

# *Image Processing and Computer Graphics*

Thomas Brox  
Matthias Teschner



# Organization

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Computer Graphics

Matthias Teschner

<https://cg.informatik.uni-freiburg.de/teaching.htm>

Image Processing

Thomas Brox

[https://lmb.informatik.uni-freiburg.de/lectures/image\\_processing/](https://lmb.informatik.uni-freiburg.de/lectures/image_processing/)

# *Computer Graphics*

## *Modeling – Rendering – Simulation*

### *Introduction*

Matthias Teschner



# Computer Graphics

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Modeling – Rendering – Simulation

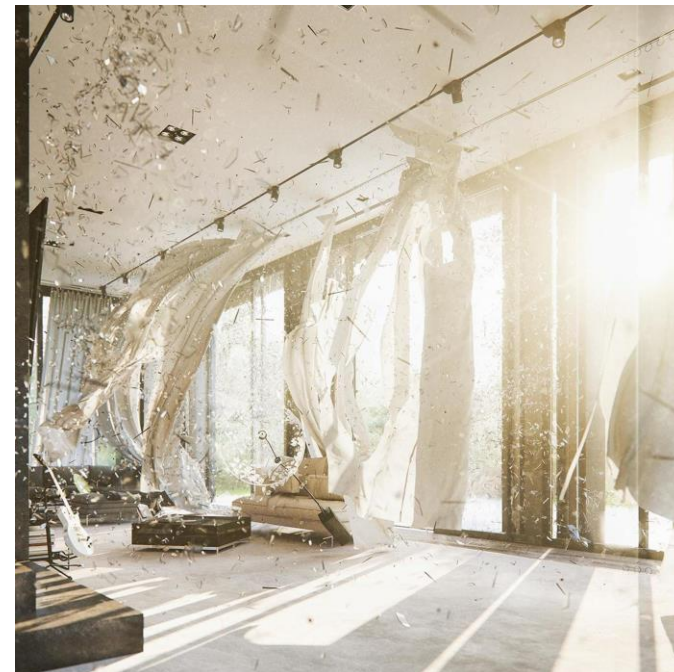
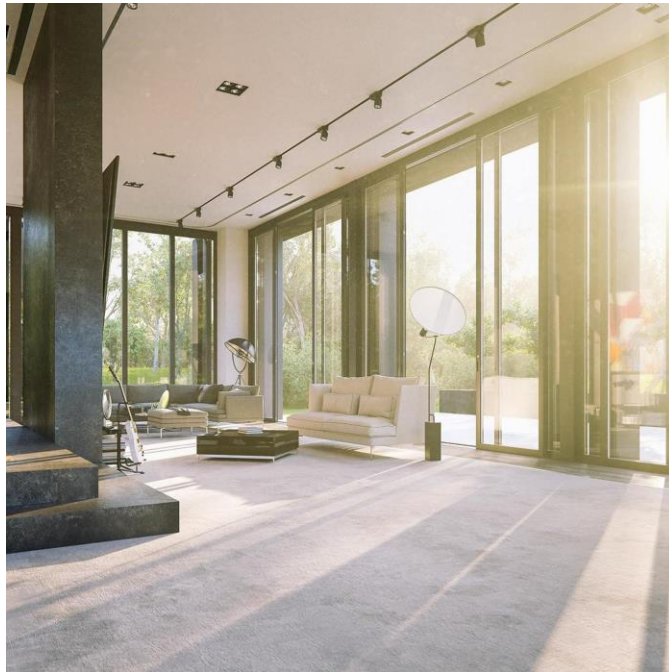


