## HW2-2

## 假設:

(z): 巻積操作的結果

•  $a = \sigma(z)$ :激活函數的輸出

• y':最終的迴歸結果

y:正確的標籤

•  $L=(y-y')^2$ : 均方誤差 (MSE) 損失函數

接著,我們使用Chain rule來推導梯度。

## 1. 對於 $w_{11}$ 的梯度:

$$\frac{\partial L}{\partial w_{11}} = \frac{\partial L}{\partial y'} \cdot \frac{\partial y'}{\partial a} \cdot \frac{\partial a}{\partial z} \cdot \frac{\partial z}{\partial w_{11}}$$

•  $rac{\partial L}{\partial u'} = 2(y-y')$  ( MSE 的梯度 )

•  $\frac{\partial y'}{\partial a} = w$  ( 假設 y' = wa )

•  $rac{\partial a}{\partial z} = \sigma'(z)$  ( 假設  $\sigma$  是 sigmoid 函數 )

•  $\frac{\partial z}{\partial w_{11}} = a_{11}$  (根據卷積操作)

將這些部分相乘,我們得到梯度:

$$rac{\partial L}{\partial w_{11}} = 2(y-y') \cdot w \cdot \sigma'(z) \cdot a_{11}$$

## 2. 對於 $a_{00}$ 的梯度:

$$rac{\partial L}{\partial a_{00}} = rac{\partial L}{\partial y'} \cdot rac{\partial y'}{\partial a} \cdot rac{\partial a}{\partial z} \cdot rac{\partial z}{\partial a_{00}}$$

•  $\frac{\partial z}{\partial a_{00}} = w_{11} \cdot \sigma'(z) \cdot w_{11}$  (根據卷積操作和激活函數的導數)

將這些部分相乘,我們得到梯度:

$$rac{\partial L}{\partial a_{00}} = 2(y-y') \cdot w \cdot \sigma'(z) \cdot w_{11} \cdot \sigma'(z) \cdot w_{11}$$