The MATL programming language

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1 Introduction

MATL is a programming language based on MATLAB and suitable for code golf. The MATL language is stack-oriented. Data are pushed onto and popped out of a stack. Functions may take a number of elements from the stack (usually those at the top) and push one or more outputs onto the stack. Since the functions use data that's already present in the stack, reverse Polish notation (or postfix notation) is used.

This in line with other code-golfing languages, and allows more compact syntax for calling functions on data. To ease stack handling, values from the stack can also be copied and pasted using several clipboards. These are similar to variables in other stack-based code-golf programming languages.

The main goal in designing the language has been to keep it as close to MAT-LAB as possible. Think of it as MATLAB shorthand with data on a stack. MATL includes most commonly used MATLAB functions. It should be very easy for a MATLAB user to start programming in MATL within minutes.

1.1 The name

"MATL" / mæt. // is pronounced to rhyme with "cattle".

The spelling is purposely *short* (few letters) and *unusual* (words ending in "-tl" are rare in English). This is intended to reflect the facts that

- the language has been designed for code golfing (*short* programs); and
- doing so requires some features that make it an weird/esoteric (unusual) language.

The name is written in capitals to follow MATLAB's official name, which is also all capitals. (Besides, that way it looks more important!)

1.2 Notation

This is how MATL code is displayed in this document: iXyD. Or sometimes with spaces for greater clarity: i Xy D.

```
MATLAB code is displayed like this: n = input(''); disp(eye(n)).
```

Auxiliary or "meta" stuff is typeset this way. This includes discussions as to why something has been done in a particular way, or things that remain to be done.

1.3 Examples

Here are some simple example programs, just to give an idea of MATL.

• Infinite loop that does nothing:

```
MATL: 'T]
MATLAB: while 1,end
```

• Get unique characters from an input string, maintaining their order:

```
MATL: j1X0H$u

MATLAB: unique(input('', 's'), 'stable')
```

• Same as above but done manually, that is, without using MATLAB's unique or its MATL equivalent u:

```
MATL: jtt!=XRa~)
MATLAB:
    s=input('', 's');s(~any(triu(bsxfun(@eq,s,s'),1)));
```

• First 10 Fibonacci numbers:

```
MATL: 1t8:"2$t+

MATLAB:
    x=[0 1];for n=1:10,disp(x(2)),x=[x(2) sum(x)]; end
```

2 The stack. Data types

The stack can be thought of as a vertical arrangement of elements. Those elements may be popped from the stack, pushed onto the top of the stack, or rearranged. Functions take stack elements as inputs, and push new elements as outputs.

Any element contained in the stack will be an *array* of one of the following types:

- Numerical arrays;
- Logical arrays;
- Character arrays;
- Cell arrays.

Either of these arrays can be 2D or multidimensional. As in MATLAB, arrays of one dimension are considered to be 2D arrays with size 1 in one of the dimensions. Numbers are considered 2D numerical arrays of size 1×1 .

2D numerical arrays are full or sparse. Their default class is double. MATL can work with all the other numerical classes. Conversion is done with a function corresponding to MATLAB's cast.

3 Statements and separators

A MATL program is divided into **statements**, **separators** and possibly **comments**.

A statement can be

- a literal;
- a function; or
- a control flow modifier (loops, conditional branches).

Literals can have a varying number of characters depending on their content. Functions and control flow modifiers consist of either

- one character (different from X, Y or Z); or
- two characters, the first of which is X, Y or Z.

Separators are sometimes needed to separate literals of the same type. For example, 12 means the number 12, whereas 1,2 means number 1 followed by number 2. Similarly, 'Padmé', 'Anakin' means string 'Padmé' followed by string 'Anakin', whereas 'Padmé''Anakin' would be interpreted as a single string containing an apostrophe between the two names (quotation marks within strings are duplicated, as in MATLAB).

Separators are not needed if the literals are of different type, such as numerical and logical: for example: T2 represents a MATLAB literal T (corresponding to true in MATLAB) followed by literal 2.

The character, (comma) is the standard separator. Blank spaces and new lines also serve as separators. For clarity (but not for code-golfing purposes!), it may

be convenient to display the program with spaces or line breaks inserted between statements.

Using several lines also allows inserting **comments** in MATL code. The convention is similar to MATLAB: % marks the start of a comment, and then everything until the end of the current line is considered to be a comment (that is, ignored).

4 Literals

Literals can be

- Numbers (equivalent to 1×1 numerical arrays)
- Numerical arrays, 2D (numerical vectors and matrices)
- Logical arrays, 2D (logical vectors and logical matrices)
- Character arrays, 2D (strings or 2D character arrays)
- Cell arrays, 2D

The effect of a literal statement is to push the element represented by that literal onto the top of the stack.

Literals correspond to one of the data types referred to in §2, but limited to 2D. It's not possible to define a multidimensional array directly as a literal (this limitation exists in MATLAB too). But it is possible, for example, to produce a 3D numerical array by concatenating several 2D arrays along the third dimension.

At any given time, the stack contents will consist of either literals or outputs produced by functions.

4.1 Numbers

Standard MATLAB formats are allowed, except that only j (not i) can be used for the imaginary unit, and only e (not E) can be used for exponents in scientific notation. Examples of valid number literals are 1.2, -.2j, 1., -1.2e3, +.25e-3j.

Characters used in number literals "stick" to each other. Therefore consecutive number literals may need a separator to avoid confusion. For example, 12 represents number 12 (1 sticks to 2), whereas 1,2 represents numbers 1 and 2. Similarly, 1+2 represents numbers 1 and +2 (+ sticks to 2), whereas 1+,2 represents number 1, function + and then number 2. On the other hand, 5.6e-7j24 is interpreted as number $5.6 \cdot 10^{-7}j$ followed by 24, even if no separator is included, because the first number literal is already complete when the j character is processed.

An exception to numerical characters sticking is that characters X, Y or Z always grab the following character to form a two-character statement. For example X123 represents function X1 followed by number literal 23.

j is interpreted as imaginary unit when used as part of literals, and as a function elsewhere. Again, a separator may be needed to avoid function j being interpreted as part of a literal. For example, 4j is a literal representing number 4j, whereas 4j, is a literal representing number 4 followed by function j. To get number $j = \sqrt{-1}$ use the number literal 1j (or the array [j]; see 4.2).

Complex numbers in general can't be introduced directly as literals; only real or imaginary numbers can. For example, 1+2j would be interpreted as literal 1 followed by literal +2j. (However, array literals allow infix operators, as discussed in §4.2; so [1+2j] would be interpreted as the complex number 1+2j.)

4.2 Numerical arrays

Notation is the same as in MATLAB: [1 2 3], [1,2,3], [1,2j;3e4,-.2e-5], [].

Colon notation can also be used: $[1:4;3 \ 7 \ 5 \ 8]$, $[1:2:5;0 \ 0 \ -1]$. For row vectors in colon notation the square brackets symbols may be omitted: .5:.5:10. In that case, a separator may be needed depending on what comes next.

The described infix colon notation can only be used in array literals. The colon symbol can also denote a function with similar meaning; but as happens for all MATL functions, it takes its inputs from the stack, and thus uses postfix notation. A separator is sometimes needed to distinguish which use of the symbol: is meant. For example, 5:8 is a numerical array literal as described above, whereas 5:,8 (or 5,:8) is the: function applied to number literal 5, followed by number literal 8.

j can be used to represent the imaginary unit within array literals. Thus [0 j] and [0 1j] are equivalent.

Operators can be used within MATL literals as in MATLAB, and they are interpreted as infix. For example, the literal [1/2 1+1/4] would define an array with the two numbers 0.5 and 1.25. Numerical arrays can also contain P, Y, N, which correspond to pi, inf and NaN respectively. These can only be used within array literals (but there are MATL functions to obtain those values outside array literals). Also, M and G can be used within arrays as shorthand for -1 and -1j respectively. For example, [1,2,j;Y,N,G] corresponds to [1,2,j;inf,NaN,-j].

Only arithmetic operators, numbers, as well as P, Y, N, M, G can appear within literals. Arrays cannot contain calls to MATLAB functions (for example, [cos(2); sqrt(3)] is not allowed).

The above is also valid for array literals entered from keyboard by means of the i (input) function, and for strings used as inputs to Yt (str2num).

Numerical array literals are full (as opposed to sparse). Although 2D sparse

Table 1: Characters that have special meaning within number literals or array literals. Italic text indicates meaning is the same as in MATLAB

Character	Numerical literals	[] or { } arrays
T, F	_	Logical values "true", "false"
Y	_	Infinity
N	_	Not a number
M, P, G	_	Numbers -1 , π , $-\sqrt{-1}$
j	In imaginary numbers	In complex numbers; number $\sqrt{-1}$
е	Exponent	Exponent
()	_	Grouping
& + - < > ^	_	Operators (infix)
	Decimal point	Decimal point; make element-wise
*, /	_	Matrix operations (infix)
\		Matrix operation (infix)
:	_	Colon operator
;		End row
=	_	In relational operators
[]		Array builders
		Grouping arrays
{ }	_	Cell array buliders
~	_	In relational operator; "not" operator

numerical arrays are supported, they cannot be introduced directly as literals.

Table 1 contains all characters that have *special meaning within number literals or array literals*. Note that outside array literals they have a different, possibly unrelated meaning.

It's important to define carefully what is permitted within arrays. For example: should these be allowed? [sqrt(1:3)], [cos(1) sin(1)], [path]. Allowing arbitrary MATLAB code within literals (that will be evaluated with eval) brings flexibility, but it's dangerous. For example, the literal [rmpath('C:\path\to\files')] would remove a folder from the path in MATLAB.

One possibility to prevent that unwanted behaviour is to check the array contents strictly: a numerical array is [...] with contents separated by commas/spaces and semicolons. Each content must be a number, a numerical array, or a character array (which will be interpreted as numbers); and content sizes must much to form a 2D array. That involves hard work when parsing the array. It's much easier to let MATLAB do that work (via the compiled code), which it does very well.

In fact, this problem already exists with MATLAB's input function: it evaluates what the user types, which is a dangerous thing to do. If the user

types $[\cos(1) \sin(2)]$ as input, evaluating that is probably fine. But what if they type addpath('c:\path\to\folder')?

Possible solutions have been discussed in Stack Overflow¹. The best approach seems to be: use regular expressions to detect function or variable names, but ignoring such names if they are within a string (for example, ['path' 115] should be allowed, and would be equivalent to 'paths). The key here is that the regular expression doesn't need to check if the array is well formed (for example, [[1 2; 3 4], [5 6]] is not well formed), because that can be done later by evaluating it in MATLAB, once evaluation has been deemed safe. The regular expression only needs to make sure the array doesn't contain any reference to variables or functions, excluding string contents (a string can safely contain anything).

The above applies also to checking the contents of cell arrays.

For safety, the input obtained from i (input) is also checked this way before being evaluated, as is the argument to XU (str2num) (even though MATLAB does not do this).

4.3 Logical arrays

T and F correspond to true and false respectively, and can be used for defining 2D arrays in MATLAB. So [T F T; F F T] or [T,F,T;F,F,T] define a logical 2D array.

For logical row vectors, the notation [T F T] or [T,F,T] can be simplified to TFT. A separator may be needed if a new logical array follows: TFT,TT. But it's not necessary in other cases: TFT3.5.

