



Virtual Fluids – Real Insights

Computer Aided Product Development

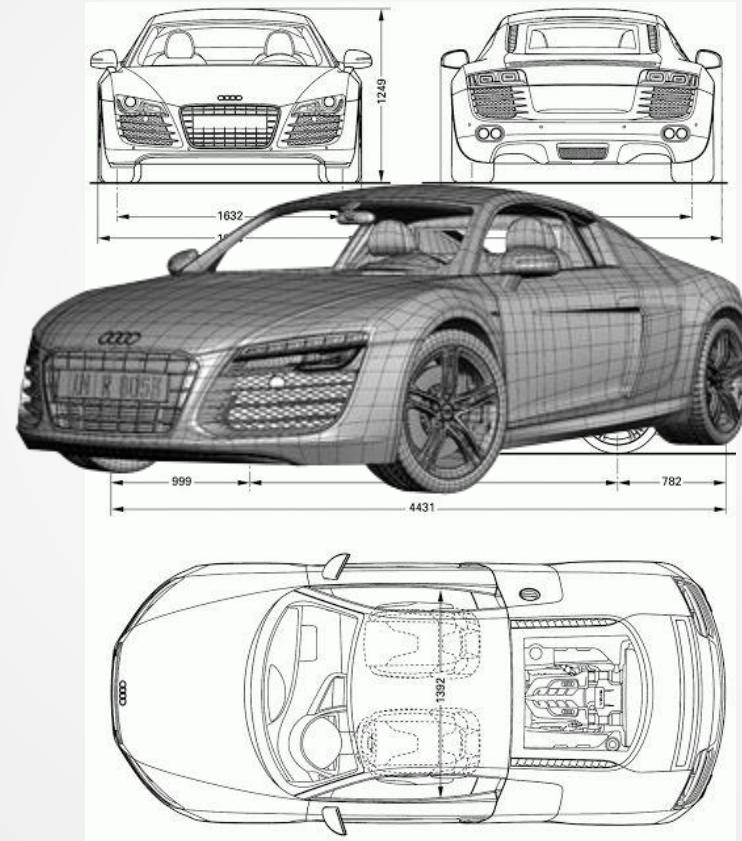
Modeling, Simulation and Rendering in the Industry

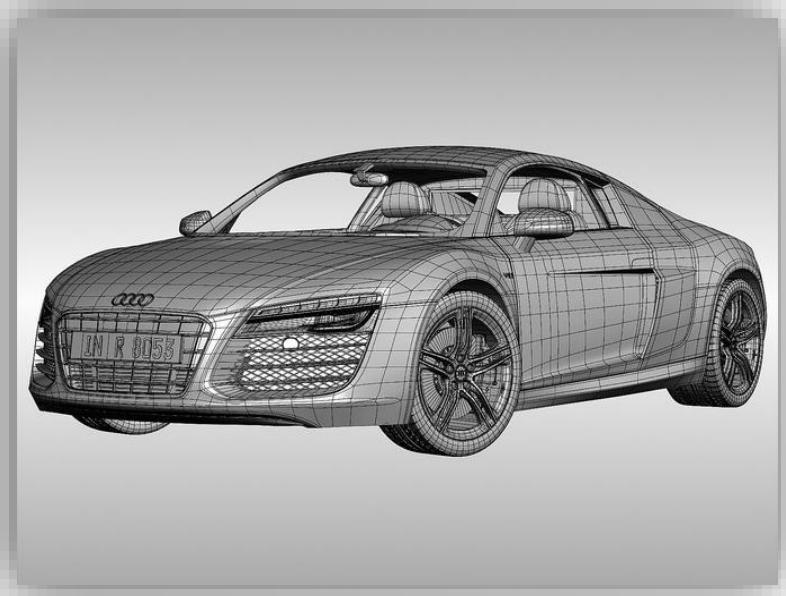
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// Product development - an iterative process





Question → 1 – 2 Years → Insights

// Problem



- Without simulation:
 - physical prototype required
 - complicated, expensive and unflexible tests
- Simulation tools:
 - require specialized knowledge by experts in the relevant simulation field
 - are slow

-> complicated and time-consuming workflows

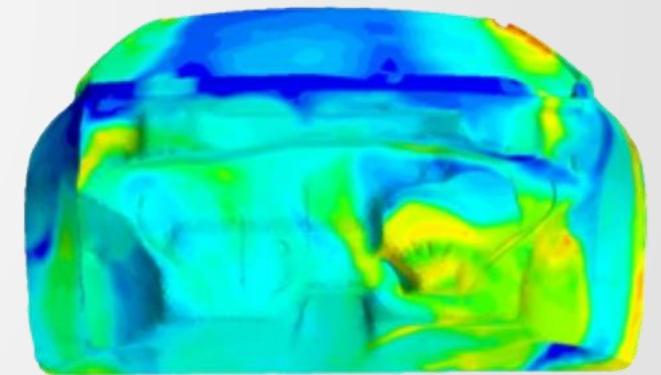
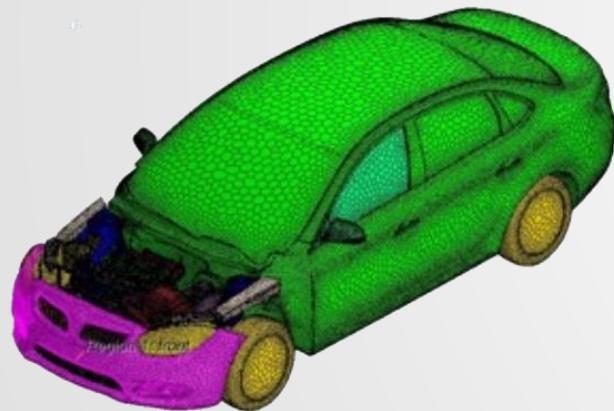
// Traditional simulation methods

Workflow wading simulation (grid-based):

3 weeks meshing
(manual work)

4 weeks
simulation

1 week data
analysis





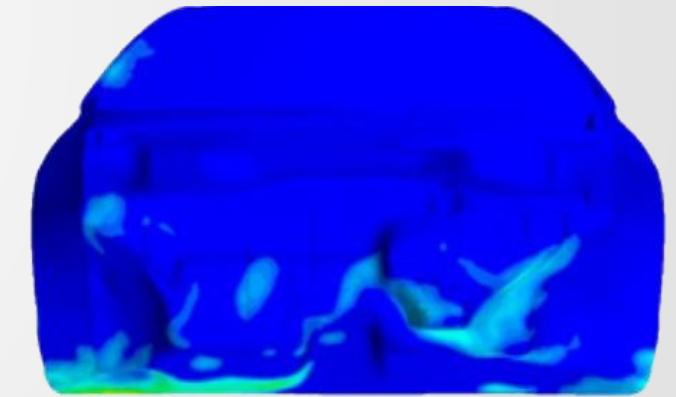
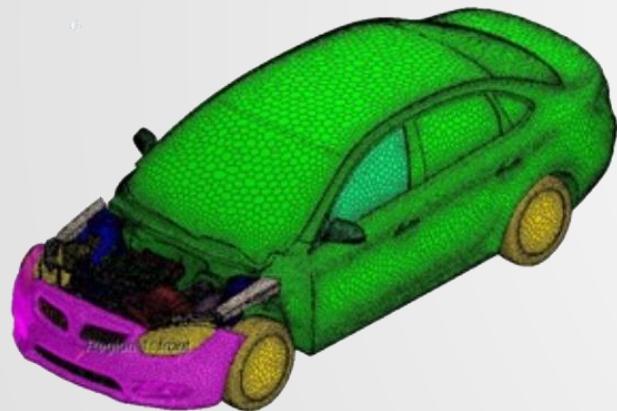
// Traditional simulation methods

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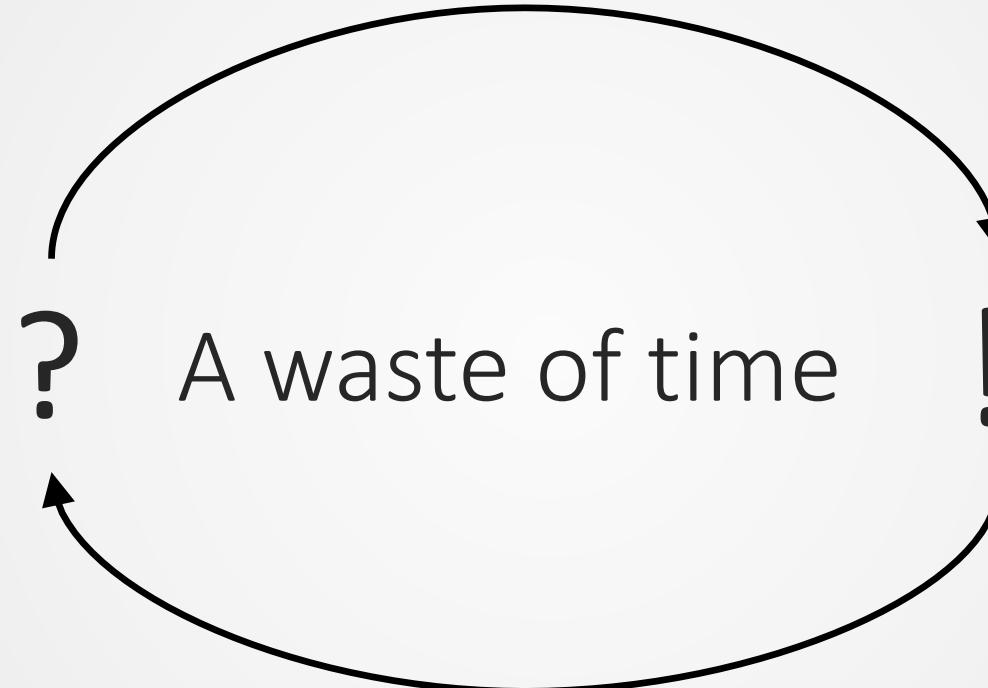
4 weeks
simulation

1 week data
analysis





// Product development - an iterative process



// Purpose of FIFTY2

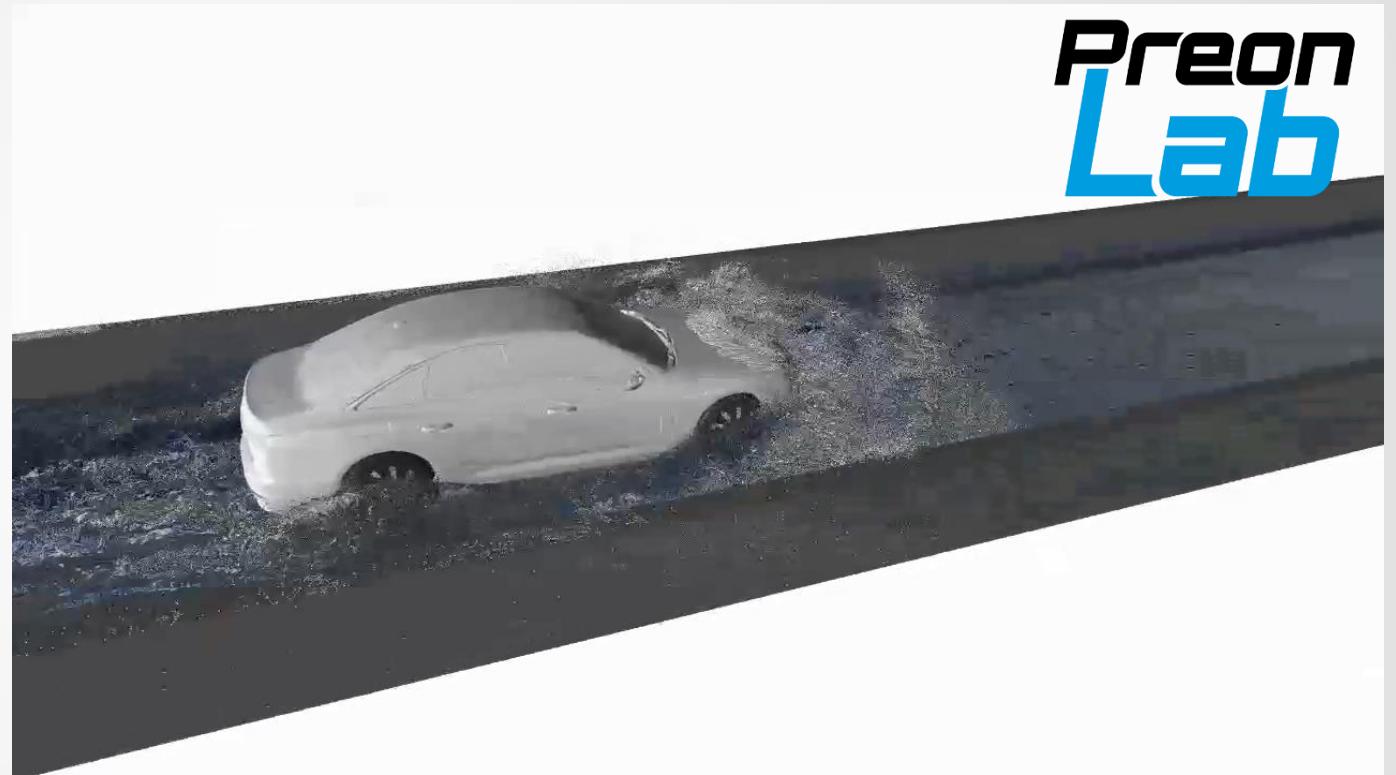
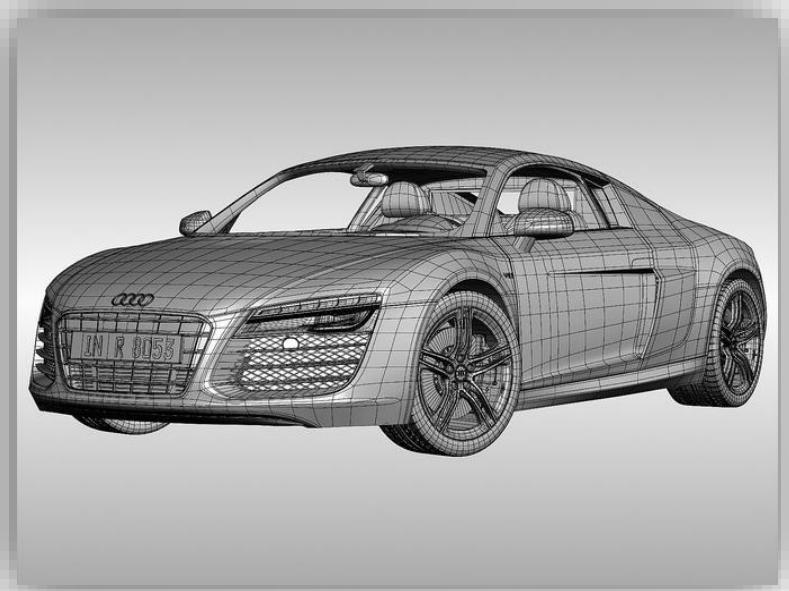


- Enable engineers and designers to craft the best version of their product together
 - Non simulation experts can describe and simulate the problem
 - Easy workflow and fast simulation
 - Results can be monitored and understood by engineers, designers, and decision makers at any time

// Promise

- We build tools that:
 - Reduce time from question to insight (Q2I)
 - Maximize insights: quality and quantity of information
 - Are enjoyable and easy to use





