1. Consider the training examples shown in Table 1 for a binary classification problem.

Table 1. Data set.

| Customer ID | Gender | Car Type | Shirt Size | Class |
|-------------|--------------|----------|-------------|-------|
| 1 | M | Family | Small | C0 |
| 2 | \mathbf{M} | Sports | Medium | C0 |
| 3 | \mathbf{M} | Sports | Medium | C0 |
| 4 | \mathbf{M} | Sports | Large | C0 |
| 5 | \mathbf{M} | Sports | Extra Large | C0 |
| 6 | \mathbf{M} | Sports | Extra Large | C0 |
| 7 | ${ m F}$ | Sports | Small | C0 |
| 8 | ${ m F}$ | Sports | Small | C0 |
| 9 | ${ m F}$ | Sports | Medium | C0 |
| 10 | ${ m F}$ | Luxury | Large | C0 |
| 11 | M | Family | Large | C1 |
| 12 | \mathbf{M} | Family | Extra Large | C1 |
| 13 | \mathbf{M} | Family | Medium | C1 |
| 14 | M | Luxury | Extra Large | C1 |
| 15 | ${ m F}$ | Luxury | Small | C1 |
| 16 | ${f F}$ | Luxury | Small | C1 |
| 17 | ${f F}$ | Luxury | Medium | C1 |
| 18 | ${ m F}$ | Luxury | Medium | C1 |
| 19 | ${f F}$ | Luxury | Medium | C1 |
| 20 | ${ m F}$ | Luxury | Large | C1 |

- a) (5%) Compute the entropy for the overall collection of training examples.
- b) (15%) What is the information gain when splitting on the **Gender** attribute?
- c) (20%) What is the information gain when splitting on the **Car Type** attribute (using multiway split)?
- d) (20%) What is the information gain when splitting on the **Shirt Size** attribute (using multiway split)?
- e) (3%) According to the information gain, which attribute is better, **Gender**, **Car Type**, or **Shirt Size**?

2. For a binary classification problem, the composition of labeled training instances at a parent node is summarized in the Table below.

| | Parent | |
|-----|--------|--|
| No | 7 | |
| Yes | 3 | |

- a) (5%) What is the Gini index of the parent node?
- b) (16%) Consider splitting a parent node into two child nodes, N1 and N2, using the **Home Owner** attribute. The composition of labeled training instances at each child node is summarized in Figure 1. What is the Gini index of each child node? What is the gain in the Gini index when splitting on this attribute? According to this impurity measure, will you consider this attribute test condition?

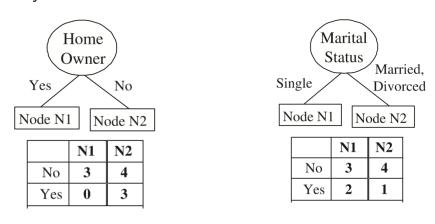


Figure 1.

Figure 2.

c) (16%) Consider splitting a parent node into two child nodes, N1 and N2, using the **Marital Status** attribute. The composition of labeled training instances at each child node is summarized in Figure 2. What is the Gini index of each child node? What is the gain in the Gini index when splitting on this attribute? According to this impurity measure, will you consider this attribute test condition?