Introduction to Information Retrieval http://informationretrieval.org

IIR 12: Language Models for IR

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Overview

- Recap
- Peature selection
- 3 Language models
- 4 Language Models for IR
- Discussion

Outline

- Recap
- 2 Feature selection
- 3 Language models
- 4 Language Models for IR
- Discussion

Naive Bayes classification rule

$$c_{\mathsf{map}} = rg \max_{c \in \mathbb{C}} \left[\log \hat{P}(c) + \sum_{1 \leq k \leq n_d} \log \hat{P}(t_k | c)
ight]$$

- Each conditional parameter $\log \hat{P}(t_k|c)$ is a weight that indicates how good an indicator t_k is for c.
- The prior $\log \hat{P}(c)$ is a weight that indicates the relative frequency of c.
- The sum of log prior and term weights is then a measure of how much evidence there is for the document being in the class.
- We select the class with the most evidence.

Parameter estimation

Prior:

$$\hat{P}(c) = \frac{N_c}{N}$$

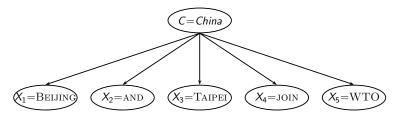
where N_c is the number of docs in class c and N the total number of docs

Conditional probabilities:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)}$$

where T_{ct} is the number of tokens of t in training documents from class c (includes multiple occurrences)

Add-one smoothing to avoid zeros

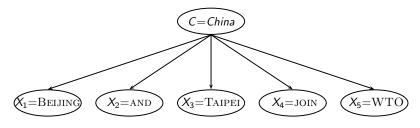


 Without add-one smoothing: if there are no occurrences of WTO in documents in class China, we get a zero estimate for the corresponding parameter:

$$\hat{P}(WTO|\textit{China}) = \frac{T_{\textit{China}},WTO}{\sum_{t' \in V} T_{\textit{China},t'}} = 0$$

- With this estimate: $[d \text{ contains WTO}] \rightarrow [P(China|d) = 0].$
- We must smooth to get a better estimate P(China|d) > 0.

Naive Bayes Generative Model



$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- Generate a class with probability P(c)
- Generate each of the words (in their respective positions), conditional on the class, but independent of each other, with probability $P(t_k|c)$

Take-away today

- Feature selection for text classification: How to select a subset of available dimensions
- Statistical language models: Introduction
- Statistical language models in IR
- Discussion: Properties of different probabilistic models in use in IR

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Feature selection

- In text classification, we usually represent documents in a high-dimensional space, with each dimension corresponding to a term.
- In this lecture: axis = dimension = word = term = feature
- Many dimensions correspond to rare words.
- Rare words can mislead the classifier.
- Rare misleading features are called noise features.
- Eliminating noise features from the representation increases efficiency and effectiveness of text classification.
- Eliminating features is called feature selection.

Example for a noise feature

- Let's say we're doing text classification for the class China.
- Suppose a rare term, say ARACHNOCENTRIC, has no information about *China* . . .
- ... but all instances of ARACHNOCENTRIC happen to occur in *China* documents in our training set.
- Then we may learn a classifier that incorrectly interprets ARACHNOCENTRIC as evidence for the class China.
- Such an incorrect generalization from an accidental property of the training set is called overfitting.
- Feature selection reduces overfitting and improves the accuracy of the classifier.

Basic feature selection algorithm

```
SELECTFEATURES(\mathbb{D}, c, k)

1 V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})

2 L \leftarrow []

3 for each t \in V

4 do A(t, c) \leftarrow \text{ComputeFeatureUtility}(\mathbb{D}, t, c)

5 APPEND(L, \langle A(t, c), t \rangle)

6 return FeaturesWithLargestValues(L, k)

How do we compute A, the feature utility?
```

Different feature selection methods

- A feature selection method is mainly defined by the feature utility measure it employs
- Feature utility measures:
 - Frequency select the most frequent terms
 - Mutual information select the terms with the highest mutual information
 - Mutual information is also called information gain in this context.
 - Chi-square (see book)