**Preon
Lab**

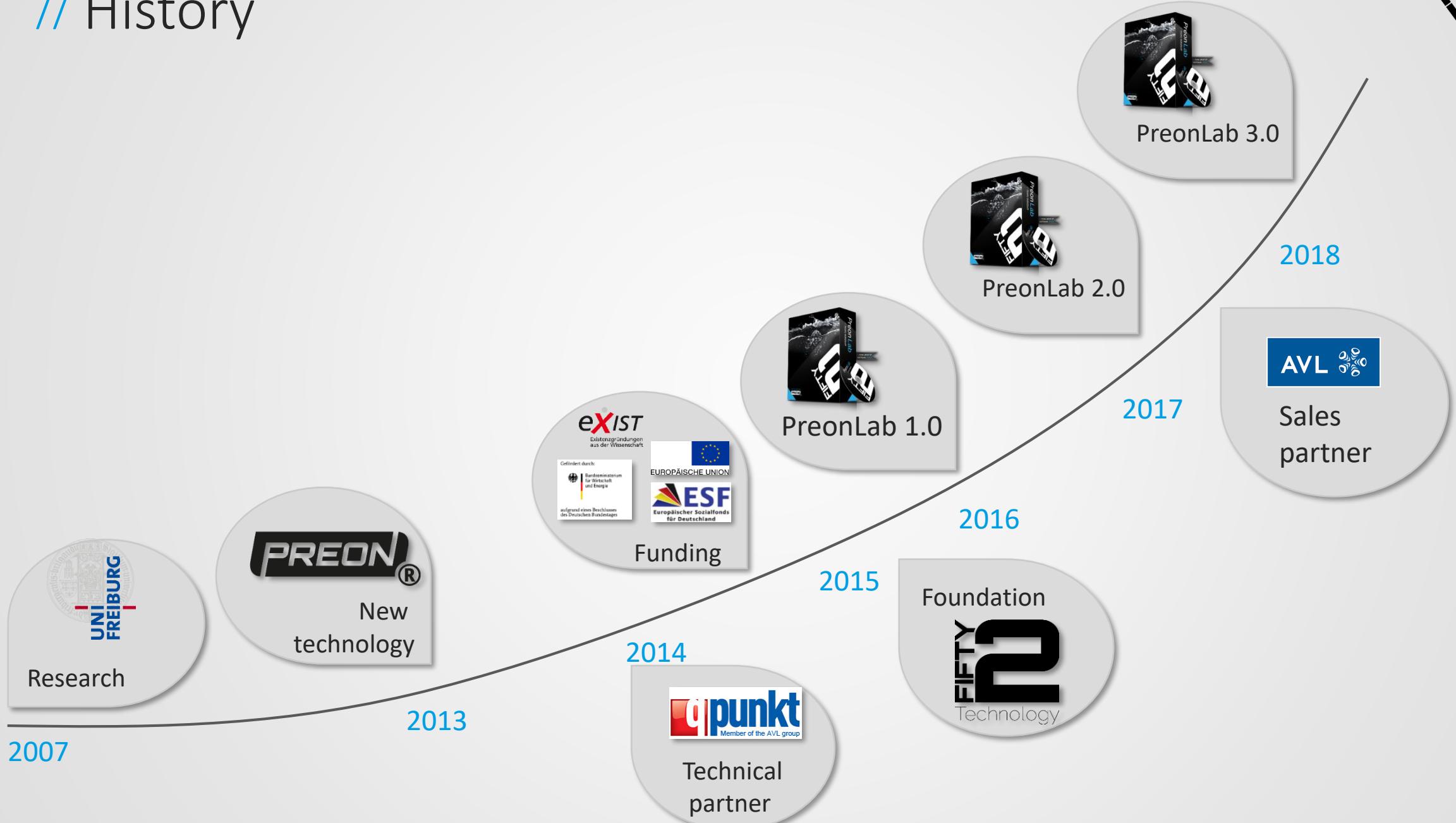
Workflow wading simulation (PreonLab):

Questions
2 hours setup

Days
1 day simulation

Insights
8 hours analysis

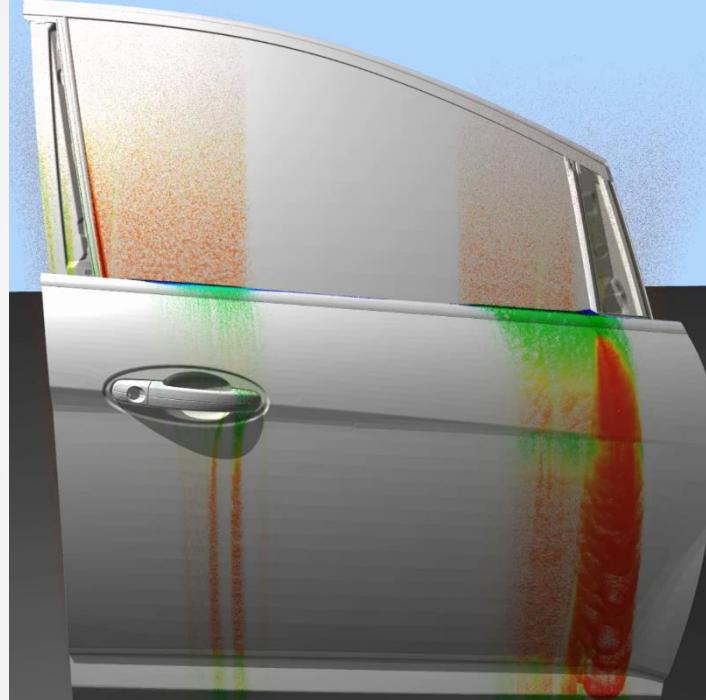
// History



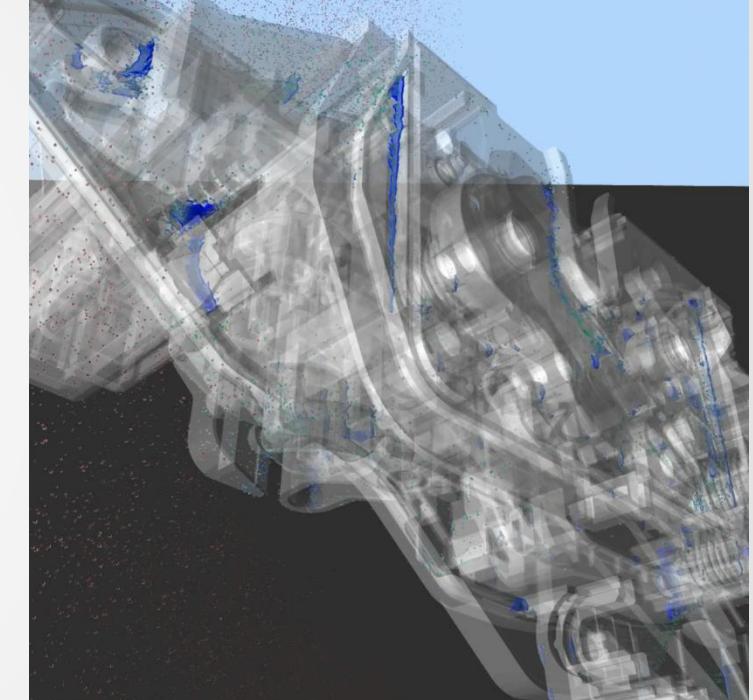
// Watermanagement



Wading



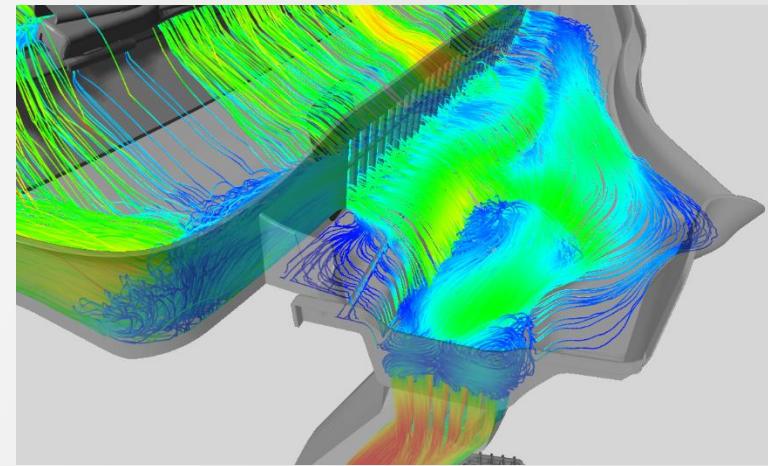
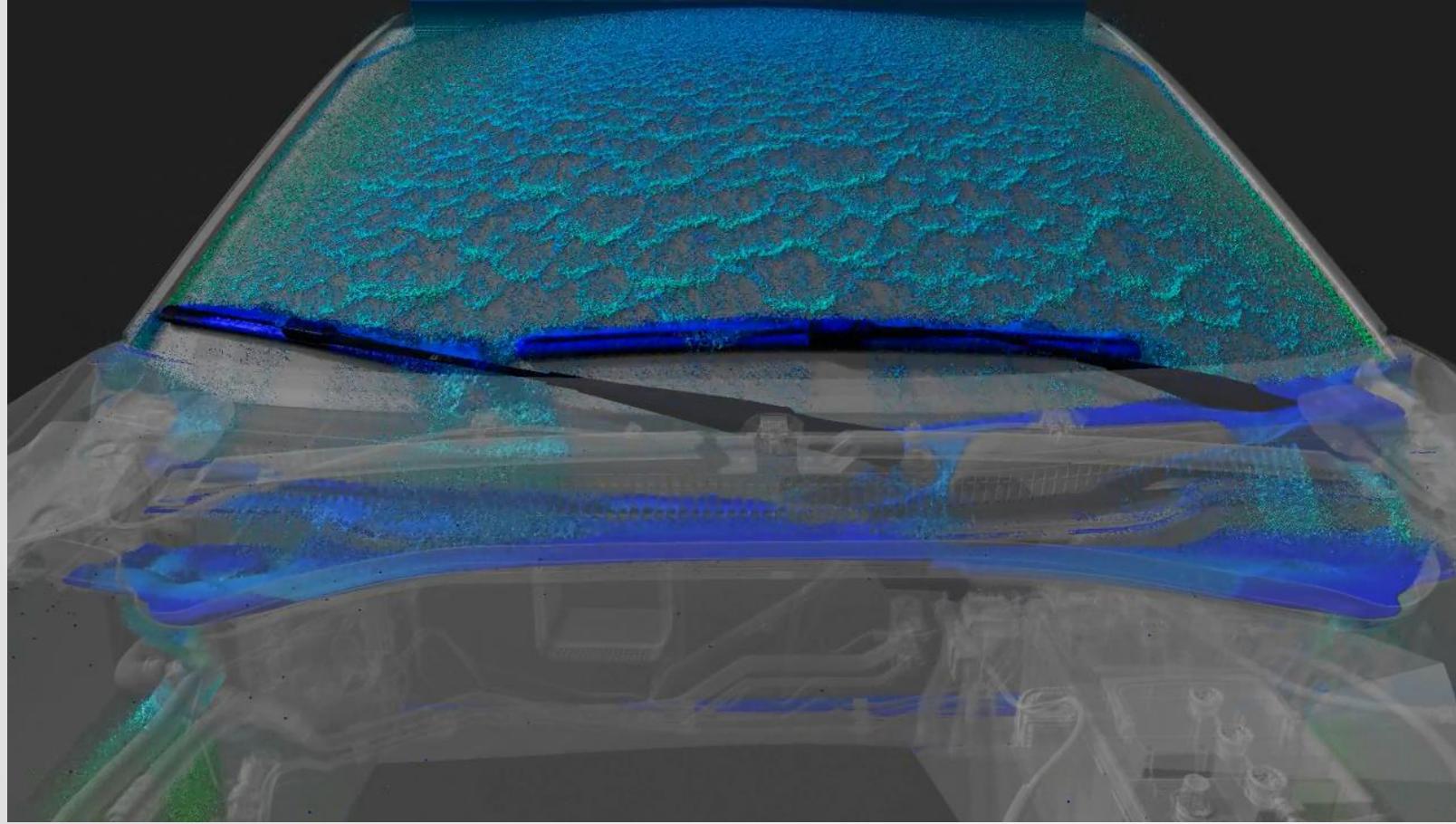
Rain



Corrosion

// Raining

FEAT

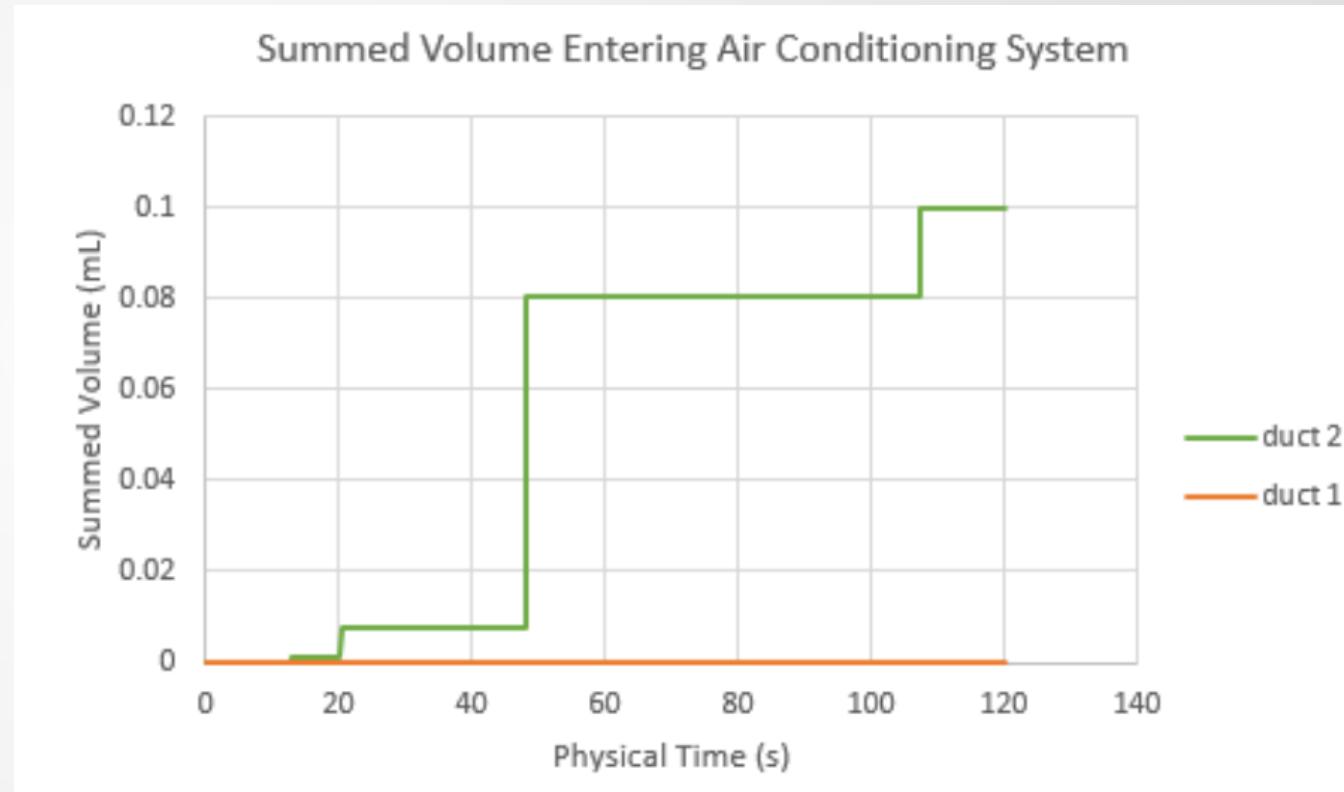


// Raining

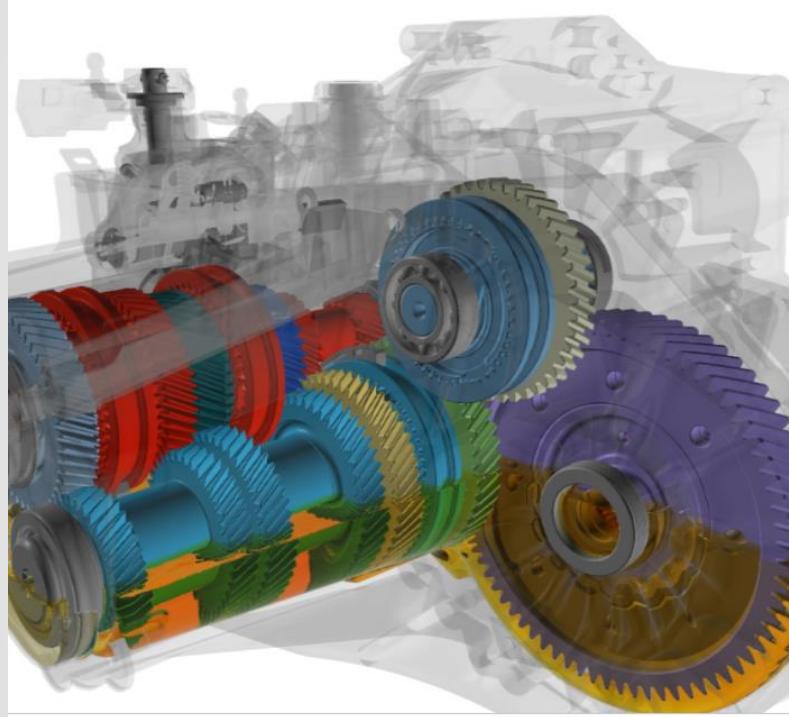


Rapid prototyping:

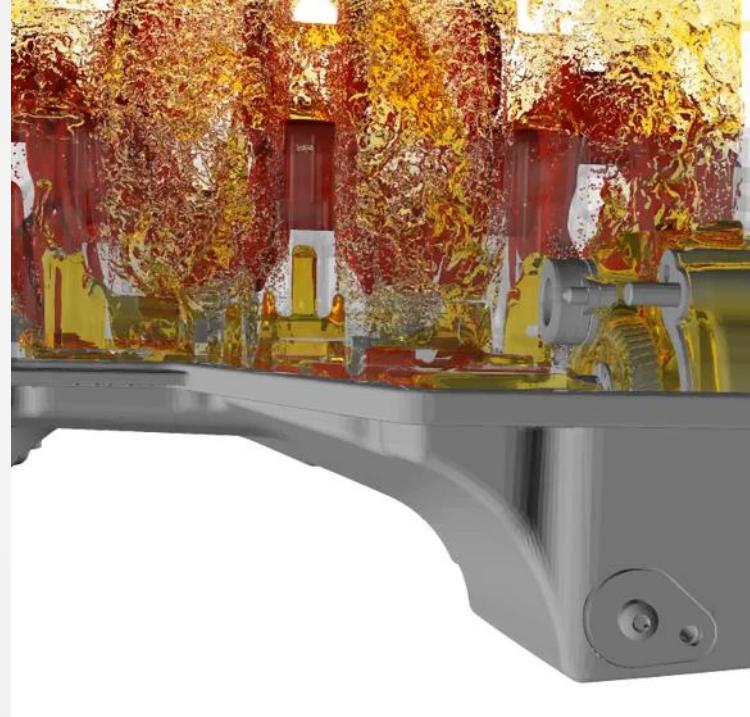
- Shorter cycles for design testing
- Allows progressive designs
- Duct 2 is a failure
- Continue with duct 1



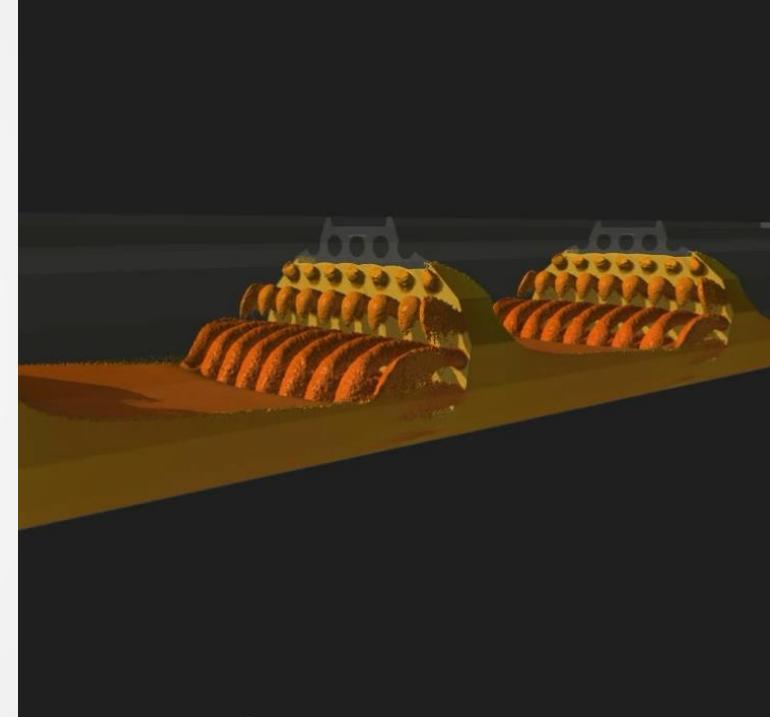
// Oil



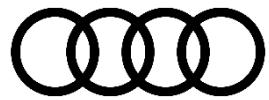
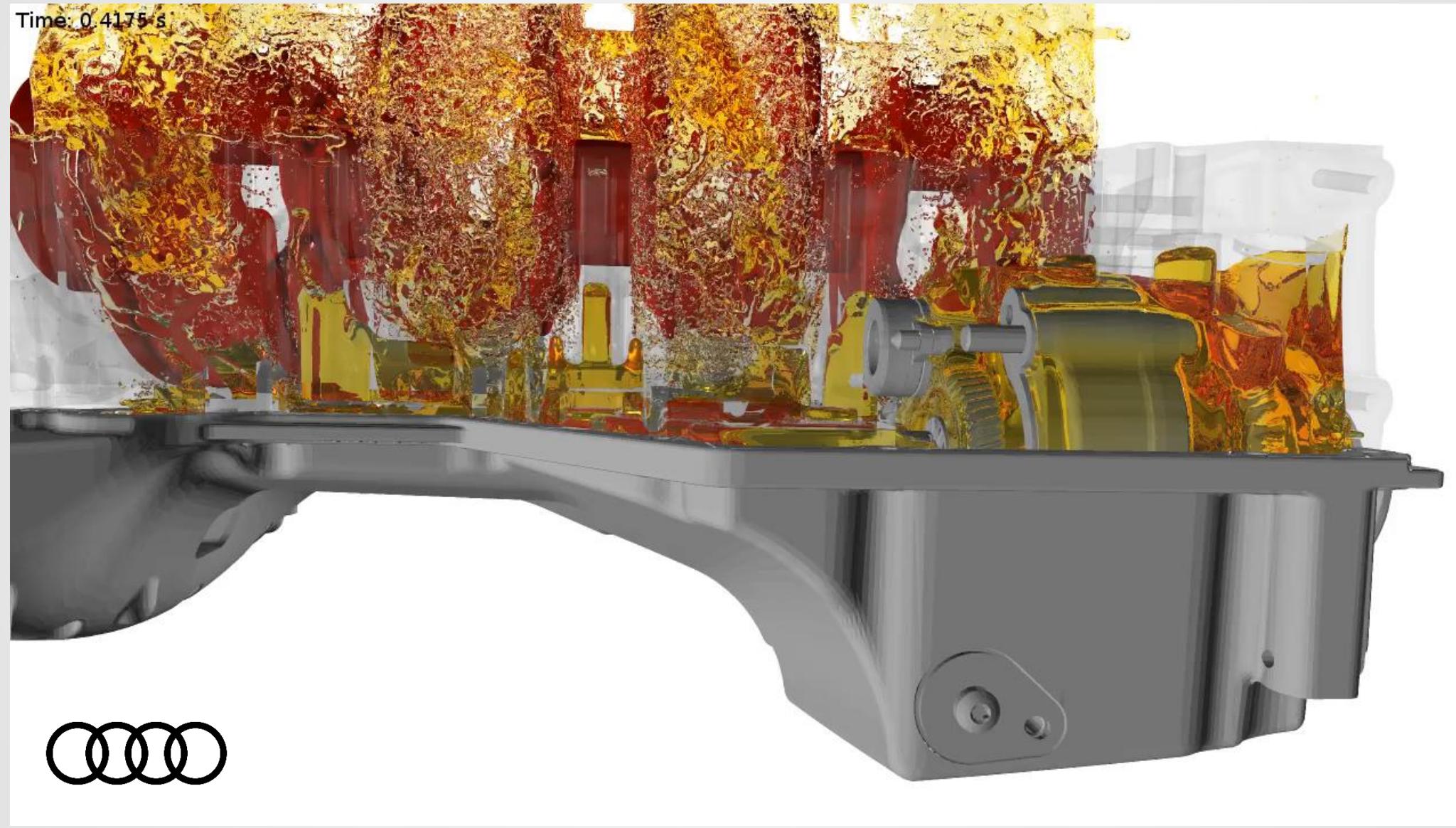
Gear box