© Warner Bros.  
Scanline VFX  
V-Ray



# Computer Graphics

## Modeling – Rendering – Simulation



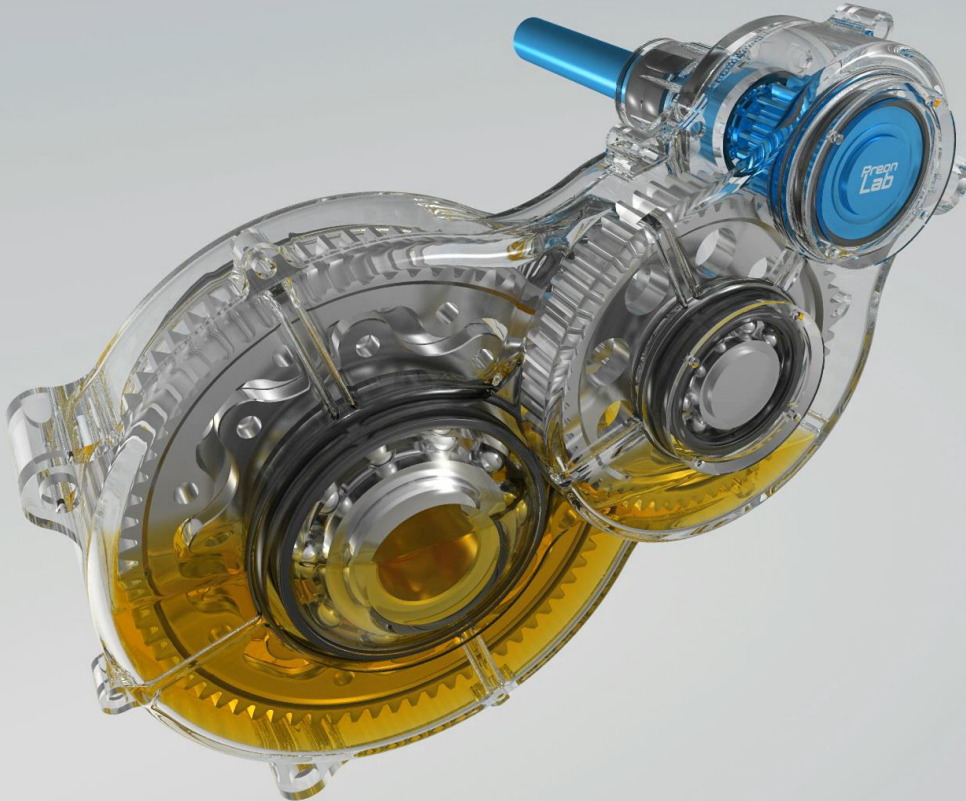
© Double Aye  
V-Ray

# Computer Graphics

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## Modeling – Rendering – Simulation

