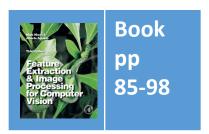
Lecture 4 Point Operators

COMP3204 & COMP6223 Computer Vision

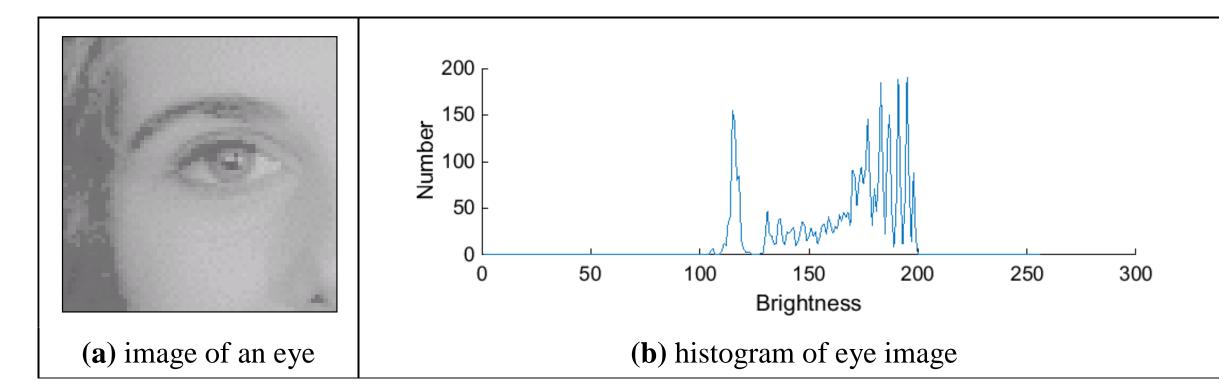
How many different operators are there which operate on image points?