Crank Case



Sloshing

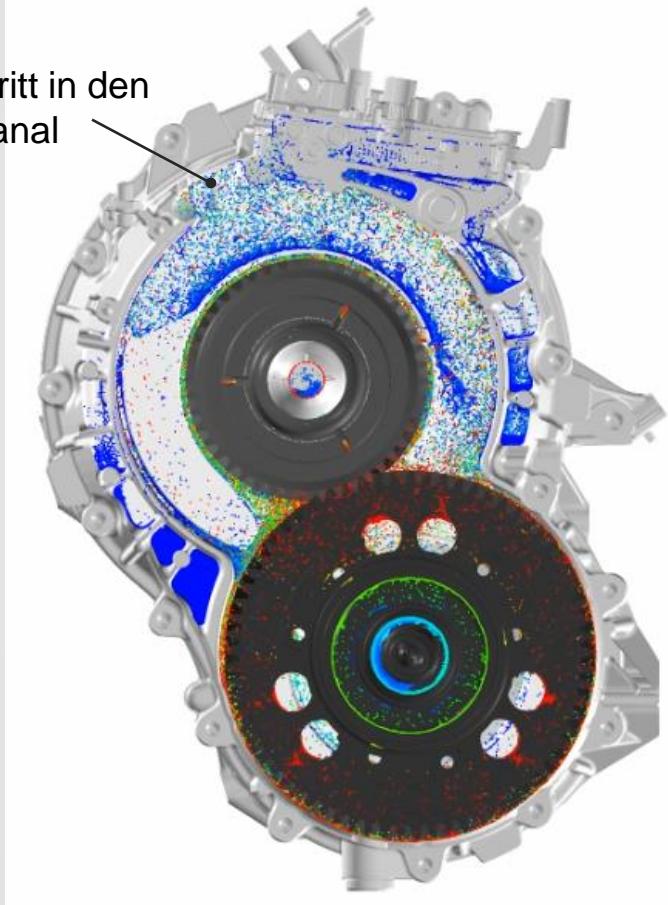


// Simulation der Ölverteilung



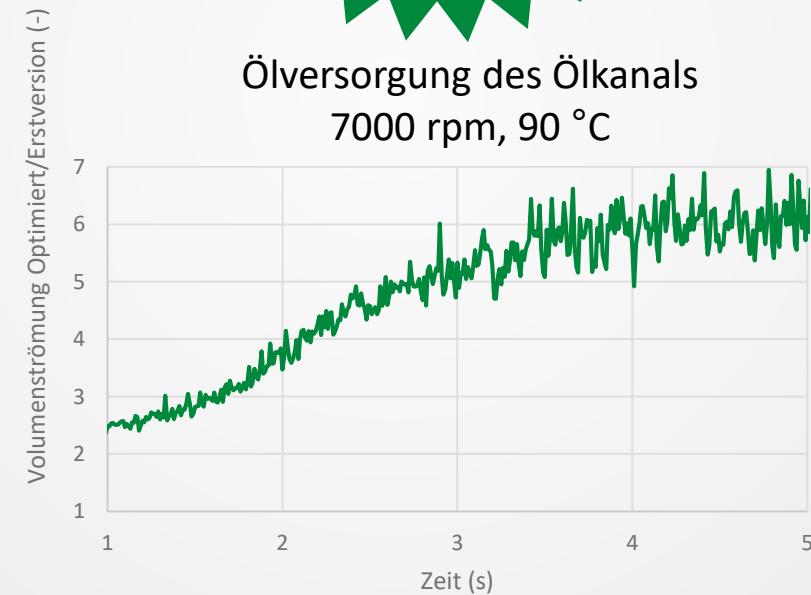
Erstversion des Einlegers

Eintritt in den
Ölkanal

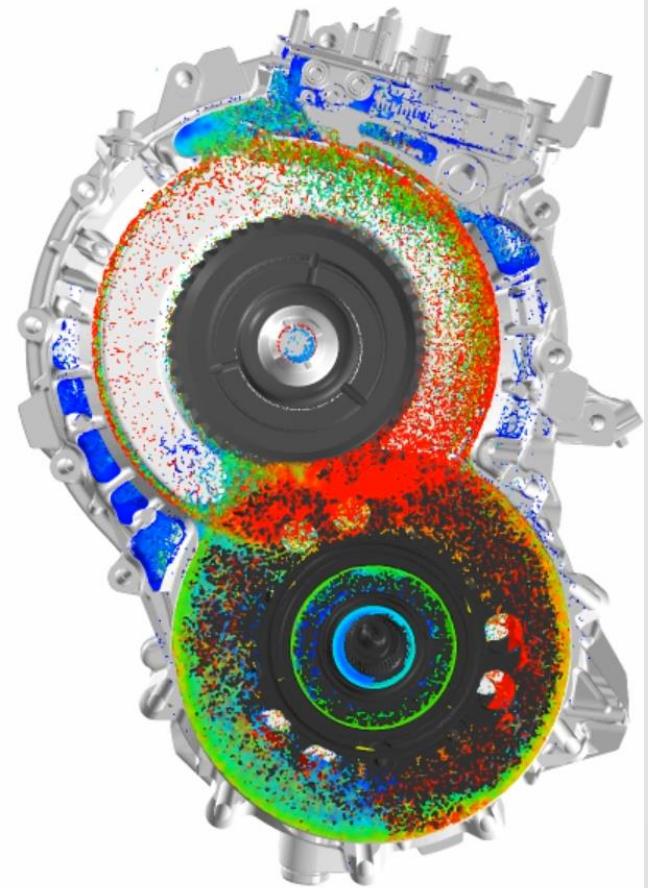


Volumen-
strom 5 bis
6-fach
erhöht

Ölversorgung des Ölkanals
7000 rpm, 90 °C



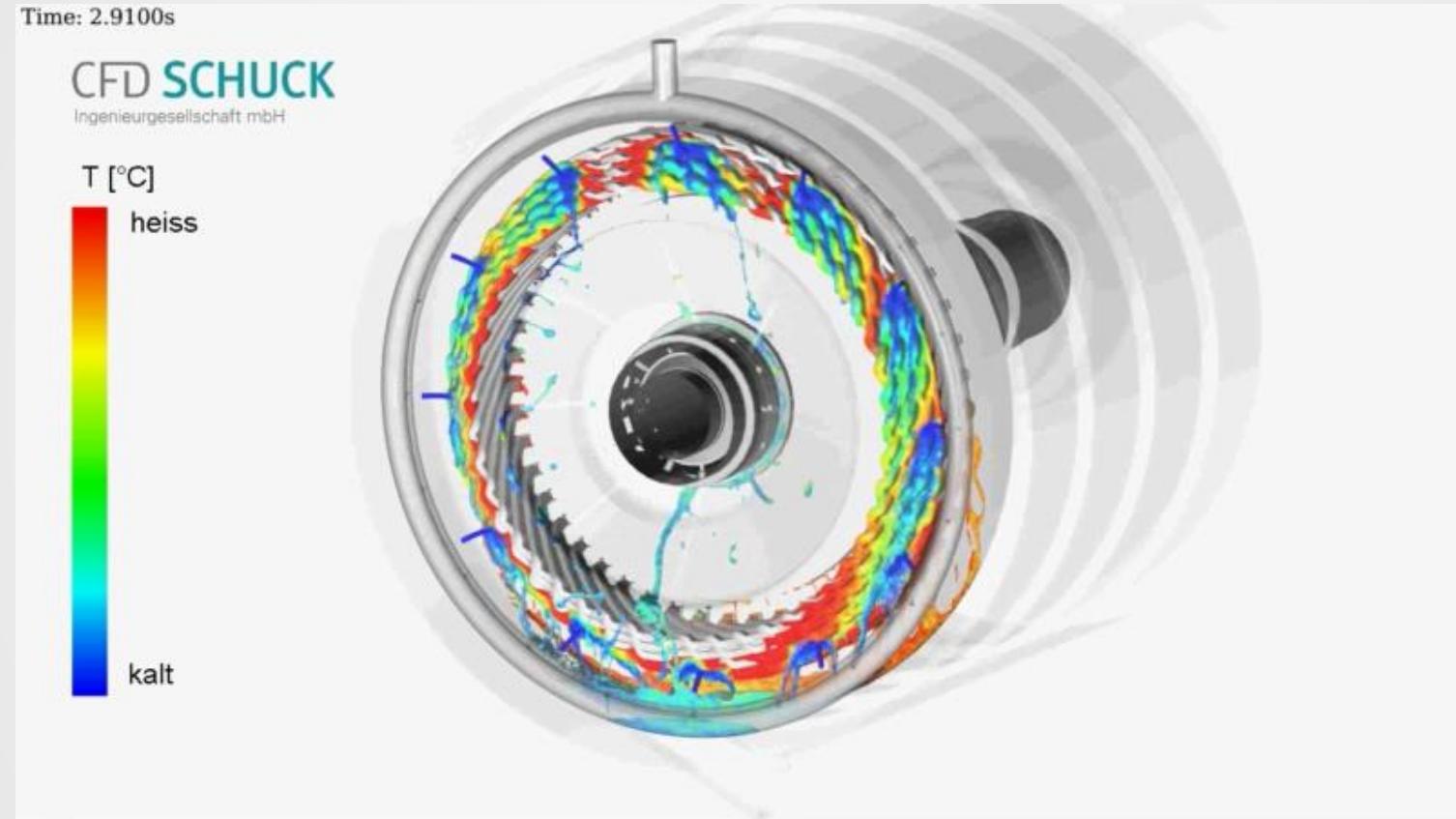
Optimierter Einleger



!

Simulationsergebnisse wurden von Versuchen bestätigt.

// E-machine cooling - Thermodynamics

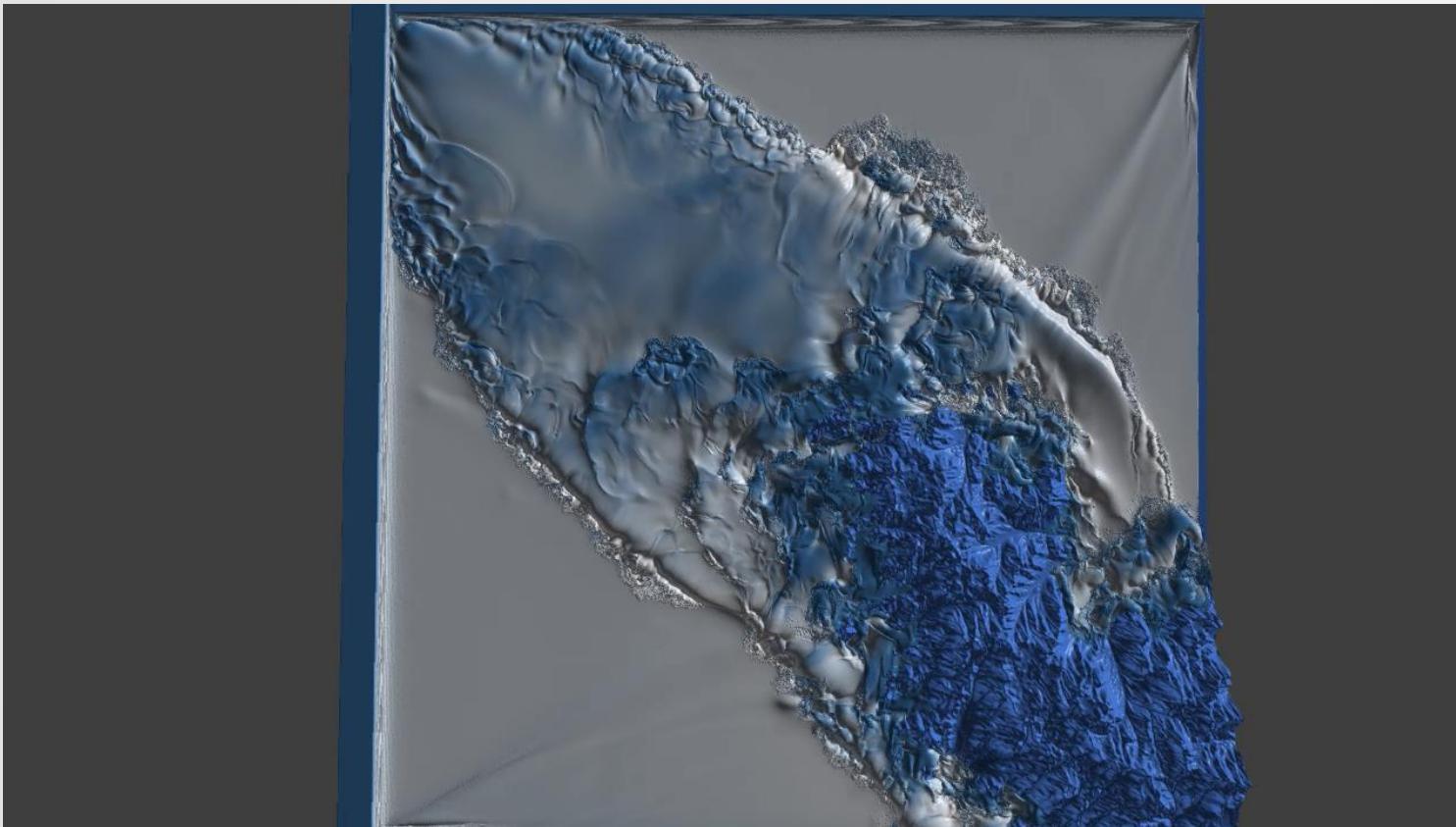


Particles carry physical quantities, e.g., temperature

// Markets



// Hydraulic engineering

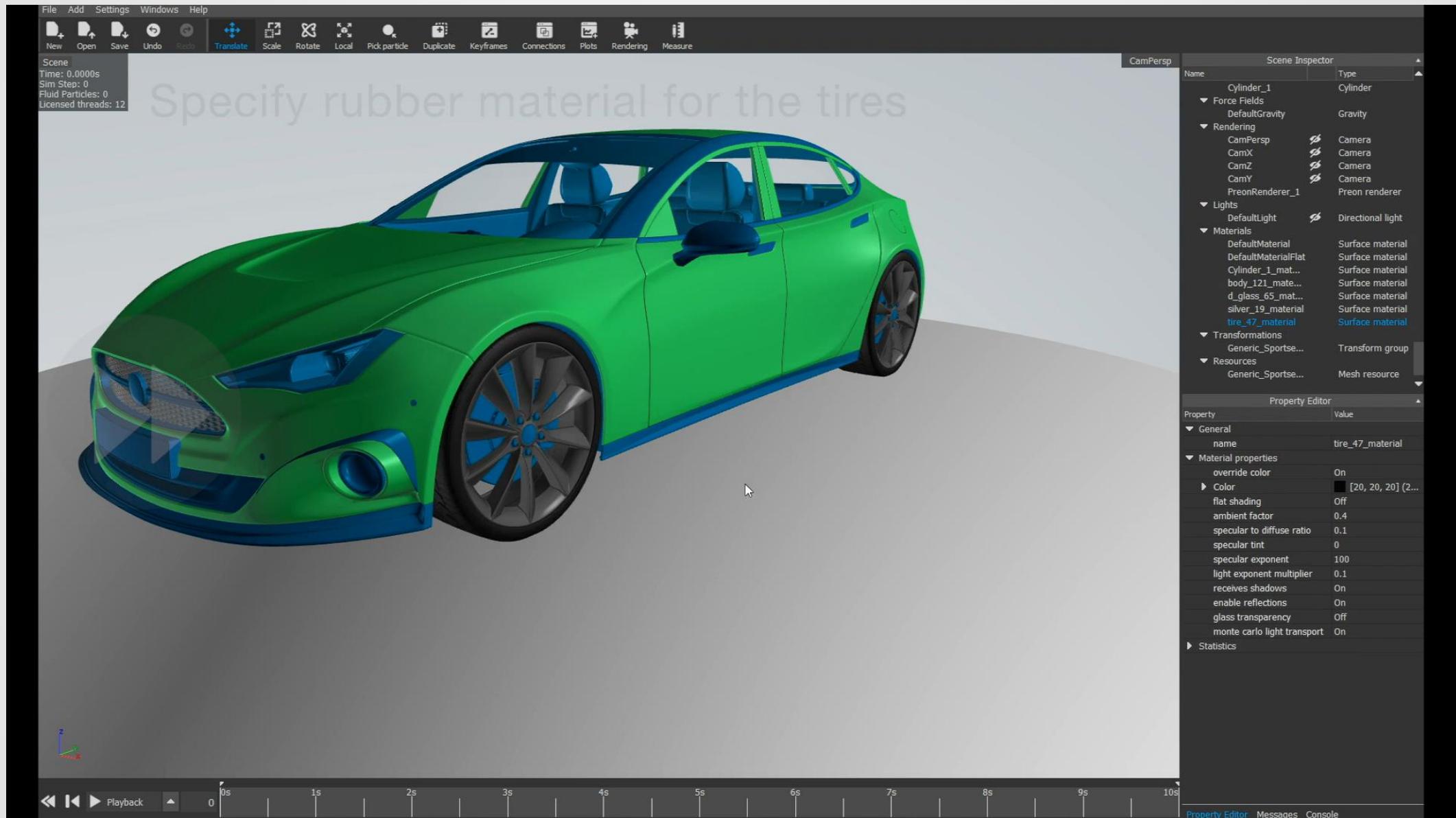


End customer:

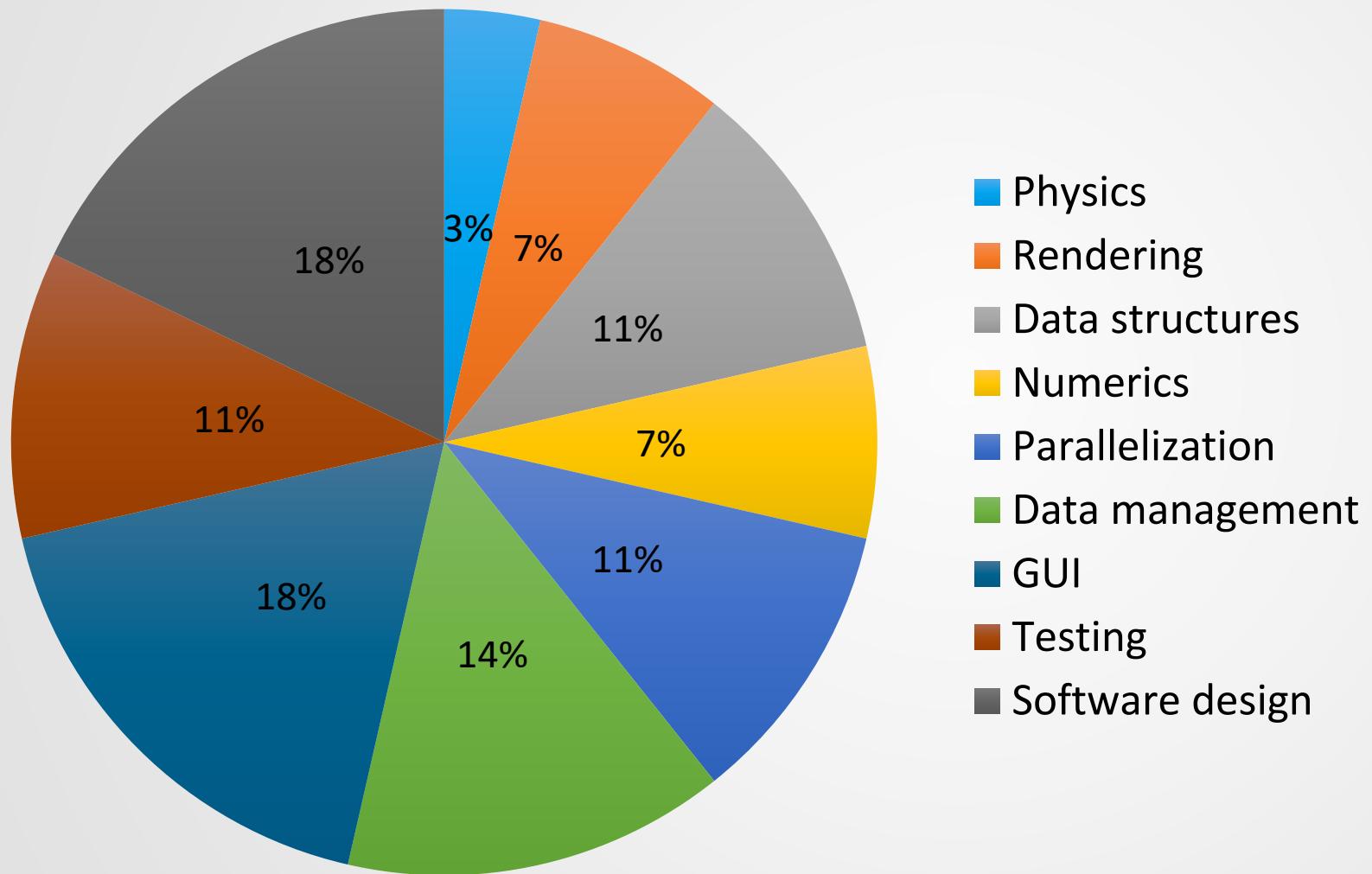
- Governments
- Assurance companies
- City administrations
- Construction companies

