STA363SecAProj2-Code Appendix

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```
# Loading the data
college <- read.csv("~/Desktop/2021Spring/STA-363/Projects/Project 2/STA363Porject2/collegedata1.csv")</pre>
# Every package required in the project is libraried here
# Package for the BSS
library(leaps)
# Packages for Ridge Regression
# Need to run the next line if the package glmnet is not installed
#install.packages("glmnet")
library(Matrix)
library(glmnet)
## Loaded glmnet 4.1-1
# For table output
library(knitr)
# For elastic net technique
# Need to run the next line if the package caret is not installed
#install.packages("caret")
library(caret)
## Loading required package: lattice
## Loading required package: ggplot2
# Show the dimension of the data set
dim(college)
## [1] 777 19
# Examinate any massing data in the data set
which(is.na(college))
## integer(0)
# Remove the column Enroll as it is usually unavailable
college <- subset(college, select = -Enroll)</pre>
# To make sure the column Enroll is actually removed
dim(college)
## [1] 777 18
# Add a column which represents the acceptance rate
college$Rate <- college$Accept / college$Apps</pre>
# Remove the column representing the number of acceptance then
college <- subset(college, select = -Accept)</pre>
# Remove the college name column
```

```
college <- subset(college, select = -College)</pre>
# Change variable Private to PrivateYes
college$PrivateYes[college$Private=="Yes"] <- 1</pre>
college$PrivateYes[college$Private!="Yes"] <- 0</pre>
# Remove the Private column
college <- subset(college, select = -Private)</pre>
# To check whether the data is actually modified
head(college)
##
     Apps Top10perc Top25perc F.Undergrad P.Undergrad Outstate Room.Board Books
## 1 1660
                 23
                            52
                                       2885
                                                    537
                                                            7440
                                                                        3300
                                                                                450
## 2 2186
                 16
                            29
                                       2683
                                                   1227
                                                            12280
                                                                        6450
                                                                                750
## 3 1428
                 22
                                       1036
                                                     99
                                                            11250
                                                                        3750
                                                                                400
                            50
## 4 417
                 60
                            89
                                        510
                                                     63
                                                            12960
                                                                        5450
                                                                                450
                 16
                            44
                                        249
                                                    869
                                                                                800
## 5 193
                                                            7560
                                                                        4120
## 6 587
                 38
                            62
                                        678
                                                     41
                                                            13500
                                                                        3335
                                                                                500
##
    Personal PhD Terminal S.F.Ratio perc.alumni Expend Grad.Rate
                                                                          Rate
                                 18.1
                                                     7041
                                                                  60 0.7421687
## 1
         2200 70
                         78
                                                12
                                                16 10527
## 2
         1500 29
                         30
                                 12.2
                                                                  56 0.8801464
                                                                  54 0.7682073
## 3
         1165 53
                         66
                                 12.9
                                                30
                                                     8735
                                                37 19016
## 4
          875 92
                         97
                                  7.7
                                                                  59 0.8369305
                                                 2 10922
## 5
         1500 76
                         72
                                 11.9
                                                                  15 0.7564767
## 6
          675 67
                         73
                                  9.4
                                                11 9727
                                                                  55 0.8160136
##
    PrivateYes
## 1
## 2
              1
## 3
              1
## 4
              1
## 5
## 6
              1
dim(college)
## [1] 777 17
# Fit and choose the best models amoung the models with different amount of variables and store
# them in BSSout.
# numax is set to be 16, since the full model contains 16 exploratory variables in it.
BSSout <- regsubsets( Apps ~ ., data = college, nvmax = 16)
# Just for checking
#BSSout$rss
#plot(BSSout$rss)
# The adjusted R-squared for the models from the stage 1
summary(BSSout)$adjr2
     \hbox{\tt [1]} \ \ 0.6629606 \ \ 0.7351032 \ \ 0.7609193 \ \ 0.7652828 \ \ 0.7691150 \ \ 0.7711374 \ \ 0.7731134 
   [8] 0.7740025 0.7742142 0.7745535 0.7747108 0.7745266 0.7743210 0.7740949
## [15] 0.7738017 0.7735079
# Plot the adjusted R-squareds for models
plot(BSSout, scale = "adjr2")
# Fit the LSLR models with the features we selected
LSLR <- lm(Apps ~ PrivateYes + F.Undergrad + P.Undergrad + Outstate + Room.Board + Terminal + perc.alum
```

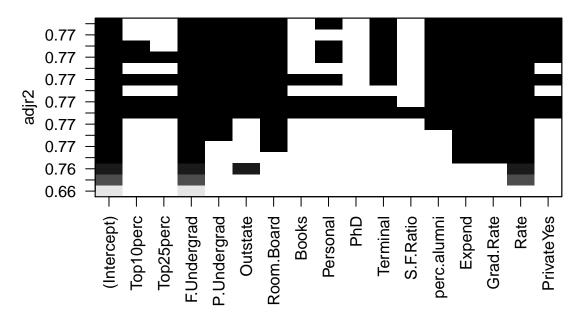


Figure 1: Adjusted R-squareds for models created in the stage 1 of BSS

