STA312Midterm1Rickey

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2/15/2022

Question 1

Part a

```
# Loading the dataset
library(faraway)
cheddar <- faraway::cheddar
# Plot the taste against lactic
plot(cheddar$Lactic,cheddar$taste,xlab = "Lactic", ylab = "taste")</pre>
```

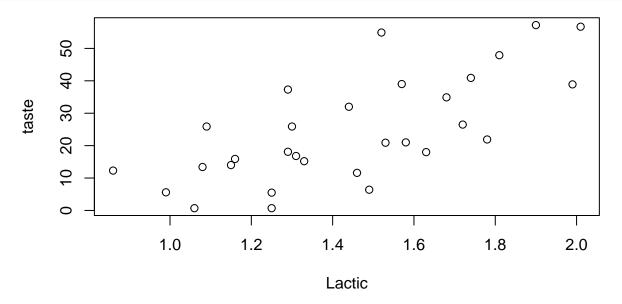


Figure 1: Plot of taste against Lactic

Part b

```
# First find the order of the variable Lactic
ord=order(cheddar$Lactic)
# Using this order to order both the taste and the Lactic
Lord=cheddar$Lactic[ord]
tord=cheddar$taste[ord]
# Creating the line of best fit
lm1 <- lm(tord~Lord)
# Show the model 1
lm1</pre>
```

```
##
## Call:
## lm(formula = tord ~ Lord)
##
## Coefficients:
## (Intercept)
                           Lord
         -29.86
                          37.72
# Creating the parabola of best fit
lm2 <- lm(tord~Lord+I(Lord^2))</pre>
# Show the model 2
1m2
##
## Call:
## lm(formula = tord ~ Lord + I(Lord^2))
##
## Coefficients:
                                     I(Lord<sup>2</sup>)
## (Intercept)
                           Lord
          22.22
                         -36.76
                                          25.51
# Creating the cubic of best fit
lm3 <- lm(tord~Lord+I(Lord^2)+I(Lord^3))</pre>
# Show the model 3
1m3
##
## lm(formula = tord ~ Lord + I(Lord^2) + I(Lord^3))
## Coefficients:
                                     I(Lord<sup>2</sup>)
                                                     I(Lord<sup>3</sup>)
## (Intercept)
                           Lord
           15.88
##
                         -22.79
                                          15.58
                                                           2.28
From the R result, we can see that
                    lm1: \widehat{taste} = -29.86 + 37.72 \cdot Lactic
                                                                                                          (1)
                    lm2: \widehat{taste} = 22.22 - 36.76 \cdot Lactic + 25.51 \cdot Lactic^2
                                                                                                          (2)
                    lm3: \widehat{taste} = 15.88 - 22.79 \cdot Lactic + 15.58 \cdot Lactic^2 + 2.28 \cdot Lactic^3
                                                                                                          (3)
Part c
```

```
plot(tord~Lord, xlab = "Lactic", ylab = "taste")
abline(lm1,col = "blue")
points(Lord, lm2$fitted, type = "l", col = "red")
points(Lord, lm3$fitted, type = "l", col = "green")
```

Part d

```
# Find the model matrix X
X <- model.matrix(lm2)
# Define y
y <- cheddar$taste
# Compute the betahat
betahat <- solve(t(X)%*%X)%*%t(X)%*%y</pre>
```

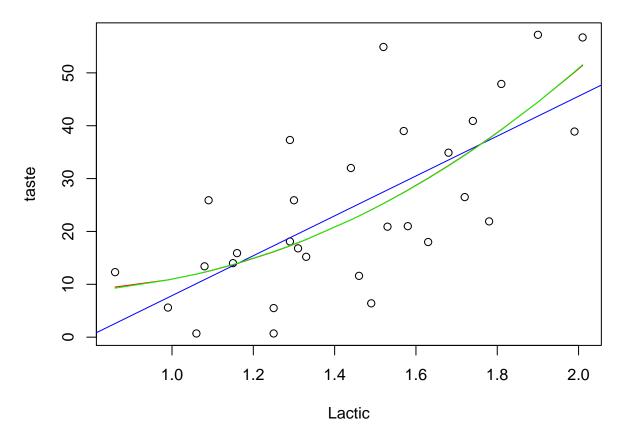


Figure 2: Plots of three models

```
# Return the betahat betahat betahat  
## [,1]  
## (Intercept) -60.64957  
## Lord 133.78175  
## I(Lord^2) -49.68197  
From the result, we know that \hat{\beta} = \begin{bmatrix} -60.64957 \\ 13378175 \\ -49.68197 \end{bmatrix}
```

