Machine Learning – June 23, 2020

Time limit: 2 hours 15 minutes.

EXERCISE 1

Consider a setting where the input space I is the set of finite strings over the characters a, b, c, \dots, z . Notice that input strings can be of different length.

Given the following dataset D:

x	\mathbf{t}
a	1
ab	1
caza	4
ayka	4
aabba	9
aaa	9
zazaa	9
accaaca	16
khaaala	16
akdfkkatyuakka	16
jhxaaksrtkaatyuap	25

- 1. Identify the learning problem at hand, in particular the form of the target function, and define a suitable linear model for it.
- 2. Apply the kernel trick to the model defined above and provide the analytical form of the corresponding error function.
- 3. Define the solution obtained with your choices for the dataset D.

EXERCISE 2

A secret string $s = b_0 b_1 b_2 b_3$ of 4 bits fulfills the following constraints:

- if $b_0 = 0$, s contains an even number of 0's and 1's;
- if $b_0 = 1$, s contains at least three 1's.

No other prior information about s is available.

- 1. Define the prior probability distribution P(s) of the hypothesis string s.
- 2. Assuming $b_0 = 0$, define the conditional probability distribution $P(s|b_0 = 0)$ and indicate all maximum a-posteriori hypotheses.
- 3. Assuming $b_0 = 1$ and $b_1 = 1$, indicate all maximum likelihood hypotheses and compute the likelihood that $b_2 = 1$.

EXERCISE 3

Consider a dataset D for the binary classification problem $f: \Re^3 \mapsto \{A, B\}$.

- Describe a probabilistic generative model for such a classification problem, assuming Gaussian distributions.
- 2. Identify the parameters of the model and determine the size of the model (i.e., the number of independent parameters).

EXERCISE 4

- 1. Describe the k-armed bandit problem (also known as One-state MDP).
- 2. Describe the Reinforcement Learning procedure to compute the optimal policy in the k-armed bandit problem with stochastic behavior and unknown functions.

EXERCISE 5

Consider that the output of layer l of a CNN is the set of feature maps M with size $256 \times 256 \times 64$

- 1. What is the size of the feature maps N when max-pooling with a 2×2 kernel and stride 2 is applied on M?
- 2. Design a convolutional layer which, when applied on M, produces feature maps with the same size as N. Describe all the relevant parameters of the layer you have designed.
- 3. What happens if the non-linear activation functions of the hidden layers of the CNN are replaced with linear functions? Is the effective depth of the network affected and how?

EXERCISE 6

Consider N convolutional neural networks trained to classify images of cats and dogs with a corresponding confidence value (output of sigmoid activation function)

- Describe a way to combine the predictions of the CNNs in order to get a single more accurate prediction.
- Assume N = 3, class '0' represents dogs, class '1' cats and for a given image the three CNN outputs are: (0.912, 0.432, 0.444). Apply the method described above to classify the image using the predictions of the three CNNs.