4.4 Character arrays

They are defined as in MATLAB. Quotation marks within strings need to be duplicated. Two example character arrays are 'I'm sorry, Dave' (a row character array, or string) and ['Deckard'; 'Rachael'] (a 2D character array).

Numbers or number arrays can be used as components of character arrays; and then they are interpreted as ASCII codes of characters (as in MATLAB). For example, ['My food ' [105 115] ' problematic'] is the same as 'My food is problematic'.

Strings (row character arrays) can also be defined using colon notation: for example, 'd':'j' is equivalent to 'defghij', and 'a':4:'z' is equivalent to 'aeimquy'. As in MATLAB, the first and last operands must be of type char.

¹http://stackoverflow.com/q/33124078/2586922

4.5 Cell arrays

They are defined as in MATLAB. Each cell can contain any of the preceding literals, or other cell arrays. An example cell array literal is {'Great-Crack', 'But seeds are not pods!', {1,2,3,'travel','swift','petal'}}.

5 Functions

Functions operate on the contents of the stack, and produce new contents that are popped onto the stack. Function outputs can be of any of the types introduced in §2.

Functions take their input data in the same order in which they are in the stack, that is, bottom to top. So for example 5,4/ gives the result 1.25. This applies even if the input data are not taken from the top. Consider for example a two-input function. As will be seen in §5.2, this could take its inputs from arbitrary positions in the stack, say from the top and three positions below. In that case, the element that is *lowest* in the stack will be the *first* input to the function.

Outputs are pushed to the stack in the order in which they are returned by the function. That is, if the function returns two outputs, the first output will be pushed first; and then the second, which will be left on top.

There are four types of functions:

- **Normal functions** take their inputs from the stack and push their outputs onto the stack. An important particular class of normal functions is that of **indexing functions**, which will be dealt with separately.
- **Meta-functions** take their inputs from the stack, and produce no output on the stack. They are used for modifying the behaviour of normal functions; specifically, for defining their numbers of inputs and outputs.
- **Stack rearranging functions** take a group of elements from the stack and rearrange them.
- Clipboard functions give access to the clipboards, which store values from the stack and push them back. They behave like variables.

Inputs used by normal functions and meta-functions are always consumed, that is, disappear from the stack. For stack rearranging functions or clipboard functions that's not necessarily the case.

5.1 Normal functions

Normal functions operate on stack inputs and produce outputs that are pushed onto the stack. A given function may accept a variable number of inputs and produce a variable number of outputs. The full list of normal functions is given in §8, and their detailed definitions appear in Appendix §A. Most MATL functions have a MATLAB equivalent. For example, MATL's u corresponds to MATLAB's unique. In MATL, each function has a minimum and maximum numbers of allowed inputs and outputs, usually the same as in MATLAB; but in addition *default numbers of inputs and outputs* are specified. Continuing with the example, u by default takes one input and produces one output. So if the top of the stack contains [1 1 2 3 2], the function u would produce [1 2 3]. The meta-functions \$ and # (see §5.2) can be used to change the number of inputs and outputs of a function.

In some cases there exists a variation of the MATL function that corresponds to another one with a certain argument input fixed. For example, MATL's Xu corresponds to MATLAB's unique(..., 'rows', ...).

MATL functions take inputs of the same data types as their corresponding MATLAB function. For example, in MATLAB numerical arrays can be added with character arrays or with logical arrays, and the result is a numerical array. Similarly, the MATL + function accepts these types of inputs and produces a numerical array as output. Thus T1+D would display a result 2 on screen (D by default displays the top of the stack), and T'a'T++D would display 99 (the character code for 'a' is 97).

Some normal functions simply push fixed, predefined literals onto the stack depending on their input. These are functions X0,...,Z9. Also, clipboards initially contain certain predefined values. The former are used mainly for strings (such as 'stable' or '@mean'), whereas the latter are used for numeric values (such as 2 or [0 -1 1]). These literals are used often, and calling the corresponding function requires less characters than actually typing the literal.

5.2 Meta-functions

Meta-functions are \$ and #. They are used for specifying, respectively, the number of inputs and outputs that will be used by the next function, whether it's a normal, stack rearranging or clipboard function. The input/output specifications done with meta-functions \$ and # are consumed (deleted) by the next normal, stack rearranging or clipboard function. If that function doesn't allow the specified number of inputs or outputs an error occurs. If a \$ or # specification is issued before the previous one has been consumed by a function, the new specification replaces the previous one.

The \$ meta-function **specifies the inputs** to be used by the next function. \$ takes as argument the top element of the stack, and consumes it. That element can be a *number* such as 3, or a *logical array* such as TTF. In the first case, the next function will use the three highest elements on the stack as inputs. In the second case, the logical values are interpreted as a logical index into the stack elements, starting from the top. So TTF\$ indicates that the function will use as inputs the

two elements below the top element.

If the \$ specification is a logical array which is not a vector, it is interpreted in *column-major* order, that is, it's implicitly linearized. Also, *leading* F values are ignored. Thus, both FTFT\$ and [F,F,F;F,T,T]\$ would be equivalent to TFT\$. This is in line with how MATLAB treats logical indices: they are automatically linearized and trailing false values are ignored. Note that here it's leading (not trailing) values that are ignored, because logical indexing into the stack is based on its top (not on its bottom): given ··· TF, the rightmost value (F) refers to the top; the value to its left (T) refers to the second highest element in the stack, etc.

Consider as an example the f function, which corresponds to MATLAB's find. The code [0,4,7,0]f would produce the output [2,3], just as find ([0,4,7,0]) in MATLAB. [0,4,7,0]1,2\$f would produce 2, corresponding to the two-input MATLAB call find ([0,4,7,0]). The same result could be obtained with [0,4,7,0]1TT\$f; and also with [0,4,7,0]1FFFTT\$f.

For an example with non-contiguous inputs, assume the stack contains, bottom to top, [0,4,7,0], 'abc', 1. Then after executing TFT\$f it will contain 'abc', 2.

The # meta-function **specifies the outputs** to be produced by the following function. # takes as input either a number or a logical array. If it's a number n, it indicates that the function will be called with n outputs. If it's a logical array, it indicates which of the possible outputs will be asked for from that function. For example, if the stack contains [0,4,7,0], 1 bottom to top, the code 2FTT#f will produce 4, 2, corresponding to $[^{\sim}, \text{col}, \text{val}] = \text{find}([0 4 7 0], 1)$ in MATLAB.

Again, logical arrays are interpreted in *column major order* when passed to #. However, in this case F values are *not ignored*. This is consistent with MATLAB's behaviour: [ii,~] = find([0 4 7 0]) and ii = find([0 4 7 0]) produce *different* results. In general, functions behave differently depending on the number of outputs with which they are called, regardless of whether some of those outputs will be ignored; and this is true even for ignored *trailing* outputs. Another example es the size function: s = size(eye(3)) produces [3 3], whereas [s,~] = size(eye(3)) produces 3. These would be done in MATL as 3Xyy and 3XyTF#y (Xy is eye, and y is size, which is called with one output argument by default).

This may be a little surprising. One tends to think that adding outputs to a function call won't affect the preceding outputs. But in some cases it does. So saying "Use the first output of find to obtain the result" is not strictly correct, because it's ambiguous: "Which first output? The one I get when calling the function with two outputs? With one output? ...?".

Note that, even if the function inputs can be taken from arbitrary positions of the stack (using \$ with a logical array), the outputs are always pushed onto the top of the stack.

When MATL processes a function, if no \$ or # specifications exist (for example, because they have been consumed by a previous function call), the default number of inputs or outputs is used for the current function. If \$ or # specifications are actually issued, they don't need to be right before the function. For example, there can be literals in between (but not another function, as it would consume those specifications). So, if the stack contains [0,4,7,0], 1, after executing TTF\$'abc'FTT#f it will contain 'abc', 4, 2.

To delete the specifications currently held by \$ or #, and thus have the next function apply the default values, use [] \$ or [] # respectively.

Another possibility would have been to define the language so that the number argument to \$ and # was interpreted as a bitmap indicating which inputs (and how many) are used. In other words, the number would be binary decoded and the result interpreted as a logical array. So 7\$ in this alternative definition would correspond to 3\$ or TTT\$ in the above definition: use as inputs the three highest elements, thus 111 in binary, which is number 7.

Pros of this alternative approach: most functions have three inputs/outputs or less, and this would thus result in more compact code (TFT\$ would become 5\$). Cons: (1) If a very large number of inputs were used the argument to \$ would become long. For example, MATLAB's cat often accepts a lot of inputs (maybe from a comma-separated list). 20 inputs would require number $2^{20} - 1 = 1048575$ as argument to \$. (2) Less natural semantics, specially for some stack rearranging functions.

So I think it's best to interpret integer numbers as number of inputs, and use logical arrays for bitmaps, as has been defined above. If desired, a number can be transformed into a logical vector corresponding to its binary expansion very easily (there's a function for that).

5.3 Stack rearranging functions

These functions rearrange the elements in the stack (by duplicating, moving, deleting, copying or pasting). They don't strictly have outputs; rather, they operate on the stack elements directly. Any # specification other than 0# will give an error (and specifying 0# is unnecessary).

- \mathbf{x} (delete). It can have an arbitrary number $n = 0, 1, 2, \ldots$ or a logical array as \$ specification; default is 1. It deletes the n top elements from the stack; or the elements specified by the logical array. For example, TTF\$ \mathbf{x} deletes the two elements below the top of the stack.
- w (swap). It can have an arbitrary number n = 0, 1, 2, ... specified to \$; by default 2. For n > 0 it swaps elements 1 (top) and n in the stack, leaving those in between intact. For n = 0 it does nothing. If the \$ specification is a logical array, the first and last indicated elements are swapped.

• t (duplicate). It can have an arbitrary number n = 0, 1, 2, ... specified to \$; by default 1. It copies the top n elements from the stack, and pastes them (without deleting them from their original positions) at the top of the stack, maintaining their order. For example, if the stack contains 'a', 'b', after 2t the stack will contain 'a', 'b', 'a', 'b'.

If a logical array is used as argument to \$, it specifies which elements should be copied, maintaining their relative order. For example, TTF\$t would copy the third- and second-highest elements and paste them at the top of the stack.

- b (bubble up). It can have an arbitrary number n = 0,1,2,... specified to \$; by default 3. It makes the *n*-th highest element "bubble up" to the top, shifting elements 1,..., n-1 one position down. For n = 0 it does nothing. If a logical array is used as argument to \$, the bubbling is done only for the indicated stack elements. For example, if the stack initially contains 'a', 'b', 'c', 'd' from bottom to top, TTFT\$b would leave the stack as 'b', 'd', 'c', 'a'.
- N (stack size). It pushes the number of elements that the stack currently has. It has no inputs (so the only allowed input specification would be 0\$, which is unnecessary anyway).

5.4 Clipboard functions

There are five clipboards (or arbitrarily many, depending on interpretation; more about that below). They are identified with the capital letters "H", ..., "L". Clipboards are used for copying from and pasting to the stack.

The first four clipboards behave as would be expected: they store values that can be retrieved later. Clipboard L is special: it consists of an arbitrarily large amount of "levels", and each level (beginning at 1) behaves as an independent clipboard. Thus clipboard L is actually an "infinite" collection of clipboards. Compared with clipboards H, ..., K, copying and pasting with clipboard L requires at least one extra character (to specify level), as will be seen.