An image and its histogram





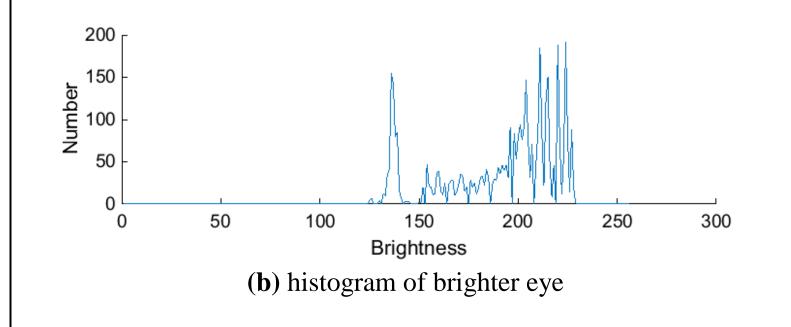
Brightening an image

$$\mathbf{N}_{x,y} = k \times \mathbf{O}_{x,y} + l$$

new image **N**; old image **O**; gain *k*; level *l*; co-ordinates *x*,*y*



(a) image of brighter eye

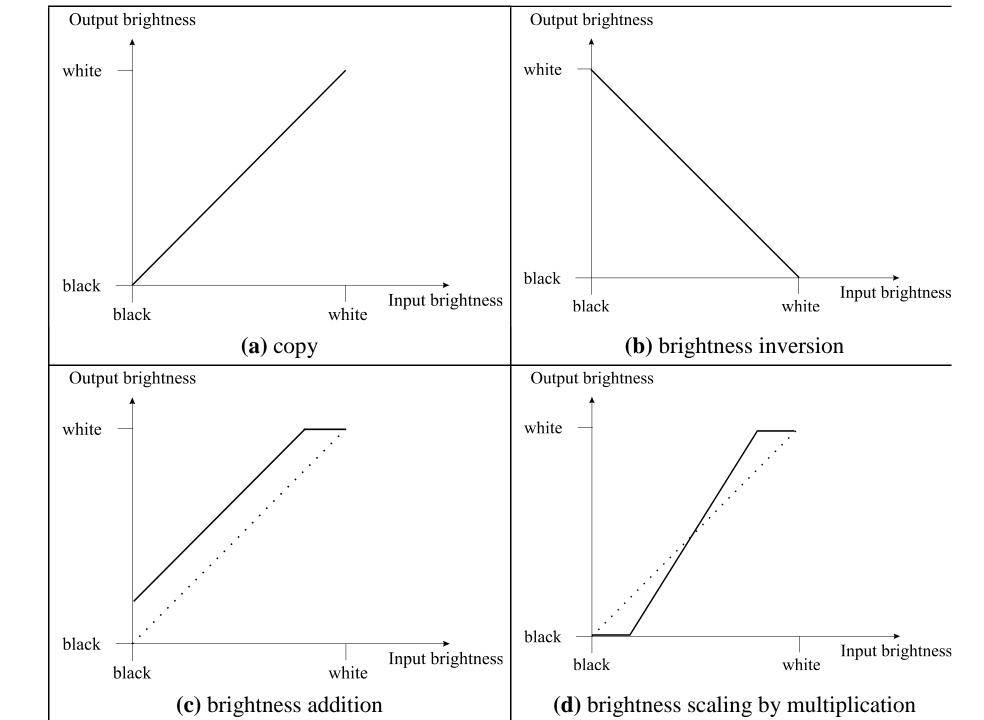






Intensity mappings





Applying exponential and logarithmic point operators



(a) logarithmic compression



(b) exponential expansion



$$\mathbf{N}_{x,y} = \log(\mathbf{O}_{x,y})$$

$$\mathbf{N}_{x,y} = \exp\left(\mathbf{O}_{x,y}\right)$$

Intensity normalisation

$$\mathbf{N}_{x,y} = \frac{\mathbf{N}max - \mathbf{N}min}{\mathbf{O}max - \mathbf{O}min} \times (\mathbf{O}_{x,y} - \mathbf{O}min) + \mathbf{N}min \qquad \forall x, y \in 1, N$$

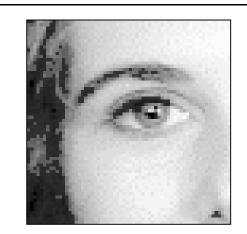
new image N; old image O; co-ordinates x,y minimum input Nmin maximum input Nmax minimum output Omin maximum output Omax

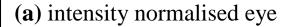
Avoids need for parameter choice

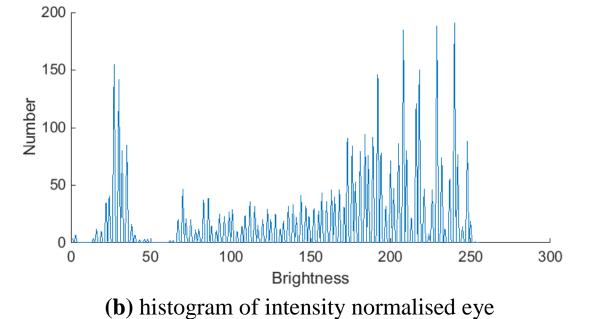


Intensity normalisation and histogram equalisation



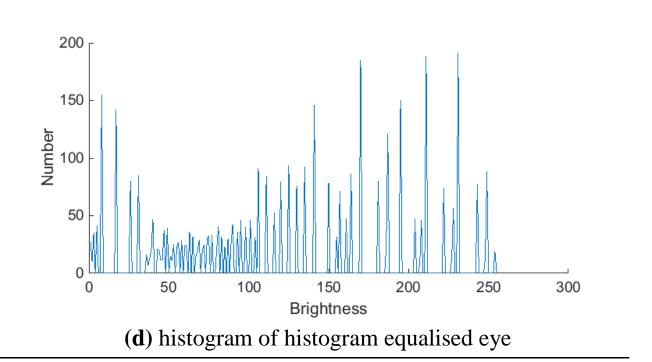








(c) histogram equalised eye



Histogram Equalisation

 N^2 points in the image; the sum of points per level is equal

$$\sum_{l=0}^{M} \mathbf{O}(l) = \sum_{l=0}^{M} \mathbf{N}(l)$$

cumulative histogram up to level *p* should be transformed to cover up to the level *q*

$$\sum_{l=0}^{p} \mathbf{O}(l) = \sum_{l=0}^{q} \mathbf{N}(l)$$

number of points per level in the output picture

$$\mathbf{N}(l) = \frac{N^2}{\mathbf{N}max - \mathbf{N}min}$$

cumulative histogram of the output picture

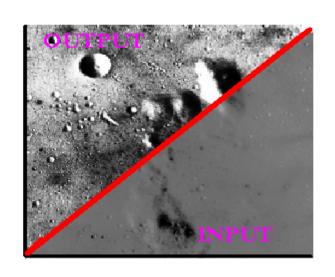
$$\sum_{l=0}^{q} \mathbf{N}(l) = q \times \frac{N^2}{\mathbf{N}max - \mathbf{N}min}$$

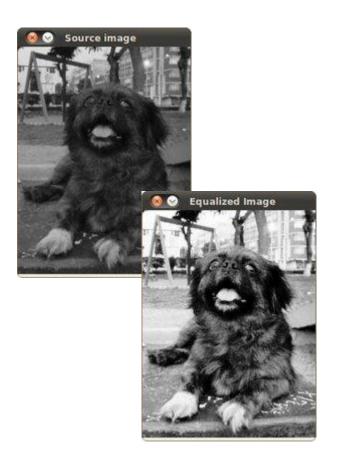


mapping for the output pixels at level q

$$q = \frac{\mathbf{N}max - \mathbf{N}min}{N^2} \times \sum_{l=0}^{p} \mathbf{O}(l)$$

