#### Homework 4

# [Question 1] Develop NEARBY14 for the KNN search in voxels

Source

For Nearby 14 voxel search, we just need to additionally search the corner 8 voxels of the search box:

However, I think it's more reasonable to define NEARBY18 instead of NEARBY14, as they are closer

```
_nearby_grids = {NNCoord(0, 0, 0), NNCoord(-1, 0, 0), NNCoord(1, 0, 0), NNCoord(0, 1, 0), NNCoord(0, -1, 0), NNCoord(0, 0, -1), NNCoord(1, 1, 0), NNCoord(1, -1, 0), NNCoord(-1, 1, 0), NNCoord(-1, -1, 0), NNCoord(0, 1, 1), NNCoord(0, 1, -1), NNCoord(0, -1, 1), NNCoord(0, -1, -1), NNCoord(1, 0, 1), NNCoord(1, 0, -1), NNCoord(-1, 0, 1), NNCoord(-1, 0, -1), NNCoord(-1, 0, 1), NNCoord(-1, 0, -1);
```

Performance is:

• 19k points, 4ms (NEARBY 18), recall: 76.6%, precision: 78.6%

### [Question 2] Proof

Prove that the solution to the question below is the largest eigen vector or Singular vector

$$d^* = argmax_d |Ad|^2$$

Proof:

$$\begin{aligned} |Ad^2| &= (Ad)^T (Ad) = d^T A^T Ad \\ \text{Using Eigen Value Decomposition:} \\ A^T A &= \\ \Rightarrow \\ |Ad^2| &= d^T V \Lambda V^T d \end{aligned}$$

Where V and  $\Lambda$  are eigen vectors and their eigen values:

$$\begin{split} V &= [v_1|v_2\cdots|v_n]\\ \Lambda &= diag(\lambda_1^2,\lambda_2^2\cdots) \end{split}$$

Let:

$$d = \alpha_1 v_1 + \alpha_2 v_2 + \dots + \alpha_n v_n$$

Then we have:

$$|Ad^2| = d^T V \Lambda V^T d = [\alpha_1 | \alpha_2 | \cdots | \alpha_n]$$

Since we have imposed the length constraint:

$$|d| = 1 = \alpha_1^2 + \alpha_2^2 + \dots + \alpha_n^2$$

Maximum of  $|Ad^2|$  is achieved when  $\alpha_n=1$  for the largest eigen value  $\lambda_n$ . d is now  $v_n$  (They are also "singular vectors if we do SVD on A")

## [Question 3] Compare The Performance of nanoflann With This Chapter's KNN Searches

J. L. Blanco and P. K. Rai, "nanoflann: a C++ header-only fork of FLANN, a library for nearest neighbor (NN) with kd-trees." https://github.com/jlblancoc/nanoflann, 2014.

Given 19k XYZI points:

The performance of Nanoflann is (max leaf size = 10):

- k = 1, 100%, 4ms
- k = 5, 100%, 4ms

The performance of my KD tree is:

- k = 1, 100%, 6ms
- k = 5, 100%, 6ms

#### Therefore, Nanoflann KD Tree is by far the best KNN Search method

Here is the code for testing:

```
#pragma once
#include <halo/common/sensor_data_definitions.hpp>
#include <nanoflann/nanoflann.hpp>
namespace halo{
struct NanoflannPointCloudAdaptor {
```

```
// Reference to the actual point cloud data
    const halo::PointCloudType &pts;
    // Constructor
    explicit NanoflannPointCloudAdaptor (const halo::PointCloudType &points) : pts(points) ·
    // Must return the number of data points
    inline size_t kdtree_get_point_count() const { return pts.points.size(); }
    // Returns the dim'th component of the idx'th point in the class:
    inline float kdtree_get_pt(const size_t idx, const size_t dim) const {
        if (dim == 0) return pts.points[idx].x;
        else if (dim == 1) return pts.points[idx].y;
        else return pts.points[idx].z;
   }
    // Optional bounding-box computation: return false to default to a standard bbox comput
    template <class BBOX>
    bool kdtree_get_bbox(BBOX & /*bb*/) const { return false; }
};
template <typename PointT, int dim>
class NanoFlannKDTree {
public:
    using CloudPtr = std::shared_ptr<pcl::PointCloud<PointT>>;
    using PointCloudAdaptor = NanoflannPointCloudAdaptor;
   // Using 3 dimensions (for 3D point clouds). If you need a different dimensionality,
    // you could templatize the dimension.
   using KDTreeType = nanoflann::KDTreeSingleIndexAdaptor<</pre>
        nanoflann::L2_Simple_Adaptor<float, PointCloudAdaptor>,
        PointCloudAdaptor,
        dim /* dimensionality */
    >;
    // Constructor:
    // The KDTree parameters (e.g., maximum leaf size).
   NanoFlannKDTree(const PointCloudAdaptor &adaptor,
                    const nanoflann::KDTreeSingleIndexAdaptorParams &params)
        : adaptor_(adaptor), kd_tree_(dim, adaptor_, params) {kd_tree_.buildIndex();}
    // This function performs a multi-threaded nearest neighbor search.
    // It expects:
   // - query cloud: the point cloud whose points will be searched against the kd-tree.
    // - matches: a pre-sized vector where each query point will yield k matches
                  (i.e. matches.size() should equal query_cloud->points.size() * k).
    // - k: the number of nearest neighbors to find for each query point.
```

```
// Returns true on success, false otherwise.
    bool search_tree_multi_threaded(const CloudPtr &query_cloud,
                                    std::vector<NNMatch> &matches, size_t k) const {
        if (!query_cloud || query_cloud->points.empty()) {
            return false;
        size_t num_points = query_cloud->points.size();
        matches.resize(num_points * k);
        const size_t num_results = k;
        // Create an index container [0, 1, 2, ..., num_points-1]
        std::vector<size_t> indices(num_points);
        std::iota(indices.begin(), indices.end(), 0);
        // Process each query point in parallel.
        std::for_each(std::execution::par_unseq, indices.begin(), indices.end(),
            [&](size_t i) {
                const auto &pt = query_cloud->points[i];
                float query_pt[3] = { pt.x, pt.y, pt.z };
                // Allocate temporary storage for this iteration.
                std::vector<typename KDTreeType::IndexType> local_ret_index(num_results);
                std::vector<float> local_out_dist_sqr(num_results);
                kd_tree_.knnSearch(query_pt, num_results, local_ret_index.data(), local_out_
                for (size_t j = 0; j < k; ++j) {</pre>
                    matches[i * k + j].idx_in_this_cloud = i;
                    matches[i * k + j].closest_pt_idx_in_other_cloud = local_ret_index[j];
            });
        return true;
    }
private:
        // We store a copy of the adaptor here. It holds a reference to the original cloud.
   PointCloudAdaptor adaptor_;
    KDTreeType kd_tree_;
};
};
TEST(TestKNN, test_nanoflann_kdtree) {
    // Load point clouds from files.
   halo::CloudPtr first(new halo::PointCloudType);
```

```
halo::CloudPtr second(new halo::PointCloudType);
   pcl::io::loadPCDFile(first_scan_path, *first);
   pcl::io::loadPCDFile(second_scan_path, *second);
   // Use the second cloud as the query set.
   halo::CloudPtr test_cloud = second;
   std::vector<halo::NNMatch> matches;
   std::vector<halo::NNMatch> ground_truth_matches =
       halo::brute_force_nn(first, test_cloud, true);
   {
       halo::RAIITimer timer;
       halo::NanoflannPointCloudAdaptor adaptor(*first);
       halo::NanoFlannKDTree<halo::PointType, 3> nano_tree(adaptor,
       nanoflann::KDTreeSingleIndexAdaptorParams(10));
       size_t k = 1;
       nano_tree.search_tree_multi_threaded(test_cloud, matches, k);
       EXPECT_EQ(matches.size(), second->points.size() * k);
   }
   evaluate_matches(matches, ground_truth_matches, 1, first, second);
}
```