Access to the clipboards is provided by means of the following functions:

• XH, XI, XJ, XK (copy to specified clipboard): copy a number of elements from the stack to one of the clipboards, without removing them from the stack. These functions have an arbitrary number of inputs 0,1,2..., and no outputs. How many or which elements should be copied to the given clipboard is specified with \$. For example, 2\$XH indicates copy the two top elements to clipboard H; and TF\$XH indicates copy the element right below the top. By default the top element is copied, corresponding to 1\$.

Copying elements to a clipboard removes its previous contents.

If the argument to \$ is 0, or a logical array containing only F values, the copying functions clear the clipboard contents.

- H, I, J, K (paste from specified clipboard): paste copied elements onto the stack, in the same relative order in which they originally were. The argument to # indicates which elements should be pasted, among those that the clipboard currently contains. By default all contents of the clipboard are pasted. These functions have no inputs.
- XL (copy to some level of clipboard L): behaves like H, but takes one last additional input that specifies the level used within clipboard L. The default number of inputs is 2. So 1XL (or 1,2\$XL, or 2\$1XL) copies the top of the stack to clipboard L, level 1. The input that specifies the level is automatically converted to double. So TXL would do the same thing.

As usual, a logical array can also be used as argument \$. If the stack contains from bottom to top 'a', 'b', 'c', the code TTFT\$4XL copies 'a', 'b' to clipboard L4 (note that the last T refers to 4, which specifies the level).

• L (paste from some level of clipboard L): behaves like XH, but takes as input one number that specifies the level used within clipboard L.

As can be seen from the above, clipboards H, I, J, K provide easier access (fewer characters) than clipboard L. In many cases four clipboards will be enough. On the other hand, clipboard L provides extended capabilities if needed, at the cost of at least one extra character to specify the level.

Clipboards H, I, J and K, as well as the first levels of clipboard L, initially contain the values indicated in Table 2.

Using for example H instead of 2 may be useful to avoid separators (commas or spaces) if that 2 is surrounded by other numbers. Values 0 and 1 can be obtained with functions 0 and U (which correspond to zeros and ones respectively; by default the take no inputs and produce a single number as output).

Clipboard L only has 12 levels initially (necessary to hold the initial contents specified in Table 2). Higher levels are created at run-time *on the fly*. For example, copying some elements to level 14 will cause MATL to create levels 13 and 14: level 13 will be empty, and level 14 will hold the copied elements. Trying to paste from level 15 gives an error, because that level doesn't exist; but level 13 now exists, and is empty. Therefore 13L is valid code, and does nothing. 0#13L is also valid, but 1#13L (or even F#13L) is not, because a non-existent first element in level 13 is being referenced.

Clipboard L effectively provides an infinite amount of "variables", but requires more characters compared with variables in other languages such

Table 2: Initial content of clipboards

Clipboard	Contents
Н	2
Ι	3
J	1j
K	4
L, level 1	[1 0]
L, level 2	[0 -1 1]
L, level 3	[1 2 0]
L, level 4	[2 2 0]
L, level 5	[1 -1j]
L, level 6	[2 0]
L, level 7	[1 -1j 0]
L, level 8	[1 3 2]
L, level 9	[3 1 2]
L, level 10	3600
L, level 11	86400

as CJam. Clipboards H, I, J and K use less characters. Why only four such clipboards? The main reason is that MATLAB has a lot of "high-level" vectorized functions compared with other languages. It's desirable to have many of those functions in MATL, and that requires reserving a significant part of character space for them, at the expense of clipboards/variables. Also, characters should be reserved in order to be able to include new functions in the future.

Also, I have a feeling that true stack-oriented programming should use as few variables/clipboards as possible, and that four clipboards are enough in almost all situations. For problems when that's not the case, one can use clipboard L with a small penalty in number of characters.

Clipboard L starts at level 1, not 0, to match MATLAB indexing. This is important for debugging. The MATL debugger makes use of MATLAB's debugging capabilities to show relevant variables. Therefore the first level of clipboard L will be shown (by MATLAB) as 1, not as 0. A less important, more subtle advantage is that this makes the above mentioned implicit conversion to double unnecessary: characters are converted implicity by MATLAB, and true used as a logical index has the same effect as the integer index 1; whereas false wouldn't have the desired effect of selecting the first (0-th) level.

5.5 Indices and indexing functions

Indexing with **round brackets** is used in MATLAB for accessing array's contents and cells of a cell array. In MATL the indexing functions (and) are used for that.

Indexing with **curly braces** in MATLAB is used for accessing cell's contents in a cell array. The MATL indexing functions X (and X) are used for that.

Like in MATLAB, indexing in MATL can be used for two purposes: **referencing** elements from an array, or **assigning** values to elements of an array. For example, in a(2,:) = b(1,:), reference indexing is being used for b, and assignment indexing is being used for a.

The four basic indexing functions in MATL are thus:

-) round-bracket reference indexing;
- (round-bracket assignment indexing;
- X) curly-brace reference indexing;
- X(curly-brace assignment indexing.

Also, there are two additional functions that correspond to MATLAB's reference indexing with colon:

- Y) round-bracket reference indexing with colon;
- Z) curly-brace reference indexing with colon.

I find it more natural to use a closing parenthesis) for reference indexing and an opening parenthesis (for assignment indexing. The latter suggests "opening" the array so it can accept new contents.

) takes an arbitrary number of inputs 2,3,4,..., by default 2. The first input is the array to be indexed, and the others are interpreted as indices into that array. For example, a(2,[1 3 4]) would be done in MATL, assuming a is currently at the top of the stack, as 2[1,3,4]3\$). The three inputs would be consumed, and the indexed array a(2,[1 3 4]) would now occupy the top of the stack.

The indices can be integer-valued or logical. For example, 2[1,3,4]3\$) would be equivalent to 2TFTT3\$). As in MATLAB, a logical index need not have the same size as the dimension it's indexing into. a(2,[true false true true]) works even if size(a,2) is greater than 4. In general, trailing false (or F) values are ignored.

To allow end-based indexing, the following convention is used in MATL: whenever an array used as index has 3 or less elements and at least one of them has zero real part it is interpreted as and end-based index. An imaginary value such as -2j corresponds to end-2, and colons are implicitly assumed between the two or three values of the array. So, for example,

- [2,-1j] (or [2, J]; see §4.2) represents 2: end-1.
- [-.5j,2,0] represents end/2:2:end.
- [1,0] represents 1: end, that is (:).

These end-based indices can be used in MATL as any other index. For example, a(2,:) would be realized in MATL, assuming the top of the stack contains a, as 2[1,0]3\$) (or 2,1L,3\$), using the fact that 1L by default produces the literal [1,0]; see Appendix §A).

I had initially dropped the idea to include end-based indexing because it seemed complicated: MATLAB's end is used within an array, and the known size of that array determines its meaning. But MATL's stack-oriented character and absence of infix notation means that the end-based array needs to be pushed onto the stack by itself, and exist independently of whichever array it will end up indexing into.

But I picked it again following a discussion with @beaker. I came up with the idea that the imaginary unit can be used as an "end label", which is left unresolved until an indexing function such as) establishes its relationship with a specific array.

Common end-based indexing expressions are predefined as initial contents of clipboard L; see Table 2).

The order of inputs used by): "destination", "data", "indices" naturally adapts to processing in a loop: in each iteration some processing is done, resulting in the data to be assigned to a destination array that was previously pushed onto the stack. The index of the assignment is then popped onto the stack and (is called.

Of course, the inputs to (and) can be specified by logical arrays (TTT\$) instead of numbers (3\$).

X) is analogous to), but corresponds to MATAB's {...} reference indexing. It takes an arbitrary number of inputs 2, 3, 4, ..., by default 2. The first input should be a cell array, and the others are interpreted as indices into that cell array. The indices can be integer or logical values. The result of that indexing in MATLAB would be a comma-separated list of the indexed cell's contents. In MATL, each element of that list is pushed onto the stack in the indexing order.

X(is similar to (, but corresponds to MATAB's $\{...\}$ assignment indexing; and has some differences. In MATLAB, an assignment like $a\{[1,2]\} = ...$ can be done in two ways:

- [a{[1,2]}] = b{[2001,2010]} (comma-separated list generated from a cell array on the right-hand side);
- [a{[1,2]}] = deal('Follow the white rabbit', '101') (deal on the right-hand side).

The first is actually equivalent to (...) indexing: it can be done as a(...) = b(...) or, more generally, a(...) = reshape(b(...),...). The second makes more sense for MATL, is actually what X(does).

Considering two indices for greater generality, a typical assignment of this type might be, in MATLAB, [a{[1,2],[3,4]}] = deal({'Mostly harmless', [],42,5}). In MATL it's done as follows. X(takes as inputs, in this order: a destination cell array (corresponding to a), an arbitrary number of data (4 in this case), an arbitrary number of indices (2 in this case) that define the exact destination of those data within the cell array, and a number that specifies how many indices exist. So in this case 8 inputs should be specified for X(. If the stack contains, bottom to top: destination cell array, 'Mostly harmless', [], 42, 5, [1,2], [3,4], 2, then 8\$X(does the assignment.

The reason why the number of indices needs to be specified as an additional input is to avoid ambiguities with end-based indexing. Suppose the number of indices were not specified, and consider the following inputs to X(: destination cell array, 'Mostly harmeless', [], 42, 5, [1,0] (note that the latter is an index interpreted as 1:end). The destination cell array, (a), initially has size $2 \times 1 \times 2$. In these conditions, there are *two* possible interpretations for the assignment: either [a{1:end}] = deal({'Mostly harmless',[],42,5}) (assign four values, using linear indexing) or [a{42,5,1:end}] = deal({'Mostly harmless',[]}) (assign two values along the third dimension).

This ambiguity occurs only because of end-based indexing. With integer-valued or logical indices, interpreting one input as index instead of data would increase or maintain the number of indexed positions in the destination array, while at the same time would reduce the amount of available data, so there would only be (at most) one valid possibility.

Having to specify the number of indices is not very nice, specially compared with (, where it's not needed. But it seems unavoidable. And after all, MATLAB also requires deal in this case, which is not needed in round-bracket assignments.

According to the above, the minimum number of inputs for X(would be 4: destination array, at least one data element, at least one index, and number of indices. The most common case is probably that of a single data element and a

single index. To alleviate notation in this case, this can be realized with only 3 inputs, omitting last one specifying the number of indices. That is, when X(is used with 3 inputs they are interpreted as destination array, one data element and one index. This is the default number of inputs for X(. Any other number above 3 is also allowed, and in that case the last input tells the number of indices.

What a mess! Couldn't this X (stuff have been made simpler?

I would have liked to, but I haven't found a way to make curly-brace assignment simpler while keeping consistence with \$ semantics. MATLAB notation [a{ind1,ind2}] = deal(data1, data2, data3, ...) is not terribly simple to begin with; and having everything in a stack can sometimes obscure things a bit (although of course it has other advantages).

In many cases the assignment will be to a single cell with a single index (a{ind} = data). In MATL that case is simple indeed, and totally analogous to round-bracket indexing: push a, then val, then ind, and X (will do the assignment. In the more general case one only has to remember to include the number of indices as a final input.

