

CST procedure

This appendix will detail the steps that should be taken to easily set up a qubit simulation in CST. First a project template needs to be created.

Creating a new project

When a new project is started, CST asks which module is going to be used. Most settings can be changed at a later time.

- After clicking '*Create project*' choose '*MW & RF & Optical*'.
- Choose '*Antennas*' and click '*Next >*'.
- Choose '*Waveguide (Horn, Cone, etc.)*'.
- Choose '*Frequency Domain*'.
- Select the units to be used, the default settings are sufficient.
- Choose a frequency domain. This can be left blank and changed at a later time.
- Click '*Next*' to see an overview of the created template.
- Click '*Finish*'.

Qubit designs can now be imported or created in CST.

The estimation of the capacitance of the qubit and the electric fields in the structure will be treated separately as the second process is more complex. Both simulations make use of the Frequency Domain Solver. Settings applicable to both processes are the frequency range and the boundaries.

- Under '*Simulation*' click '*Frequency*' and set the desired values.
- Again under '*Simulation*' click '*Boundaries*' and set the fields as in figure 1.1
- Click '*Open Boundary...*' and under '*Automatic minimum distance to structure*' select '*Fraction of wavelength*' and set to 8. Click '*OK*'.

The capacitance

As shown in equation (1.1) the capacitance of the structure must be known to calculate the total energy in the qubit. The value of the capacitance converges very quickly as the mesh is refined. This simulation should always include a Discrete Port connected to the capacitor pads.

$$W = \frac{1}{2} CV^2 \quad (1.1)$$

Where C is the total capacitance of the system and V the voltage over the systems.

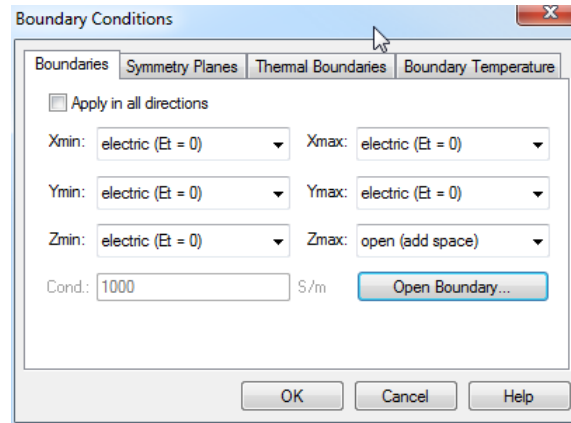


Figure 1.1: Settings for the boundary conditions of the simulations. All except 'Zmax' are set to 'electric ($E_t = 0$)'. 'Zmax' is set to 'open(add space)'.

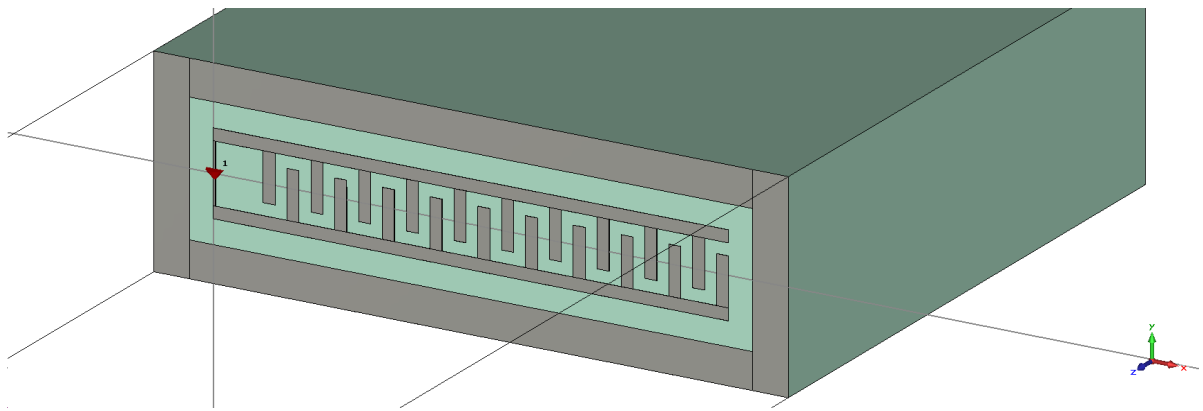


Figure 1.2: An example of a qubit design with the substrate in green, the metal parts in grey and the port indicated by the red cone. No lumped element representing the Josephson junction is present in the model.

Modeling

The qubit design can be imported to CST or created in CST itself. Figure 1.2 shows a qubit designed in CST. It includes two perfectly electrical conducting (PEC) pads connected by a discrete port. The pads must be modelled using their actual thickness in order to include the lossy layers on their sides. A discrete port can be added as follows:

- Under 'Simulation' click 'Discrete Port'.
- Now select the location in the model or input the coordinates numerically. Ensure that the discrete port connects the two PEC pads.
- Leave all other settings as default.

