

*Computer Vision & Multimedia Analysis Course*

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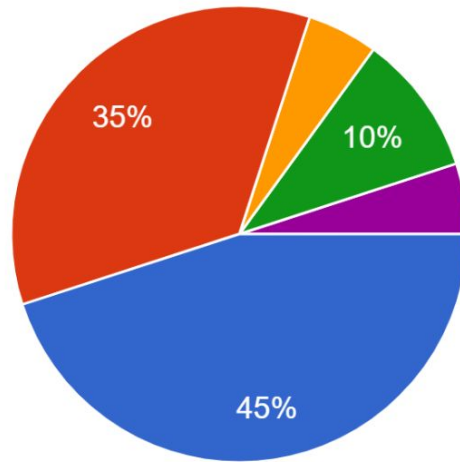
# Lab 3: Tracking

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# Feedback

Which is your background?

20 risposte

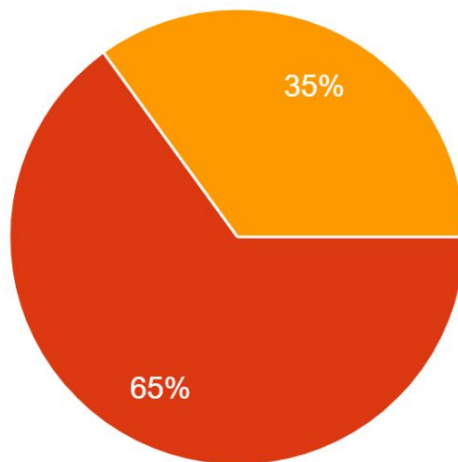


- Computer Science
- Communication Engineering
- Mechanical Engineering
- Information Engineering
- Mathematics

# Feedback

The Lab so far:

20 risposte



- Too easy, I would like something more challenging
- It's ok, I can easily follow
- I'll need to look again into something, but mostly ok
- so-so, I'm not confident with what we have done so far
- hard to follow, it is not clear

# What you asked for

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- More OpenCV “*behind the scenes*” 🚧
- More individual tasks 📄





# What's up today (and next time?)

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- Good Features to Track + Lucas Kanade optical flow
- Meanshift/Camshift algorithm
- Kalman filter

# Good Features to Track

- For each candidate point, compute:

$$\mathbf{Z} = \begin{bmatrix} \sum_W J_x^2 & \sum_W J_x J_y \\ \sum_W J_y J_x & \sum_W J_y^2 \end{bmatrix}$$

- $\mathbf{J}_x$  and  $\mathbf{J}_y$  are the gradients evaluated on the point in  $\mathbf{x}$  and  $\mathbf{y}$  direction within  $\mathbf{W}$  ( $n \times n$  window)
- A good feature point is where the smallest **eigenvalue** of  $\mathbf{Z}$  is larger than a specified threshold
- *In practice, it highlights corner points and textures*



# Lucas-Kanade optical flow estimation

- Two-frame differential method for **optical flow estimation** developed by *Bruce D. Lucas* and *Takeo Kanade* (1981)
- Consider  $\mathbf{u}=[u_x, u_y]$  in frame  $\mathbf{I}$  and  $\mathbf{v}=[v_x, v_y]$  in frame  $\mathbf{J}$
- The goal is to find  $\mathbf{d}$  that satisfies  $\mathbf{v}=\mathbf{u}+\mathbf{d}$  such as  $\mathbf{I}$  and  $\mathbf{J}$  are similar (translational model)
- Because of the **aperture problem**, similarity must be defined in 2D
- $\mathbf{d}$  is the vector that minimizes

$$\epsilon(\mathbf{d}) = \epsilon(d_x, d_y) = \sum_{x=u_x-\omega_x}^{u_x+\omega_x} \sum_{y=u_y-\omega_y}^{u_y+\omega_y} (I(x, y) - J(x + d_x, y + d_y))^2.$$