```
# Output the estimates for the LSLR model
knitr::kable(summary(LSLR)$coefficients, caption = "\\label{tab:LSLRbetas}The estimates for the LSLR model
```

Table 1.	The estimat	es for the	LSLR	model
Table 1.	THE ESTINAT	co for one	$\mathbf{L} \mathbf{D} \mathbf{L} \mathbf{L} \mathbf{L}$	moder

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	1994.5038628	701.8798770	2.841660	0.0046072
PrivateYes	-353.5375145	240.8623931	-1.467799	0.1425694
F.Undergrad	0.6555742	0.0201696	32.503022	0.0000000
P.Undergrad	-0.1597435	0.0554461	-2.881058	0.0040742
Outstate	0.0838324	0.0328084	2.555209	0.0108046
Room.Board	0.2356826	0.0844043	2.792307	0.0053638
Terminal	-9.8869963	5.8877399	-1.679251	0.0935108
perc.alumni	-20.1480419	7.0000823	-2.878258	0.0041101
Expend	0.0689980	0.0187457	3.680732	0.0002489
Grad.Rate	19.0549834	5.0978967	3.737813	0.0001994
Rate	-4812.5857721	525.3775219	-9.160243	0.0000000

```
# Implement the k-fold technique
# Create two null matrices to store the residuals of the LSLR model
residualskfold <- matrix(NA, nrow=777, ncol=1)</pre>
# Set up k
# Choose 21, since 21 is a factor of the number of rows 777
k <- 21
#set random seed
set.seed(100)
#create folds
folds <- sample(rep(1:k, 37),777,replace = FALSE)</pre>
#for loop
for(i in 1:k){
  \#find\ the\ rows\ in\ fold\ i
  infold <- which(folds==i)</pre>
  #create a kfoldCV training set
  kfoldCVTraining <- college[-infold,]</pre>
                                                3
  #create a kfoldCV test set
  kfoldCVTest <- college[infold,]</pre>
  #train the LSLR model
  lefaldICID /- lm (Am
```

