

STA365_homework1_code

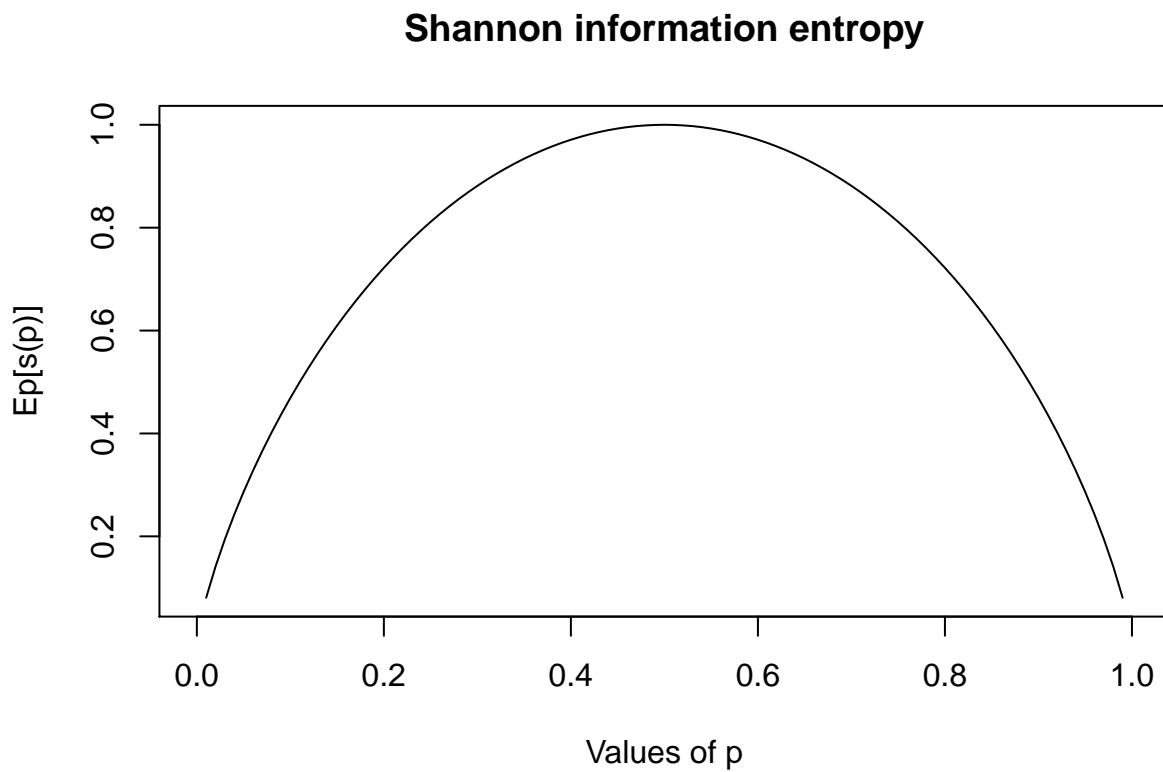
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03/02/2022