Part e

```
# Find the hat matrix H
H \leftarrow X%*\%solve(t(X)%*\%X)%*\%t(X)
# Return the hat matrix
Η
##
                                                                        5
## 1
       0.425017578 0.260488247
                                 0.1856092842
                                               0.1659784919
                                                              0.156456962
       0.260488247
                                                0.1207107679
## 2
                    0.172325086
                                 0.1315144342
                                                              0.115451688
## 3
       0.185609284
                    0.131514434
                                 0.1059610914
                                                0.0991197346
                                                              0.095775656
       0.165978492
                   0.120710768
                                 0.0991197346
                                                0.0933087973
                                                              0.090462984
       0.156456962
                    0.115451688
## 5
                                 0.0957756559
                                                0.0904629836
                                                              0.087858156
## 6
       0.103441908 0.085895755
                                 0.0767835798
                                                0.0742232696
                                                              0.072950309
## 7
       0.095291753 0.081302857
                                 0.0737969665 0.0716558453
                                                              0.070585855
## 8
       0.030756347 0.044249375 0.0492154377 0.0503386738
                                                              0.050851019
```

```
## 9
      0.030756347 0.044249375 0.0492154377 0.0503386738
                                                            0.050851019
## 10
      0.007167624 0.030255551
                                0.0396180422
                                              0.0418983935
                                                            0.042972795
      0.007167624
                   0.030255551
                                0.0396180422
                                              0.0418983935
                                                            0.042972795
      0.001760220
                   0.026995017
                                0.0373463595
## 12
                                              0.0398877483
                                                            0.041089086
## 13 -0.003451273
                   0.023829652
                                0.0351257433
                                              0.0379168730
                                                            0.039239717
                                                            0.035643995
## 14 -0.013286527
                  0.017784429
                                0.0308377103
                                              0.0340944321
## 15 -0.053372803 -0.008659726
                                0.0109047819
                                              0.0159145573
                                                            0.018322764
## 16 -0.058114376 -0.012230559
                                0.0079444773
                                              0.0131261346
                                                            0.015619857
## 17 -0.063757406 -0.016873042
                                0.0038870189
                                              0.0092417750
                                                            0.011823038
## 18 -0.067637239 -0.020659005
                               0.0002891589
                                              0.0057153448
                                                            0.008335270
## 19 -0.068538695 -0.021730655 -0.0008079949
                                             0.0046194079
                                                            0.007241359
## 20 -0.070185412 -0.025065567 -0.0046859451 0.0006333596
                                                            0.003209105
## 21 -0.070107314 -0.025661373 -0.0055277664 -0.0002637276
                                                            0.002286888
## 22 -0.066778163 -0.027212869 -0.0089708760 -0.0041526149 -0.001809107
## 23 -0.058551243 -0.026385143 -0.0111373237 -0.0070472540 -0.005046627
## 24 -0.048443314 -0.024009923 -0.0119512853 -0.0086471065 -0.007018542
## 25 -0.042213884 -0.022251300 -0.0120518673 -0.0092084132 -0.007798464
  26 -0.027404096 -0.017592027 -0.0116402335 -0.0098537875 -0.008946242
  27 -0.014239692 -0.013098300 -0.0107953101 -0.0099202339 -0.009446516
      ##
  29
      0.101773870 0.031850980 0.0039257941 -0.0028023960 -0.005958085
                   ##
      0.118582481
                 6
                              7
##
                                           8
                                                        9
                                                                    10
## 1
      0.1034419080
                    0.095291753
                                 0.030756347
                                              0.030756347
                                                           0.007167624
## 2
      0.0858957548
                    0.081302857
                                 0.044249375
                                              0.044249375
                                                           0.030255551
## 3
      0.0767835798
                    0.073796966
                                 0.049215438
                                              0.049215438
                                                           0.039618042
##
  4
      0.0742232696
                    0.071655845
                                 0.050338674
                                              0.050338674
                                                           0.041898394
## 5
      0.0729503092
                    0.070585855
                                 0.050851019
                                              0.050851019
                                                           0.042972795
## 6
      0.0654132728
                    0.064173888
                                 0.053235264
                                              0.053235264
                                                           0.048498362
## 7
                    0.063106556
                                 0.053517667
                                              0.053517667
                                                           0.049265816
      0.0641738878
## 8
      0.0532352640
                    0.053517667
