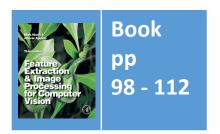
Lecture 5 Group Operators

COMP3204 & COMP6223 Computer Vision

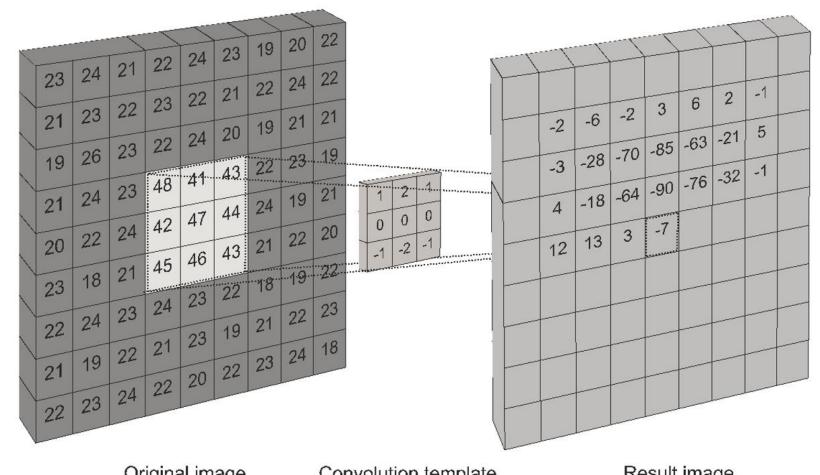
How do we combine points to make a new point in a new image?



Department of Electronics and Computer Science



Template convolution





Original image

Convolution template

Result image

Template convolution

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ı	1 1 1	u	Θ	C

100	100	200	200	200
100	100	200	200	200
100	100	200	200	200
200	200	400	400	400
300	300	400	400	400

0	0	0	0	0
0	400	400	0	0
0	400	400	0	0
0	400	400	0	0
0	0	0	0	0

C	٠,
	у

Resul	t
	ч

0	0	0	0	0
0	400	400	Q-	0
0	640	806	800	0
0	894	894	800	0
0	0	0	0	0

0	0	0	0	0
0	0	0	0	0
0	500	700	800	0
0	800	800	800	0
0	0	0	0	0





3×3 template and weighting coefficients

w_0	w_I	W2
W3	w_4	W5
W6	w_7	w_8

$$\mathbf{N}_{x,y} = \sum_{i \in \text{template } j \in \text{template}} w_{i,j} \times \mathbf{O}_{x(i),y(j)}$$



where $w_{i,j}$ are the weights and x(i), y(j) denote the position of the point that matches the weighting coefficient position

3×3 averaging operator

$$\mathbf{N}_{x,y} = \frac{1}{9} \sum_{i \in 3} \sum_{j \in 3} \mathbf{O}_{x(i),y(j)}$$

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

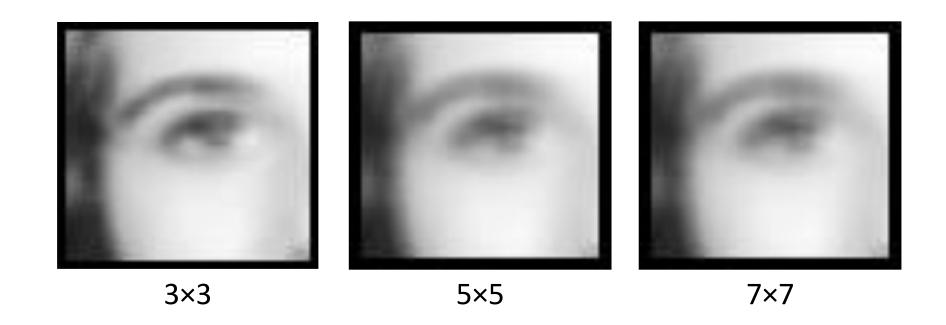








Illustrating the effect of window size





Template convolution via the Fourier transform

Allows for fast computation for template size $\geq 7 \times 7$

$$\mathbf{P} * \mathbf{T} = \mathfrak{I}^{-1} \left(\mathfrak{I}(\mathbf{P}) . \times \mathfrak{I}(\mathbf{T}) \right)$$

Template convolution *

Fourier transform of the picture, $\mathfrak{I}(\mathbf{P})$

Fourier transform of the template, $\Im(T)$

Point by point multiplication (.x).