```
Apps
##
                            Top10perc
                                         Top25perc F.Undergrad P.Undergrad
                1.0000000
                            0.3388337
                                        0.35163990
                                                   0.81449058 0.39826427
## Apps
                0.33883368
## Top10perc
                            1.0000000
                                        0.89199497
                                                    0.14128873 -0.10535628
## Top25perc
                0.35163990
                            0.8919950
                                        1.00000000
                                                    0.19944466 -0.05357664
## F.Undergrad
                0.81449058
                            0.1412887
                                        0.19944466
                                                    1.00000000
                                                                0.57051219
## P.Undergrad
                0.39826427 -0.1053563 -0.05357664
                                                    0.57051219
                                                                1.00000000
                                        0.48939383 -0.21574200 -0.25351232
## Outstate
                0.05015903
                            0.5623305
## Room.Board
                0.16493896
                            0.3714804
                                        0.33148989
                                                   -0.06889039 -0.06132551
## Books
                0.13255860
                            0.1188584
                                        0.11552713
                                                    0.11554976
                                                                0.08119952
## Personal
                0.17873085 -0.0933164 -0.08081027
                                                    0.31719954
                                                                0.31988162
## PhD
                0.39069733
                            0.5318280
                                        0.54586221
                                                    0.31833697
                                                                 0.14911422
## Terminal
                0.36949147
                            0.4911350
                                        0.52474884
                                                    0.30001894
                                                                0.14190357
                                                                0.23253051
## S.F.Ratio
                                                    0.27970335
                0.09563303 -0.3848745 -0.29462884
  perc.alumni -0.09022589
                            0.4554853
                                        0.41786429 -0.22946222 -0.28079236
  Expend
                0.25959198
                            0.6609134
                                        0.52744743
                                                    0.01865162 -0.08356842
##
  Grad.Rate
                0.14675460
                            0.4949892
                                        0.47728116 -0.07877313 -0.25700099
## Rate
               -0.39255498 -0.4786754 -0.43467244 -0.15565379 -0.09228664
## PrivateYes
               -0.43209471
                            0.1641322
                                        0.09575224 -0.61556054 -0.45208775
##
                  Outstate
                            Room.Board
                                               Books
                                                        Personal
                                                                          PhD
## Apps
                0.05015903
                            0.16493896
                                        0.132558598 0.17873085
                                                                  0.39069733
                                                                  0.53182802
## Top10perc
                0.56233054
                            0.37148038
                                        0.118858431 -0.09331640
## Top25perc
                0.48939383
                            0.33148989
                                        0.115527130 -0.08081027
                                                                  0.54586221
## F.Undergrad -0.21574200 -0.06889039
                                         0.115549761
                                                     0.31719954
                                                                  0.31833697
## P.Undergrad -0.25351232 -0.06132551
                                        0.081199521
                                                     0.31988162
                                                                  0.14911422
## Outstate
                1.00000000
                            0.65425640
                                         0.038854868 -0.29908690
                                                                  0.38298241
                0.65425640
## Room.Board
                            1.00000000
                                         0.127962970 -0.19942818
                                                                   0.32920228
## Books
                0.03885487
                            0.12796297
                                         1.000000000
                                                      0.17929476
                                                                   0.02690573
  Personal
                                        0.179294764
                                                     1.00000000 -0.01093579
##
               -0.29908690 -0.19942818
## PhD
                0.38298241
                            0.32920228
                                         0.026905731 -0.01093579
                                                                   1.0000000
## Terminal
                0.40798320
                            0.37453955
                                        0.099954700 -0.03061311
                                                                   0.84958703
## S.F.Ratio
               -0.55482128 -0.36262774 -0.031929274
                                                     0.13634483
                                                                 -0.13053011
  perc.alumni 0.56626242
                            0.27236345 -0.040207736 -0.28596808
                                                                  0.24900866
## Expend
                0.67277862
                            0.50173942
                                         0.112409075 -0.09789189
                                                                   0.43276168
## Grad.Rate
                            0.42494154
                                        0.001060894 -0.26934396
                0.57128993
                                                                  0.30503785
## Rate
               -0.24095073 -0.31030204 -0.174072883
                                                     0.01997851 -0.31833394
                            0.34053206 -0.018548975 -0.30448505 -0.15671437
## PrivateYes
                0.55264990
##
                  Terminal
                             S.F.Ratio perc.alumni
                                                         Expend
                                                                    Grad.Rate
## Apps
                0.36949147
                            0.09563303 -0.09022589
                                                     0.25959198
                                                                 0.146754600
                0.49113502 -0.38487451
                                        0.45548526
                                                     0.66091341
                                                                 0.494989235
## Top10perc
## Top25perc
                0.52474884 -0.29462884
                                        0.41786429
                                                     0.52744743
                                                                 0.477281164
## F.Undergrad
                0.30001894
                            0.27970335 -0.22946222
                                                     0.01865162 -0.078773129
## P.Undergrad
                0.14190357
                            0.23253051 -0.28079236 -0.08356842 -0.257000991
## Outstate
                0.40798320 -0.55482128
                                        0.56626242
                                                     0.67277862
                                                                 0.571289928
## Room.Board
                0.37453955 -0.36262774
                                        0.27236345
                                                     0.50173942
                                                                 0.424941541
## Books
                0.09995470 -0.03192927 -0.04020774
                                                     0.11240908
                                                                 0.001060894
## Personal
               -0.03061311
                            0.13634483 -0.28596808
                                                    -0.09789189
                                                                -0.269343964
## PhD
                0.84958703 -0.13053011
                                        0.24900866
                                                     0.43276168
                                                                 0.305037850
                1.00000000 -0.16010395
## Terminal
                                         0.26713029
                                                     0.43879922
                                                                 0.289527232
## S.F.Ratio
               -0.16010395
                            1.00000000 -0.40292917 -0.58383204 -0.306710405
  perc.alumni
               0.26713029 -0.40292917
                                         1.00000000
                                                     0.41771172
                                                                 0.490897562
## Expend
                0.43879922 -0.58383204
                                         0.41771172
                                                     1.00000000
                                                                 0.390342696
## Grad.Rate
                0.28952723 -0.30671041
                                        0.49089756
                                                     0.39034270
                                                                 1.000000000
```