All in all, notation may get a little complicated in the general case. On the positive side, some people consider code obfuscation to be, well, a good thing... specially in a weird/esoteric language worth that name!

On a more serious note, MATL indexing supports integer/logical indexing; multidimensional/linear/partially linear indexing; curly braces (cell contents) and round brackets (cells, standard arrays); reference (getting values from an array) and assignment (putting values into an array); all working on a stack. I hope notation is just about as complicated as it needed to be.

- Y) takes an input array and applies MATLAB's (:) reference indexing. This has the effect of linearizing the array into a column. The number of inputs and outputs is 1. For example, [1,2;3,4]Y) would replace the input array [1,2;3,4] by [1;3;2;4].
- Z) takes one input, which must be a cell array, and applies MATLAB's {:} reference indexing. This has the effect of "unboxing" the cell array, that is, it produces its contents (in column-major order), which are pushed onto the stack. The output specification for Z) can be arbitrary, and controls how many or which of the input contents are pushed onto the stack. By default all contents are pushed. For example, {{'Gödel' 'Escher' 'Bach'} 'Hofstadter' 1979} Z) would consume the input cell array and push onto the stack, in this order: cell array {'Gödel' 'Escher' 'Bach'}, string 'Hofstadter', and number 1979.

6 Control flow: conditional branches and loops

6.1 Conditional branches: "if...else"

An "if" branch is begun with ?, ended by], and can optionally contain }. These correspond to MATLAB's if, end and else respectively. ? pops (consumes) the top array from the stack, and the statements until } or] are executed if the real part of that array has all nonzero elements (as in MATLAB). Otherwise the statements between } and], if any, are executed.

6.2 Loops: "for", "do... while" and "while"

A "for" loop is begun by " (double quotation symbol) and ended by]. The statement "takes (consumes) the top array from the stack. That element array is split into pieces, namely the columns of the array (or in general second-dimension slices, like MATLAB's for); and those pieces are iterated on (loop variable). In each iteration, all statements until] are executed. The current piece of the array can be obtained with the statement ©; see below. The loop normally ends when all pieces have been iterated on. However, statements . (conditional break) and X. (conditional continue) can modify this behaviour, as will be discussed later.

A "do... while" loop is begun by ' (back tick) and ended by]. A "do... while" loop is different from MATLAB's "while" loop in that the loop condition is evaluated at the end, not at the beginning. MATL initially executes all statements between ' and]. It then takes (consumes) the top array of the stack and checks if its real part has all nonzero elements (like MATLAB's while does). If so it goes back to the beginning of the loop; else it exits the loop. As an example, 10'1-t] counts from 9 down to 0. Statements . and X. can also be used in "do... while" loops. @ in this type of loops pushes the current iteration index.

A "while" loop is begun by X and ended by]. In this case the loop condition is evaluated at the beginning, as happens with MATLAB's while loops. Statements . and X. can also be used, and @ pushes the current iteration index.

The statement ⁰ within a "for" loop pushes the current value of the loop variable, that is, the current part of the array that is being iterated on. Within a "do…while" or "while" loop it pushes the current iteration index, starting at 1. The output of ⁰ is that corresponding to the *innermost* loop.

The statement . takes (consumes) the top of the stack. If the real part of that array has all nonzero elements (as in MATLAB's if), the innermost "for", "do... while" or "while" loop is exited. Similarly, X. takes (consumes) the top of the stack, and if the real part of that array has all nonzero elements, the current iteration of the innermost loop is ended, and the loop proceeds with the next iteration, if any.

Statements] at the very end of the program can be omitted; see §7.

I initially defined MATL with "for" and 'while" loops only, as in MAT-LAB. But I realized that all "while" loops I was writing had a T before to force the loop code to be executed at least once. So I introduced "do…while" loops.

7 Initial and final implicit actions

When a MATL program is run, it begins with format compact, format long, warning('off', 'all'). The seed of the random number generator is set using rng('shuffle').

If a file called defin exists when program execution is started, its contents are read in as bytes and converted to char type. A string (row vector of characters) containing all those values is pushed onto the stack before the first program statement is executed. (There is also a function for manually reading a file; see §8).

At the end of the program, any loops or conditional branches that have not been ended by a corresponding] statement are implicitly ended. That is, as many] as needed are implicitly included after the last (explicit) statement in the source code.

After that, the display function XD is implicitly called. This function (see §8 and §A) by default takes each element from the stack, converts it to string and prints it on screen. Cell array inputs are unboxed and their contents are displayed in linear order. Nested cell arrays are allowed. For example, consider that the stack contains two elements: number 1 and the cell array {'aa' {3 4; 5 6}}. Then the displayed values will be, in this order: 1, aa, 3, 5, 4, 6.

The number of inputs for the implicit display function can be modified by one final call to \$. For example, to display only the top of the stack specify 1\$ at the end of the program. To prevent the implicit display function from displaying any stack contents use 0\$ (or empty the stack).

All screen output generated by the program is saved to a text file called de fout. This file is overwritten if it previously existed. (There is also a function for manually writing to a file; see §8).

When the program finishes, the original MATLAB warning state is restored.

Is there anything else that should be defined as initial conditions? Set digits to a large value such as 50 (for vpa)?

8 Table of functions

Table 3 shows the set of MATL functions, as well as control flow modifiers, separator and comment characters. The detailed definition of each function appears in Appendix §A.

The table is under development. Functions may be added, removed, or changed.

e and j, when used as a functions, may need a separator to isolate them from a preceding number.

Similarly:, when used as a function, may need a separator to prevent it from being interpreted as part of a colon numerical vector.

Most MATL functions correspond to MATLAB functions. These have been selected based on perceived most common use. They include @Divakar's list², and most functions from a list by Mathworks³.

In some cases the MATLAB function has been extended or slightly modified. This is indicated in the function description of Appendix §A.

All MATLAB operators supported by **bsxfun** have automatic singleton expansion in MATL.

Most strings that are used as inputs to functions (for example, 'stable' option for unique) can be produced by calling one of the functions X0...Z9 with a numeric input. See §A for details.

Table 4 summarizes function behaviour regarding their consumption of inputs and of input/output specifications.

Some functions I didn't include, and the reasons why:

- true, false functions; they can be done with zeros and ones (which is included) followed by conversion to logical or by negation (each is just one character).
- ipermute: I don't think it's used often; and can be substituted by permute.
- ndims: it can be realized in two characters with size followed by
- length. I followed @chappjc's advice⁴: "Never use length. Ever."
- I initially thought it would be cool to have function equivalent to eval in MATL. But it would be hard to implement, and probably not very useful anyway.
- cellstr: function mat2cell(x, ones(size(x,1),1), size(x,2),
 ..., size(x,ndims(x))) exists. It's a generalization of cell2str
 that also works for numeric and logical values, and for any number of
 dimensions.
- shiftdim: it seems unnecessary with permute.
- clock: it seems unnecessary when now is available.

²http://stackoverflow.com/users/3293881/divakar

³http://es.mathworks.com/help/matlab/functionlist.html

⁴https://web.archive.org/web/20150915161950/http://stackexchange.com/users/3302774/chappjc