Beware of clowns ... Oxford

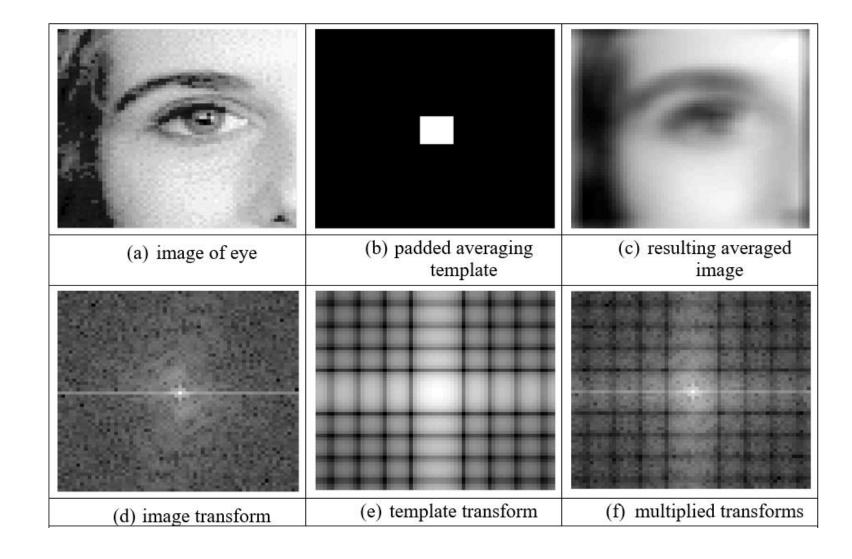
$$f(x,y) * h(x,y) \Leftrightarrow F(u,v)H(u,v)$$

Imperial

$$w(t) = u(t) * v(t) \Leftrightarrow W(f) = U(f)V(f)$$

it's point by point!!

Template Convolution via the Fourier Transform





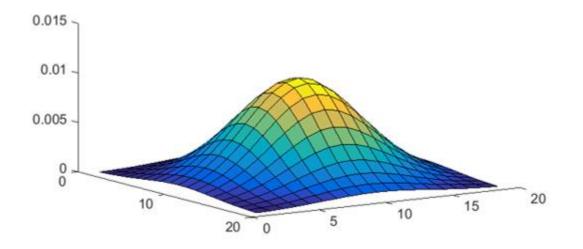
2D Gaussian function

$$g(x,y,\sigma) = \frac{1}{2\pi\sigma^2} e^{\frac{-(x^2+y^2)}{2\sigma^2}}$$

- Used to calculate template values
- Note compromise between variance σ^2 and window size
- Common choices 5×5, 1.0; 7×7, 1.2; 9×9, 1.4



2D Gaussian function and template

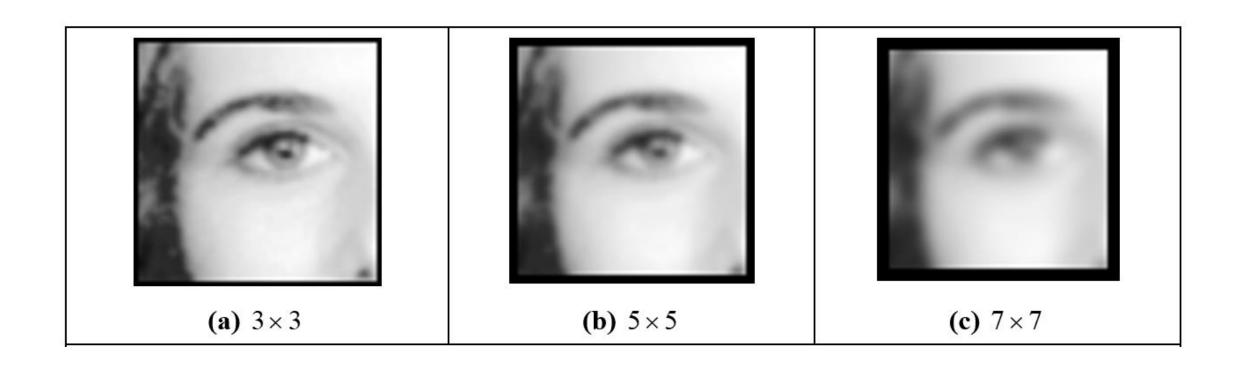


0.002	0.013	0.022	0.013	0. 002
0.013	0.060	0. 098	0.060	0.013
0.022	0. 098	0.162	0. 098	0.022
0.013	0.060	0.098	0.060	0.013
0. 002	0.013	0.022	0.013	0. 002



Template for the 5×5 Gaussian Averaging Operator ($\sigma = 1.0$).