- $\omega$  is the integration window



# GFF+LK tracking



Detect and select good Features  
using GFF



Track detected feature using  
LK optical flow



# Exercises

## Part 1

- Track features in the environment using

```
corners, status, err = cv2.calcOpticalFlowPyrLK(prev_frame, frame, prev_corners, None)
```

## Part 2 (optional)

- Draw trajectory of tracked points

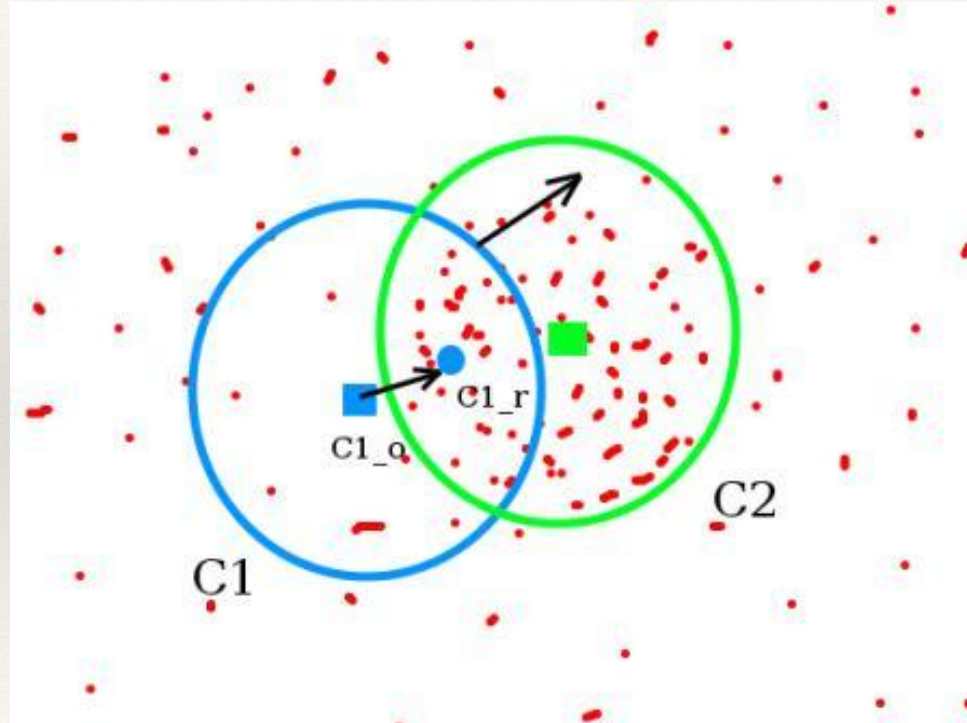
# Exercises

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## Part 3 🤔

- How to avoid losing features after some time?
  - Re-detect features using GFF

# Meanshift algorithm





# Meanshift algorithm



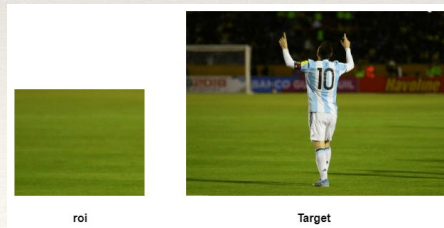
roi



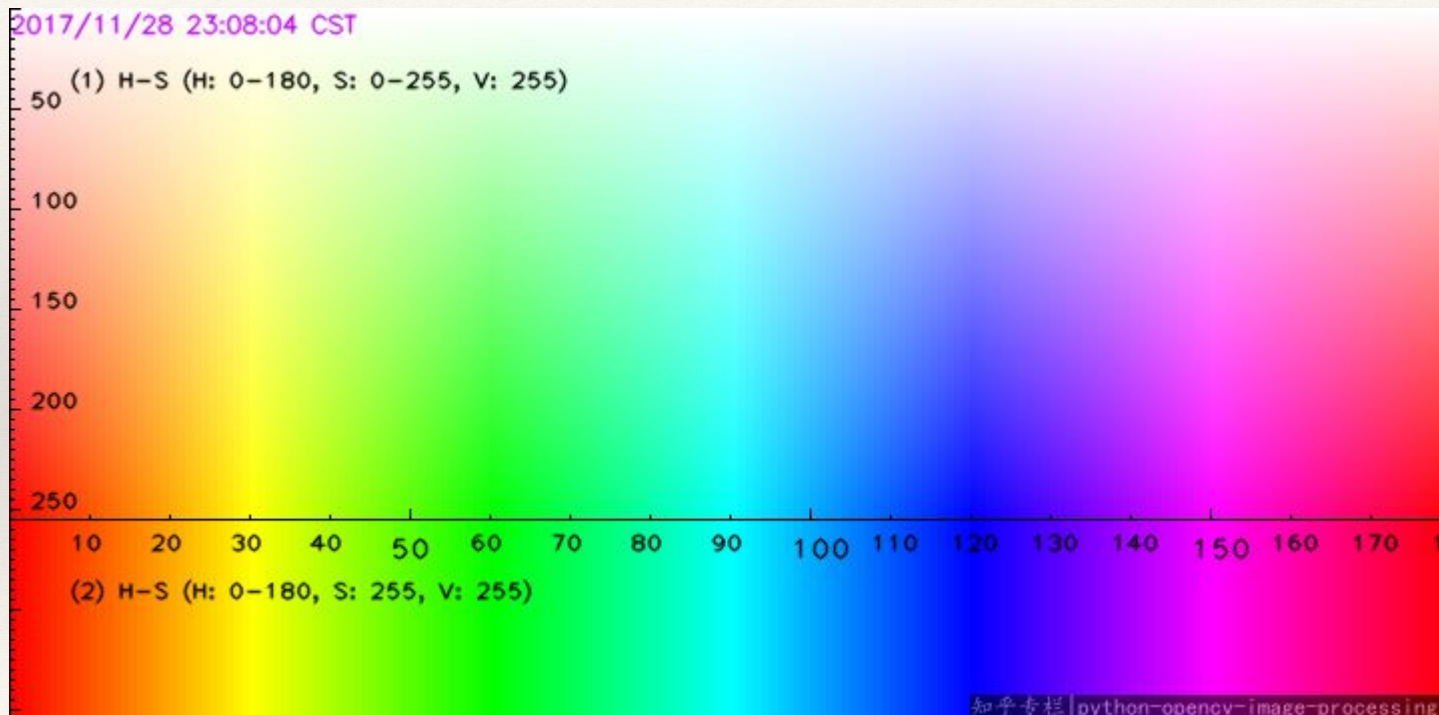
Target



# Meanshift algorithm



# Meanshift algorithm





# Meanshift algorithm

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- RGB to HSV image conversion
- Manually select Region Of Interest (ROI)
- Calculate histogram of ROI
- Back projection of the histogram
- Tracking





# Camshift algorithm

- Finds an object center using MeanShift
- Adjusts the window size and finds the optimal rotation.

## Exercise

- Implement camShift algorithm instead of MeanShift
- Check documentation on the website
- Display the window using the poly lines function

```
pts = cv2.boxPoints(ret).astype(int)
img2 = cv2.polylines(frame, [pts], True, 255, 2)
```
- Bonus: display backprojection and plot histograms



# Kalman filter

$$\mathbf{x}_k = \mathbf{A}_k \mathbf{x}_{k-1} + \mathbf{w}_{k-1}$$

$$\mathbf{z}_k = \mathbf{H}_k \mathbf{x}_k + \mathbf{v}_k$$

- $\mathbf{x}_k$  → **current state**
- $\mathbf{x}_{k-1}$  → previous state
- $\mathbf{A}_k$  → state transition matrix
- $\mathbf{w}_k$  → process noise
- $\mathbf{z}_k$  → **actual measurement**
- $\mathbf{H}_k$  → measurement matrix
- $\mathbf{v}_k$  → measurement noise