Mutual information

- Compute the feature utility A(t, c) as the mutual information (MI) of term t and class c.
- MI tells us "how much information" the term contains about the class and vice versa.
- For example, if a term's occurrence is independent of the class (same proportion of docs within/without class contain the term), then MI is 0.
- Definition:

$$I(U; C) = \sum_{e_t \in \{1,0\}} \sum_{e_c \in \{1,0\}} P(U = e_t, C = e_c) \log_2 \frac{P(U = e_t, C = e_c)}{P(U = e_t)P(C = e_c)}$$

How to compute MI values

 Based on maximum likelihood estimates, the formula we actually use is:

$$I(U;C) = \frac{N_{11}}{N} \log_2 \frac{NN_{11}}{N_{1.}N_{.1}} + \frac{N_{01}}{N} \log_2 \frac{NN_{01}}{N_{0.}N_{.1}} + \frac{N_{10}}{N} \log_2 \frac{NN_{10}}{N_{1.}N_{.0}} + \frac{N_{00}}{N} \log_2 \frac{NN_{00}}{N_{0.}N_{.0}}$$

• N_{10} : number of documents that contain t ($e_t = 1$) and are not in c ($e_c = 0$); N_{11} : number of documents that contain t ($e_t = 1$) and are in c ($e_c = 1$); N_{01} : number of documents that do not contain t ($e_t = 1$) and are in c ($e_c = 1$); N_{00} : number of documents that do not contain t ($e_t = 1$) and are not in c ($e_c = 1$); $N = N_{00} + N_{01} + N_{10} + N_{11}$.

How to compute MI values (2)

Alternative way of computing MI:

$$I(U;C) = \sum_{e_t \in \{1,0\}} \sum_{e_c \in \{1,0\}} P(U = e_t, C = e_c) \log_2 \frac{N(U = e_t, C = e_c)}{E(U = e_t)E(C = e_c)}$$

- $N(U=e_t, C=e_c)$ is the count of documents with values e_t and e_c .
- $E(U=e_t, C=e_c)$ is the expected count of documents with values e_t and e_c if we assume that the two random variables are independent.

MI example for *poultry*/EXPORT in Reuters

$$e_c = e_{poultry} = 1$$
 $e_c = e_{poultry} = 0$
 $e_t = e_{\text{EXPORT}} = 1$ $N_{11} = 49$ $N_{10} = 27,652$ Plug $e_t = e_{\text{EXPORT}} = 0$ $N_{01} = 141$ $N_{00} = 774,106$ these values into formula:

$$I(U;C) = \frac{49}{801,948} \log_2 \frac{801,948 \cdot 49}{(49+27,652)(49+141)}$$

$$+ \frac{141}{801,948} \log_2 \frac{801,948 \cdot 141}{(141+774,106)(49+141)}$$

$$+ \frac{27,652}{801,948} \log_2 \frac{801,948 \cdot 27,652}{(49+27,652)(27,652+774,106)}$$

$$+ \frac{774,106}{801,948} \log_2 \frac{801,948 \cdot 774,106}{(141+774,106)(27,652+774,106)}$$

$$\approx 0.000105$$

MI feature selection on Reuters

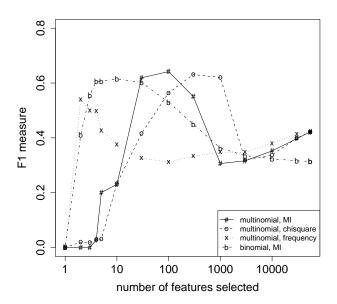
Class:	coffee

term	MI
COFFEE	0.0111
BAGS	0.0042
GROWERS	0.0025
KG	0.0019
COLOMBIA	0.0018
BRAZIL	0.0016
EXPORT	0.0014
EXPORTERS	0.0013
EXPORTS	0.0013
CROP	0.0012

Class: sports

MI			
0.0681			
0.0515			
0.0441			
0.0408			
0.0388			
0.0386			
0.0301			
0.0299			
0.0284			
0.0264			

Naive Bayes: Effect of feature selection



(multinomial = multinomial Naive Bayes, binomial = Bernoulli Naive Bayes)

Feature selection for Naive Bayes

- In general, feature selection is necessary for Naive Bayes to get decent performance.
- Also true for many other learning methods in text classification: you need feature selection for optimal performance.