Technical and theoretical background

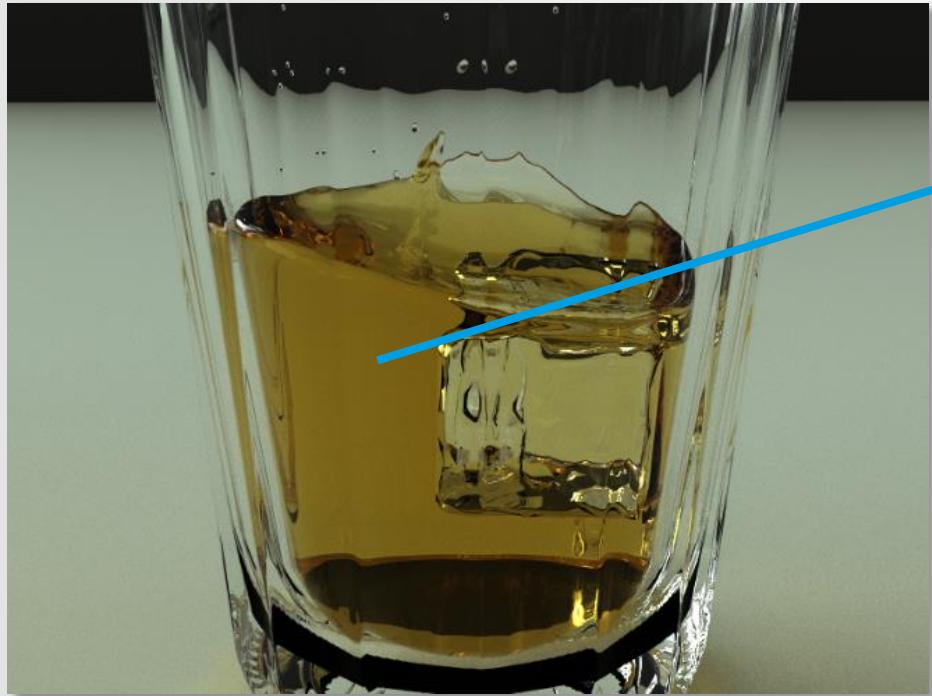
// PreonLab experience



// PreonLab ingredients



// Fluid simulation



For any point \mathbf{x} in fluid volume and time t compute position $\mathbf{x}(t)$. Same for any physical quantity $A(\mathbf{x}, t)$

Requires:

- velocity \mathbf{v} at any point
- velocity change $d\mathbf{v}$

// CFD Solver – Navier-Stokes Equation



602 billion trillion
molecules per 18ml
250 916 670 000 000 000 terabytes

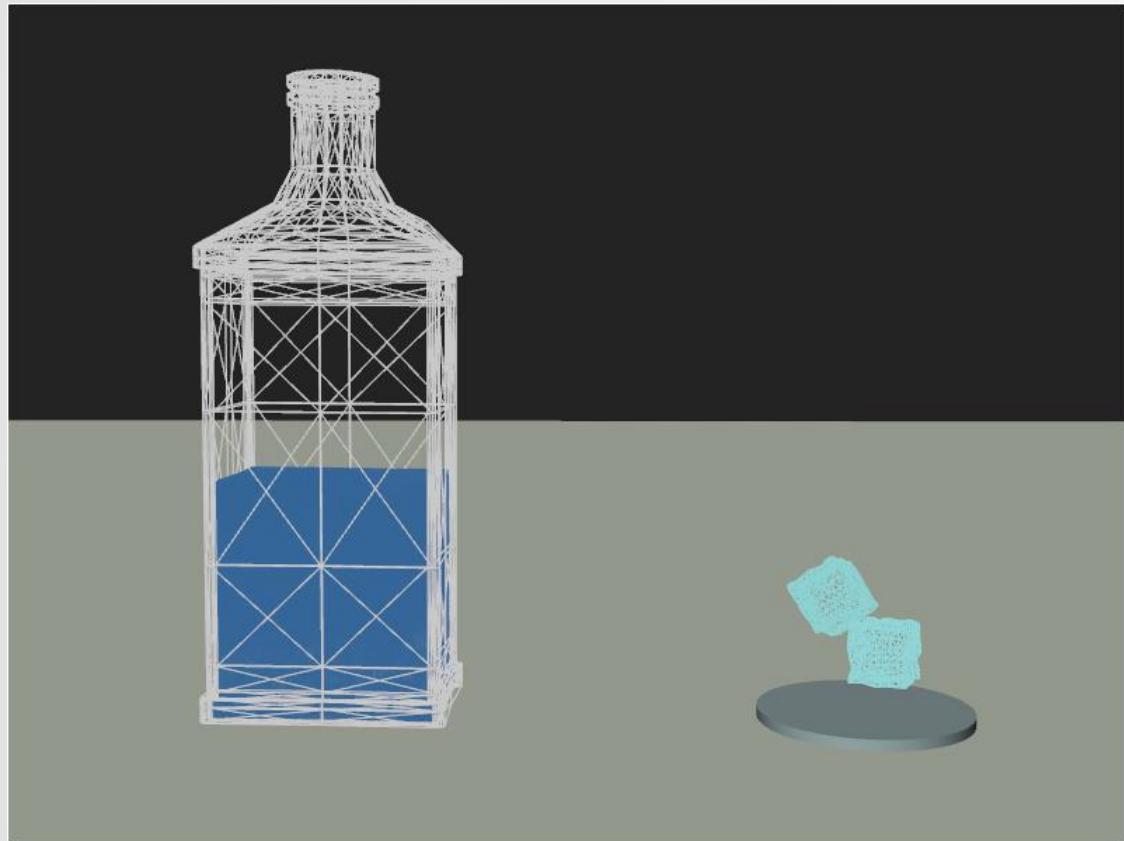
$$\frac{D\vec{v}}{Dt} = -\frac{1}{\rho} \nabla p + \nu \nabla^2 \vec{v} + \vec{g}$$

pressure term (solver)

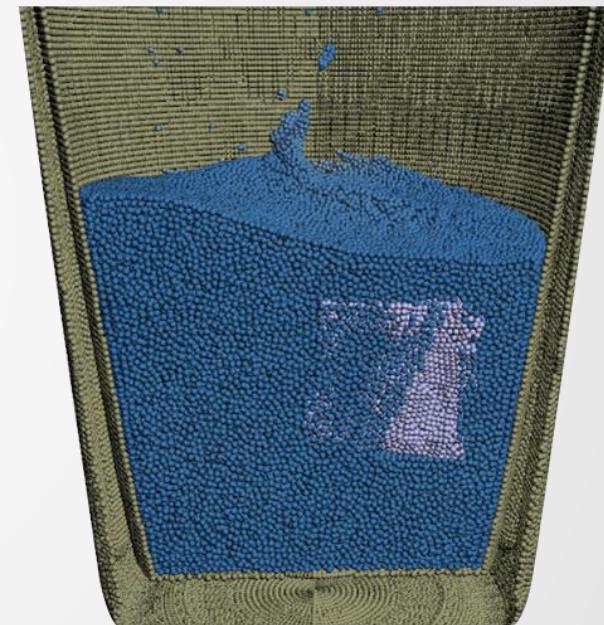
viscosity term (explicit)

body forces /gravity (explicit)

// Fluid simulation

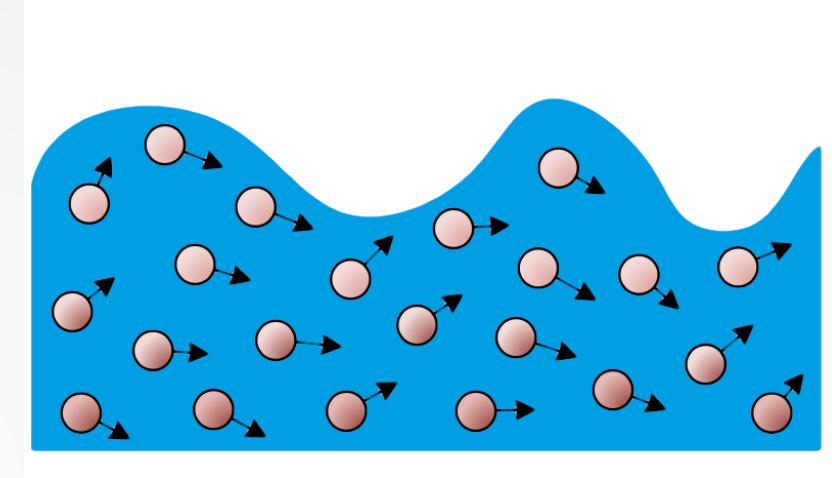
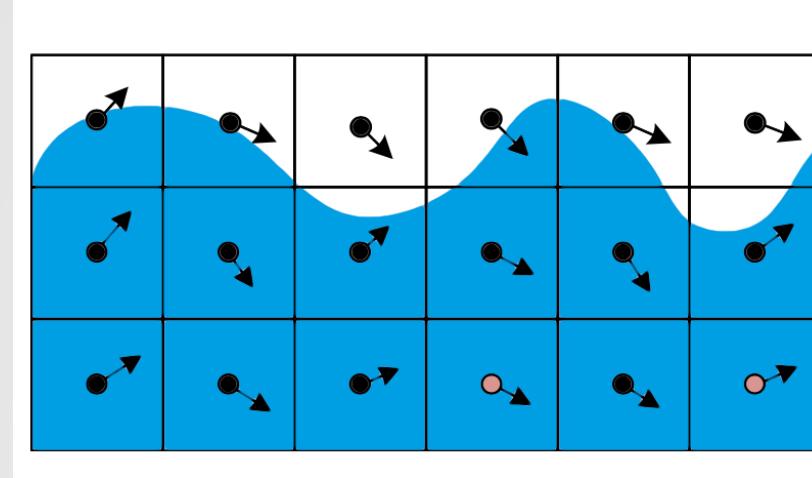


Discretize volume and time



40 megabytes

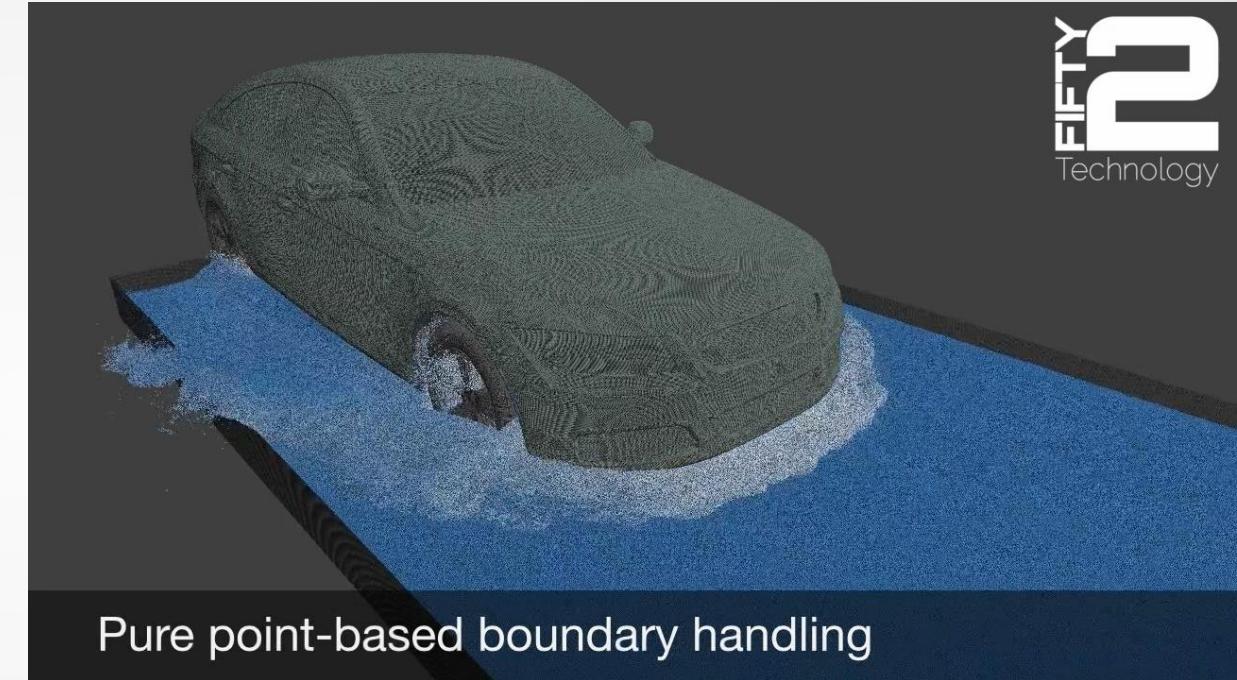
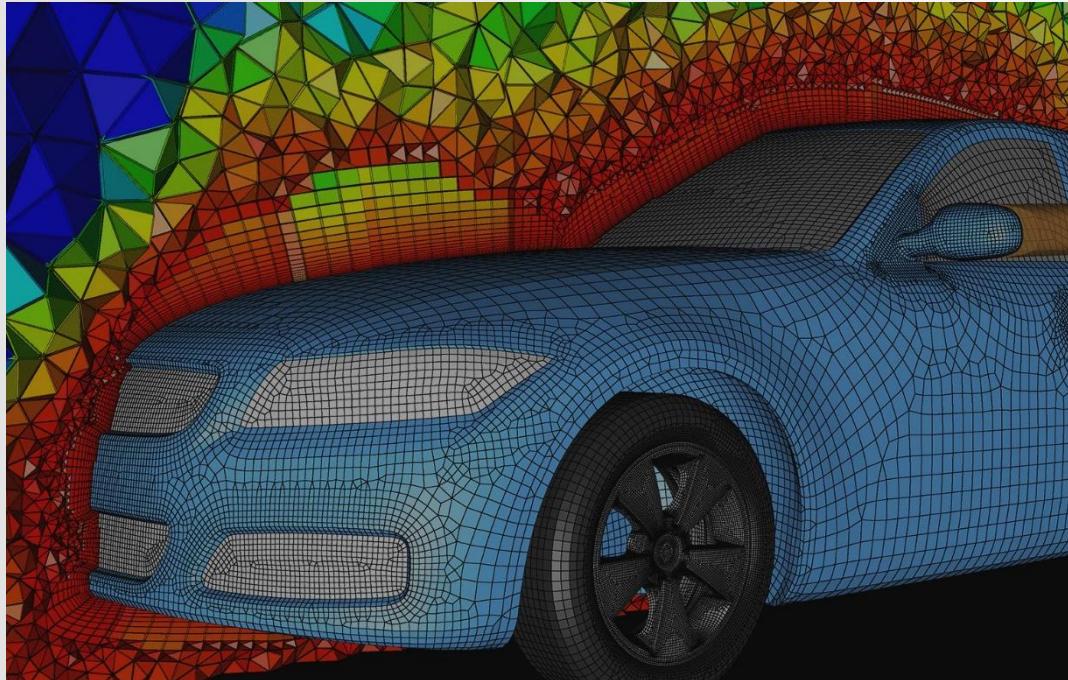
// Spatial Discretization



- Euler
 - Grid cells represent partial volumes
 - Complete domain has to be discretized
 - Spatial derivatives efficiently computed
 - Advection expensive to compute