# Kalman filter: predict and correct

$$\hat{\mathbf{x}}_k^- = \mathbf{A}_k \hat{\mathbf{x}}_{k-1}$$

$$\mathbf{P}_k^- = \mathbf{A}_k \mathbf{P}_{k-1} \mathbf{A}_k^T + \mathbf{Q}_{k-1}$$

$$\mathbf{K}_k = \mathbf{P}_k^- \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_k^- \mathbf{H}_k^T + \mathbf{R}_k)^{-1}$$

$$\hat{\mathbf{x}}_k = \hat{\mathbf{x}}_k^- + \mathbf{K}_k (\mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{x}}_k^-)$$

$$\mathbf{P}_k = (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_k^-$$



# Kalman filter applied on mouse motion

- Motion equation:  $P_t = P_0 + V * t$

$$x_k = A_k x_{k-1} + w_{k-1}$$

$$z_k = H_k x_k + v_k$$

- $x_k$  is the current state → a vector with the position and velocity
- $A_k$  is the state transition matrix → matrix that describe the system, in our case the motion equation
- $H_k$  is the measurement matrix → determined by the current measured position of the mouse
- $z_k$  is the actual measurement → used to compute the “posteriori”



# Transition matrix $A_t$

$$X_{t+1} = A_t X_t$$

$$\begin{bmatrix} x_{t+1} \\ y_{t+1} \\ vx_{t+1} \\ vy_{t+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_t \\ y_t \\ vx_t \\ vy_t \end{bmatrix}$$



# Transition matrix

$$X = [x, y, v_x, v_y]^t$$

- $x_{t+1} = x_t + v_x$   $\rightarrow [1, 0, 1, 0]$
- $y_{t+1} = y_t + v_y$   $\rightarrow [0, 1, 0, 1]$
- $v_{x_{t+1}} = v_x$   $\rightarrow [0, 0, 1, 0]$
- $v_{y_{t+1}} = v_y$   $\rightarrow [0, 0, 0, 1]$

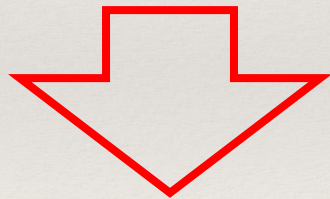
$$X_{t+1} = A_t X_t$$

$$\begin{bmatrix} x_{t+1} \\ y_{t+1} \\ vx_{t+1} \\ vy_{t+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_t \\ y_t \\ vx_t \\ vy_t \end{bmatrix}$$

# Exercise

Insert **acceleration** in the transition matrix of the Kalman filter

$$X_t = X_0 + v_x * t$$



$$X_t = X_0 + v_x * t + 1/2 a_x * t^2$$

# Transition matrix

$$X = [x, y, v_x, v_y, a_x, a_y]^t$$

- $x_{t+1} = x_t + v_{x_t} + 0.5 a_{x_t}$
- $y_{t+1} = y_t + v_{y_t} + 0.5 a_{y_t}$
- $v_{x_{t+1}} = v_{x_t} + a_{x_t}$
- $v_{y_{t+1}} = v_{y_t} + a_{y_t}$
- $a_{x_{t+1}} = a_{x_t}$
- $a_{y_{t+1}} = a_{y_t}$

$$X_{t+1} = A_t X_t$$

$$\begin{bmatrix} x_{t+1} \\ y_{t+1} \\ vx_{t+1} \\ vy_{t+1} \\ ax_{t+1} \\ ay_{t+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1 & 0 & \frac{1}{2} & 0 \\ 0 & 1 & 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_t \\ y_t \\ vx_t \\ vy_t \\ ax_t \\ ay_t \end{bmatrix}$$