Exercise

(i) Compute the "export"/POULTRY contingency table for the "Kyoto"/JAPAN in the collection given below. (ii) Make up a contingency table for which MI is 0- that is, term and class are independent of each other. "export"/POULTRY table:

	$e_c = e_{poultry} = 1$	$e_c = e_{poultry} = 0$
$e_t = e_{\text{EXPORT}} = 1$	$N_{11} = 49$	$N_{10} = 27,652$
$e_t = e_{\text{EXPORT}} = 0$	$N_{01} = 141$	$N_{00} = 774,106$

Collection:

	docID	words in document	in $c = Japan$?
training set	set 1 Kyoto Osaka Taiwan		yes
	2	Japan Kyoto	yes
	3	Taipei Taiwan	no
	4	Macao Taiwan Shanghai	no
	5	London	no

Outline

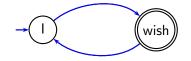
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Using language models (LMs) for IR

- LM = language model
- We view the document as a generative model that generates the query.
- What we need to do:
- Define the precise generative model we want to use
- Estimate parameters (different parameters for each document's model)
- Smooth to avoid zeros
- Apply to query and find document most likely to have generated the query
- Present most likely document(s) to user
- Note that 4-7 is very similar to what we did in Naive Bayes.

What is a language model?

We can view a finite state automaton as a deterministic language



model.

I wish I wish I wish I wish . . . Cannot generate: "wish I wish"

or "I wish I" Our basic model: each document was generated by a

different automaton like this except that these automata are probabilistic.

A probabilistic language model



W	$P(w q_1)$		$P(w q_1)$	
STOP	0.2	toad	0.01	_
the	0.2	said	0.03	
а	0.1	toad said likes that	0.02	
frog	0.01	that	0.04	
				This

is a one-state probabilistic finite-state automaton – a unigram language model – and the state emission distribution for its one state q_1 . STOP is not a word, but a special symbol indicating that

the automaton stops. frog said that toad likes frog STOP

 $P(\text{string}) = 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2$

= 0.0000000000048

A different language model for each document

language model of d_1			language model of d_2				
W	P(w .)	W	P(w .)	W	P(w .)	W	P(w .)
STOP	.2	toad	.01	STOP	.2	toad	.02
the	.2	said	.03	the	.15	said	.03
а	.1	likes	.02	а	.08	likes	.02
frog	.01	that	.04	frog	.01	that	.05

query: frog said that toad likes frog STOP $P(\text{query}|M_{d1}) = 0.01$

$$\cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2 = 0.00000000000048 = 4.8 \cdot 10^{-12}$$

 $P(\text{query}|M_{d2}) = 0.01 \cdot 0.03 \cdot 0.05 \cdot 0.02 \cdot 0.02 \cdot 0.01 \cdot 0.2$

$$= 0.000000000120 = 12 \cdot 10^{-12} \quad P(\mathsf{query}|M_{d1}) < P(\mathsf{query}|M_{d2})$$

Thus, document d_2 is "more relevant" to the query "frog said that toad likes frog STOP" than d_1 is.

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Using language models in IR

- Each document is treated as (the basis for) a language model.
- Given a query q
- Rank documents based on P(d|q)

$$P(d|q) = \frac{P(q|d)P(d)}{P(q)}$$

- P(q) is the same for all documents, so ignore
- P(d) is the prior often treated as the same for all d
 - But we can give a higher prior to "high-quality" documents, e.g., those with high PageRank.
- P(q|d) is the probability of q given d.
- For uniform prior: ranking documents according according to P(q|d) and P(d|q) is equivalent.

Where we are

- In the LM approach to IR, we attempt to model the query generation process.
- Then we rank documents by the probability that a query would be observed as a random sample from the respective document model.
- That is, we rank according to P(q|d).
- Next: how do we compute P(q|d)?

How to compute P(q|d)

 We will make the same conditional independence assumption as for Naive Bayes.