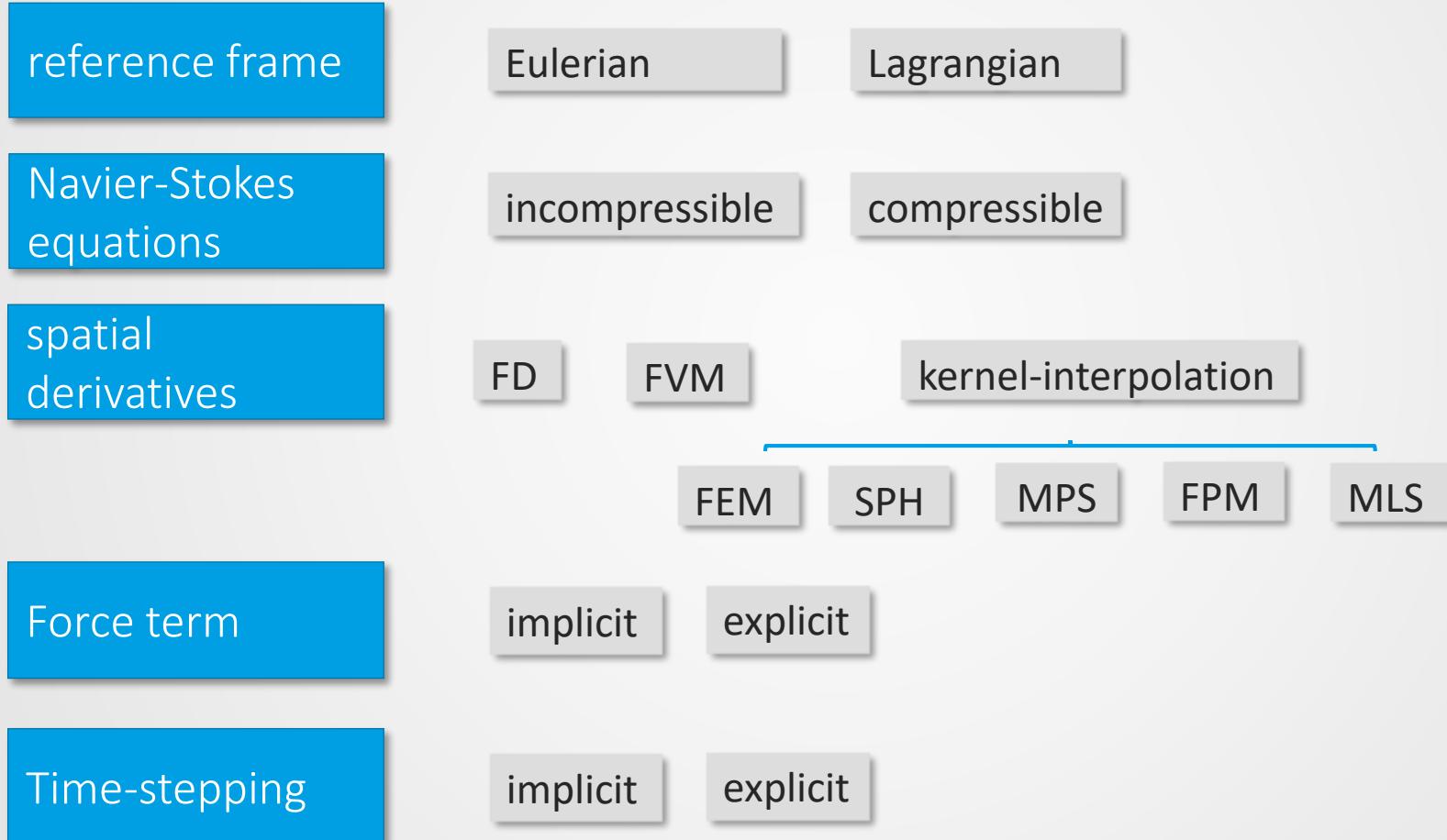
- Lagrange
 - Particles represent partial volumes
 - Only liquid phase has to be discretized
 - Advection efficiently computed
 - Spatial derivatives expensive to compute

// Spatial Discretization



- Euler
 - Grid cells represent partial volumes
→ Align fluid cells with CAD model
- Lagrange
 - Particles represent partial volumes
→ Fluid can move arbitrarily and aligns naturally

// Numerical building blocks of a CFD Solver



// Implicit formulation – Discretizing time



$$\underbrace{\frac{D\mathbf{v}_i}{Dt}}_{\text{acceleration}} = \underbrace{-\frac{\nabla p_i}{\rho_{i,0}}}_{\text{pressure term}} + \underbrace{\nu_i \nabla^2 \mathbf{v}_i}_{\text{viscosity term}} + \underbrace{\nabla \Phi_i}_{\text{surface tension}} + \underbrace{\mathbf{f}_i^b}_{\text{body forces}}$$

1. Explicit calculation of all terms except the pressure term

$$\mathbf{v}_i^* = \mathbf{v}_i + \Delta t \left(\underbrace{\nu_i \nabla^2 \mathbf{v}_i}_{\text{viscosity term}} + \underbrace{\nabla \Phi_i}_{\text{surface tension}} + \underbrace{\mathbf{f}_i^b}_{\text{body forces}} \right)$$

2. Implicit computation of the pressure field

$$\nabla^2 p_i = \frac{\rho_{i,0} - \rho_i^*}{\Delta t^2} \quad \xleftarrow{\hspace{1cm}} \quad \rho_i^* = \rho_i - \Delta t \rho_{i,0} \nabla \cdot (\mathbf{v}_i^*)$$

$$\mathbf{v}_{i,t+\Delta t} = \mathbf{v}_i^* - \Delta t \frac{\nabla p_i}{\rho_{i,0}}$$

$$\mathbf{x}_{i,t+\Delta t} = \mathbf{x}_i + \Delta t \mathbf{v}_{i,t+\Delta t}$$

// Kernel weighting – Discretizing space



- Value interpolation at position \mathbf{x}
- Over finite local support domain
- Weighting is color coded
- Riemann sum

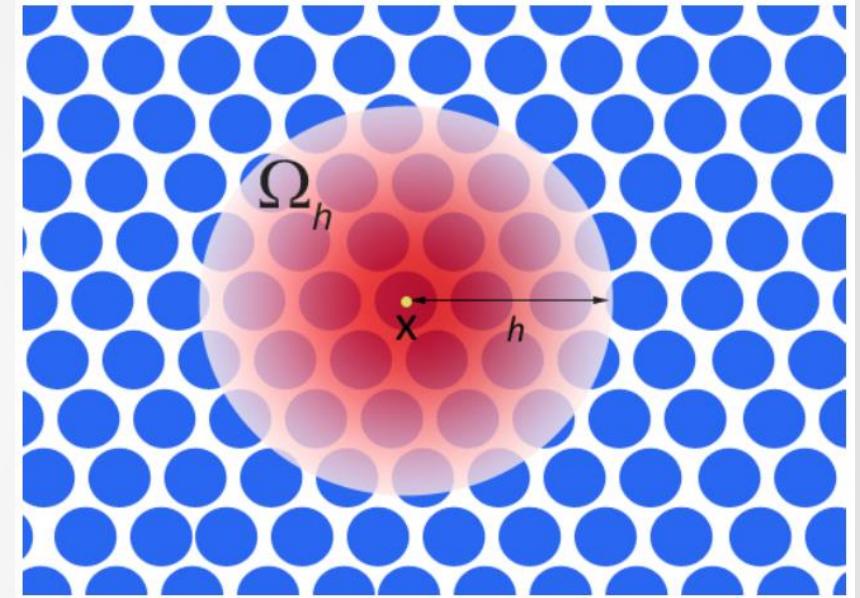
$$A(\mathbf{x}) = \int A(\mathbf{x}') \delta(\mathbf{x} - \mathbf{x}') d\mathbf{x}'$$



$$\langle A(\mathbf{x}) \rangle = \int_{\Omega} A(\mathbf{x}') W(\mathbf{x} - \mathbf{x}', h) d\mathbf{x}'$$



$$\langle A(\mathbf{x}_i) \rangle = \sum_j V_j A(\mathbf{x}_j) W(\mathbf{x}_i - \mathbf{x}_j, h)$$



// Simulation loop

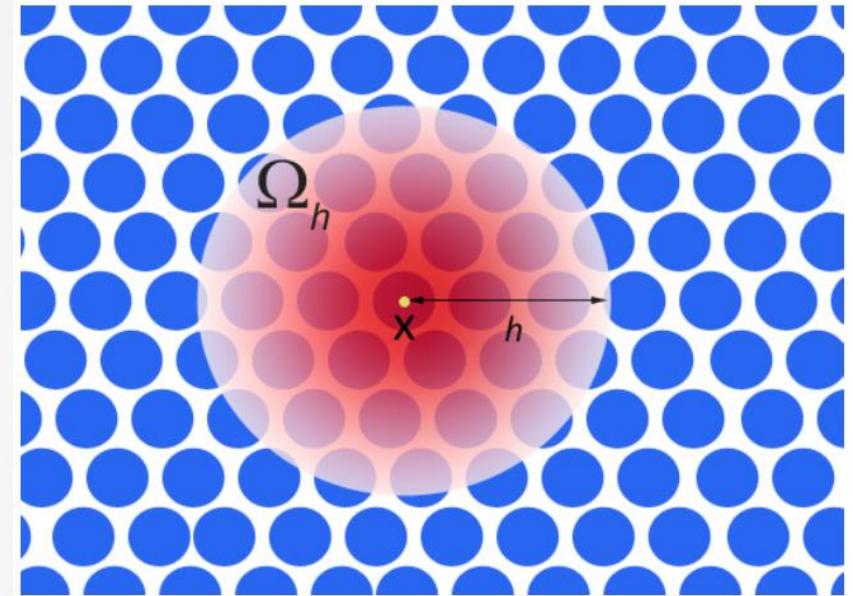
1. Find neighbors
2. Compute explicit forces
3. Solve for implicit forces
4. Update velocities, positions and other physical quantities of partial volume (particles)



// Performance – Neighbor search



- Typically 30 to 40 particles in influence domain
- 1 million particles: 20ms
- Reduce number of queries
 - Compact hashing
 - Z-index sorting
 - kd-trees





// Performance – System of equations

- Pressure term
 - Enforce volume conservation of fluid
 - Solve for unknown pressure field
 - Pressure gradient results in forces
- Viscosity term
 - Minimize strain-rate tensor
 - Changes the velocity gradient

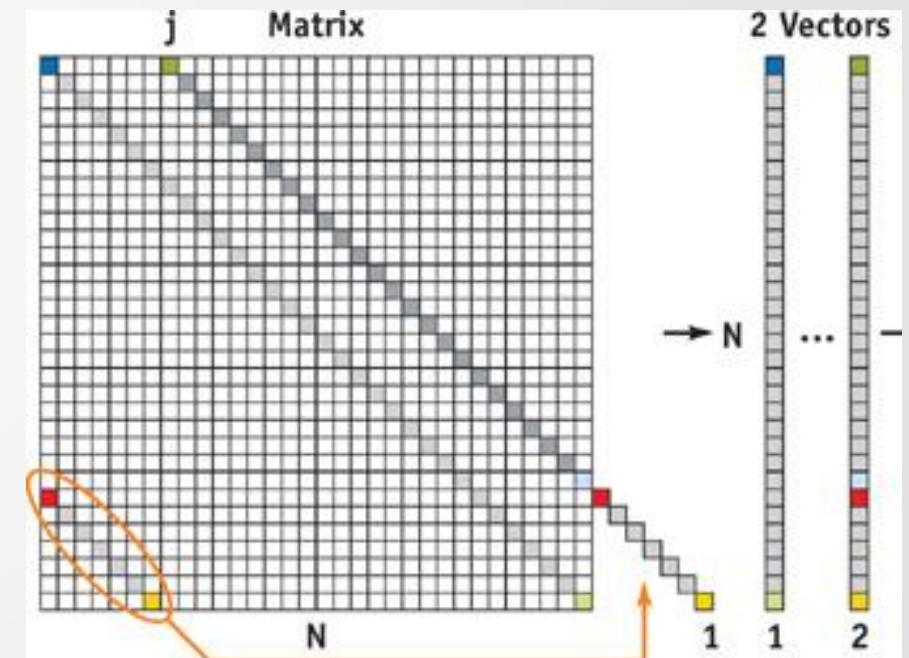
$$\mathbf{D} = \frac{1}{2}(\nabla \mathbf{v} + (\nabla \mathbf{v})^T)$$

// Performance – System of equations



- Simulation with 100 million particles
- Linear system of size 100M x 100M
 - Conjugate gradient
 - Relaxed Jacobi
 - Gauss-Seidel
- System is sparsely filled
 - Matrix-free and compact implementation

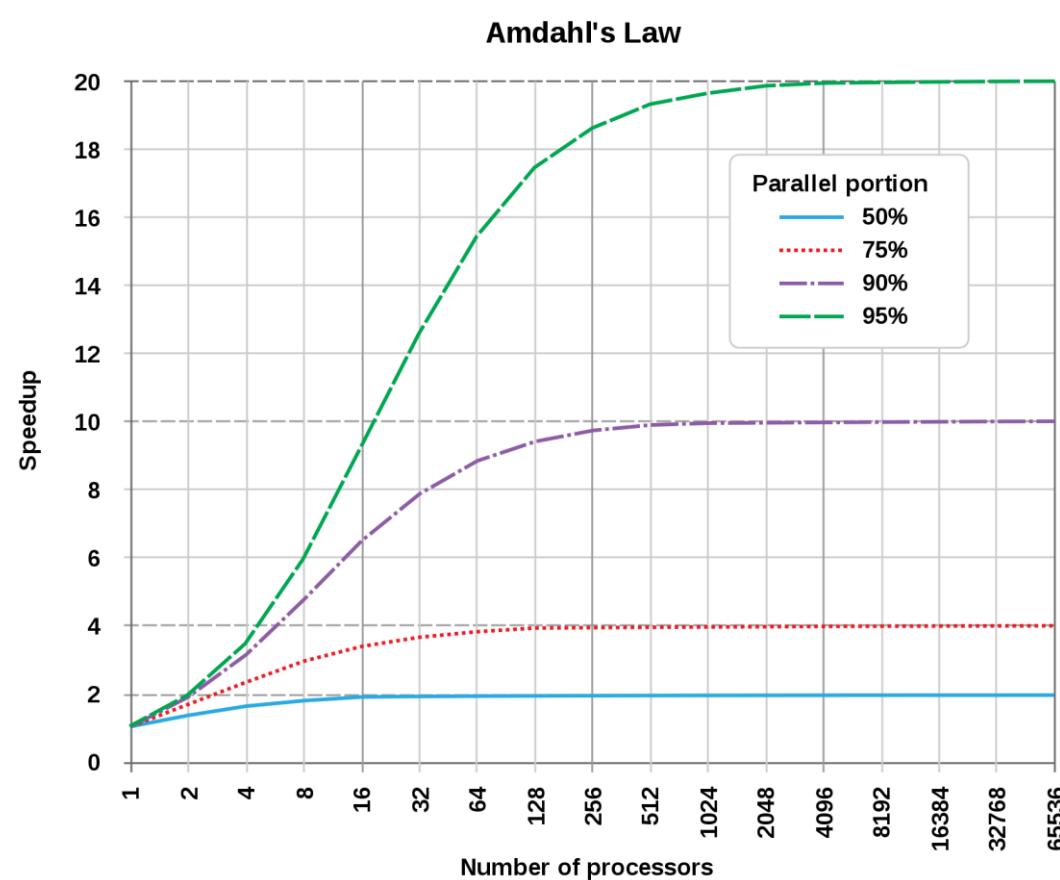
$$\mathbf{A}\mathbf{x} = \mathbf{b}$$



// Performance - Parallelization



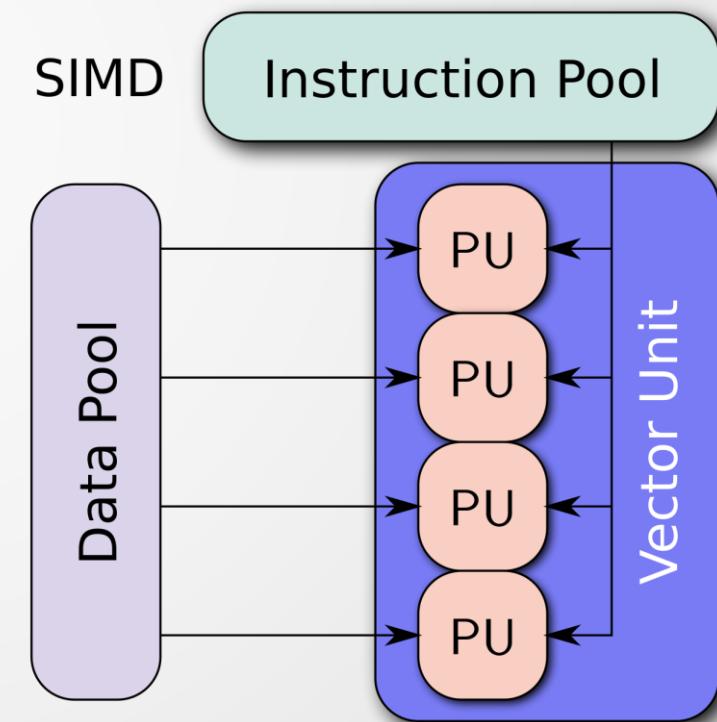
- Expectable speed-up obeys Amdahl's law