                                 0.054581104
                                              0.054581104
                                                           0.054199675
## 9
      0.0532352640
                    0.053517667
                                 0.054581104
                                              0.054581104
                                                           0.054199675
## 10
      0.0484983619
                    0.049265816
                                 0.054199675
                                              0.054199675
                                                           0.055252412
## 11
      0.0484983619
                    0.049265816
                                 0.054199675
                                              0.054199675
                                                           0.055252412
      0.0473261275
                    0.048203803
                                 0.054022195
                                              0.054022195
##
  12
                                                           0.055405972
## 13
      0.0461586897
                    0.047142170
                                 0.053811867
                                              0.053811867
                                                           0.055515683
      0.0438382035
                    0.045020043
                                 0.053292665
                                              0.053292665
                                                           0.055603556
                    0.033375508
                                 0.048088364
                                              0.048088364
                                                           0.052951613
## 15
      0.0314184774
## 16
      0.0292226997
                    0.031263258
                                 0.046715093
                                              0.046715093
                                                           0.051899397
## 17
      0.0259650066
                    0.028097733
                                 0.044408822
                                              0.044408822
                                                           0.049992202
## 18
      0.0227504819
                    0.024935627
                                 0.041806911
                                              0.041806911
                                                           0.047690360
      0.0216885666
                    0.023882351
                                              0.040873910
##
  19
                                 0.040873910
                                                           0.046835380
##
  20
      0.0174888703
                    0.019673047
                                 0.036813418
                                              0.036813418
                                                           0.042976966
      0.0164509375
                                              0.035716173
##
  21
                    0.018621671
                                 0.035716173
                                                           0.041902738
## 22
      0.0113332203
                    0.013370488
                                 0.029737217
                                              0.029737217
                                                           0.035873857
## 23
      0.0063354151
                    0.008128803
                                 0.022937041
                                              0.022937041
                                                           0.028748736
## 24
      0.0024235076
                    0.003942292
                                 0.016905623
                                              0.016905623
                                                           0.022259348
      0.0004963327
                    0.001851316
                                 0.013692821
                                              0.013692821
                                                           0.018751556
## 26 -0.0033004593 -0.002326077
                                 0.006873033
                                              0.006873033
                                                           0.011209778
## 27 -0.0060976902 -0.005455133 0.001413279
                                              0.001413279
                                                           0.005093024
## 28 -0.0142303732 -0.014821787 -0.016739816 -0.016739816 -0.015625115
## 29 -0.0219745412 -0.024157670 -0.037553662 -0.037553662 -0.039895070
## 30 -0.0236427061 -0.026228132 -0.042540297 -0.042540297 -0.045770738
##
                           12
                                        13
               11
                                                     14
```

```
## 1
                    0.00176022 -0.003451273 -0.013286527 -0.0533728027
##
  2
       0.030255551
                     0.02699502
                                 0.023829652
                                              0.017784429 -0.0086597260
##
  3
       0.039618042
                     0.03734636
                                 0.035125743
                                               0.030837710
                                                            0.0109047819
                     0.03988775
                                 0.037916873
                                               0.034094432
##
  4
       0.041898394
                                                             0.0159145573
##
   5
       0.042972795
                     0.04108909
                                 0.039239717
                                               0.035643995
                                                             0.0183227644
##
  6
       0.048498362
                    0.04732613
                                 0.046158690
                                               0.043838203
                                                             0.0314184774
##
  7
       0.049265816
                     0.04820380
                                 0.047142170
                                               0.045020043
                                                             0.0333755081
## 8
       0.054199675
                     0.05402220
                                 0.053811867
                                               0.053292665
                                                             0.0480883640
##
  9
       0.054199675
                     0.05402220
                                 0.053811867
                                               0.053292665
                                                             0.0480883640
## 10
       0.055252412
                     0.05540597
                                 0.055515683