Table 3: Table of MATL statements

	X	Y	Z
separator	rot00	evetem	f. II
.' (transpose) / permute	rot90 repmat	system repelem (run-length decoding)	full
enacify outputs	reprilat		blanks fopen, fwrite, fclose
specify outputs		rng	
specify inputs	alass	char(vpa())	fopen, fread, fclose
comment	class	cast	typecast
and	intersect		bitand
Not used. String delimiter		run-length encoding	now
ound-bracket assignment indexing	curly-brace assignment indexing		
ound-bracket reference indexing	curly-brace reference indexing	linearize array	comma-separated list
<u>*</u>	kron	matrix product	Cartesian product
l	conv	conv2	convmtx
separator	cos	sin	tan
•	setdiff	deconv	
break	continue	pause	bitget
J.	angle	matrix /	unwrap
Not used	predefined literals	predefined literals	
Not used	predefined literals	predefined literals	
Not used	predefined literals	predefined literals	
Not used	predefined literals		
Not used	predefined literals		
Not used	predefined literals		
Not used Not used	predefined literals		
Not used	predefined literals		
	predefined literals		
Not used			
Not used	predefined literals	gallony	hitoot
colon (function)	0000	gallery	bitset
	acos	asin	atan2
<	min	cummin	
=	isequal	strcmp	strncmp
>	max	cummax	
t e			sparse
push "for" value / "while" index		perms	randperm
all		dec2base. Larger base, any symbols	base2dec. Larger base, any symbols
ogical(dec2bin()-'0')	bin2dec(char(+'0'))	dec2bin	bin2dec
	histcounts	im2col	
disp(num2str(,))	disp(num2str())	sprintf / fprintf	disp
Not used. False (literal)		format	
	plot	image	colormap
Paste from clipboard H	Copy to clipboard H		
Paste from clipboard I	Copy to clipboard I		
Paste from clipboard J	Copy to clipboard J		
Paste from clipboard K	Copy to clipboard K		
Paste from level of clipboard L	Copy to level of clipboard L		
adio nomiovoi di dipodara E	copy to level of emparative		
stack size		NaN	isnan
zeros	datestr	datenum	datevec
	flipud		pdist2
flip	ilipud	pi	polyval
			polyvai
rin	triu/ 1)	teil	teil/ 1)
	triu(,1)	tril	tril(,-1)
sort	triu(,1) sortrows	circshift	tril(,-1) sign
sort Not used. True (literal)	sortrows	circshift toeplitz	
sort Not used. True (literal)		circshift	
sort Not used. True (literal)	sortrows	circshift toeplitz	
sort Not used. True (literal) str2double	sortrows str2num	circshift toeplitz num2str	
sort Vot used. True (literal) str2double Vot used	sortrows	circshift toepiliz num2str regexprep	sign
sort Vot used. True (literal) str2double Vot used Vot used Vot used	sortrows str2num	circshift toeplitz num2str	
sort Not used. True (literal) StrZdouble Not used Vot used Vot used	str2num regexp	circshift tioeplitz num2str regexprep inf	sign
sort Not used. True (literal) str2double Vot used Not used Not used Not used Not used. Not used.	sortrows str2num regexp ind2sub	circshift toeplitz num2str regexprep inf floor	sign
sort Not used. True (literal) strzdouble Not used Vot used Vot used Vot used. Vot used. Array delimiter mod	sortrows str2num regexp ind2sub mod(1)+1	circshift toeplitz num2str regexprep inf floor matrix \	sign
sort Not used. True (literal) strzdouble Not used Vot used Vot used Vot used. Vot used. Array delimiter mod	sortrows str2num regexp ind2sub	direshift toeplitz num2str regexprep inf floor matrix \ ceil	sign
sort Vot used True (literal) str2double Vot used	sortrows str2num regexp ind2sub mod(1)+1	circshift toeplitz num2str regexprep inf floor matrix \	sign
sort Vot used True (literal) str2double Vot used	sortrows	direshift toeplitz num2str regexprep inf floor matrix \ ceil	sign
sort Vot used True (literal) str2double Vot used Vot used Vot used Vot used Vot used Not used and and anary minus onwhile	sortrows	direshift toeplitz num2str regexprep inf floor matrix \ ceil	sign
sort Not used. True (literal) strzdouble Not used Not used Not used Not used Not used. Array delimiter mod and (loops or conditional branches) A unary minus 10while any	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix ^ tic	Sign Sinf
sort Not used. True (literal) strzdouble Not used Not used Not used Not used Not used. Array delimiter mod and (loops or conditional branches) A unary minus 10while any	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix ^	Sign Sinf
sort Vot used. True (literal) str2double Not used Vot used Vot used Vot used. Array delimiter mod end (loops or conditional branches) A unary minus dowhile supple	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix ^ tic	Sign Sinf
sort Not used. True (literal) strzdouble Not used Not used Not used Not used Not used not used. Array delimiter mod and (loops or conditional branches) Anary minus towhile any bubble char liff	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while	circshift toeplitz num2str regexprep inf floor matrix \\ ceil matrix \^ tic strsplit	sign isinf toc
sort Not used. True (literal) strzdouble Not used Not used Not used Not used Not used not used. Array delimiter mod and (loops or conditional branches) Anary minus towhile any bubble char liff	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat	circshift toeplitz num2str regexprep inf floor matrix \ ceil mt tic strsplit strcat	sign isinf toc strjoin
sort Not used. True (literal) str2double Not used ond (loops or conditional branches) and (loops or conditional branches) unary minus dowhile any bubble thar siff reshape / squeeze	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat	circshift toeplitz num2str regexprep inf floor matrix \ ceil mt tic strsplit strcat	sign Isinf toc strjoin qod
sort Not used. True (literal) str2double Not used Not used Not used Not used. Not used. Array delimiter mod end (loops or conditional branches) A unary minus towhile any bubble char diff eshape / squeeze lind	sortrows str2num regexp ind2sub mod(1)+1 sub2md sqrt while cat diag	circshift toeplitz nuni2str regexprep inf floor matrix \ ceil matrix \ tic strsplit strcat bikdiag	sign Isinf toc strjoin qod
sort Not used. True (literal) str2double Not used Not used Not used Not used Not used Not used and loops or conditional branches) on, while any bubble char diff eshape / squeeze ind ogical	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind	circshift toeplitz nuni2str regexprep inf floor matrix \ ceil matrix \ tic strsplit strcat bikdiag	sign isinf toc strjoin god exp
sort Not used. True (literal) str2double Not used not used. Array delimiter mod and (loops or conditional branches) A unary minus dowhile any pubble har liff reshape / squeeze ind ogical norizeat	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ tic strsplit strcat blkdiag factor	sign isinf toc strjoin god exp gammain
sort Not used. True (literal) strzdouble Not used Not used Not used Not used Not used. Array delimiter mod end (loops or conditional branches) A unary minus 10while any bubble char lift eshape / squeeze ind ogical orzcat pput	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid (,.)	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ tic strsplit stroat blkdiag factor hankel	sign isinf toc strjoin god exp gammain
sort Vot used. True (literal) str2double Vot used Vot used Vot used Vot used Vot used vot used and (loops or conditional branches) anay minus to., while any usuble bhar iff eshape / squeeze ind ogical iorzcat rput nput mput mput mput mput mput mput mput m	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {} urlead real	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix ^ ttc strsplit streat blikdiag factor hankel imread	sign isinf toc strjoin qcd exp gammain hypergeom
sort Not used. True (literal) str2double Not used Not used Not used Not used Not used. Array delimiter mod end (loops or conditional branches) \(\(\lambda \) unary minus 10\(\text{mile} \) unary minus 10\(mil	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid () uriread real upper	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ itc strsplit strcat blkdiag factor hankel imread imag	sign isinf toc strjoin god exp gammain hypergeom
sort Not used. True (literal) str2double Not used one dicops or conditional branches) anary minus dowhile any bubble char siff reshape / squeeze find ogical norzcat input nput nput,s') ower ones	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {} urlead real	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix ^ tic strsplit strcat blkdiag factor hankel imread imag log. With two inputs, specifies base mean	sign isinf toc strjoin qcd exp gammain hypergeom
sort Not used Vot use	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid (,) urlread real upper abs ismember(,'rows')	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix ^ tic strsplit strcat blkdiag factor hankel imread imag log. With two inputs, specifies base mean	sign isinf toc strjoin god exp gammain hypergeom conj
sort Not used. True (literal) str2double Not used Not us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sugrt while cat diag strfind ndgrid () urfread real upper abs ismember(,'rows') nchoosek	circshift toeplitz nuni2str regexprep inf floor matrix \ ceil matrix \ tic strsplit strcat blictiag factor hankel immead imag log. With two inputs, specifies base mean interp1	sign isinf toc strjoin god exp gammain hypergeom conj
sort Not used. True (literal) Str2double Not used No	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid (,) urfread real upper abs ismember(, 'rows') nchoosek uint64	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ dic strsplit stroat blkdiag factor hankel imread imread imag log, With two inputs, specifies base mean interp1 round	sign isinf toc strjoin gcd exp gammain hypergeom conj log2 lcm
sort Vot used. True (literal) str2double Vot used vot us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid (,) uurfread real uupper abs inchoosek uint64 cumprod	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ tic strsplit strcat blkdiag factor hankel imread imag log. With two inputs, specifies base mean interp1 round primes	sign isinf toc strjoin god exp gammain hypergeom conj
sort Not used. True (literal) str2double Not used literal sort used not used not used not used not used not used not used literal sort used litera	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {} urlread real upper abs ismember(,rows') nchoosek uint64 cumprod quantile	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ tic strsplit stroat blkdiag factor hankel imread imag log. With two inputs, specifies base mean interp1 round primes n-th prime	sign isinf toc ttripin gcd exp gammaln hypergeom conj log2 lcm fix isprime
sort Not used Vot use	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {} urlread real upper abs ismember(,rows') nchoosek uinif64 cumprod quantilie randn	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ it it strsplit strcat blkdiag factor hankel imread imag imag imag interp1 cound primes n-th prime randi	sign isinf toc strjoin gcd exp gammain hypergeom conj log2 lem fix isprime randsample
sort Vot used. True (literal) str2double Vot used Vot us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {} urlread real upper abs ismember(,rows') nchoosek uint64 cumprod quantile	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ tic strsplit stroat blkdiag factor hankel imread imag log. With two inputs, specifies base mean interp1 round primes n-th prime	sign isinf toc strjoin qcd exp gammaIn hypergeom conj log2 lcm fix isprime randsample std
sort Not used. True (literal) strzdouble Not used Not us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid (,) urlread real upper abs ismember(, 'rows') nchoosek uinif64 cumprod quantile randn sum(, 1,)	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ it it strsplit strcat blkdiag factor hankel imread imag imag imag interp1 cound primes n-th prime randi	sign isinf toc strjoin qcd exp gammain hypergeom conj log2 lcm fix isprime randsample std strrep
sort Vot used. True (literal) str2double Vot used vot used Vot used vo	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {} urlread real upper abs ismember(,rows') nchoosek uinif64 cumprod quantilie randn	circshift toeplitz nuni2str regexprep inf floor matrix \ cell strsplit strcat blkdiag factor hankel immead imag log. With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum	sign isinf toc strjoin god exp gammain hypergeom conj log2 lcm fix isprime randsample stid strrep strjust
sort Vot used. True (literal) strzdouble Vot used Indicate (literal) Vot used Vot u	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid (,) urlread real upper abs ismember(, 'rows') nchoosek uinif64 cumprod quantile randn sum(, 1,)	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ it it strsplit strcat blkdiag factor hankel imread imag imag imag interp1 cound primes n-th prime randi	sign isinf toc strjoin qcd exp gammaln hypergeom conj log2 lcm fix isprime randsample std strep
sort Vot used. True (literal) str2double Vot used vot us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {,} urfread real upper abs ismember(, rows') nchoosek uint64 cumprod quantile randn sum(, 1,) unique(, 'rows') unique(, 1,)	circshift toeplitz nuni2str regexprep inf floor matrix \ cell strsplit strcat blkdiag factor hankel immead imag log. With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum	sign isinf toc strjoin god exp gammain hypergeom conj log2 lcm fix isprime randsample stid strrep strjust
sort Not used. True (literal) str2double Not used Not us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sgrt while cat diag strfind ndgrid () urfread real upper abs ismember(,'rows') nchoosek uin164 cumprod quantile randn sum(1,) unique(1,) unique(1,)	circshift toeplitz numizstr regexprep inf floor matrix \ ceil fstroat blkdiag factor hankel inread imag log. With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum	sign isinf toc strjoin god exp gammain hypergeom conj log2 lcm fix isprime randsample stid strrep strjust
sort Not used. True (literal) str2double Not used not used. Array delimiter mod and (loops or conditional branches) A unary minus dowhile any bubble char diff reshape / squeeze find ogical notzcat nput nput(,s') ower oner semember numel double brod accumarray and sum duplicate unique vertcat swap delete from stack size	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {,} urifead real upper abs ismember(, rows') nchoosek uint64 cumprod quantile randn sum(, 1,) unique(, 'rows') clc eye	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ it	sign isinf toc strjoin god exp gammain hypergeom conj log2 lcm fix isprime randsample stid strrep strjust
sort Not used. True (literal) str2double Not used Not us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sigrt while cat diag strfind ndgrid () urricad real upper abs ismember(,rows') nchoosek uint64 cumprod quantile randn sum(1,) unique(,,rows') unique(,,rows') clc eye eye nonozeros	circshift toeplitz nuni2str regexprep inf floor matrix \ tic strsplit streat bikdiag factor hankel imread imag log. With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum strtrim	sign isinf toc strjoin god exp gammain hypergeom conj log2 lem fx isprime randsample std strrep strjust deblank
any boubble char diff exeshape / squeeze find logical horzcat input imput (,'s') lower ones simember numel double prod accumarray rand sum diput execution in the saccumarray rand sum diput exercise swap delete from stack size into to sed. Cell array delimiter	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {,} urlread real upper abs ismember(, rows') nchoosek uinit64 cumprod quantile randn sum(, 1,) unique(,, rows') unique(,, rows') clc eye eye nonzeros nnum2cell	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ dic strsplit stroat blkdiag factor hankel imread imag log, With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum strtrim hypot lsempty mat2ceil	sign isinf toc strjoin gcd exp gammain hypergeom conj log2 tcm fix isprime randsample stid strrep strjust deblank mat2cell(x,ones(size(x,1),1),size(x,2)
sort Not used. True (literal) str2double Not used Not us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sigrt while cat diag strfind ndgrid () urricad real upper abs ismember(,rows') nchoosek uint64 cumprod quantile randn sum(1,) unique(,,rows') unique(,,rows') clc eye eye nonozeros	circshift toeplitz nuni2str regexprep inf floor matrix \ toell strsplit streat bikdiag factor hankel immead imag log. With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum strtrim hypot isempty mat2cell norm	sign isinf toc strjoin god exp gammain hypergeom conj log2 lcm fix isprime randsample stid strrep strjust deblank mat2cell(x.ones(size(x,1),1),size(x,2) bitor
sort Not used. True (literal) str2double Not used Not us	sortrows str2num regexp ind2sub mod(1)+1 sub2ind sqrt while cat diag strfind ndgrid {,} urlread real upper abs ismember(, rows') nchoosek uinit64 cumprod quantile randn sum(, 1,) unique(,, rows') unique(,, rows') clc eye eye nonzeros nnum2cell	circshift toeplitz num2str regexprep inf floor matrix \ ceil matrix \ dic strsplit stroat blkdiag factor hankel imread imag log, With two inputs, specifies base mean interp1 round primes n-th prime randi cumsum strtrim hypot lsempty mat2ceil	sign isinf toc strjoin gcd exp gammain hypergeom conj log2 tcm fix isprime randsample stid strrep strjust deblank mat2cell(x,ones(size(x,1),1),size(x,2)

