

Forster Edge Detection (93-122)

i). Carry designed for

- a). Optimal response — no noise
- b). Single response — thin edges
- c). good localization — in the right place.

Approximate

Gaussian smoothing \rightarrow Sobel \rightarrow non-maximum suppression
(peak detection)

3×3
 5×5 Sobel

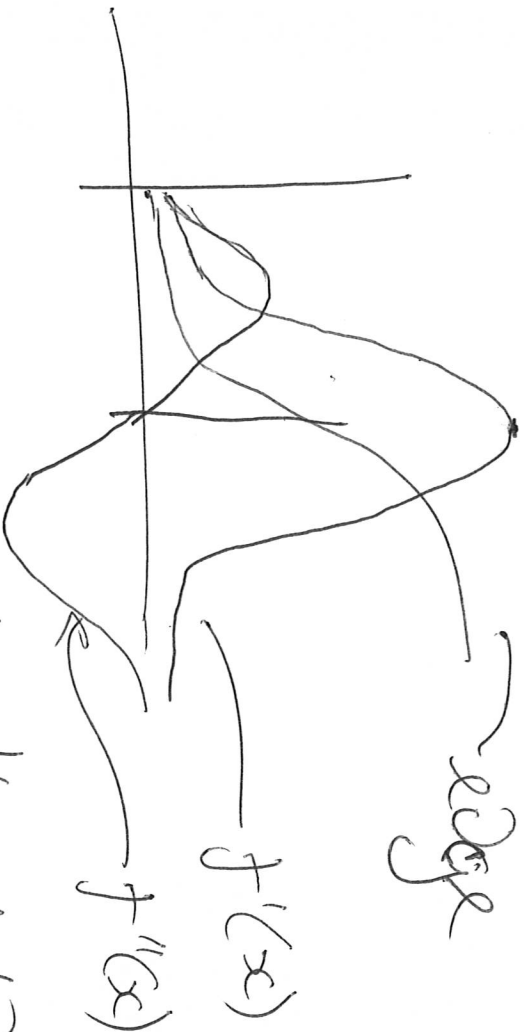
\downarrow
hysteresis thresholding.

more complex than Sobel but 'better'

ii) second order operators.

$$f'(x) = f_{x,y} - f_{x+1,y}$$

$$f''(x) = f'(x) - f'(x+1)$$



1st order $f'(x)$ for threshold
2nd $f''(x)$ for zero crossing detection.

iii)

$$f''(x) = f'(x) - f'(x+1)$$

$$(f_{xy} - f_{x+1,y}) - (f_{x+1,y} - f_{x+2,y})$$

template

$$\begin{bmatrix} 1 & -2 & 1 \end{bmatrix}$$

3x3

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Laplace

but junk.

no averaging

IV. Laplacian of Gaussian
 differentiable Gaussian filter

$$g = e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

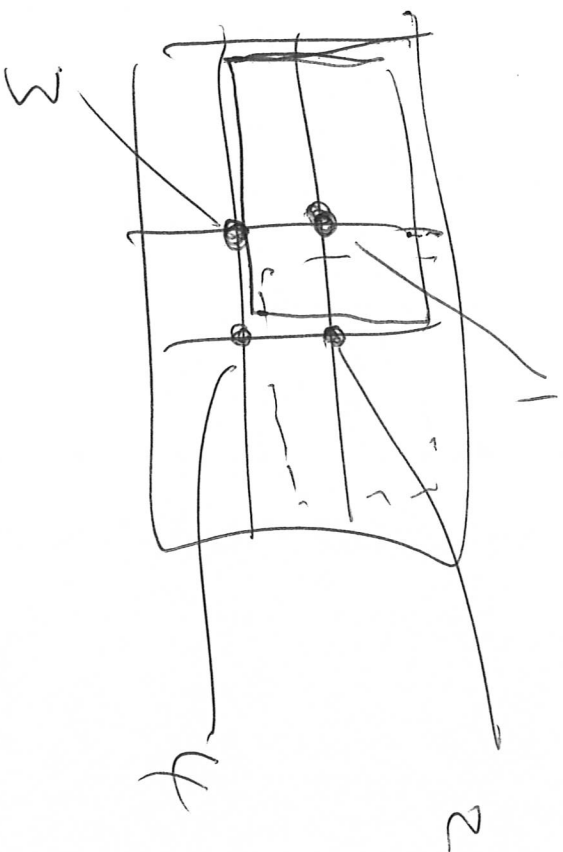
$$\frac{\partial g}{\partial x} = -\frac{2x}{2\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

$$\frac{\partial^2 g}{\partial x^2} = \frac{1}{\sigma^2} \left(-1 + \frac{2x^2}{2\sigma^2} \right) e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

$$\frac{\partial^2 g}{\partial y^2} = \frac{1}{\sigma^2} \left(-1 + \frac{y^2}{\sigma^2} \right) e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

$$\nabla^2 g = \frac{1}{\sigma^2} \left(-2 + \frac{x^2+y^2}{\sigma^2} \right) e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

V. zero crossing.



if $(\max(1-\epsilon) > 0) \cdot (\min(1-\epsilon) < 0)$
the edge point.

edge locations are connected, but lack direction.