                                               0.055603556
                                                             0.0529516130
##
       0.055252412
                     0.05540597
                                 0.055515683
                                               0.055603556
                                                             0.0529516130
   11
##
   12
       0.055405972
                     0.05563632
                                 0.055820436
                                               0.056049949
                                                             0.0540062908
                                               0.056443810
##
   13
       0.055515683
                     0.05582044
                                 0.056076708
                                                             0.0549965148
##
   14
       0.055603556
                     0.05604995
                                 0.056443810
                                               0.057073937
                                                             0.0567836016
                                                             0.0620041338
##
  15
       0.052951613
                     0.05400629
                                 0.054996515
                                               0.056783602
##
   16
       0.051899397
                     0.05303363
                                 0.054103123
                                               0.056047899
                                                             0.0621154224
                                                             0.0617989521
##
       0.049992202
                     0.05122785
                                 0.052399431
                                               0.054550355
   17
       0.047690360
                     0.04900594
                                 0.050259415
                                               0.052580024
##
   18
                                                             0.0609023977
  19
                                                             0.0604746387
##
       0.046835380
                    0.04817283
                                 0.049449115
                                               0.051818183
##
   20
       0.042976966
                     0.04437801
                                 0.045723110
                                               0.048245501
                                                             0.0581190650
##
  21
       0.041902738
                    0.04331371
                                 0.044670407
                                               0.047221001
                                                             0.0573690372
                                 0.038679686
##
  22
       0.035873857
                     0.03729865
                                               0.041310520
                                                             0.0526520913
                                                             0.0463238010
## 23
       0.028748736
                     0.03012765
                                 0.031476951
                                               0.034086743
##
  24
       0.022259348
                     0.02355857
                                 0.024842113
                                               0.027362146
                                                             0.0401010009
##
  25
       0.018751556
                    0.01999661
                                 0.021233811
                                               0.023684656
                                                             0.0366028782
   26
       0.011209778
                    0.01231783
                                 0.013435440
                                               0.015699294
                                                             0.0288331875
                    0.00607326
                                 0.007077616
##
   27
       0.005093024
                                              0.009158687
                                                             0.0223291548
##
   28
      -0.015625115 -0.01515729 -0.014613805 -0.013299856 -0.0006634469
   29 -0.039895070 -0.04013308 -0.040232151 -0.040013483 -0.0288768043
##
   30 -0.045770738 -0.04619187 -0.046458402 -0.046527696 -0.0358554308
##
                16
                              17
                                             18
                                                            19
##
      -0.058114376 \ -0.063757406 \ -0.0676372390 \ -0.0685386951 \ -0.0701854116
  1
##
      -0.012230559
                   -0.016873042 -0.0206590053 -0.0217306554 -0.0250655669
##
  3
                    0.003887019
                                  0.0002891589 -0.0008079949 -0.0046859451
       0.007944477
                    0.009241775
                                  0.0057153448
                                                 0.0046194079
##
   4
       0.013126135
                                                                0.0006333596
## 5
       0.015619857
                    0.011823038
                                  0.0083352704
                                                 0.0072413592
                                                                0.0032091045
##
  6
       0.029222700
                     0.025965007
                                  0.0227504819
                                                 0.0216885666
                                                                0.0174888703
## 7
                     0.028097733
       0.031263258
                                  0.0249356268
                                                 0.0238823511
                                                                0.0196730473
                     0.044408822
##
  8
       0.046715093
                                  0.0418069113
                                                 0.0408739102
                                                                0.0368134182
##
  9
       0.046715093
                     0.044408822
                                  0.0418069113
                                                 0.0408739102
                                                                0.0368134182
##
  10
       0.051899397
                     0.049992202
                                  0.0476903599
                                                 0.0468353802
                                                                0.0429769657
                     0.049992202
##
   11
       0.051899397
                                  0.0476903599
                                                 0.0468353802
                                                                0.0429769657
  12