Question 2

Part b

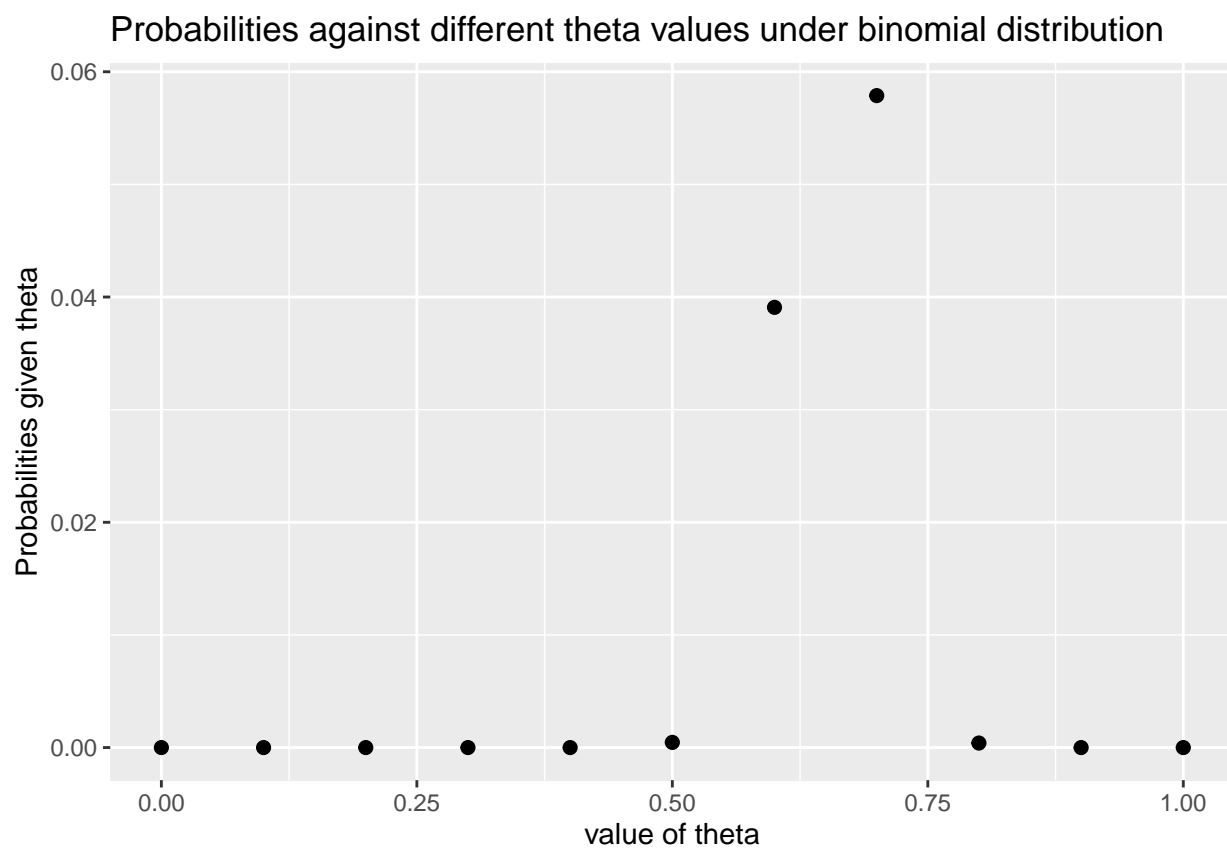
```
# Assume that  $r = p$   
p <- seq(0, 1, by=0.01)  
Ep_Sp <- -log2(p)*p - (1-p)*log2(1-p)  
plot(p, Ep_Sp,type="l", xlab="Values of p", ylab="Ep[s(p)]", main = "Shannon information entropy")
```



Question 4

Part C

```
theta <- seq(0, 1, by=0.1)
prob_X <- dbinom(66, size = 100, prob = theta)
prob_likelihood <- tibble(theta, prob_X)
ggplot(prob_likelihood, aes(x=theta, y=prob_X)) +
  geom_point(size = 2) + labs(x="value of theta",
  y="Probabilities given theta",
  title="Probabilities against different theta values under binomial distribution")
```