•

$$P(q|M_d) = P(\langle t_1, \dots, t_{|q|} \rangle | M_d) = \prod_{1 \leq k \leq |q|} \frac{P(t_k | M_d)}{P(t_k | M_d)}$$

 $(|q|: length of q; t_k: the token occurring at position k in q)$

This is equivalent to:

$$P(q|M_d) = \prod_{\text{distinct term } t \text{ in } q} P(t|M_d)^{\text{tf}_{t,q}}$$

- $tf_{t,q}$: term frequency (# occurrences) of t in q
- Multinomial model (omitting constant factor)

Parameter estimation

- Missing piece: Where do the parameters $P(t|M_d)$ come from?
- Start with maximum likelihood estimates (as we did for Naive Bayes)

$$\hat{P}(t|M_d) = \frac{\operatorname{tf}_{t,d}}{|d|}$$

(|d|: length of d; $tf_{t,d}$: # occurrences of t in d)

- As in Naive Bayes, we have a problem with zeros.
- A single t with $P(t|M_d) = 0$ will make $P(q|M_d) = \prod P(t|M_d)$ zero.
- We would give a single term "veto power".
- For example, for query [Michael Jackson top hits] a document about "top songs" (but not using the word "hits") would have $P(q|M_d) = 0$. Thats's bad.
- We need to smooth the estimates to avoid zeros.

Smoothing

- Key intuition: A nonoccurring term is possible (even though it didn't occur), . . .
- ... but no more likely than would be expected by chance in the collection.
- Notation: M_c : the collection model; cf_t : the number of occurrences of t in the collection; $T = \sum_t \operatorname{cf}_t$: the total number of tokens in the collection.

•

$$\hat{P}(t|M_c) = \frac{\mathrm{cf}_t}{T}$$

• We will use $\hat{P}(t|M_c)$ to "smooth" P(t|d) away from zero.

Jelinek-Mercer smoothing

- $P(t|d) = \lambda P(t|M_d) + (1-\lambda)P(t|M_c)$
- Mixes the probability from the document with the general collection frequency of the word.
- High value of λ: "conjunctive-like" search tends to retrieve documents containing all query words.
- Low value of λ : more disjunctive, suitable for long queries
- ullet Correctly setting λ is very important for good performance.

Jelinek-Mercer smoothing: Summary

 $P(q|d) \propto \prod_{1 \leq k \leq |q|} (\lambda P(t_k|M_d) + (1-\lambda)P(t_k|M_c))$

- What we model: The user has a document in mind and generates the query from this document.
- The equation represents the probability that the document that the user had in mind was in fact this one.

Example

- Collection: d_1 and d_2
- d₁: Jackson was one of the most talented entertainers of all time
- d₂: Michael Jackson anointed himself King of Pop
- Query q: Michael Jackson
- Use mixture model with $\lambda = 1/2$
- $P(q|d_1) = [(0/11 + 1/18)/2] \cdot [(1/11 + 2/18)/2] \approx 0.003$
- $P(q|d_2) = [(1/7 + 1/18)/2] \cdot [(1/7 + 2/18)/2] \approx 0.013$
- Ranking: $d_2 > d_1$

Exercise: Compute ranking

- Collection: d_1 and d_2
- d_1 : Xerox reports a profit but revenue is down
- d₂: Lucene narrows quarter loss but revenue decreases further
- Query q: revenue down
- Use mixture model with $\lambda = 1/2$
- $P(q|d_1) = [(1/8 + 2/16)/2] \cdot [(1/8 + 1/16)/2] = 1/8 \cdot 3/32 = 3/256$
- $P(q|d_2) = [(1/8 + 2/16)/2] \cdot [(0/8 + 1/16)/2] = 1/8 \cdot 1/32 = 1/256$
- Ranking: $d_1 > d_2$

Dirichlet smoothing

•

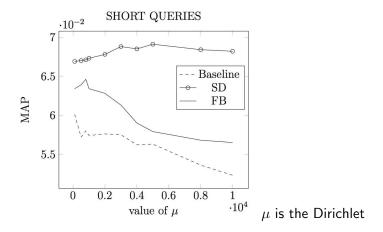
$$\hat{P}(t|d) = \frac{\operatorname{tf}_{t,d} + \alpha \hat{P}(t|M_c)}{L_d + \alpha}$$

- The background distribution $\hat{P}(t|M_c)$ is the prior for $\hat{P}(t|d)$.
- Intuition: Before having seen any part of the document we start with the background distribution as our estimate.
- As we read the document and count terms we update the background distribution.
- The weighting factor α determines how strong an effect the prior has.