##
       0.053033629
                     0.051227855
                                  0.0490059432
                                                 0.0481728309
                                                                0.0443780069
##
                                  0.0502594149
                                                 0.0494491150
   13
       0.054103123
                     0.052399431
                                                                0.0457231098
##
  14
       0.056047899
                     0.054550355
                                  0.0525800238
                                                 0.0518181831
                                                                0.0482455009
## 15
       0.062115422
                     0.061798952
                                  0.0609023977
                                                 0.0604746387
                                                                0.0581190650
##
   16
       0.062377019
                     0.062283882
                                  0.0616081066
                                                 0.0612533728
                                                                0.0591870610
##
   17
       0.062283882
                     0.062530703
                                  0.0622008334
                                                 0.0619627236
                                                                0.0603695178
##
   18
       0.061608107
                     0.062200833
                                  0.0622345562
                                                 0.0621215741
                                                                0.0610485303
##
   19
       0.061253373
                    0.061962724
                                  0.0621215741
                                                 0.0620521909
                                                                0.0611629912
##
   20
       0.059187061
                     0.060369518
                                  0.0610485303
                                                 0.0611629912
                                                                0.0610614522
##
  21
       0.058508639
                     0.059811025
                                  0.0606249905
                                                 0.0607877745
                                                                0.0608962217
## 22
       0.054145464
                     0.056057410
                                  0.0575756183
                                                 0.0579941908
                                                                0.0592309955
## 23
       0.048163848
                    0.050701878
                                  0.0529734576
                                                 0.0536714397
                                                                0.0561673124
```

```
0.0527094770
##
  25
      0.038849568
                   0.042160711
                                0.0454011840
                                              0.0464656374
                                                             0.0506449297
                   0.035185066
                                              0.0404384354
##
  26
      0.031345294
                                0.0391107708
                                                             0.0458445758
                                0.0337407897
##
  27
      0.025037344
                   0.029280527
                                              0.0352757836
                                                             0.0416569585
##
  28
       0.002617661
                   0.008106772
                                0.0142768233
                                              0.0164848267
                                                             0.0260734399
  29 -0.025045771 -0.018257191 -0.0102181779 -0.0072606324
##
                                                             0.0059589212
  30 -0.031905314 -0.024820693 -0.0163447384 -0.0132102347
                                                             0.0008737072
##
                 21
                              22
                                           23
                                                        24
                                                                      25
##
     -0.0701073138 -0.066778163 -0.058551243 -0.048443314 -0.0422138842
  1
##
  2
     -0.0256613727 -0.027212869 -0.026385143 -0.024009923 -0.0222512997
  3
     -0.0055277664 -0.008970876 -0.011137324 -0.011951285 -0.0120518673
##
      -0.0002637276 -0.004152615 -0.007047254 -0.008647107 -0.0092084132
##
  5
      0.0022868884 - 0.001809107 - 0.005046627 - 0.007018542 - 0.0077984645
       0.0164509375
                                              0.002423508
## 6
                     0.011333220
                                 0.006335415
                                                            0.0004963327
## 7
       0.0186216711
                     0.013370488
                                 0.008128803
                                              0.003942292
                                                            0.0018513163
## 8
       0.0357161733
                     0.029737217
                                  0.022937041
                                               0.016905623
                                                            0.0136928214
## 9
       0.0357161733
                     0.029737217
                                  0.022937041
                                              0.016905623
                                                            0.0136928214
      0.0419027382
                     0.035873857
                                  0.028748736
                                              0.022259348
##
  10
                                                            0.0187515562
##
      0.0419027382
                     0.035873857
                                 0.028748736
                                              0.022259348
                                                            0.0187515562
  11
##
  12
       0.0433137071
                     0.037298646
                                 0.030127646
                                              0.023558572
                                                            0.0199966095
##
  13
      0.0446704072
                     0.038679686
                                 0.031476951
                                              0.024842113
                                                            0.0212338106
## 14
      0.0472210005
                     0.041310520
                                 0.034086743
                                              0.027362146
