



Advanced Databases and Information Systems
Summerterm 2019
Discussion on 27/06/2019

10. Sheet: Conjunctive Queries

Exercise 1 (Evaluation of conjunctive queries)

Consider the following sample instantiation \mathcal{I} of a database.

Sales	PName	SName	CName	Part	PName	Type
	Audi A7	Autohaus Wenz	Meier		Audi A8	Auto
	Audi A8	Autohaus Klein	Meier		Audi A7	Auto
	Audi A8	Autohaus Wenz	Smith		Suzuki GSX	Motorrad
	Suzuki GSX	Motorsport AG	Hofmann			

Cust	CName	CAddr	Supp	SName	SAddr
	Meier	Freiburg		Autohaus Wenz	Freiburg
	Smith	Freiburg		Autohaus Klein	Mannheim
	Hofmann	Mannheim		Motorsport AG	Mannheim

Compute the evaluation result of the following queries on instance \mathcal{I} and informally describe their meaning. Note that constants inside the queries are distinguished by *italic font*.

- a) $q_1: \text{ans}(C) \leftarrow \text{Sales}(P, S, C), \text{Cust}(C, \textit{Freiburg}), \text{Supp}(S, \textit{Freiburg})$
- b) $q_2: \text{ans}(S, P) \leftarrow \text{Sales}(P, S, \textit{Meier}), \text{Supp}(S, \textit{Mannheim}), \text{Part}(P, \textit{Auto})$
- c) $q_3: \text{ans}(S, P) \leftarrow \text{Sales}(P, S, \textit{Meier}), \text{Supp}(S, \textit{Mannheim}), \text{Part}(P, \textit{Auto})$
- d) $q_4: \text{ans}(C_1, C_2) \leftarrow \text{Cust}(C_1, \textit{Freiburg}), \text{Cust}(C_2, \textit{Freiburg}), \text{Sales}(P_1, S_1, C_1), \text{Sales}(P_2, S_2, C_2), \text{Supp}(S_1, X), \text{Supp}(S_2, X)$

Exercise 2 (Containment)

Consider the following pairs of Conjunctive Queries and decide for each pair q_i, q'_i if $q_i \sqsubseteq q'_i$, $q'_i \sqsubseteq q_i$, and $q_i \equiv q'_i$ holds. If such relationships hold provide the corresponding containment mappings. Otherwise, show that no such mapping exists.

- a) $q_1: \text{ans}(X, Y) \leftarrow R(X, Z), R(Z, T), S(T, Y)$ und $q'_1: \text{ans}(X, Z) \leftarrow R(X, X), S(X, Z)$
- b) $q_2: \text{ans}(X) \leftarrow R(X, Y), S(Y, Z), S(Y', Z')$ und $q'_2: \text{ans}(Y) \leftarrow S(A, B), R(Y, A), R(Y', A)$
- c) $q_3: \text{ans}(U, Z) \leftarrow R(U, V), R(X, Y), S(Y, Z), S(V, X)$ und $q'_3: \text{ans}(U, V) \leftarrow R(Y, U), R(U, X), S(U, V), S(X, Y)$

Exercise 3 (Containment)

Consider the following pairs of Conjunctive Queries and decide if $q_i \sqsubseteq q'_i$, $q'_i \sqsubseteq q_i$, and $q_i \equiv q'_i$ hold using the method of the canonical instance.

- a) $q_1: \text{ans}(X) \leftarrow R(X,Y,X), R(X,Z,Y), S(Y,X)$ und $q'_1: \text{ans}(X) \leftarrow R(X,Y,Z), S(Y,Z)$
b) $q_2: \text{ans}(X) \leftarrow R(X,Y), R(Y,Z), R(Z,X)$ und $q'_2: \text{ans}(X) \leftarrow R(X,Y), R(Y,Z), R(Z,U), R(U,V)$

Exercise 4 (NP-Completeness)

Prove the Conjunctive Query Containment problem is NP-Complete. To show NP-Hardness, you need to find an NP-Complete problem and make a reduction to the containment problem.