Normal function	Normal function: indexing	Normal function: literal	Meta-function	Stack rearranging function
Clipboard function	Control flow	Used only in literals	Separator, comment	Not used

Table 4: Behaviour of functions regarding consumption of inputs and of input/output specifications

	Consume inputs	Consume input and
		output specifications
Normal	Yes	Yes
Meta	Yes	No
Stack rearranging	No	Yes
Clipboard	No	Yes

- iscolumn, isvector etc: they can be realized with size, and are not much used anyway, I think.
- issorted: it can be easily realized by comparing with the result of sort. Of course issorted would be more time-efficient, but time efficiency is not the main purpose of code golfing.
- rem: probably having mod is enough.
- matrix inverse: not used very often; and can be done with eye and matrix division
- det, rank, matrix pseudoinverse, matrix decompositions, matrix power: probably too specialized
- isequaln: not used very often, is it?
- swapbytes: too specialized. Or is it worth including it?
- sign: it can be done in three characters with abs and element-wise division.
- factorial: it can be done with: and prod.
- bitshift, bitcmp: other bit-wise functions have been included. These two can be easily done with arithmetic operations.
- strcmpi: there's strcmp.
- discretize: the third output of histcounts gives that.

9 The MATL compiler

9.1 Usage

The official MATL compiler is written in MATLAB. It takes a source program in MATL and produces an output (compiled) program that is run in MATLAB.

It can be used in any of the following ways:

matl -options program, or matl -options 'program' (command syntax);

• matl('-options', 'program') (function syntax).

In either case, the first input specifies processing options, starting with the character -; and the second input is a string or character array that contains the MATL program, or the name of a text file where the MATL program is stored. Both input arguments are optional.

The **first input** argument can specify the following options for the matl command:

- p: parse. Writes parsed program, with one line for each statement and using indenting, in text file MATLp.txt.
- 1: listing. The parsed MATL program listing is shown on screen with one line for each statement and using indenting. Implies p.

Two single-digit numeric options can be used to specify the indenting base (number of spaces to be included before any statement) and the indenting step (number of additional spaces for each nesting level). Default values are 4 and 2 respectively. If only one numeric option is provided, it is interpreted as the indenting base.

If a *third* numeric option is provided, it is interpreted as the minimum number of spaces before comment symbol. A comment symbol is included at the end of each line, with all comment symbols vertically aligned and separated at least the specified number of spaces from the corresponding statement. This is useful for adding explanations to the code.

Numeric options can be digits 0, ..., 9; or they can be *capital* letters A, B, ..., Z, which are interpreted as numbers 10 (A), 11 (B), ..., 35 (Z).

File MATLp.txt containing the parsed program uses the indenting step, but not the indenting base.

If options c, r or d have also been provided, the matl command stops at this point and waits for a key press before continuing, in order to give the user time to see or copy the displayed listing.

• e: listing with comments. It's like option 1 but automatic comment texts are added depending on the statement. These provide a good starting point to explain what the code does. Implicit statements (see §7) are also indicated, as comments only.

In addition to the three numeric options used for option 1, a *fourth* number can be specified (using capital letters 10, 11, ...). This is interpreted as the number of spaces between comment symbols and comment text. If less than four numeric options are provided, the rest take their default values. The third and fourth numeric options have default values 6 and 1 respectively.

File MATLp. txt doesn't include comments.

As happens with 1, if options c, r or d have been provided in addition to e, the mat1 command stops at this point and waits for a key press before continuing.

- c: compile. Produces a .m file called MATLc.m that can be run in MATLAB. Implies p.
- r: run. Runs the compiled program in MATLAB. Implies p and c. If an error occurs in the program, the error message includes a link to open the parsed MATL file at the line of the statement that caused the error.
- d: debug. Runs the compiled program in MATLAB in debug mode. Implies p and c. Breakpoints are set at the beginning of (the MATLAB code corresponding to) each MATL statement, to allow step-by-step execution. The variable editor is opened to show the MATL stack (variable STACK), input and output specifications (S_IN and S_OUT), and clipboard contents (CB_H, ..., CB_L).
- f: file. Indicates that the second input argument will not be MATL code, but the name of a file containing the code.
- v: verbose. Causes the compiler to provide detailed information about what it's doing.
- h: help. provides command-line help.

If no options are provided (or only option f is provided), the matl program defaults to -r (or -rf).

The **second input** argument is a string that represents one of the following, depending on the selected options:

- 1. The program code (options p, 1, e, c, r, r,);
- 2. The name of a file containing the program code (option f);
- 3. Search text to get help (option h).

If the program code, file name or search text have commas, spaces, or other symbols that cause MATLAB to misinterpret the string, it needs to be enclosed in quotation marks; and then quotation marks contained within the string need to be duplicated.

In cases 1 and 2 the second input argument may be omitted. In this event the matl command waits for input from the keyboard containing the MATL program or the file name. The MATLAB prompt is changed to a single > symbol, which indicates MATL input mode. A program may be entered in a single line or in several lines (Enter key), and the end of the program is indicated by a blank line (Enter key twice). A file name is entered in a single line.

In case 3, if no string is provided as second input, general help about matl options is displayed. If a string is provided, it may contain the name of a MATL statement, or arbitrary search text. In the former case the information about that statement will be printed. In the latter, the search is based on case-insensitive partial matching with descriptions of MATL statements (which include equivalent MATLAB function names) and with automatic comment texts.

Examples:

- matl: waits for user input, and runs the program represented by that input. Files MATLp.txt and MATLc.m are produced.
- matl 10; "@D]: runs the program 10; "@D]. Files MATLp.txt and MATLc.m are produced.
- matl -d '3,4+D': runs the program 3,4,+D in debug mode (quotation marks are needed because the code contains a comma). Files MATLp.txt and MATLc.m are produced.
- matl -cf file.txt: compiles the program contained in file file.txt and produces files MATLp.txt and MATLc.m.
- matl('-182v', myProgram): parses the program held in character array myProgram, shows the parsed result without automatic comments, using the numeric options for indenting, and produces file MATLp.txt. Detailed information about the process is also shown on screen.
- mat1 -e0291 1t8: "2\\$t+]: parses the program provided as string input (code for the Fibonacci sequence given in §1.3) and shows the parsed result with automatic comments, using the numeric options for indenting. The parsed file MATLp.txt is also produced. The result printed on screen is as shown in Figure 1.
- matl -h sort would produce the result shown in Figure 2.

9.2 Structure

The matl program consists of a main function, matl, which calls three other functions, corresponding to the parser, compiler, and runner/debugger.

The parse function, matl_parse, separates the program into statements. It includes the array checking referred to in page 6. Optionally it calls a display function, matl_disp, to print the listing of parsed code on screen. The output of the parser is a MATLAB struct array S in which each entry is a statement, with fields describing the source code of the statement, the statement type and other information useful for the compiler.

```
1
         % number literal
t
         % duplicate
8
         % number literal
         % vector of equally spaced values
         % for
         % number literal
  \
         % modulus after division (element-wise, singleton expansion)
  $
         % input specification
  t
         % duplicate
         % addition (element-wise, singleton expansion)
         % (implicit) end
         % (implicit) convert to string and display
```

Figure 1: Example of parsed code with automatic comments

```
S sort
    1--3 (1); 1--2 (1)
    sort. If 2 inputs: a negative value of the second input
    corresponds to descending order
XS sort rows
    1--2 (1); 1--2 (1)
    sortrows
```

Figure 2: Example of command-line help

The **compile function**, matl_compile, generates MATLAB code corresponding to each statement: literals, functions and control flow statements.

Each function is defined by the MATLAB code that the compiler generates for that function. That code is divided into *preamble*, *function body* and *postamble*. Most of the preamble and postamble code is common to different groups of functions: take inputs from stack, push results onto stack, delete \$ and # specifications). The function body, as well as some parameters to be used in the preamble and postamble, are specific to each function, and define what the function actually does.

Functions are defined by means of a *function definition file*, funDef.txt. It is a tab-separated plain text file that for each function contains the function body (directly as MATLAB code) and information that controls how the preamble and postamble code should be generated. This information includes allowed numbers of inputs and outputs, and whether the inputs should be consumed (deleted from the stack). The file also contains the text used in automatic comments.

The information about allowed and default inputs and outputs for a given function needs not (and cannot, for certain functions) be a fixed number. Consider as an example function H, which pastes the contents of clipboard H. Its default num-

ber of outputs is the number of elements contained by the clipboard, and thus can only be determined at run-time. This means that this default number is not known in advance. Instead, in the function definition file this parameter is defined by a *string* that gets directly inserted into the compiled code. The string can refer to the run-time information it needs, such as number of elements in the clipboard.

The function definition file is processed by a genFunDef function, which generates a function definition struct array, F, to be used by the compiler. This array contains the same information as the text file, and is saved into a funDef.mat file for future use. When the compiler encounters a function in the MATL parsed code, it looks it up in array F and generates the compiled (MATLAB) code accordingly. To speed up compilation, the generation of struct array F is only done when the function definition file is found to be newer than the processed file funDef.mat; otherwise the latter is loaded.

For functions that generate predefined literals, these are specified on a separate predefined literal file, preLit.txt. It is a plain text file that for each function defines a set of key-value pairs. This is processed by a genPreLit function, which generates a predefined literal struct array, L, to be used by the compiler. This array contains the same information as the text file, and is saved into a preLit.mat file for future use.

Lines of compiled code are stored in a cell array of strings C, from which the compiled file MATLc.m will be written.

The function definition file and predefined literal file centralize all information about functions. This allows to define new functions without actually modifying the compiler code.

The **run function**, matl_compile, executes the compiled program. If an error is found, an error message is issued with a link to the MATL statement that generated the error. In debug mode it inserts breakpoints and opens relevant variables (taking advantage of MATLAB's openvar).

The **help function**, matl_help, provides command-line help. It uses a struct array H that contains help information for all MATL functions and statements. This struct array is generated from the function definition file, the predefined literal file and additional information by a genHelp function, and is stored in file help.mat.

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⁵http://chat.stackoverflow.com/transcript/message/26114026#26114026

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Appendix A Detailed function definitions

MATL functions are defined in Table 5. The notation for allowed and default numbers of inputs and outputs is as follows. Consider for example the u function (which corresponds to MATLAB's unique). Then "u 1–4 (1) 1–3 (1)" means that this function can accept 1 to 4 inputs, with 1 as default; and can produce 1 to 3 outputs, with 1 as default. This notation may be abbreviated if the number of inputs or outputs is unbounded or is fixed: "(3–(3) 1" means that the number of inputs can be any integer starting at 3 and the number of outputs is always 1.