                                                            0.0236846564
      0.0573690372
                     0.052652091
                                 0.046323801
                                              0.040101001
                                                            0.0366028782
## 15
##
  16
       0.0585086389
                     0.054145464
                                 0.048163848
                                              0.042213278
                                                            0.0388495676
                     0.056057410
## 17
      0.0598110248
                                 0.050701878
                                              0.045264073
                                                            0.0421607105
  18
      0.0606249905
                     0.057575618
                                 0.052973458
                                              0.048173721
                                                            0.0454011840
##
  19
       0.0607877745
                     0.057994191
                                 0.053671440
                                              0.049112238
                                                            0.0464656374
##
  20
       0.0608962217
                     0.059230995
                                 0.056167312
                                              0.052709477
                                                            0.0506449297
                                              0.053569579
##
  21
      0.0607876613
                     0.059430825
                                 0.056717267
                                                            0.0516701224
## 22
      0.0594308253
                     0.059773747
                                  0.059022955
                                              0.057634848
                                                            0.0566783031
## 23
       0.0567172667
                     0.059022955
                                 0.060588504
                                              0.061308043
                                                            0.0614901797
##
  24
       0.0535695794
                     0.057634848
                                 0.061308043
                                              0.063964307
                                                            0.0651983420
##
   25
       0.0516701224
                     0.056678303
                                  0.061490180
                                               0.065198342
                                                            0.0670053102
##
  26
      0.0472199813
                     0.054240231
                                 0.061499186
                                              0.067478216
                                                            0.0705250205
       0.0433125520
                     0.051952318
                                 0.061195082
                                               0.069023451
                                                            0.0730823555
##
   27
##
  28
      0.0286597430
                     0.042726158
                                 0.058684070
                                              0.072812280
                                                            0.0803303436
##
  29
       0.0096111525
                     0.029956366
                                 0.053775009
                                               0.075330792
                                                            0.0869423063
##
  30
                     0.026637401
                                               0.075717949
                                                            0.0883252575
      0.0047811744
                                 0.052358445
                             27
                                           28
                                                        29
##
                26
                                                                      30
##
     -0.027404096 -0.014239692 0.0358327029
                                              0.101773870
                                                            0.1185824811
  1
  2
     -0.017592027 -0.013098300 0.0055220015
                                              0.031850980
                                                            0.0387487217
     -0.011640233 -0.010795310 -0.0055029503
                                              0.003925794
##
  .3
                                                            0.0065828019
##
  4
     -0.009853788 -0.009920234 -0.0079719971 -0.002802396 -0.0012161266
     -0.008946242 -0.009446516 -0.0090930306 -0.005958085 -0.0048837018
##
  5
## 6
     -0.003300459 -0.006097690 -0.0142303732 -0.021974541 -0.0236427061
     -0.002326077 -0.005455133 -0.0148217872 -0.024157670 -0.0262281324
## 7
## 8
       0.006873033
                   0.001413279 -0.0167398162 -0.037553662 -0.0425402972
## 9
       0.006873033
                   0.001413279 -0.0167398162 -0.037553662 -0.0425402972
## 10
      0.011209778
                   0.005093024 -0.0156251154 -0.039895070 -0.0457707380
##
       0.011209778
                   0.005093024 -0.0156251154 -0.039895070 -0.0457707380
                   0.006073260 -0.0151572903 -0.040133079 -0.0461918664
  12
##
      0.012317835
## 13
      0.013435440
                   0.007077616 -0.0146138053 -0.040232151 -0.0464584022
## 14
      0.015699294
                   0.009158687 -0.0132998556 -0.040013483 -0.0465276955
```

```
## 16 0.031345294 0.025037344 0.0026176610 -0.025045771 -0.0319053139
## 17 0.035185066 0.029280527 0.0081067725 -0.018257191 -0.0248206933
## 18 0.039110771 0.033740790 0.0142768233 -0.010218178 -0.0163447384
## 19 0.040438435 0.035275784 0.0164848267 -0.007260632 -0.0132102347
## 20
      0.045844576 0.041656958 0.0260734399 0.005958921 0.0008737072
## 21 0.047219981 0.043312552 0.0286597430 0.009611152 0.0047811744
## 22 0.054240231 0.051952318 0.0427261576 0.029956366 0.0266374010
## 23 0.061499186 0.061195082 0.0586840704 0.053775009 0.0523584452
## 24
      0.067478216 0.069023451
                               0.0728122795  0.075330792  0.0757179492
## 25  0.070525021  0.073082356  0.0803303436  0.086942306  0.0883252575
## 26 0.076733207 0.081489603
                               0.0962743910 0.111832581 0.1153949863
                               0.1090268559 0.131959127 0.1373205063
## 27
      0.081489603 0.088048297
## 28 0.096274391 0.109026856
                               0.1513698866 0.199841372 0.2114450723
      0.111832581 0.131959127
## 29
                               0.1998413719 0.278977526 0.2980916471
## 30  0.115394986  0.137320506  0.2114450723  0.298091647  0.3190469613
```