Question 5

Part C

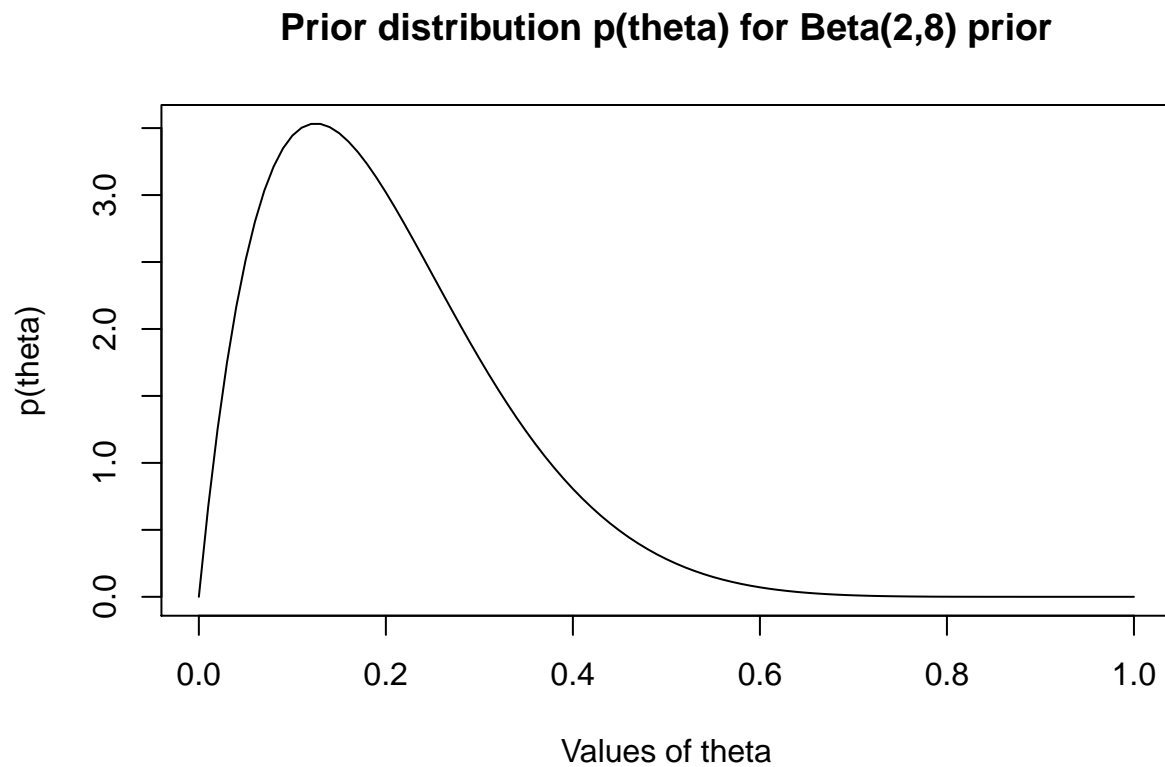
```
# 95% Credible interval for prior Beta(2,8)  
qbeta(c(0.025, 0.975), 17, 36)
```

```
## [1] 0.2032978 0.4510240
```