Table 5: Function definitions

```
!
     1-2(1)
                        With 1 input: .' (transpose). With 2 inputs: permute
              1
    1-2(1)
X!
              1
                        rot90
Y!
    1
              0-2(2)
                        system
Z!
     1
               1
                        full
Х"
     2-(3)
                        repmat
Υ"
    2-(2)
              1
                        repelem (run-length decoding)
Z"
               1
     1
              0
                        specify outputs for next function
Y# 1-2 (1) 0
    1-3(1)
Z#
                        Appends first input to file inout, creating it if necessary.
                        If the input is an array it is converted to char and written.
                        If the input is a cell array input, the contents of each cell
                        are converted to char and written, with a newline (char-
                        acter 10) in between. With 2 inputs: second input speci-
                        fies filename; if empty defaults to inout. With 3 inputs:
                        third input specifies whether any previous contents of file
                        should be kept.
     1
              0
                        specify inputs for next function
```

⁶http://chat.stackoverflow.com/transcript/message/25584017#25584017

```
1-(2)
              0-(1)
                        execute Matlab function specified by first input, using the
                        rest of the inputs as arguments.
                        char(vpa(...))
     1-2(1)
              1
Z$
     0-1(0)
              1
                        Reads bytes from specifed file. The output is a row vector
                        of char. If 0 inputs or empty input: file name is inout.
Х%
               1
                        class of input (class with one input)
     1
Y%
     2-3(2)
              1
                        cast
Z%
    2
               1
                         typecast
     1-(2)
               1
                        & (and), element-wise with singleton expansion
X& 2-4 (2)
              1-3(1)
                        intersect
    2-3(2)
              1
                         bitand
γ,
     1
               2
                        run-length encoding (inverse of repelem). Input may be
                        an array or cell array. Numeric values must be finite
Z,
     0
               1
                        now
(
     3-(3)
               1
                        assignment ( ) indexing
    3-(3)
               1
                        assignment { } indexing
X (
     2-(2)
               1
                        reference ( ) indexing
)
X)
    2-(2)
               1
                        reference { } indexing
Y)
               1
                        linearize to column array ((:))
    1
               0-(\triangle)
Z)
    1
                        generate comma-separated list from cell array ({:}) and
                        push each element onto stack
     1-(2)
              1
                         .* (times), element-wise with singleton expansion
Х*
     2
               1
                        kron
Υ*
     2
               1
                        matrix product, * (mtimes)
     1-(2)
               1
                        Cartesian product. Given an n of vectors of possibly dif-
                        ferent sizes, generates an n-column matrix whose rows de-
                        scribe all combinations of elements taken from those vec-
                        tors
     1-(2)
               1
                        + (plus), element-wise with singleton expansion
     2-3(2)
              1
X+
                         conv
Y+
     2-4(2)
              1
                        conv2
     2
Z+
               1
                         convmtx
Χ,
     1
               1
                        cos
     1
               1
Υ,
                        sin
     1
               1
Ζ,
                        tan
     2
               1
                         - (minus), element-wise with singleton expansion
X –
     2-4(2)
              1-2(1)
                        setdiff
Υ.
     0-1(1)
                        pause (without outputs)
              0
Ζ.
     2-3(2)
              1
     2
               1
                         ./(rdivide), element-wise with singleton expansion
X/
     1
               1
                         angle
Υ/
     2
               1
                        right matrix division, / (mrdivide)
    1-3(1)
Z/
              1
                         unwrap
XO
    1
               1
                        predefined literal depending on input
               1
                        predefined literal depending on input
YO
    1
```

```
1
X1
     1
                         predefined literal depending on input
Y1
     1
               1
                         predefined literal depending on input
X2
     1
               1
                         predefined literal depending on input
Y2
     1
               1
                         predefined literal depending on input
Х3
     1
               1
                         predefined literal depending on input
Y3
               1
                         predefined literal depending on input
     1
               1
X4
     1
                         predefined literal depending on input
     1
               1
Y4
                         predefined literal depending on input
               1
X5
     1
                         predefined literal depending on input
X6
     1
               1
                         predefined literal depending on input
X7
     1
               1
                         predefined literal depending on input
X8
     1
               1
                         predefined literal depending on input
X9
     1
               1
                         predefined literal depending on input
     1-3(1)
               1
:
                         colon (with three inputs x, y, z produces x:y:z; with two
                         inputs x, y produces x:y). If one input: produces 1:x
                         gallery. Also includes functions magic, hilb, invhilb,
Y:
     1-(2)
               1-(1)
                         hadamard, pascal, spiral
Z:
     2-3(2)
               1
                         bitset
Х;
     1
               1
                         acos
               1
Υ;
     1
                         asin
     2
Ζ;
               1
                         atan2, element-wise with singleton expansion
     2
<
               1
                         <(lt), element-wise with singleton expansion
X<
     1-3(1)
               1-2(1)
                         min. If 2 inputs: element-wise with singleton expansion
     1-3(1)
               1
Y<
     2
               1
                         == (eq), element-wise with singleton expansion
X =
     2-(2)
               1
                         isequal
Y=
     2
               1
                         strcmp
Z=
     3
               1
                         strncmp
     2
>
               1
                         > (gt), element-wise with singleton expansion
              1-2(1)
     1-3(1)
                         max. If 2 inputs: element-wise with singleton expansion
X>
Y>
     1-3(1)
               1
                         cummax
Z?
     1-6(3)
               1
                         sparse
Y@
     1
               1
                         perms
Z@
     1-3(1)
                         randperm (produces a row vector as output). With 3 out-
                         puts: third output indicates number of permutations, each
                         in a different row.
Α
     1-2(1)
               1
                         all
    2-4(2)
YA
               1
                         dec2base. If second input has more than one element:
                         it defines the symbols, which can be characters or num-
                         bers. The number of symbols defines the base, which can
                         exceed 36
    2
               1
                         base2dec. If second input has more than one element:
ZA
                         it defines the symbols, which can be characters (case-
                         sensitive) or numbers. The number of symbols defines the
                         base, which can exceed 36
```

```
logical(dec2bin(...)-'0')
В
     1-2(1)
              1
              1
                        bin2dec(char(...+'0'))
XB
    1-2(1)
YB
              1
                        dec2bin
ZB
     1
              1
                        bin2dec
XC
    1-7(2)
              1-3(1)
                        histcounts
YC
    2-4(2)
              1
                        im2col
     0-(1)
D
              0
                        If 1 input: disp(num2str(..., '%.16g')). If sev-
                        eral inputs: disp(num2str(eachInput,lastInput)),
                        where eachInput loops over all inputs but the last. In
                        either case, (nested) cell arrays are (recursively) unboxed
                        in linear order. See also XD, YD, ZD
    0-(^{\ddagger})
XD
              0
                        disp(num2str(eachInput)), where eachInput loops
                        over all inputs. (Nested) cell arrays are (recursively) un-
                        boxed in linear order. See also D, YD, ZD
              0-2(1)
                        sprintf.
                                      If 0 outputs:
                                                       prints to screen using
     1-(2)
YD
                        fprintf(...) (without file identifier). See also D, XD,
ZD
     0-(1)
              0
                        disp for each input. See also D, XD, YD
YF
    0-1(1)
              0
                        format
    1-(1)
                        plot. Calls drawnow to update figure immediately
XG
              0
    0-3(1)
                        image(...), axis ij, axis image. Calls drawnow
YG
              0
                        to update figure immediately
ZG
     1
              0-1(0)
                        colormap. With 0 outputs, calls drawnow to update figure
                        immediately
              0-(^{\dagger})
H
                        paste from clipboard H
XH
    0-(1)
              0
                        copy to clipboard H
              0-(^{\dagger})
Ι
     0
                        paste from clipboard I
XI
    0-(1)
              0
                        copy to clipboard I
              0-(^{\dagger})
                        paste from clipboard J
J
     0
                        copy to clipboard J
ХJ
    0-(1)
              0
              0-(^{\dagger})
     0
                        paste from clipboard K
K
                        copy to clipboard K
XK
    0-(1)
              0
              0-(^{\dagger})
                        paste from multi-level clipboard L. Input specifies level
L
     0
                        copy to multi-level clipboard L. Topmost input specifies
XL
    1-(2)
              0
                        level
N
              1
                        number of elements in the stack
    0-(0)
              1
YN
                        NaN function. If 0 inputs: produces literal NaN.
              1
ZN
    1
     0-(0)
              1
0
                        zeros (if 0 inputs: produces output 0)
XO
    1-4(1)
              1
                        datestr
YO
    1-6(1)
              1
                        datenum
    1-3(1)
              1-6(1)
Z0
                        datevec
     1-2(1)
P
              1
                        flip. See also XP
XP
     1
              1
                        flipud. See also P
              1
ΥP
    0
                        рi
```

```
pdist2. Only predefined distance functions are allowed
ZP
    2-5(2)
             1
    2-3(2)
             1
                       If 2 inputs p and x: y = polyval(p, x). If 3 inputs p, x
ZQ
                       and mu: y = polyval(p,x,[],mu)
R
    1-2(1)
             1
                       triu. See also XR.
XR
    1
              1
                       triu(..., 1). See also R.
YR 1-2 (1)
             1
                       tril. See also ZR.
                       tril(..., -1). See also YR.
ZR
    1
              1
             1-2(1)
                       sort. If 2 inputs: a negative value of the second input
    1-3(1)
                       corresponds to descending order
XS
    1-2(1)
             1-2(1)
                       sortrows
    2-3(2)
YS
             1
                       circshift
ZS
    1
              1
                       sign
   1-2(2)
YT
             1
                       toeplitz
U
              1
                       str2double
XU
              1-2(1)
                      str2num with content checking
    1-2(1)
YU
                       num2str
    2-9(2)
             1-6(1)
                      regexp. With 2 inputs: regexp(..., 'match')
XX
YX
    3-5(3)
             1
                       regexprep
YY
    0-(0)
              1
                       inf function. If 0 inputs: produces literal inf.
ZY
              1
    1
                       isinf
X [
    2
              1-(2)
                       ind2sub
Υ[
    1
              1
                       floor
    2
              1-2(1)
                       mod, element-wise with singleton expansion. With 2 out-
                       puts: second output is 'floor(.../...)'.
X \setminus
    2
              1
                       mod(...-1)+1, element-wise with singleton expansion
    2
                       left matrix division, \ (mldivide)
Υ\
              1
X]
    3-(3)
              1
                       sub2ind
Y]
    1
              1
                       ceil
    2
              1
                       .^ (power), element-wise with singleton expansion
X^
              1
    1
                       sqrt
    2
Υ^
              1
                       ^ (mpower)
                       unary - (uminus)
    1
Υ·
    0
             0-1(0)
                       tic
Z۴
    0-1(0)
             0-1(1)
                       toc
    1-2(1)
             1
                       any
a
b
    0-(3)
             0
                       bubble up element in stack
Yb
    1-(1)
             1-2(1)
                       strsplit
    1-(1)
             1
С
                       char
Хc
    3-(3)
             1
                       cat
Yc = 2-(2)
             1
                       strcat
Zc 1–2 (1)
             1
                       strjoin
    1-3(1)
             1
d
                       diff
Xd 1–2 (1)
             1
                       diag
Yd 1-(2)
              1
                       blkdiag
```

```
1-2(2)
             1-3(1)
                       gcd. With 1 input and 1 output, computes the greatest
                       common divisor of all elements of the input
     1-(3)
                       With more than 1 input: reshape. With 1 input: squeeze.
е
              1
Ze
    1
              1
                       exp
f
     1-3(1)
             1-3(1)
                       find
    2-4(2)
Xf
              1
                       strfind
    1
              1
Yf
                       factor
     1
              1
                       logical
g
    1-(2)
                       ndgrid
Xg
              1-(2)
Zg
    1
              1
                       gammaln
h
     1-(2)
              1
                       horzcat
Xh
    0-(^{\ddagger})
              1
                       concatenate into cell array (\{\ldots,\ldots\})
    1-2(2)
Yh
             1
                       hankel
    3
              1
                       hypergeom. If any input is of type char: returns char out-
Zh
i
    0-2(0)
             1
                       input with content checking. If 0 inputs: uses default
                       prompt string. See also j.
Xi
    1-5(1)
             1-2(1)
                       urlread
Yi
    1-(1)
              1-3(1)
                       imread
    0-1(0)
             1
                       input(..., 's'). If 0 inputs: uses default prompt
j
                       string. See also i.
              1
                       real
Хj
    1
Υj
    1
              1
                       imag
Ζį
    1
              1
                       conj
k
     1
              1
                       lower
Xk
    1
              1
                       upper
    0-(0)
1
              1
                       ones (if 0 inputs: produces output 1)
X1
    1
              1
Yl
    1-2(1)
              1
                       log. If two inputs: second input specifies logarithm base
Z1
    1
              1-2(1)
                       log2
    2-4(2)
             1-2(1)
                       ismember. See also Xm
m
                       ismember(..., 'rows', ...). See also m
    2-3(2)
             1-2(1)
Xm
Ym
    1-4(1)
             1
    1-2(2)
             1
                       1cm. With 1 input, computes the least common multiple
Zm
                       of all elements of the input
     1
              1
                       numel
n
    2
              1
Xn
                       nchoosek
    1-5(2)
Yn
             1
                       interp1. 'pp' option not supported
              1
0
     1
                       double
Χo
    1
              1
                       uint64
Yo
    1-3(1)
             1
                       round
Zo
    1
              1
                       fix
     1-3(1)
             1
                       prod
р
Xp 1-3 (1)
             1
                       cumprod
              1
    1
                       primes
Υp
```

```
Zp
    1
              1
                       isprime
    2-6(2)
              1
                        accumarray
q
                       quantile
Χq
    2-3(2)
              1
    1
              1
                       Finds the n-th prime for each value n in the input array
Υq
    0-(0)
              1
                       rand
r
    0-(0)
              1
Xr
                       randn
    1-(1)
Yr
              1
                       randi. If 1 input: randi (..., 1)
                       randsample. Does not support stream specification
Zr
    2-4(2)
              1
     1-4(1)
              1
                        sum. See also Xs
s
Xs
    1-3(1)
              1
                        sum(..., 1, ...). See also s
Ys
    1-3(1)
              1
                        cumsum
Zs
    1-4(1)
              1
                       std
t
    0-(1)
              0
                       duplicate elements in stack
    3
              1
Zt
                       strrep
     1-4(1)
              1-3(1)
                       unique. See also Xu.
u
                       unique(..., 'rows',...). See also u.
Xu
    1-3(1)
             1-3(1)
    1-2(1)
Zu
              1
                       strjust
     1-(2)
              1
                       vertcat
v
    1
              1
Yv
                       strtrim
              1
Ζv
    1
                       deblank
    0-(2)
              0
                       swap elements in stack
W
                       delete from stack
    0-(1)
              0
x
xx
    0
              0
                       clc
     1-2(1)
              1-(1)
У
                       size
Хy
    1-4(1)
              1
                        eye
Yу
    2
              1
                       hypot, element-wise with singleton expansion
     1
              1
z
                       nnz
Xz
    1
              1
                       nonzeros
    1
              1
Yz
                       isempty
X{
    1-2(1)
              1
                       num2cel1
    2-(3)
Y{
              1
                       mat2cell
              1
                       mat2cell(x, ones(size(x,1),1),
Z{
    1
                       size(x,2),...,size(x,ndims(x))).
                                                                 It's a gen-
                       eralization of cellstr that works for numeric, logical or
                       char arrays of any number of dimensions
1-(2)
              1
                        (or), element-wise with singleton expansion
             1-3(1)
X |
    2-4(2)
                       union
    1-2(1)
Y |
              1
                       norm
    2-3(2)
              1
Z \mid
                       bitor
Y}
    1
              1
                       cell2mat
              1-(^{\triangledown})
Z
    1
                       split array into its elements in linear order
              1
                       ~ (not)
     1
χ~
    2-4(2)
             1-3(1)
                       setxor
Υ~
    2
              1
                       xor, element-wise with singleton expansion
Z~
    2-3(2)
              1
                       bixtor
```