The pads are surrounded by a PEC ground sheet. For the determination of the capacitance, the inductor representing the Josephson junction should be omitted from the simulation.

Meshing

The default settings for the tetrahedral meshing can be used during calculation of the capacitance. This will yield a very rough initial mesh with few mesh elements and will ensure short simulation times.

Post processing

In the post processing templates window, the capacitance of the simulated structure can be retrieved;

- Under 'Post Processing' select 'Template Based Post Processing'.

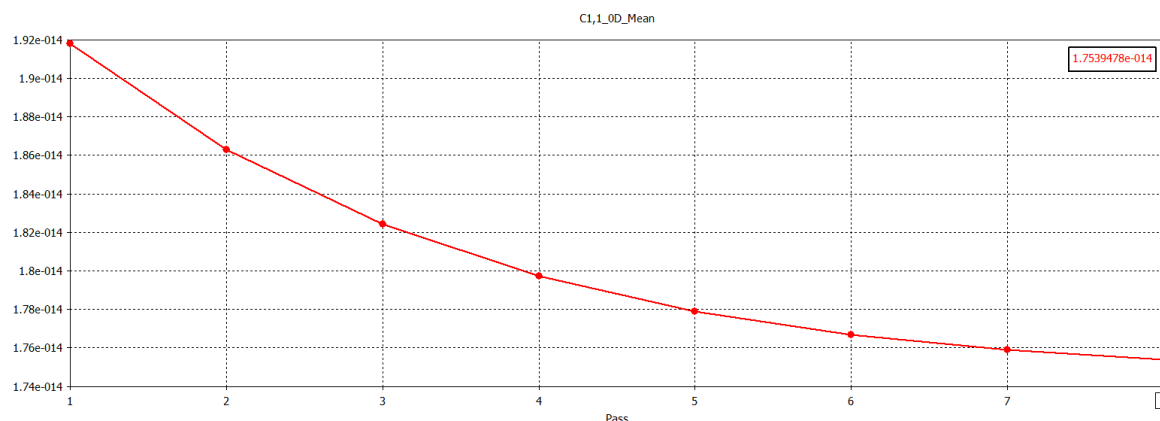


Figure 1.3: An example of the data retrieved on the capacitance of a qubit design. On the y-axis is the capacitance in Farad. On the x-axis is the number of mesh refinement passes. Highlighted is the value of the capacitance after 8 passes.

- In the pop-up window, in the first selection box choose '*S-Parameters*'.
- In the second selection box choose '*Z-parameter*'.
- In the pop-up window check the '*C*' option and click '*OK*'.

This will yield a 2D graph showing the capacitance of the structure as a function of frequency. Now include a second template;

- In the first selection box choose '*General 1D*'.
- In the second selection box choose '*0D or 1D Results from 1D Result (Rescale, Derivation, etc)*'.
- In the pop-up window select '*y at given x*' and set '*Evaluate at x =*' to the desired frequency. Click '*OK*'.

After simulation, the result should be a single value of the capacitance at the required frequency.

Simulation setup

To ensure convergence of the capacitance, results from the post processing templates can be used as targets for the simulation;

- Under '*Simulation*' choose '*Setup Solver*'.
- Under '*Adaptive mesh refinement*' make sure the '*Adaptive tetrahedral mesh refinement*' is checked and click '*Properties*'.
- In the pop-up window under '*Number of passes*' set the maximum to at least 8.
- Under '*Check after broadband calculation*:' mark the '*0D result Template...*' as active and select the 0D result of the capacitance from the post processing template above.
- Set the required Threshold and Checks as desired and click '*OK*'.

This will ensure the simulation keeps refining the mesh until your demands on accuracy are met or until maximum amount of mesh refinement passes is reached. After every mesh refinement pass the results are updated and can be checked. In the Navigation Tree click '*Tables*' → '*0D Results*' → '*C1,1_0D_yAtX*'. The first result will be viewable once the first pass of the simulation is completed. When the simulation is finished the capacitance of the structure can be extracted from the plot. An example is given in figure 1.3.

The electric field

Now that the capacitance of the structure is known the more extensive simulation of the electric field can be set up.

Modeling

Using equation (1.2) the inductance needed to reach a certain resonance frequency can be calculated.

$$L = \frac{1}{(2\pi)^2 f_0^2 C} \quad (1.2)$$

Where f_0 is the required qubit frequency and C its capacitance.