```
## Rate
              -0.30379999 0.10998188 -0.13210402 -0.40862232 -0.286971505
## PrivateYes -0.12961994 -0.47220474 0.41477493 0.25846068 0.336162290
                     Rate PrivateYes
##
              -0.39255498 -0.43209471
## Apps
## Top10perc
             -0.47867539 0.16413220
## Top25perc -0.43467244 0.09575224
## F.Undergrad -0.15565379 -0.61556054
## P.Undergrad -0.09228664 -0.45208775
## Outstate -0.24095073 0.55264990
## Room.Board -0.31030204 0.34053206
## Books
             -0.17407288 -0.01854897
## Personal
              0.01997851 -0.30448505
## PhD
              -0.31833394 -0.15671437
## Terminal -0.30379999 -0.12961994
## S.F.Ratio 0.10998188 -0.47220474
## perc.alumni -0.13210402 0.41477493
             -0.40862232 0.25846068
## Expend
## Grad.Rate -0.28697150 0.33616229
## Rate
              1.00000000 0.08499047
## PrivateYes 0.08499047 1.00000000
# Create the design matrix, using all variables we have
XD <- model.matrix(Apps ~ ., data = college)</pre>
# Doing the cross validation to choose the best tuning parameter
set.seed(100)
# As requested by the client, we want try the tuning parameters from 0 to 1000 by 0.5
cv.ridge <- cv.glmnet(XD[, -1], college$Apps, alpha = 0, nfold = 21, lambda = seq(from = 0, to = 1000,
# Plot the result
plot(cv.ridge)
# Return the smallest test MSE and the corresponding Lambda
min(cv.ridge$cvm)
## [1] 3567052
#cv.ridge$lambda.min
# Compute the RMSE for the full model and ridge model
sqrt(cv.ridge$cvm[1])
## [1] 2014.712
sqrt(cv.ridge$cvm[which.min(cv.ridge$cvm)])
## [1] 1888.664
# Show the percentage in improvement
(sqrt(cv.ridge$cvm[1]) - sqrt(cv.ridge$cvm[which.min(cv.ridge$cvm)])) / sqrt(cv.ridge$cvm[1])
## [1] 0.06256349
# Create the final Ridge model
RidgeModel <- glmnet(XD[, -1], college$Apps, alpha = 0, lambda = cv.ridge$lambda.min)
# Create a matrix to store the coefficients for the Full and Ridge model
Mat <- cbind(FullModel = coefficients(glmnet(XD[,-1],college$Apps, alpha = 0, lambda = 0)), Shrinkage =
Mat <- as.matrix(Mat)</pre>
# Add name to the matrix
colnames(Mat) <- c("Full Model", "Shrinkage")</pre>
```

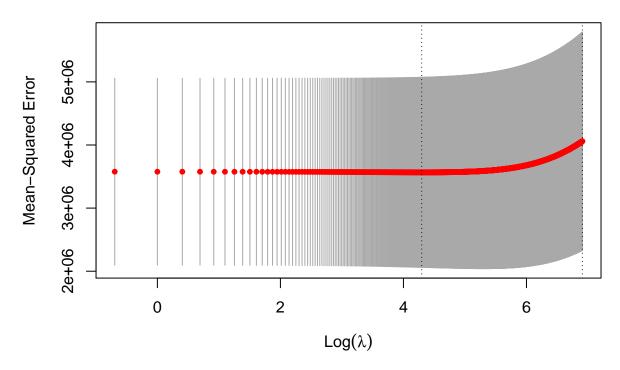


Figure 2: test MSE vs. log(Lambda) for the Ridge model