Some things I'm not sure of:

Is it better to have 1 or 2 inputs to vpa by default? If 1, what's an appropriate initial condition for digits?

Functions X0...Z9 produce predefined literals depending on their numeric input. These are specified in Table 6.

 $^{^{\}dagger}$ Current number of elements in clipboard (H, I, J, K), or in clipboard level (L). ‡ Current number of elements in stack.

 $^{^{\}triangle}$ Number of elements of input cell array.

[▽] Number of elements of input array.

Table 6: Output of predefined literal functions

Function X0						
1	'stable'	2	'sorted'	3	'rows'	
4	'last'	5	'reverse'	10	'first'	
11	'forward'	12	'legacy'			

	Function X1						
1	'bank'	2	'compact'	3	'hex'		
4	'short'	5	'shortg'	6	'long'		
7	'longg'	8	'loose'	9	'rat'		
10	'longe'	11	'longeng'	12	'shorte'		
13	'shorteng'						

	Function X2						
1	'double'	2	'int8'	3	'int64'		
4	'uint8'	5	'uint64'	6	'char'		
7	'logical'	8	'single'	10	'int16'		
11	'int32'	12	'uint16'	13	'uint32'		
14	'like'	15	'decimals'	16	'includenan'		
17	'native'	18	'omitnan'	19	'significant'		

	Function X3						
1	'start'	2	'end'	3	'tokenExtents'		
4	'match'	5	'tokens'	6	'names'		
7	'split'	8	'once'	10	'ignorecase'		
11	'preservecase'						

	Function X4						
1	'CollapseDelim	2	'DelimiterType'	3	'RegularExpression'		
	iters'						
4	'center'	5	'left'	6	'local'		
10	'right'						

Table 6: Output of predefined literal functions—continued

	Function X5						
1	'full'	2	'same'	3	'valid'		
6	'linear'	7	'nearest'	8	'next'		
9	'previous'	10	'spline'	11	'pchip'		
12	'cubic'	13	'v5cubic'	14	'extrap'		
20	'distinct'	21	'sliding'	22	'indexed'		

	Function X6						
1	'get'	2	'post'	3	'Timeout'		
9	'none'	11	'Frames'	12	'BackgroundColor'		
13	'Index'	14	'Info'	15	'ReductionLevel'		
16	'PixelRegion'	17	'V79Compatible'				

	Function X7						
1	'BinWidth'	2	'BinLimits'	3	'Normalization'		
4	'count'	5	'probability'	6	'countdensity'		
7	'pdf'	8	'cumcount'	9	'cdf'		
10	'BinMethod'	11	'auto'	12	'scott'		
13	'fd'	14	'integers'	15	'sturges'		
16	'sqrt'						

	Function X8						
1	'cityblock'	2	'minkowski'	3	'chebychev'		
4	'cosine'	5	'correlation'	6	'hamming'		
10	'euclidean'	11	'seuclidean'	12	'mahalanobis'		
13	'spearman'	14	'jaccard'	15	'fro'		
16	'Smallest'	17	'Largest'				

Function X9							
1	'shuffle'	2	'default'	3	'twister'		
4	'simdTwister'	5	'combRecursive'	6	'multFibonacci'		
10	'v5uniform'	11	'v5normal'	12	'v4'		

Table 6: Output of predefined literal functions—continued

	Function Y0						
1	'Color'	2	'LineStyle'	3	'LineWidth'		
4	'Marker'	5	'MarkerSize'	6	'on'		
7	'off'	8	'CDataMapping'	9	'scaled'		
20	'auto'	21	'LineJoin'	22	'chamfer'		
23	'miter'	24	'round'	25	'square'		
26	'diamond'	27	'pentagram'	28	'hexagram'		
29	'visible'	30	'Clipping'	31	'MarkerEdgeColor'		
32	'MarkerFaceColor'	40	'direct'	41	'AlphaData'		
42	'AlphaDataMapping'	43	'Cdata'	44	'Xdata'		
45	'Ydata'	46	'ZData'	50	'autumn'		
51	'bone'	52	'colorcube'	53	'cool'		
54	'copper'	55	'flag'	56	'gray'		
57	'hot'	58	'hsv'	59	'jet'		
60	'lines'	61	'parula'	62	'pink'		
63	'prism'	64	'spring'	65	'summer'		
66	'winter'						

	Function Y1						
1	'mean'	2	'min'	3	'max'		
4	'{sort(x)}'	5	'{sort(x)."}'	10	'sum'		
11	'x(end)'	12	'{cumsum(x)}'	13	'{cumsum(x)."}'		
14	'nansum'	15	'nanmean'	16	'nanmin'		
17	'nanmax'	18	'{cummax(x)}'	19	'{cummax(x)."}'		

	Function Y2						
1	'A':'Z'	2	'a':'z'	3	['A':'Z' 'a':'z']		
4	'0':'9'	5	['0':'9' 'A':'F']	11	'aeiou'		
12	'AEIOU'	13	'aeiouAEIOU'	20	['Mon';'Tue';'Wed'; 'Thu';'Fri';'Sat'; 'Sun']		
21	[298 302 288 305 289 296 310]						

Table 6: Output of predefined literal functions—continued

	Function Y3							
1	'magic'	2	'hilb'	3	'invhilb'			
4	'hadamard'	5	'pascal'	6	'spiral'			
10	'binomial'	11	'cauchy'	12	'chebspec'			
13	'chebvand'	14	'chow'	15	'circul'			
16	'clement'	17	'compar'	18	'condex'			
19	'cycol'	20	'dorr'	21	'dramadah'			
22	'fiedler'	23	'forsythe'	24	'frank'			
25	'gcdmat'	26	'gearmat'	27	'grcar'			
28	'hanowa'	29	'house'	30	'integerdata'			
31	'invhess'	32	'invol'	33	'ipjfact'			
34	'jordbloc'	35	'kahan'	36	'kms'			
37	'krylov'	38	'lauchli'	39	'lehmer'			
40	'leslie'	41	'lesp'	42	'lotkin'			
43	'minij'	44	'moler'	45	'neumann'			
46	'normaldata'	47	'orthog'	48	'parter'			
49	'pei'	50	'poisson'	51	'prolate'			
52	'qmult'	53	'randcolu'	54	'randcorr'			
55	'randhess'	56	'randjorth'	57	'rando'			
58	'randsvd'	59	'redheff'	60	'riemann'			
61	'ris'	62	'sampling'	63	'smoke'			
64	'toeppd'	65	'toeppen'	66	'tridiag'			
67	'triw'	68	'uniformdata'	69	'wathen'			
70	'wilk'							