Now to include such an inductor;

- In the simulation menu add a '*Lumped element*'.
- Set the element '*Type*' to be '*RLC parallel*'
- Set the value of the inductance as calculated and leave the other values at zero.
- Make sure the '*Monitor voltage and current*' is checked.
- Set the location as desired or use picked points.

Next, to ensure a fine initial mesh, the edges on the side of the pads are rounded. In order to make this possible each pad must be a single object. To achieve this the '*Boolean*' operation can be used to combine multiple object into one;

- In the Navigation Tree, under '*Components*' select all objects pertaining to one pad.
- Under '*Modeling*' click '*Boolean*'.

Now that the pad consists of a single object, its side edges can be rounded.

- Under '*Modeling*' click '*Picks*' and choose '*Pick Edge Chain*' (or use Shift+E)
- Select all the edges laying in the xy -plane.

Figure 1.4 show what the selection should look like. Once the right edges are selected they can be rounded;

- Under '*Modeling*' click '*Blend*'.
- Set the '*radius*' to be half the height of the pad.

The result should be as in figure 1.4.

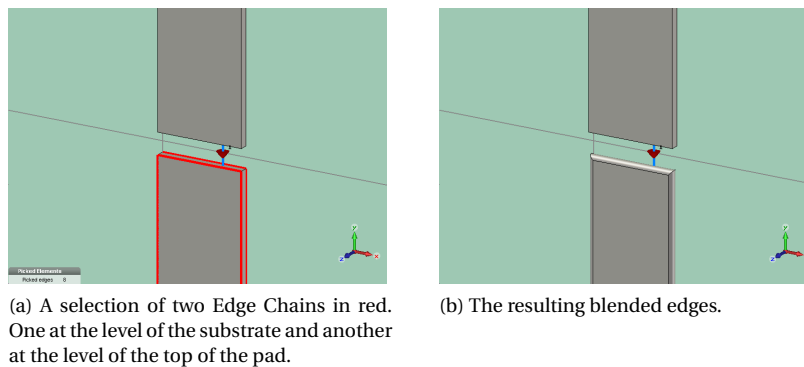


Figure 1.4: Before and after blending the edges

Meshing

In order to obtain a fine initial mesh the *Global mesh properties* can be changed;

- Under '*Simulation*' click '*Global mesh properties*'.
- In the pop-up window click '*Specials*'.
- Under the '*Mesh Control*'-tab set '*Smooth mesh with equilibrate ratio*' to around 1.15. Use this value to fine tune the number of mesh elements in the initial mesh.
- Set '*Normal tolerance*' to 1 degree.
- **Uncheck** the '*Anisotropic curvature refinement*'.
- Click '*OK*' and '*Update*' to see the resulting mesh.

Again, use the '*Smooth mesh with equilibrate ratio*' to tune the amount of mesh elements in the initial mesh. See figure 1.5 for the settings.

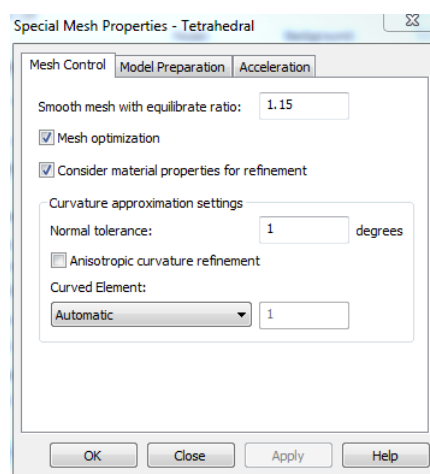


Figure 1.5: The required settings for the Mesh Properties. The Anisotropic curvature refinement must be unchecked!

Simulation setup

To be able to view and save field data, include a field monitor;

- Under '*Simulation*' click '*Field Monitor*'.
- In the pop-up window select the E-Field monitor and choose a frequency.
- Click '*OK*', the monitor should be visible in the Navigation Tree.

The simulation is now ready to run.

Exporting data

To calculate the participation ratio the simulated electric field is exported as an ASCII file. In order to separate data pertaining to different lossy layers the data for the field on the Pads, Substrate and Ground must be exported separately.

- In the Navigation Tree under '*Components*' hide all objects until only the Pads are visible.
- Again in the Navigation Tree open the '*2D/3D Results*' folder.
- Select the '*Abs*' component of the '*E-Field*'.
- Under '*Post Processing*' click '*Import/Export*' and click '*Plot Data (ASCII)*'.

Repeat these steps for the Substrate and Ground.

The last value needed from CST is the voltage over the Lumped element.

- In the Navigation Tree open '*1D Results*'.
- Open '*Lumped Elements*' and select '*Voltages*'.
- Select the element representing the Josephson Junction and extract the peak voltage at the resonance frequency from the graph.