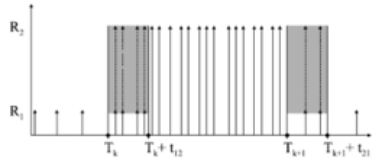


## Unbiased approximation (response time)



$$R = \sum_{i=1}^H w_i R_i \quad w_i = \frac{p_i \lambda_i}{\sum_{j=1}^H p_j \lambda_j}$$

$$p'_i = p_i + \sum_{j: \lambda_i > \lambda_j} p_i \alpha_{ij} t_{ij} - \sum_{j: \lambda_i < \lambda_j} p_j \alpha_{ji} t_{ji}$$

## Approximation construction

Identification of H(M1,...,MH)MMPP states  
Id of arrival rates  
Ev of steady state prob for each state Si of MMPP  
Ev of cumulative dist. function  
(linear combination of H states Mi/M/1)

### Unbiased approximation (response time)

It is approximated using as weights, probabilities pi,  
for MMPP to stay in each state Si

### Lower bound approximation

Systematic overestimation of the queue length during transient periods  
Ev of steady state prob for each state Si of MMPP  
(using standard results in queuing theory)  
Ev of the transient phases durations (classic queuing theory)  
Ev of modified probability  
Generation of lower bound by performing  
a weighted superposition of Mi/M/1

### Upper bound approximation

Systematic underestimation of queue ...

## XIV\_Approximate analytical models for networked servers subject to MMPP Arrival Process

### Markov Modulated Poisson Process

Goal: a technique to evaluate MMPP/M/1 with complexity as M/M/1

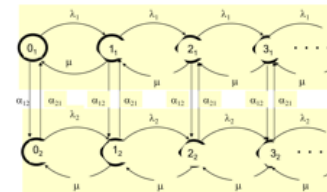
### SLA & penalty minimization

Process flow: shows the process in analysis

SLA risk analysis:

- 1) Def of params in the SLA
- 2) Workload characterization and svc time ident.
- 3) platform and resource allocation policy modeling and evaluation
- 4) Economical risk identification

### MMPP/M/1 states representation



Basic idea: model as a  
combo of M/M/1 process

Approx must be used to evaluate platforms subject to SLA constraints;  
response time must be less of T (e.g. 3 seconds) for a given P (e.g.95%)

$$F_{\text{approximation}}(T) < F_{\text{MMP/M/1}}(T) < P$$

### Basic idea (2/2)