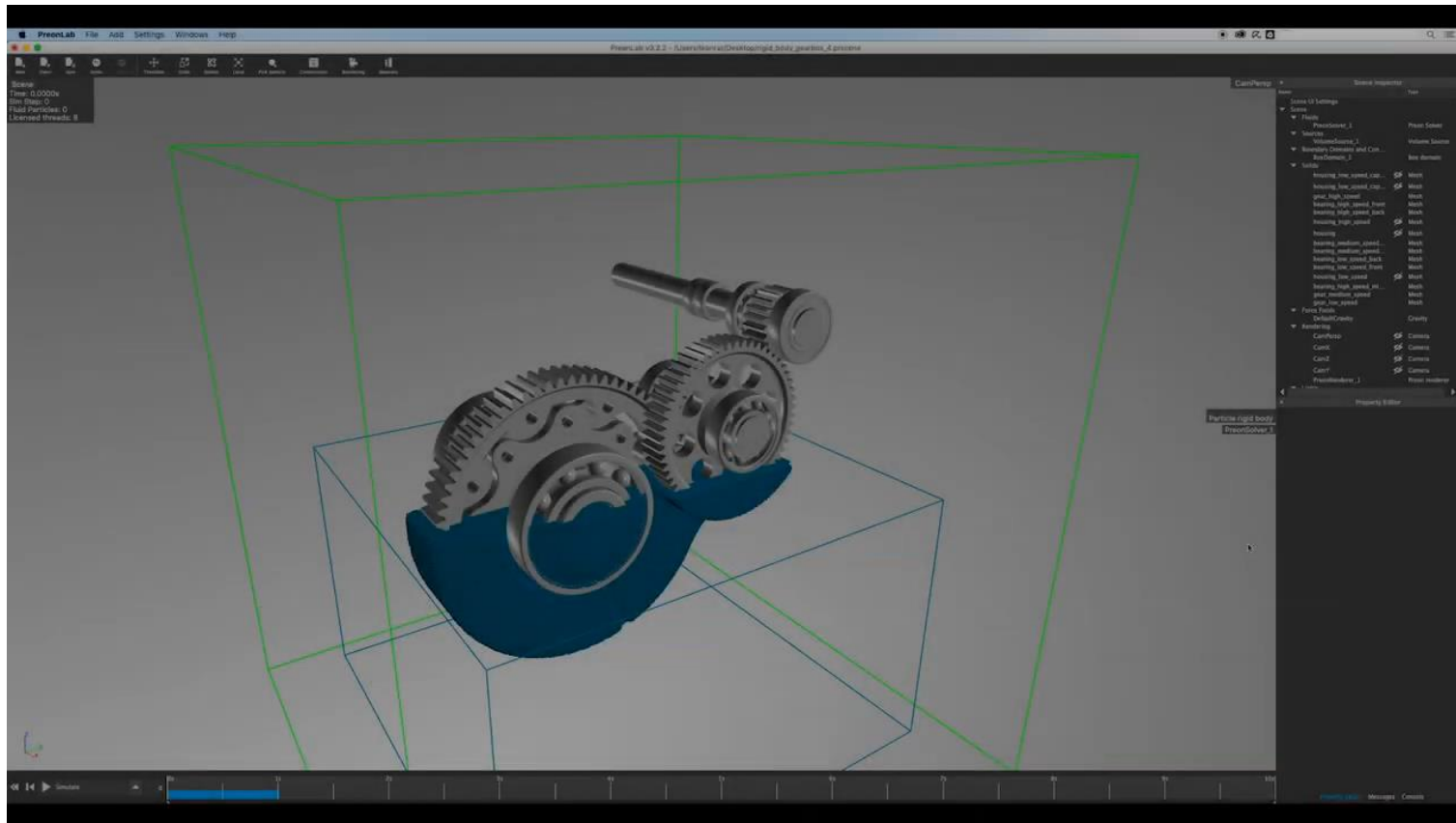
slow motion: 5x



FIFTY2 Technology

# Computer Graphics

## Modeling – Rendering – Simulation



FIFTY2 Technology

# *Application Areas*

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- Visual effects (movies, commercials)
- Architecture
- Engineering
- Medical imaging
- Scientific visualization
- Games
- Virtual reality / augmented reality

