[ ]:      0
u[1]  0.0000e+00
v[1]  0.0000e+00
fi[1]  0.0000e+00
u[2]  5.8585e-03
v[2]  1.3700e-06
fi[2]  5.2184e-04
u[3]  5.8433e-03
v[3]  1.4330e-05
fi[3]  7.3404e-04
u[4]  0.0000e+00
v[4]  0.0000e+00
fi[4]  2.5546e-03
```

```
In [ ]: # calculate internal forces by formula ---  $F = F' + k * \delta$ 
def barInternalForces(modelDisplacements, barSolution):

    bar = barSolution["bar"]
    barProps = barSolution["barProps"]

    # get bar displacements (delta)
    delta_1 = modelDisplacements.loc[bar.codeNumbers[0]:bar.codeNumbers[2]]
    delta_2 = modelDisplacements.loc[bar.codeNumbers[3]:bar.codeNumbers[5]]
    deltaBar = pd.concat([delta_1, delta_2])

    # get bar matrices
    A0 = barSolution["A0"]
    k = barSolution["k"]

    #  $u = k * \delta$ 
    u = k.dot(deltaBar)

    #  $F'$  --- node A
    A0_A_parsed = parseMatrixIndexes(A0, bar.codeNumbers[0:3])
    FA_g = barSolution["FA_g"]
    F_A_g_parsed = parseMatrixRows(FA_g, bar.codeNumbers[0:3])

    #  $F'$  --- node B
    A0_B_parsed = parseMatrixIndexes(A0, bar.codeNumbers[3:6])
    FB_g = barSolution["FB_g"]
    F_B_g_parsed = parseMatrixRows(FB_g, bar.codeNumbers[3:6])

    #  $F' + u$  --- node A
    local = u.loc[bar.codeNumbers[0]:bar.codeNumbers[2]]+F_A_g_parsed
    F1 = A0_A_parsed.T.dot(local)
    forces_AB = parseMatrixRows(F1, ["N", "V", "M"])
```

```
# F' + u --- node B
local = u.loc[bar.codeNumbers[3]:bar.codeNumbers[5]]+F_B_g_parsed
F2 = A0_B_parsed.dot(local)
forces_BA = parseMatrixRows(F2, ["N","V","M"])

forces = pd.concat([forces_AB, forces_BA], axis=1)
print(parseMatrixColumns(forces, [bar.point_a.name, bar.point_b.name]))
return forces
```

Vnúťorné sily

```
In [ ]: forces12 = barInternalForces(modelDisplacements, bar12_Solution)
```

bod 1 bod 2
N -0.5425 -0.5425
V 18.9920 -6.0080
M -28.1966 -4.2635

```
In [ ]: forces23 = barInternalForces(modelDisplacements, bar23_Solution)
```

bod 2 bod 3
N 6.0080 -6.0080
V -0.5425 -9.4575
M 4.2635 18.0239

```
In [ ]: forces34 = barInternalForces(modelDisplacements, bar34_Solution)
```

bod 3 bod 4
N -9.4575 -9.4575e+00
V 6.0080 6.0080e+00
M -18.0239 -3.0314e-15

```
In [ ]: forces_final = pd.concat([forces12, forces23, forces34], axis=1)
forces_final
```

Out[]:

	bod 1	bod 2	bod 2	bod 3	bod 3	bod 4
N	-0.5425	-0.5425	6.0080	-6.0080	-9.4575	-9.4575e+00
V	18.9920	-6.0080	-0.5425	-9.4575	6.0080	6.0080e+00
M	-28.1966	-4.2635	4.2635	18.0239	-18.0239	-3.0314e-15

