

# Instrumental variable

Motivation: i.e. wage v.s. education.

OLS  
↓  
Biased.

$$\log(\text{wage}) = \beta_0 + \beta_1 \text{ed} + \beta_2 \text{exp} + \beta_3 \text{exp}^2 + \varepsilon$$

↑  
pure noise

Endogenous

is  $E(\varepsilon | \text{ed}, \text{exp}) = 0$ ? maybe not.

⇒ unobservable corr with exp & ed.

- intelligence

- persistence

} examples

Basic idea

$$\Rightarrow E(\hat{\beta}_1) \neq \beta_1$$

IV is independent from  $\varepsilon$ .

↓ effect

(ed) Independent variables

↓

(wage) dependent variables

$\times \varepsilon$

example: ① Distance to nearest college.  
(postcode)

② Quarter of Birth

## Requirements

1. Must be corr. with endogenous variable
2. Must only affect the dependent variable through its effect on the endogenous variable. (No direct effect)

$\boxed{\text{ed}}$   $\begin{matrix} \nearrow \text{part 1} \\ \rightarrow \text{part 2} \\ \searrow \text{part 3} \end{matrix}$

1. corr. with  $E(\text{ed})$
2. corr. IV. (Not  $\varepsilon$ ) ← Allow to only use this.
3. corr. everything else

## Two stage least squares.

stage 1:  $ed = \gamma_0 + \gamma_1 z + \gamma_2 \exp + \gamma_3 \exp^2 + u$

predict.  $\hat{e}_d = \hat{\gamma}_0 + \hat{\gamma}_1 z + \hat{\gamma}_2 \exp + \hat{\gamma}_3 \exp^2$

•  $\hat{e}_d$  is unbiased estimate of  $e_d$ .

- $\epsilon_2$  uncorrelated with  $z$ .

stage 2:  $\log(\text{wage}) = \beta_0 + \beta_1 \hat{e}_d + \beta_2 \text{exp} + \beta_3 \text{exp}^2 + v$   
 $\downarrow$   
 unbais.

Problem : weak T.V.

- corr of IV and endogenous variable must be sufficiently strong.

- F-Test : • null hypothesis that the coeff. on the IV in the 1<sup>st</sup> stage are 0.

- $F \sim 12$  (at least 10).

## Move

① multiple IV  $\rightarrow$  Sargan test / Wu-Hausman test

② IV does not give you the ATE.  
↳ local ATE.

③ 2SLS  $\Rightarrow$  estimation error in 1<sup>st</sup> stage  $\Rightarrow$  SE wrong in 2<sup>nd</sup>