Applying Gaussian averaging





Finding the median from a 3×3 template

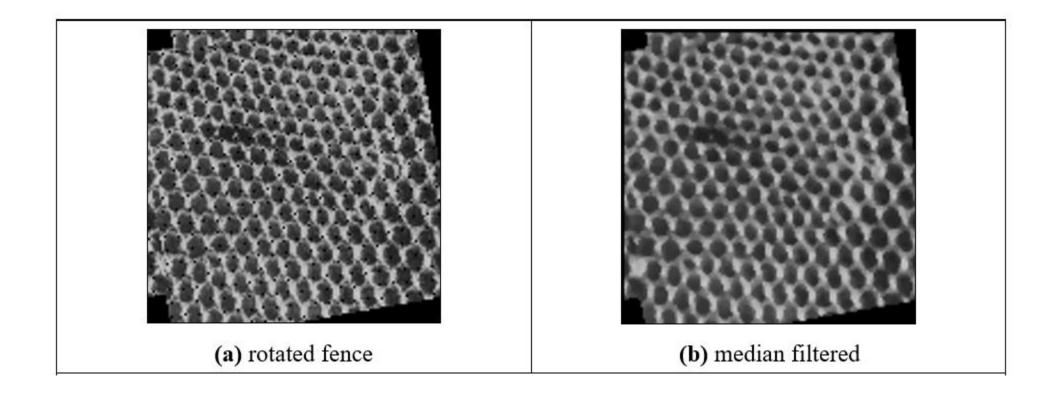
2 8 7 4 0 6 3 5 7	2 4 3 8 0 5 7 6 7
(a) 3×3 template	(b) unsorted vector
	0 2 3 4 5 6 7 7 8 ↑ median
	(c) sorted vector, giving median



Finding the median from a 3×3 template

Preserves edges

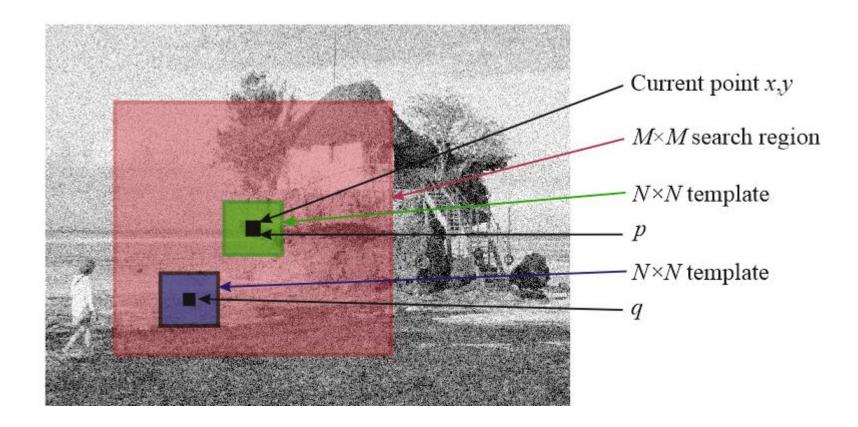
Removes salt and pepper noise





Newer stuff: non local means

Averaging which preserves regions



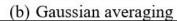


Applying non local means



(a) original image





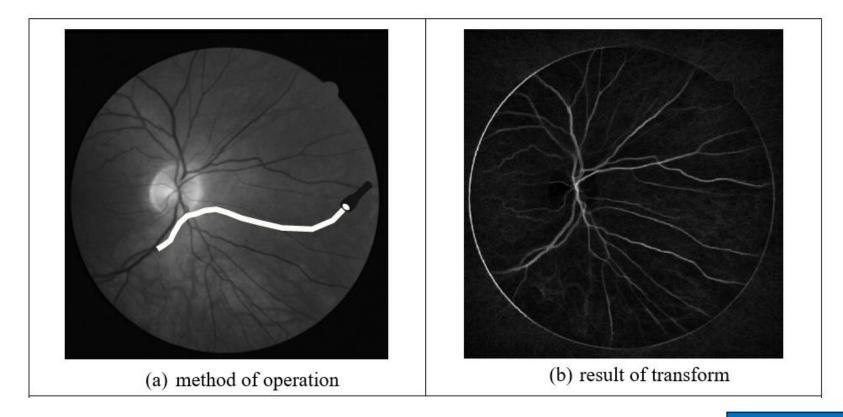


(c) nonlocal means



Even newer stuff: Image Ray Transform

Use analogy to light to find shapes, removing remainder





Applying Image Ray Transform