// Performance - Parallelization

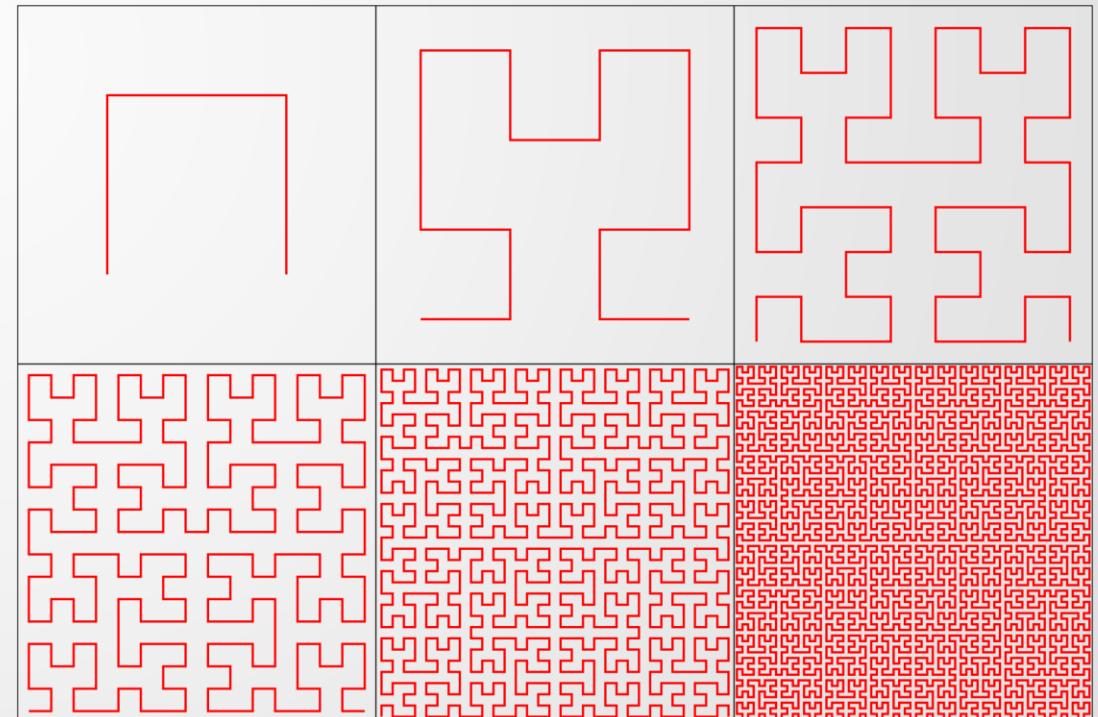
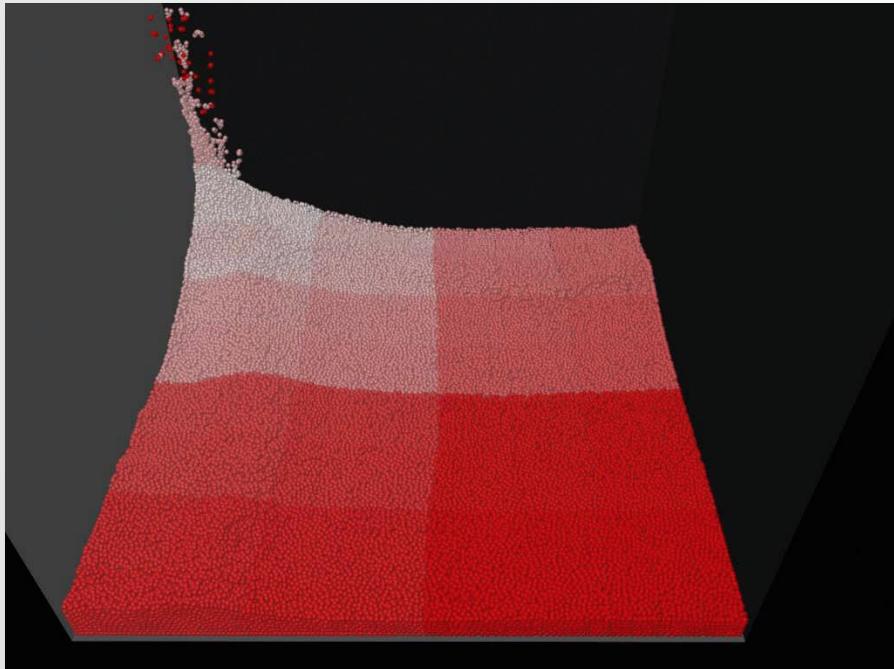


- Expectable speed-up obeys Amdahl's law
- Reduce latencies
 - SIMD: Optimized data structures



// Performance - Parallelization

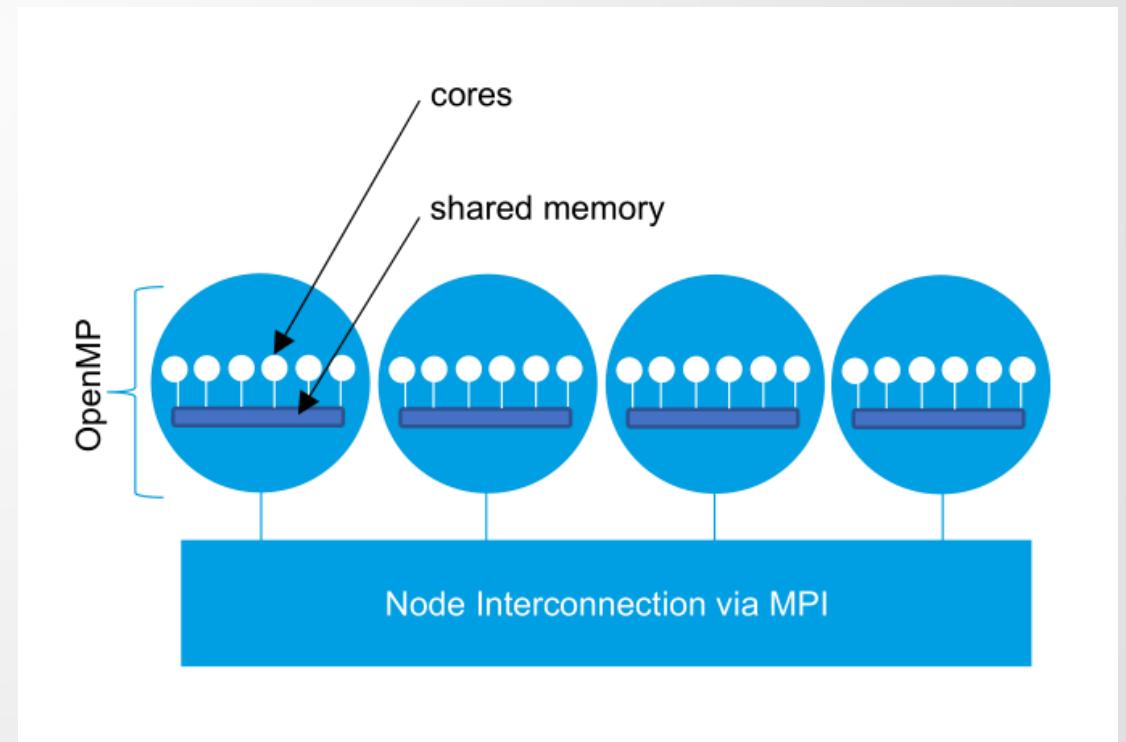
- Expectable speed-up obeys Amdahl's law
- Reduce latencies
 - Single Instruction Multiple Data
 - SMP: Increase cache coherency



// Performance - Parallelization



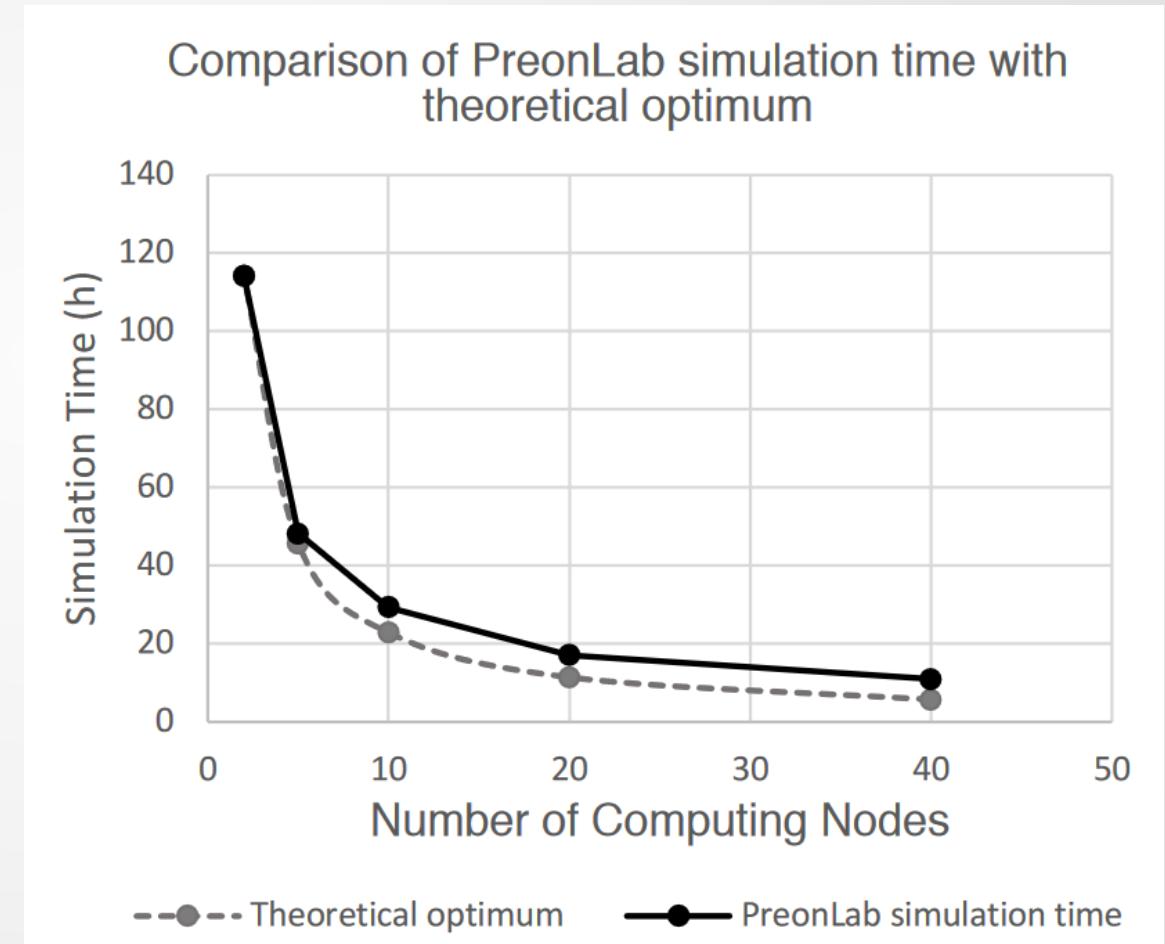
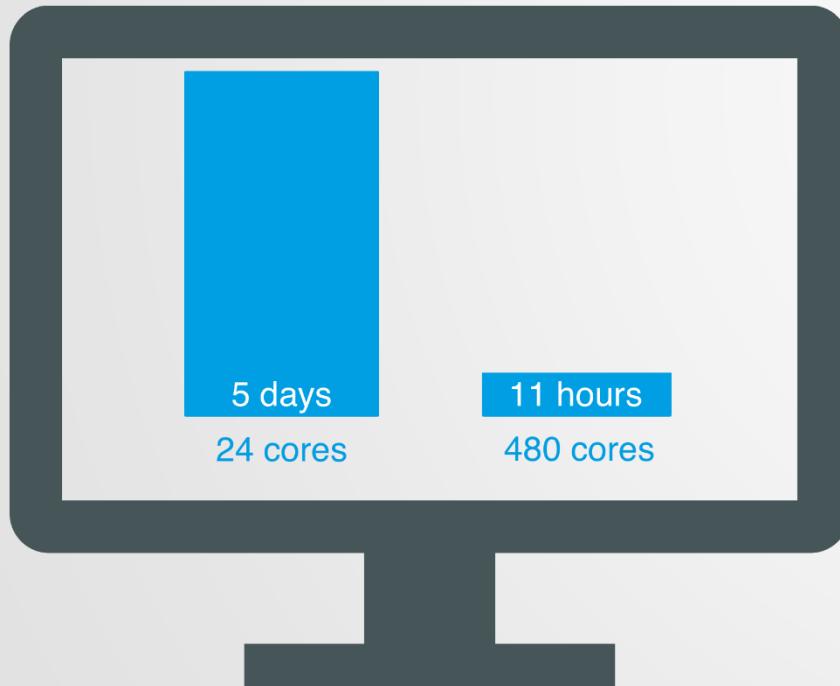
- Expectable speed-up obeys Amdahl's law
- Reduce latencies
 - SMP: Increase cache coherency
 - SIMD: Optimized data structures
 - MMP: Load balancing



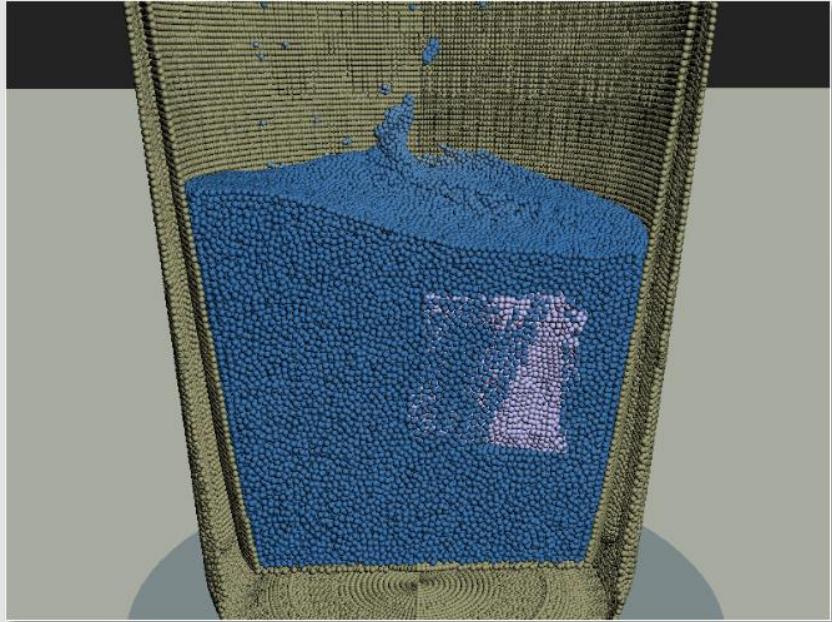
// Performance – Hybrid parallel implementation



73500 liter
157 Million particles
40 sec



// Rendering



Simulation:

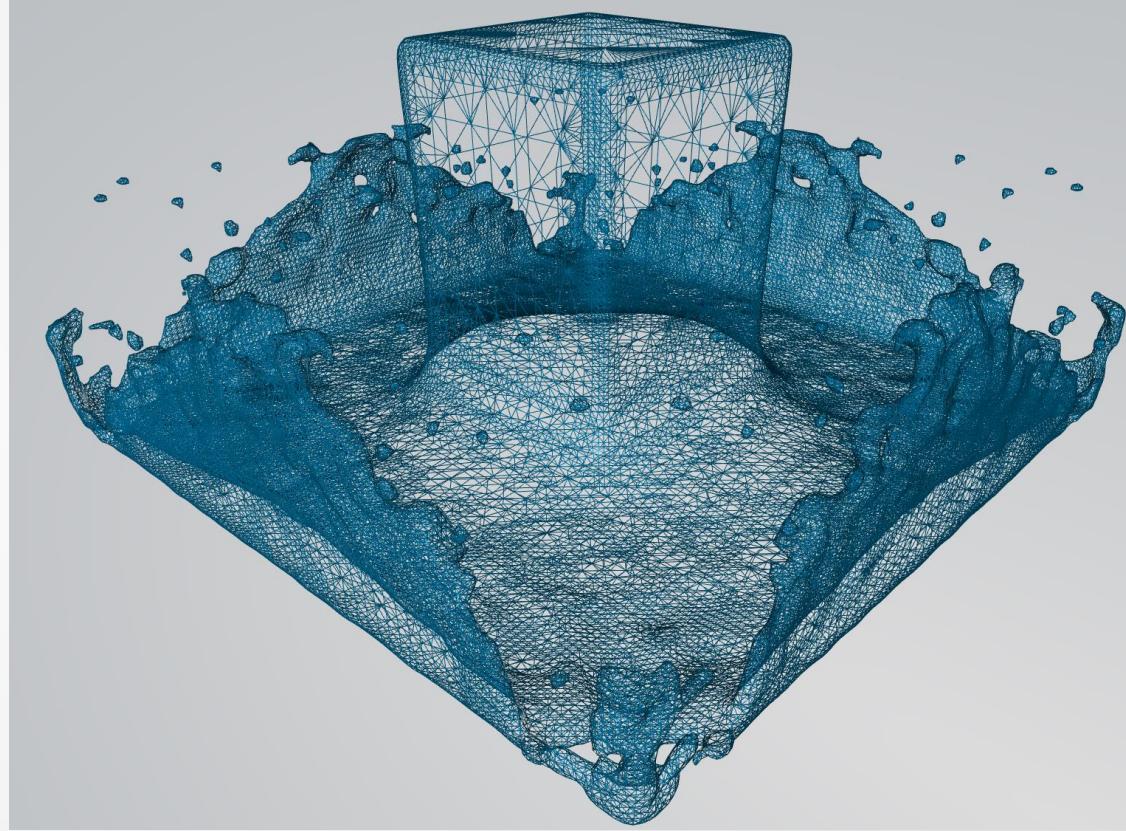
- Discrete representation

Visualization:

- Continuous volume
- Simulate absorption, reflection and transmission of light

// Classical approaches

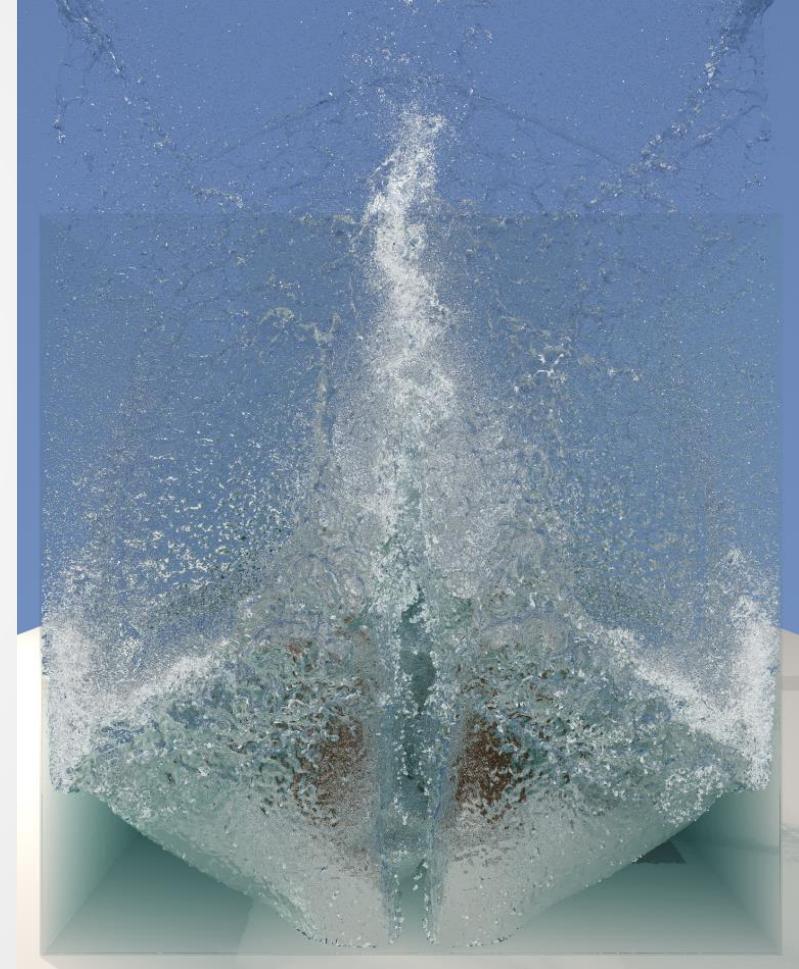
- Create triangle mesh from particles
- Isosurface generation via
 - Marching cubes
 - Dual contouring
 - Adaptive dual marching cubes
- Mesh files can be used
 - By any raytracing program
- But
 - Time-consuming to construct
 - Consume a lot of memory





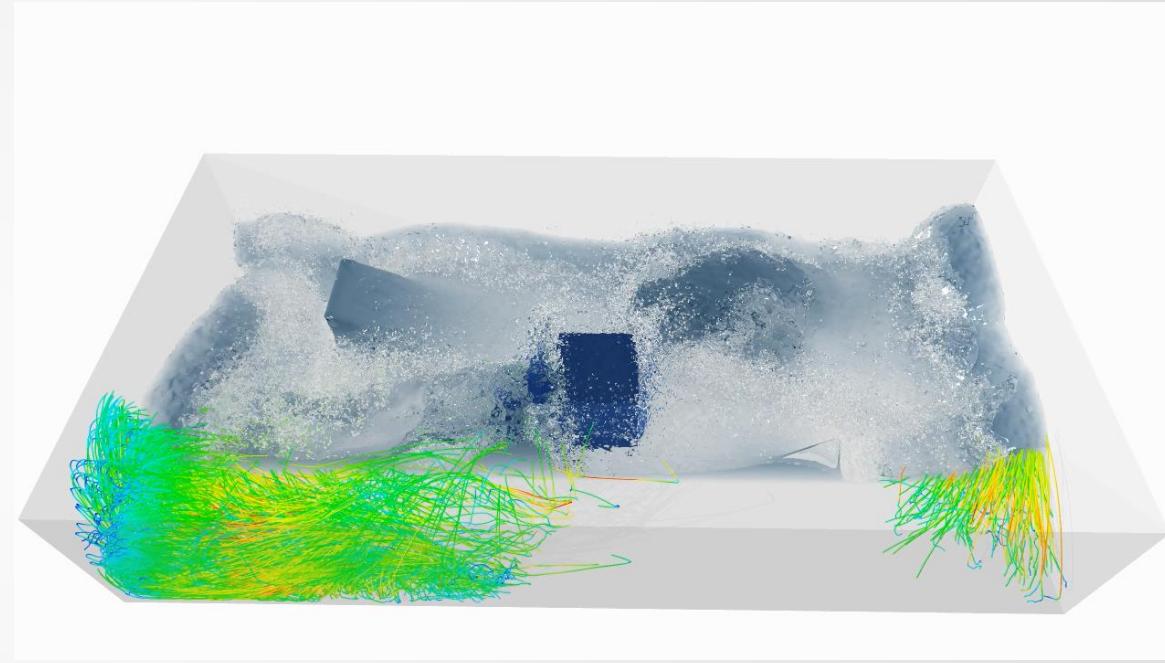
// Preon renderer

- Renders fluid as smooth surface without generating an explicit mesh
- CPU-based ray tracer which works on systems without graphic cards / cluster
- Fast generation by using neighbor search data structure
- Implicit foam rendering
- Output is image per frame



// Preon renderer

- Physically-based stochastic raytracer
- Photon mapping
- Fluid properties can be colorized on virtual surface and sensors can be visualized





What's next?

// Product development



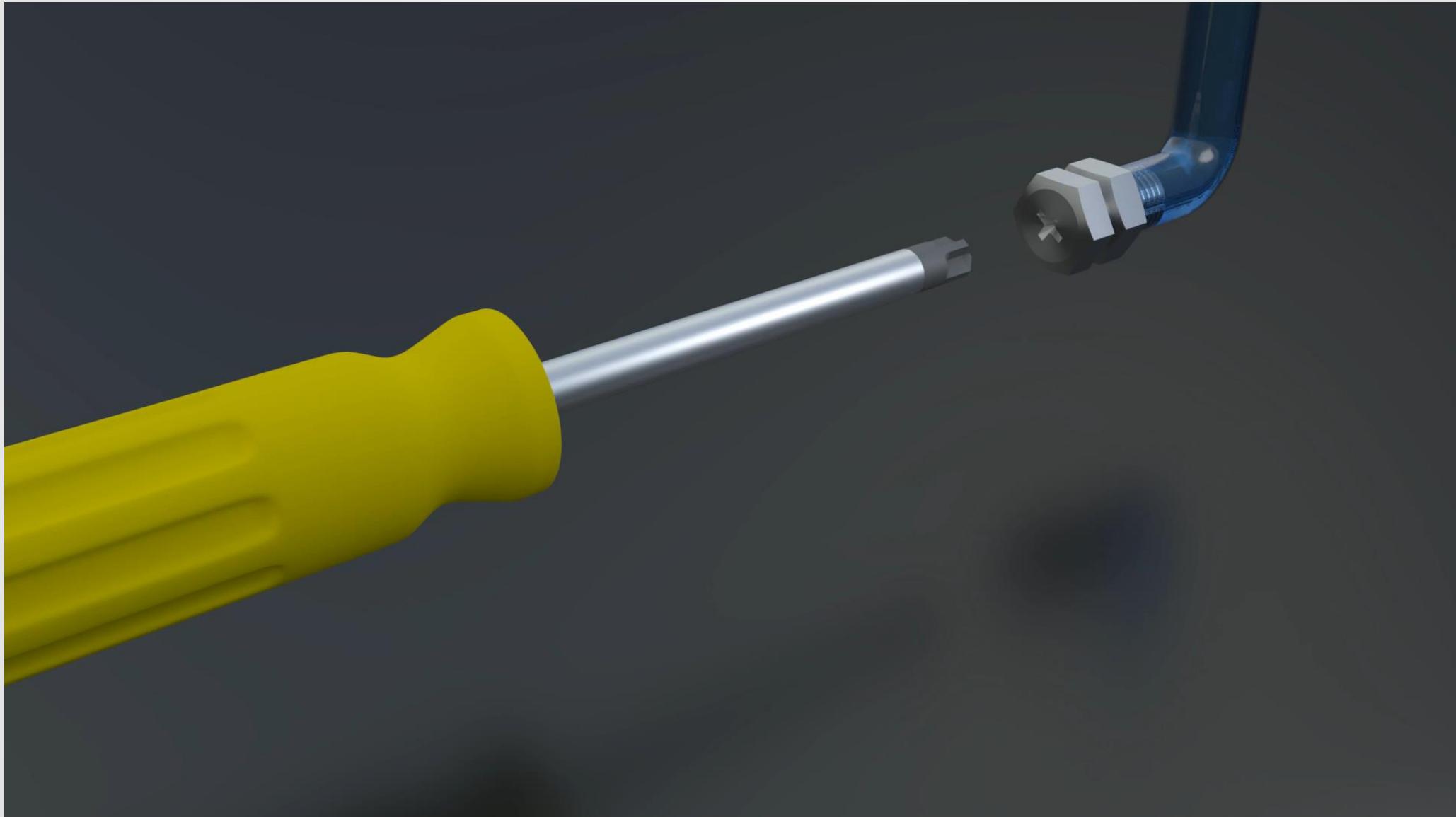
Include more physics:

- Improve quality
- New applications

Optimizations:

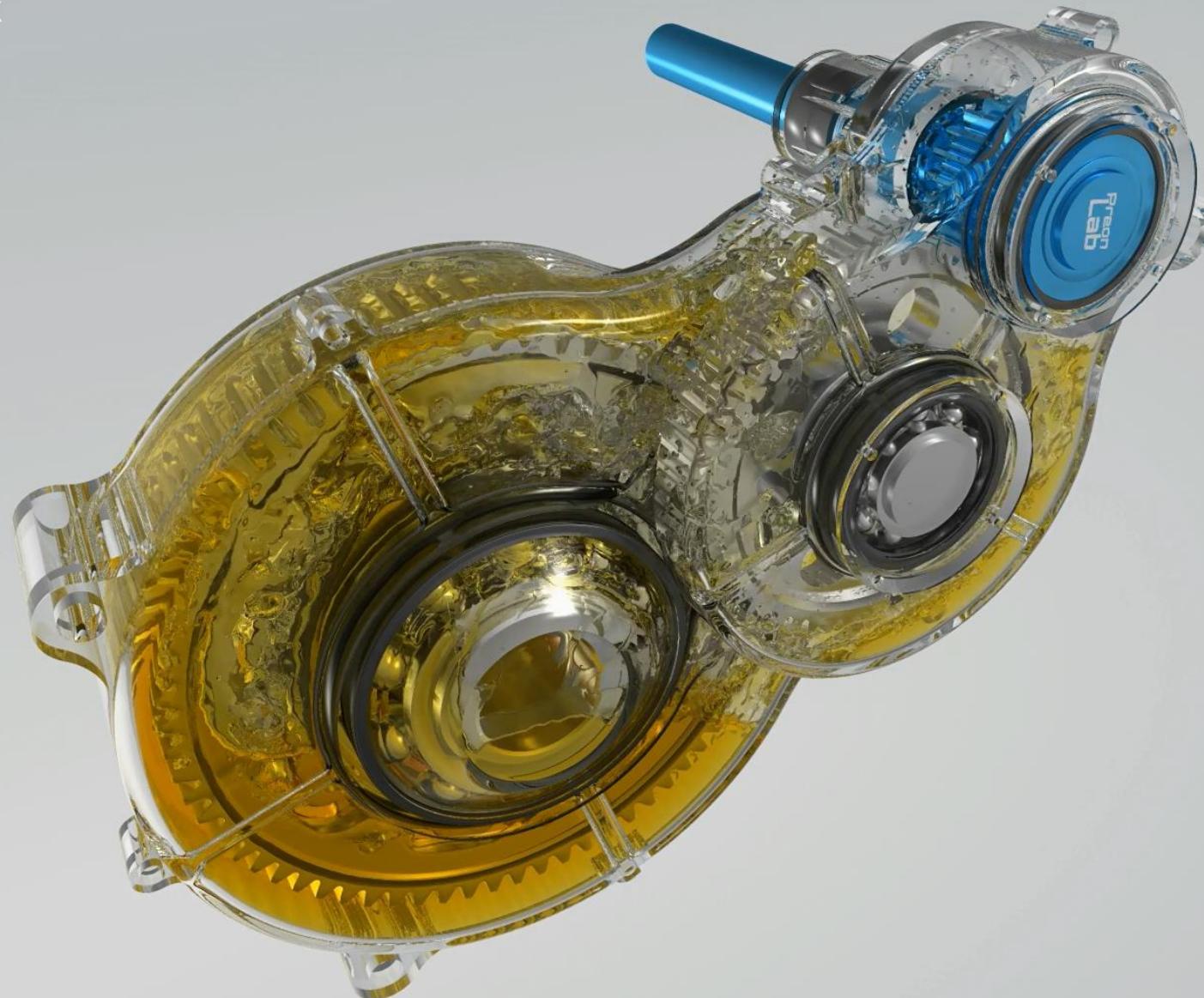
- Performance
- Workflow

// Particle-based rigid body solver



Foto

slow motion: 5x



// Highly viscous fluids