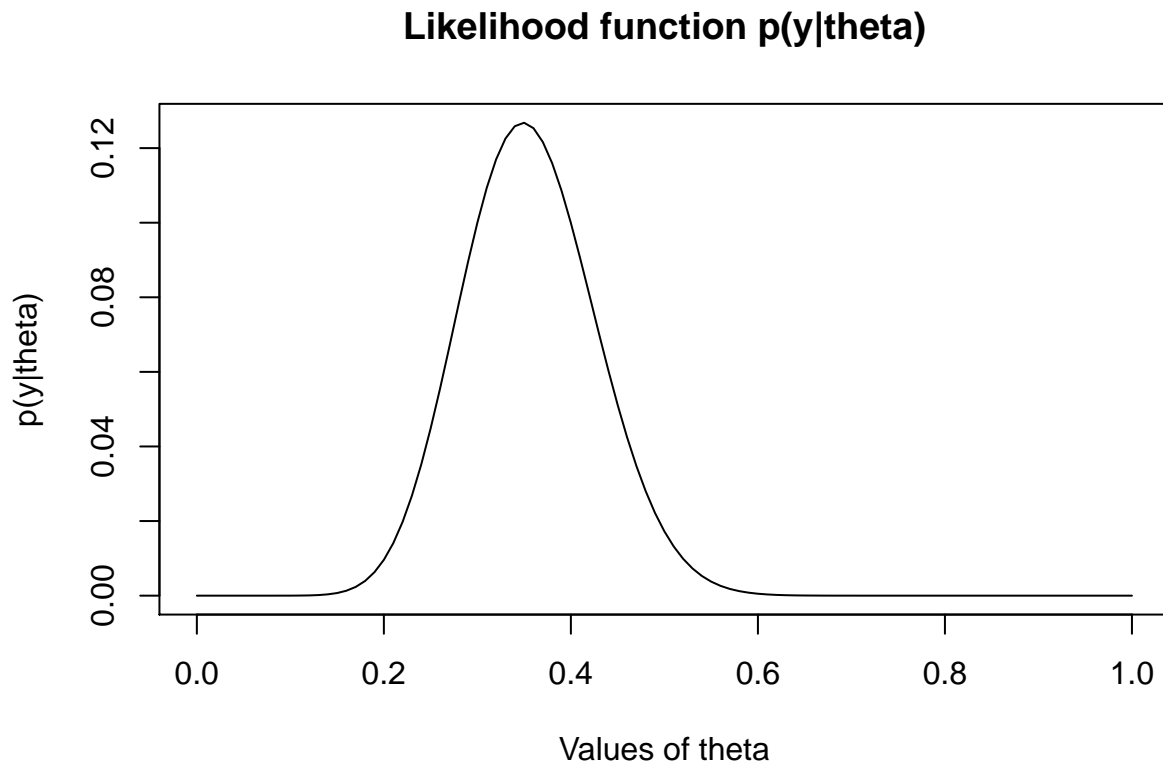
Part D

```
# Plot prior, likelihood, and posterior functions for Beta(2,8) prior
y = 15
n = 43
a_1 = 2
b_1 = 8
a_p1 = 17
b_p1 = 36
theta_1 <- seq(0, 1, 0.01)

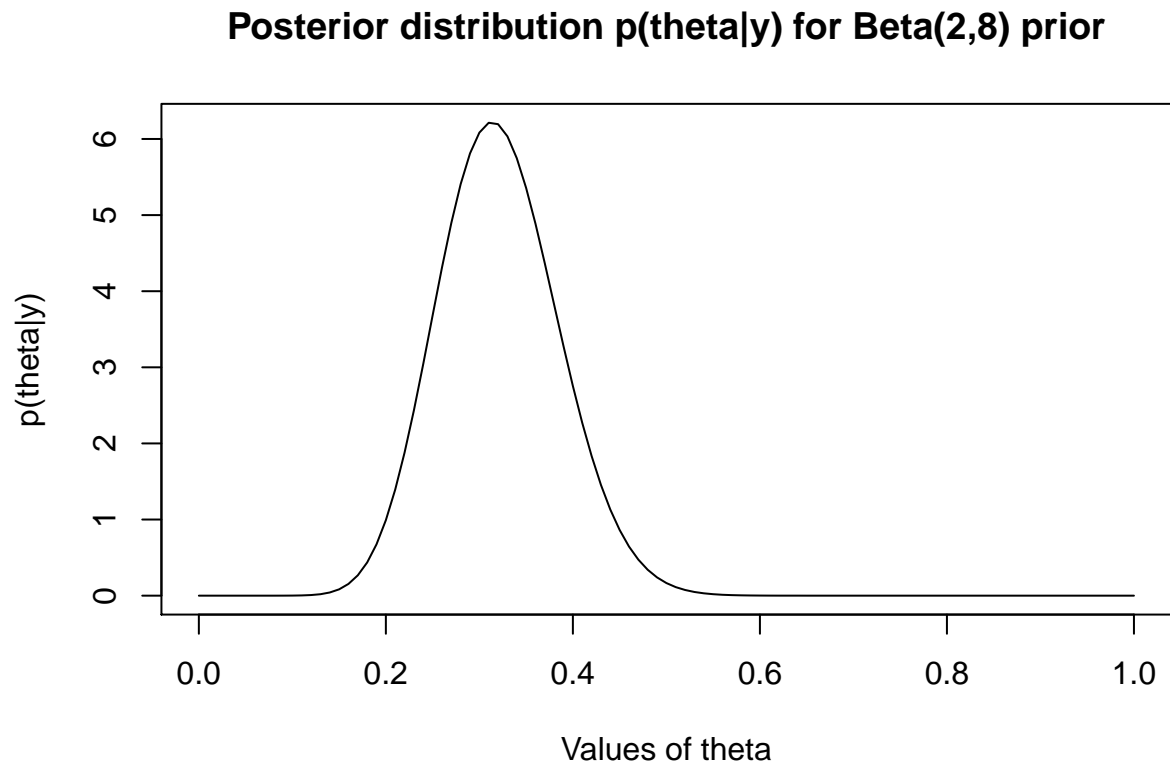
# Prior distribution p(theta)
plot(theta_1, dbeta(theta_1, shape1 = a_1, shape2 = b_1), type = 'l',
      xlab="Values of theta", ylab="p(theta)",
      main = "Prior distribution p(theta) for Beta(2,8) prior")
```



```
# Likelihood function  $P(y|\theta)$ 
plot(theta_1, dbinom(15, size = 43, prob = theta_1), type = 'l',
      xlab="Values of  $\theta$ ", ylab="p(y| $\theta$ )",
      main = "Likelihood function p(y| $\theta$ )")
```



```
# Posterior distribution  $p(\theta|y)$ 
plot(theta_1, dbeta(theta_1, shape1 = a_p1, shape2 = b_p1), type = 'l',
      xlab="Values of theta", ylab="p(theta|y)",
      main = "Posterior distribution p(theta|y) for Beta(2,8) prior")
```