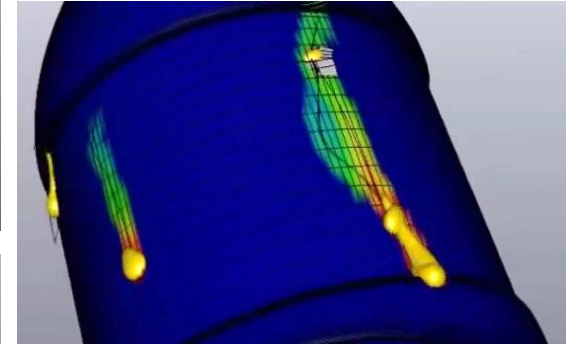
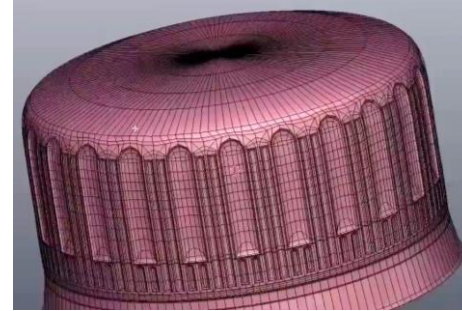
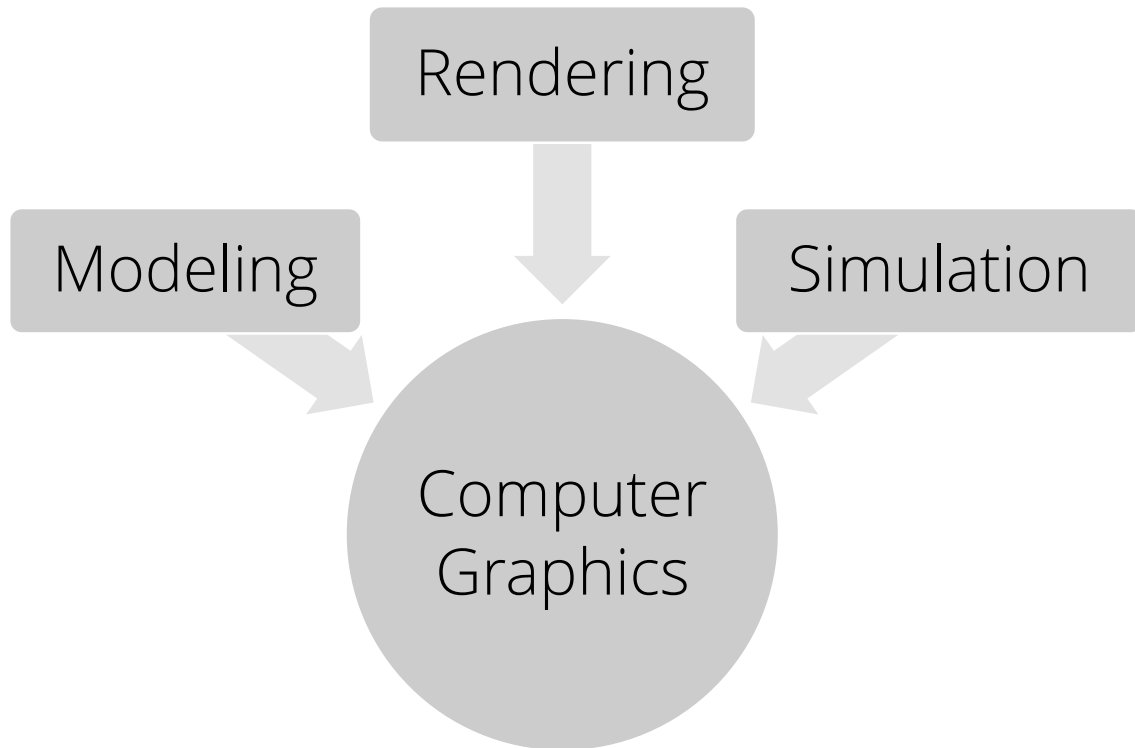


# Computer Graphics

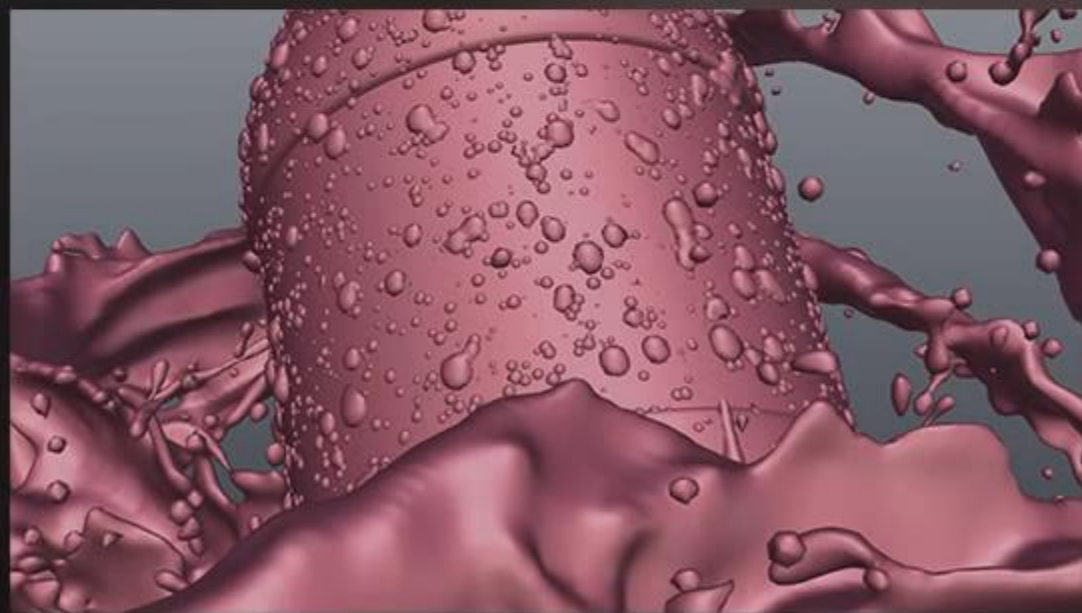
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- Light
  - Energy or photons transported along lines
  - Generated by light sources, measured / absorbed by sensors, interacts at surfaces and with participating media
- Modeling
  - Geometry, materials, participating media, illumination
- Rendering
  - Computation of light transport
- Simulation
  - Dynamic rigid bodies, deformable objects and fluids