```
# Store the data into a dataframe
Mat <- data.frame(Mat)
# Output the coefficients for the full model and the Ridge model side by side
knitr::kable(Mat, caption = "\label{tab:Ridgebetas}Comparing the Coefficients: Full model vs. Ridge model</pre>
```

Table 2: Comparing the Coefficients: Full model vs. Ridge model

	Full.Model	Shrinkage
(Intercept)	2347.9828469	2053.3203010
Top10perc	7.8638193	8.4805942
Top25perc	-4.0746483	-2.3875501
F.Undergrad	0.6573680	0.6285696
P.Undergrad	-0.1459711	-0.1101358
Outstate	0.0784838	0.0729730
Room.Board	0.2395610	0.2425719
Books	-0.2110964	-0.1702510
Personal	-0.1280348	-0.1100649
PhD	-0.9091787	-0.8032072
Terminal	-9.2029383	-7.9782245
S.F.Ratio	2.6902737	6.0486138
perc.alumni	-21.5745533	-21.5946430
Expend	0.0662131	0.0676779
Grad.Rate	18.1436018	18.6297680
Rate	-4740.8089022	-4562.0644359
PrivateYes	-347.5734261	-449.8102435

```
# Create the design matrix, using all variables we have
XD <- model.matrix(Apps ~ ., data = college)
# Doing the cross validation to choose the bast tuning parameter
set.seed(100)
# As requested by the client, we want try the tuning parameters from 0 to 1000 by 0.5
cv.lasso <- cv.glmnet(XD[, -1], college$Apps, alpha = 1, nfold = 21, lambda = seq(from = 0, to = 1000, fractions)</pre>
```

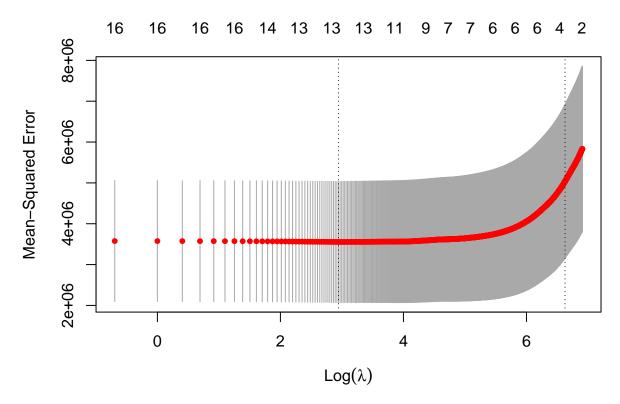


Figure 3: test MSE vs. log(Lambda) for the Lasso model

```
# Create the final Ridge model
LassoModel <- glmnet(XD[, -1], college$Apps, alpha = 1, lambda = cv.lasso$lambda.min)

# Create a matrix to store the coefficients for the Full model, Ridge model, and Lasso model
Mat <- cbind(FullModel = coefficients(glmnet(XD[,-1],college$Apps, alpha = 0, lambda = 0)), Shrinkage =
Mat <- as.matrix(Mat)

# Add name to the matrix
colnames(Mat) <- c("Full Model", "Shrinkage", "Lasso")

# Store the data into a dataframe
Mat <- data.frame(Mat)

# Output the coefficients for the full model, the Ridge model, and the Lasso model side by side
knitr::kable(Mat, caption = "\\label{tab:Lassobetas}Comparing the Coefficients: Full model vs. Ridge model</pre>
```

Table 3: Comparing the Coefficients: Full model vs. Ridge model vs. Lasso model

	Full.Model	Shrinkage	Lasso
(Intercept)	2347.9828469	2053.3203010	1970.8274189
Top10perc	7.8638193	8.4805942	2.8468785
Top25perc	-4.0746483	-2.3875501	0.0000000
F.Undergrad	0.6573680	0.6285696	0.6494415
P.Undergrad	-0.1459711	-0.1101358	-0.1205914
Outstate	0.0784838	0.0729730	0.0633135
Room.Board	0.2395610	0.2425719	0.2233467
Books	-0.2110964	-0.1702510	-0.0799176
Personal	-0.1280348	-0.1100649	-0.1005813
PhD	-0.9091787	-0.8032072	0.0000000

	Full.Model	Shrinkage	Lasso
Terminal	-9.2029383	-7.9782245	-5.8787418
S.F.Ratio	2.6902737	6.0486138	0.0000000
perc.alumni	-21.5745533	-21.5946430	-18.3912000
Expend	0.0662131	0.0676779	0.0648436
Grad.Rate	18.1436018	18.6297680	17.1839692
Rate	-4740.8089022	-4562.0644359	-4701.8525447
${\bf Private Yes}$	-347.5734261	-449.8102435	-213.7627808