The hat matrix is shown in the R result, which is a huge 30×30 matrix.

Part f

```
# Find the SSE
SSE <- t(y)%*%(diag(30)-H)%*%y
# Define n and p
n <- 30
p <- 3
# Find an estimate for the sigmasq
sigmasq <- SSE[1]/(n - p)
#Return the estimate for sigmasq
sigmasq</pre>
```

[1] 246.0115

Under Gauss-Markov assumptions, we know that $E(SSE) = \sigma^2(n-p)$, then $\sigma^2 \approx \frac{SSE}{n-p} = 246.0115$.

Part g

```
# Find variance of betahat using matrices varbetahat <- sigmasq*solve(t(X)%*%X)  
# Show the result varbetahat  
## (Intercept) Lord I(Lord^2)  
## (Intercept) 3914.526 -5445.052 1819.5161  
## Lord -5445.052 7688.690 -2601.9369  
## I(Lord^2) 1819.516 -2601.937 891.1995  
From the result, Var(\hat{\beta}) = \begin{bmatrix} \frac{3914.526}{-5445.052} & \frac{75485.052}{7688.690} & \frac{2601.9369}{-2601.9369} \\ \frac{1819.516}{1819.516} & \frac{-2601.937}{-2601.937} & \frac{891.1995}{891.1995} \end{bmatrix}
```

Part h

```
# Find the standard error for beta2
SEbeta2 <- sqrt(7688.690)
# Show the result
SEbeta2</pre>
```

```
## [1] 87.68518
```

From the code above, we can see that $SE_{\hat{\beta}_2} = 8768518$.

Question 2

```
# Creating the dataset
x1 \leftarrow runif(100,0,10)
x2 \leftarrow runif(100,5,15)
# Creating two lists each of length 1000 with NA as entries
sebeta2hats <- vector(mode = "double", length = 1000)</pre>
beta2hats <- vector(mode = "double", length = 1000)</pre>
# Construct sebeta2hats and beta2hats
#Set seed in order to keep the randomized process unchanged
set.seed(2022)
for (i in seq(1,1000)){
  # Creating 1000 random y for each time of iteration
  y \leftarrow 2*x1-x2+rnorm(100,0,5)
  # Fitting model with each y
  modeli <-lm(y~x1+x2)
  # Storing the betahats into the vector
  beta2hats[i] <- modeli$coefficient[2]</pre>
  # Finding the covariance matrix for each iteration
  covi <- vcov(modeli)</pre>
  # Storing the standard error of the beta2hat into the vector
  sebeta2hats[i] <- sqrt(diag(covi)[2])</pre>
# Finding the standard deviation of the beta2hat list
sd(beta2hats)
```

```
## [1] 0.1844253
```

```
# Finding the mean of the sebeta2hats list
mean(sebeta2hats)
```

[1] 0.1788813

From the result, we can see that the standard deviation of $\hat{\beta}_2$ and mean of the $SE_{\hat{\beta}_2}$ are almost the same. the standard deviation of $\hat{\beta}_2$ measures how these 1000 $\hat{\beta}_2$ deviate from the real value of β_2 , while $SE_{\hat{\beta}_2}$ measures the average standard deviation for $each\hat{\beta}_2$ of the 1000 models. Both of the measures are exploring how our estimated $\hat{\beta}_2$ is away from the real value, but they calculate the standard deviation for the whole population and for each individual separately. This makes the two values be almost the same, since, in a large population like 1000 case, the trend is the consistent.