Applying intensity normalisation and histogram equalisation







http://homepages.inf.ed.ac.uk/rbf/HIPR2/histeq.htm;

http://docs.opencv.org/doc/tutorials/imgproc/histograms/histogram_equalization/histogram_equalization.html;
http://www.softpedia.com/get/Multimedia/Video/Other-VIDEO-Tools/Easy-Histogram-Equalization.shtml

Thresholding an eye image

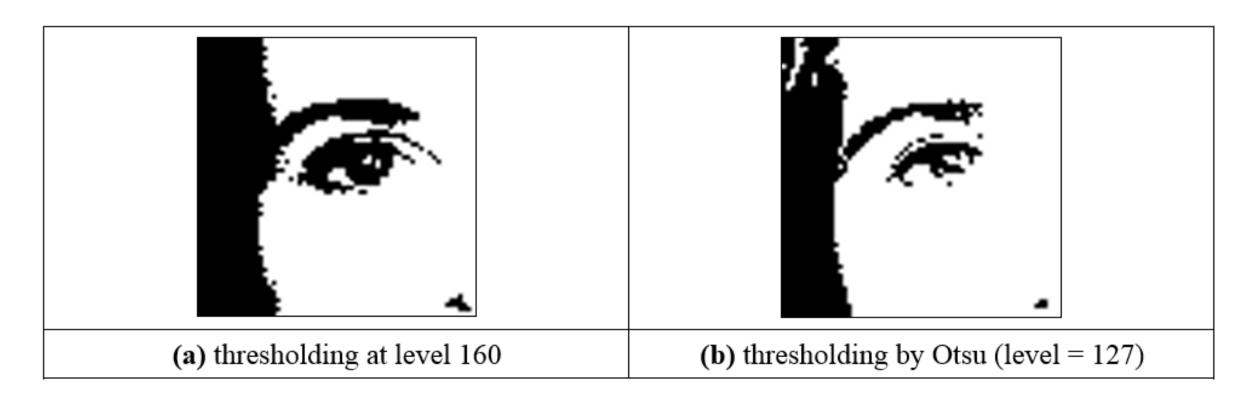
$$\mathbf{N}_{x,y} = \begin{vmatrix} 255 & if & \mathbf{N}_{x,y} > threshold \\ 0 & otherwise \end{vmatrix}$$





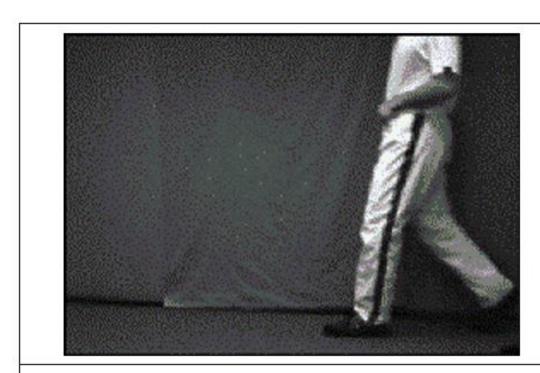


Thresholding an eye image: manual vs automatic





Thresholding an image of a walking subject



(a) walking subject

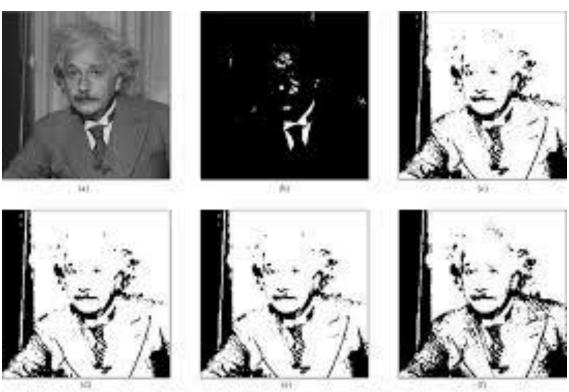


(b) automatic thresholding by Otsu

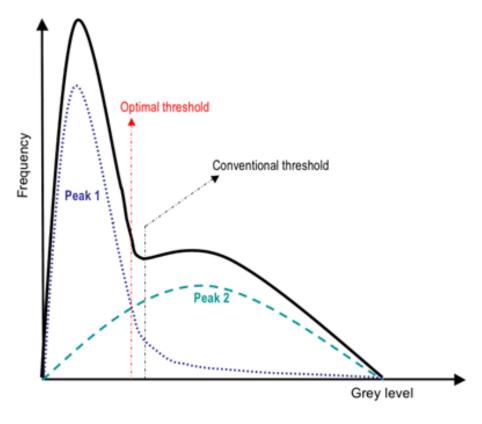


Advanced thresholding

Entropic thresholding (2010)



Optimal thresholding



http://opticalengineering.spiedigitallibrary.org/article.aspx?articleid=1096546; https://www.cs.auckland.ac.nz/courses/compsci773s1c/lectures/ImageProcessing-html/topic3.htm