Jelinek-Mercer or Dirichlet?

- Dirichlet performs better for keyword queries, Jelinek-Mercer performs better for verbose queries.
- Both models are sensitive to the smoothing parameters you shouldn't use these models without parameter tuning.

Sensitivity of Dirichlet to smoothing parameter



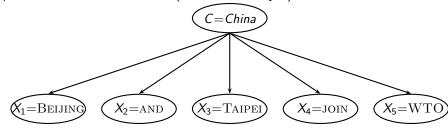
smoothing parameter (called α on the previous slides)

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Language models are generative models

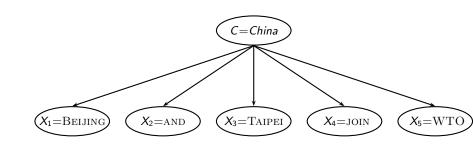
We have assumed that queries are generated by a probabilistic process that looks like this: (as in Naive Bayes)



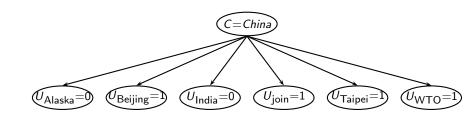
Naive Bayes and LM generative model s

- We want to classify document d.
 We want to classify a query q.
 - Classes: e.g., geographical regions like *China*, *UK*, *Kenya*. Each document in the collection is a different class.
- Assume that d was generated by the generative model.
 Assume that q was generated by a generative model
- Key question: Which of the classes is most likely to have generated the document? Which document (=class) is most likely to have generated the query q?
 - Or: for which class do we have the most evidence? For which document (as the source of the query) do we have the most evidence?

Naive Bayes Multinomial model / IR language models



Naive Bayes Bernoulli model / Binary independence model



Comparison of the two models

/ BIM
!
ırs in doc
$\ldots, e_M \rangle,$
$e_i = e_i c$
ort docs
fewer
≈ 1.0

Vector space (tf-idf) vs. LM

		precision		significant	
Rec.	tf-idf	LM	%chg		
0.0	0.7439	0.7590	+2.0		
0.1	0.4521	0.4910	+8.6		
0.2	0.3514	0.4045	+15.1	*	The
0.4	0.2093	0.2572	+22.9	*	rne
0.6	0.1024	0.1405	+37.1	*	
0.8	0.0160	0.0432	+169.6	*	
1.0	0.0028	0.0050	+76.9		
11-point average	0.1868	0.2233	+19.6	*	

language modeling approach always does better in these experiments ... but note that where the approach shows significant gains is at higher levels of recall.

Vector space vs BM25 vs LM

- BM25/LM: based on probability theory
- Vector space: based on similarity, a geometric/linear algebra notion
- Term frequency is directly used in all three models.
 - LMs: raw term frequency, BM25/Vector space: more complex
- Length normalization
 - Vector space: Cosine or pivot normalization
 - LMs: probabilities are inherently length normalized
 - BM25: tuning parameters for optimizing length normalization
- idf: BM25/vector space use it directly.
- LMs: Mixing term and collection frequencies has an effect similar to idf.
 - Terms rare in the general collection, but common in some documents will have a greater influence on the ranking.
- Collection frequency (LMs) vs. document frequency (BM25, vector space)

Language models for IR: Assumptions

- Simplifying assumption: Queries and documents are objects of the same type. Not true!
 - There are other LMs for IR that do not make this assumption.
 - The vector space model makes the same assumption.
- Simplifying assumption: Terms are conditionally independent.
 - Again, vector space model (and Naive Bayes) make the same assumption.
- Cleaner statement of assumptions than vector space
- Thus, better theoretical foundation than vector space
 - ... but "pure" LMs perform much worse than "tuned" LMs.

Take-away today

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- Discussion: Properties of different probabilistic models in use in IR

Resources

- Chapter 13 of IIR (feature selection)
- Chapter 12 of IIR (language models)
- Resources at http://cislmu.org
 - Ponte and Croft's 1998 SIGIR paper (one of the first on LMs in IR)
 - Zhai and Lafferty: A study of smoothing methods for language models applied to information retrieval. ACM Trans. Inf. Syst. (2004).
 - Lemur toolkit (good support for LMs in IR)