```
# Training the Elastic Net Model
ElnetModel <- train(
   Apps ~ ., data = college,
   method = "glmnet",
   trControl = trainControl(method = "cv", number = 21)
)

# Create a matrix to store the coefficients for the Full model, Ridge model, Lasso model, and Elastic N
Mat <- cbind(FullModel = coefficients(glmnet(XD[,-1],college$Apps, alpha = 0, lambda = 0)), Shrinkage =
Mat <- as.matrix(Mat)

# Add name to the matrix
colnames(Mat) <- c("Full Model", "Shrinkage", "Lasso", "Elastic Net")

# Store the data into a dataframe
Mat <- data.frame(Mat)

# Output the coefficients for the full model, the Ridge model, the Lasso model, the Elastic Net model s
knitr::kable(Mat, caption = "\\label{tab:Elnetbetas}Comparing the Coefficients: Full model vs. Ridge model</pre>
```

Table 4: Comparing the Coefficients: Full model vs. Ridge model vs. Lasso model vs. Elastic Net model

	Full.Model	Shrinkage	Lasso	Elastic.Net
(Intercept)	2347.9828469	2053.3203010	1970.8274189	2012.2948856
Top10perc	7.8638193	8.4805942	2.8468785	5.4355978
Top25perc	-4.0746483	-2.3875501	0.0000000	-0.1753023
F.Undergrad	0.6573680	0.6285696	0.6494415	0.6322090
P.Undergrad	-0.1459711	-0.1101358	-0.1205914	-0.1097671
Outstate	0.0784838	0.0729730	0.0633135	0.0681927
Room.Board	0.2395610	0.2425719	0.2233467	0.2376621
Books	-0.2110964	-0.1702510	-0.0799176	-0.1330824
Personal	-0.1280348	-0.1100649	-0.1005813	-0.1060022
PhD	-0.9091787	-0.8032072	0.0000000	0.0000000
Terminal	-9.2029383	-7.9782245	-5.8787418	-7.8027002
S.F.Ratio	2.6902737	6.0486138	0.0000000	2.1517864
perc.alumni	-21.5745533	-21.5946430	-18.3912000	-20.6252852
Expend	0.0662131	0.0676779	0.0648436	0.0670443
Grad.Rate	18.1436018	18.6297680	17.1839692	18.1880286
Rate	-4740.8089022	-4562.0644359	-4701.8525447	-4584.7702978
PrivateYes	-347.5734261	-449.8102435	-213.7627808	-387.0064176

```
# return the test RMSE
ElnetModel
```

```
## glmnet
##
```

```
## 777 samples
## 16 predictor
##
## No pre-processing
## Resampling: Cross-Validated (21 fold)
## Summary of sample sizes: 739, 741, 740, 740, 740, 740, ...
## Resampling results across tuning parameters:
##
     alpha lambda
##
                       RMSE
                                 Rsquared
                                            MAE
             6.300427 1628.784 0.8313788 1000.6191
##
     0.10
##
    0.10
            63.004271 1624.236 0.8323231
                                             997.4237
##
     0.10
           630.042706 1684.448 0.8262015
                                            1004.9927
##
    0.55
             6.300427 1628.888 0.8315239
                                             999.4192
##
     0.55
            63.004271 1625.509 0.8328906
                                             988.5645
##
    0.55
           630.042706 1764.469 0.8242229
                                            1012.9412
##
     1.00
             6.300427
                       1627.798 0.8318897
                                             997.7343
##
     1.00
            63.004271 1628.953 0.8326987
                                             982.0657
     1.00
            630.042706 1903.976 0.7999342 1122.9951
##
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were alpha = 0.1 and lambda = 63.00427.
```

Table 5: Models with their test RMSE

models	test RMSE
LSLR model	1881.8
Ridge model	1888.64
Lasso model	1885.252
Elastic Net model	1624.236