Knowledge Representation and Semantic Technologies – 14/9/2021

LAST NAME:
FIRST NAME:
ID (MATRICOLA):

Autorizzo la pubblicazione del mio voto di questo esame sul sito web http://www.diag.uniroma1.it/rosati/krst, secondo quanto prevede il decreto legislativo 196/2003 (codice in materia di protezione dei dati personali) che dichiaro di conoscere. In fede,

Exercise 1 Given the following \mathcal{ALC} TBox:

$$\begin{array}{cccc} A & \sqsubseteq & C \\ D & \sqsubseteq & \exists R.C \\ E & \sqsubseteq & \forall R.F \\ E & \sqsubseteq & B \\ F & \sqsubseteq & \neg B \\ G \sqcap B & \sqsubseteq & \exists R.A \\ H & \sqsubseteq & G \\ H & \sqsubseteq & \exists R.B \end{array}$$

- (a) tell whether the TBox \mathcal{T} is satisfiable, and if so, show a model for \mathcal{T} ;
- (b) tell whether the concept $E \sqcap G$ is satisfiable with respect to \mathcal{T} , and if so, show a model for \mathcal{T} where $E \sqcap G$ is satisfiable;
- (c) tell whether the concept $E \sqcap H$ is satisfiable with respect to \mathcal{T} , and if so, show a model for \mathcal{T} where $E \sqcap H$ is satisfiable;
- (d) given the ABox $\mathcal{A} = \{E(a), R(a, b)\}$, use the tableau method to establish whether the knowledge base $\langle \mathcal{T}, \mathcal{A} \rangle$ entails the assertion F(b).

Exercise 2 Given the following ASP program P:

```
\begin{array}{lll} r(x,y) &:= p(x,y,v)\,. \\ s(x,y) &:= p(v,x,y)\,. \\ t(x,z) &:= r(x,y)\,, \; s(y,z)\,, \; \text{not} \; r(x,z)\,. \\ t(x,z) &:= t(x,y)\,, \; t(y,z)\,, \; \text{not} \; r(x,z)\,. \\ u(x,y) &:= t(x,y)\,, \; \text{not} \; s(x,y)\,. \\ v(x,y) &:= u(y,x)\,. \\ w(x,z) &:= r(x,y)\,, \; s(y,z)\,, \; \text{not} \; u(x,z)\,. \\ w(x,y) &:= t(x,y)\,, \; \text{not} \; v(x,y)\,. \\ w(x,y) &:= v(x,y)\,, \; \text{not} \; t(x,y)\,. \\ p(a,b,c)\,. \; p(c,d,e)\,. \; p(e,f,f)\,. \end{array}
```

- (a) tell whether P is stratified;
- (b) compute the answer sets of P.

Exercise 3

We want to formalize knowledge about persons and kinship relationships. In particular, we want to formalize the following statements:

- 1. every person has a father and has a mother;
- 2. fathers are male and mothers are female;
- 3. the father of a father is a grandfather;
- 4. the mother of a mother is a grandmother;
- 5. the brother of a parent is an uncle.
- (a) Choose the most appropriate knowledge representation language for expressing the above knowledge among the following ones: \mathcal{ALC} , Datalog, Datalog with constraints, ASP, OWL, $DL\text{-}Lite_R$, \mathcal{EL} , RL, RDFS, motivating your choice;
- (b) express the above knowledge in the formalism chosen at the previous point.

Exercise 4

- (a) Write an RDF/RDFS model representing the following statements about URIs Employee, Manager, Division, TopManager, Person, Man, Woman, City, livesIn, worksWith, isManagerOf, leadsDivision, worksInDivision, locatedIn, Ann, Bob, Jane, Joe, Rome, Naples, Milan, ABC, XYZ.
 - 1. Employee, Manager, TopManager, Division, Man, Woman and City are classes;
 - 2. TopManager is a subclass of Manager which is a subclass of Employee;
 - 3. worksWith, livesIn, isManagerOf, leadsDivision and locatedIn are properties;
 - 4. isManagerOf is a subproperty of worksWith;
 - 5. isManagerOf has domain Manager and range Employee;

- 6. both worksInDivision and leadsDivision have domain Employee and range Division;
- 7. worksWith has domain Employee and range Employee;
- 8. livesIn has domain Person and range City;
- 9. locatedIn has domain Division and range City;
- 10. Jane is a manager;
- 11. Bob and Ann are employees;
- 12. Joe is manager of Bob;
- 13. Jane lives in Rome;
- 14. Mary leads division XYZ of the company;
- 15. division ABC is located in Milan.
- (b) Write SPARQL queries corresponding to the following requests: (b1) return every employee that works in a division located in Naples, and, optionally, the manager of such an employee; (b2) return every division that is located in the city where the manager that leads the division lives in; (b3) return every top manager that leads a division for which Ann works, and, optionally, the city where the manager lives.

Exercise 5

Given the RL knowledge base $\langle \mathcal{T}, \mathcal{A} \rangle$, where \mathcal{T} is the following TBox:

```
hasMother \sqsubseteq hasParent

hasFather \sqsubseteq hasParent

hasParent^- \sqsubseteq hasChild

\exists hasChild. \top \sqsubseteq PARENT

\exists hasChild.PARENT \sqsubseteq GRANDPARENT

\exists hasChild.GRANDPARENT \sqsubseteq GREAT-GRANDPARENT
```

and A is the following ABox:

```
hasMother(John, Ann), hasFather(John, Bob), hasMother(Ann, Mary), hasFather(Ann, Paul), hasMother(Bob, Jane), hasMother(Paul, Liz)
```

- 1. compute the materialization of the ABox \mathcal{A} with respect to the TBox \mathcal{T} ;
- 2. tell whether the concept assertion GREAT-GRANDPARENT(Liz) is entailed by $\langle \mathcal{T}, \mathcal{A} \rangle$.