Part E

```
# 95% Credible interval for prior Beta(8,2)
qbeta(c(0.025, 0.975), 23, 30)
```

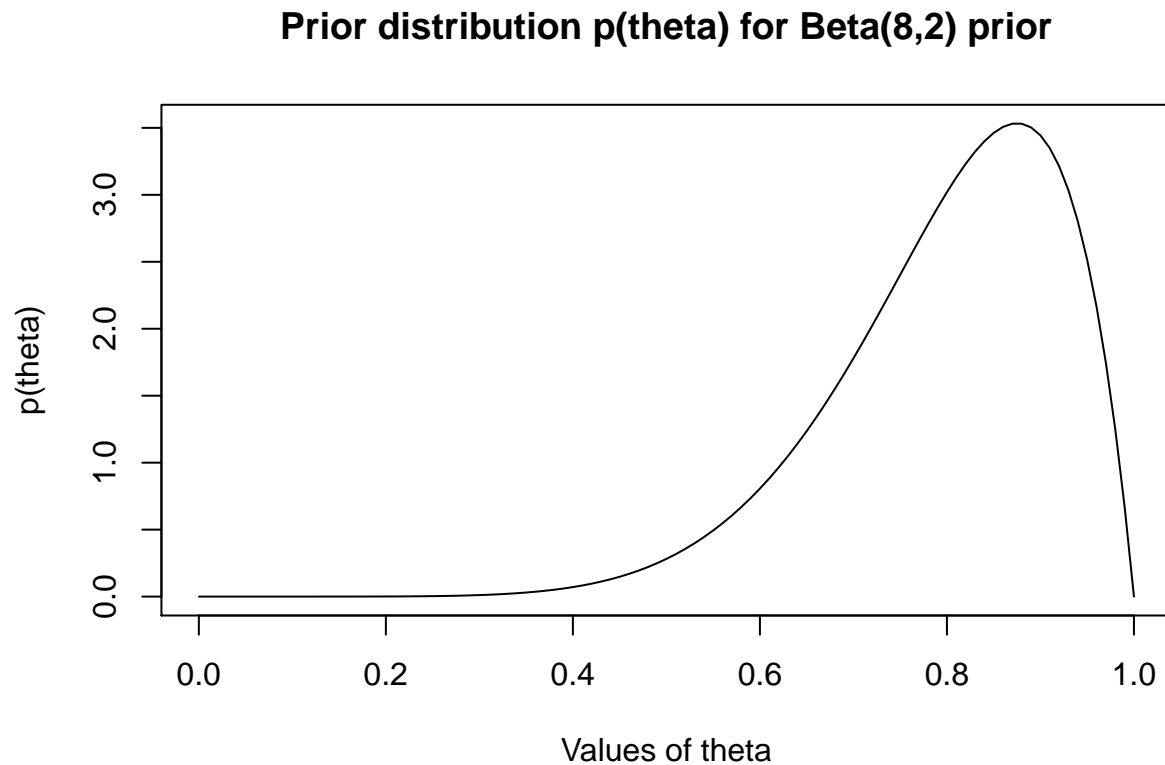
```
## [1] 0.3046956 0.5679528
```

```

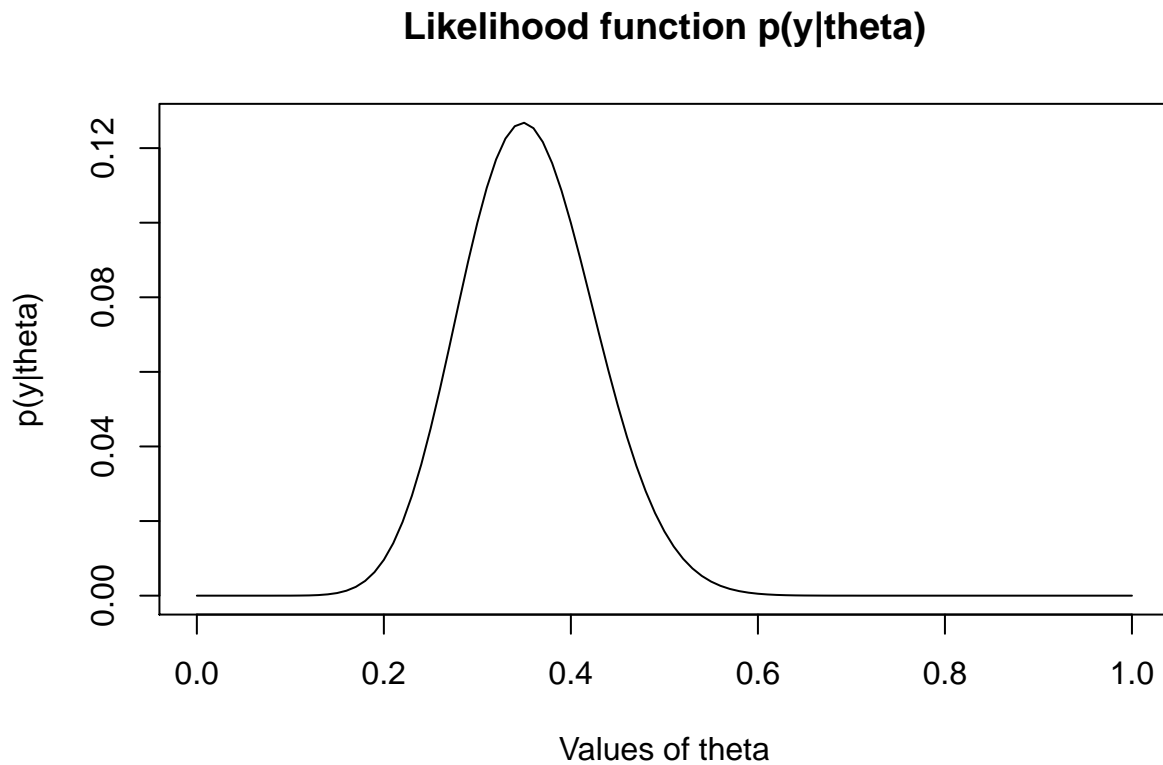
# Plot prior, likelihood, and posterior functions for Beta(8,2) prior
y = 15
n = 43
a_2 = 8
b_2 = 2
a_p2 = 23
b_p2 = 30
theta_1 <- seq(0, 1, 0.01)

# Prior distribution p(theta)
plot(theta_1, dbeta(theta_1, shape1 = a_2, shape2 = b_2), type = 'l',
      xlab="Values of theta", ylab="p(theta)",
      main = "Prior distribution p(theta) for Beta(8,2) prior")

```




```
# Likelihood function  $P(y|\theta)$ 
plot(theta_1, dbinom(15, size = 43, prob = theta_1), type = 'l',
      xlab="Values of  $\theta$ ", ylab="p(y| $\theta$ )",
      main = "Likelihood function p(y| $\theta$ )")
```



```
# Posterior distribution  $p(\theta|y)$ 
plot(theta_1, dbeta(theta_1, shape1 = a_p2, shape2 = b_p2), type = 'l',
      xlab="Values of  $\theta$ ", ylab="p( $\theta|y$ )",
      main = "Posterior distribution p( $\theta|y$ ) for Beta(8,2) prior")
```