# Computer Graphics



CGI Making of Share a Coke VFX  
Breakdown by ARMA



# MAKING OF “SHARE A COKE”



Music by: Chocolate Puma & Firebeatz  
I Can't Understand (Original Mix)

# Outline

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- Organization
- Our research
- Image generation
- Course topics

# Graphics Courses

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- Key course
  - Image processing and computer graphics (modeling, rendering, simulation)
- Specialization courses
  - Advanced computer graphics (global illumination)
  - Simulation in computer graphics (deformable and rigid solids, fluids)
- Master project, lab course, Master thesis
  - Simulation track, rendering track



# *Seminars / Projects / Theses in Graphics*

Semester	Simulation Track	Rendering Track
Winter	Simulation Course	
Summer	Key Course Lab Course - Simple fluid solver Simulation Seminar	Key Course Lab Course - Simple Ray Tracer Rendering Seminar
Winter	Master Project - PPE fluid solver Rendering Seminar	Rendering Course Master Project - Monte Carlo RT Simulation Seminar
Summer	Master Thesis Research-oriented topic	Master Thesis Research-oriented topic

# Material – Exam

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- Slide sets and recordings
- Slides, recordings, exercises, solutions and test exam on <https://cg.informatik.uni-freiburg.de/teaching.htm>
- Written exam

# Selected Readings

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- Andrew S. Glassner.  
*Principles of digital image synthesis*. Morgan Kaufmann, 1995.  
Free download on <https://www.realtimerendering.com/>
- Matt Pharr, Wenzel Jakob, Greg Humphreys.  
*Physically based rendering: From theory to implementation*. Morgan Kaufmann, 2016.  
Free online version: <http://www.pbr-book.org/>
- Steve Marschner, Peter Shirley.  
*Fundamentals of computer graphics*. CRC Press, 2015.
- Alan Watt. *3D computer graphics*. Addison-Wesley, 1999.
- James D. Foley, Andries van Dam, Steven K. Feiner.  
*Computer graphics: principles and practice*. Pearson Education, 2014.
- Andrew S. Glassner. *An introduction to ray tracing*. Elsevier, 1989.
- Thomas Akenine Moeller: *Real-time rendering*. Taylor & Francis, 2018.

# Exercises

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- Introduction to OpenGL >3.0
  - Programming interface for rendering
- Four exercises
- Two tasks / topics per exercise
  - Related to rasterization, homogeneous notation, projection, Phong shading (check course curriculum)
- Support
  - Student assistant
- Optional

# *Recommended Prerequisites*

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- Linear algebra
  - Vector
  - Matrix
- Calculus
  - Differentiation
  - Integration
- Programming language
  - C, ...



# Outline

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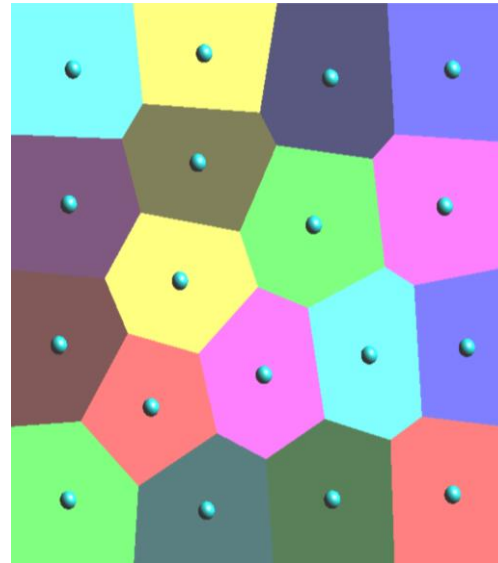
- Organization
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# Lagrangian Simulation



Fluid / Elastic  
object / Rigid  
object



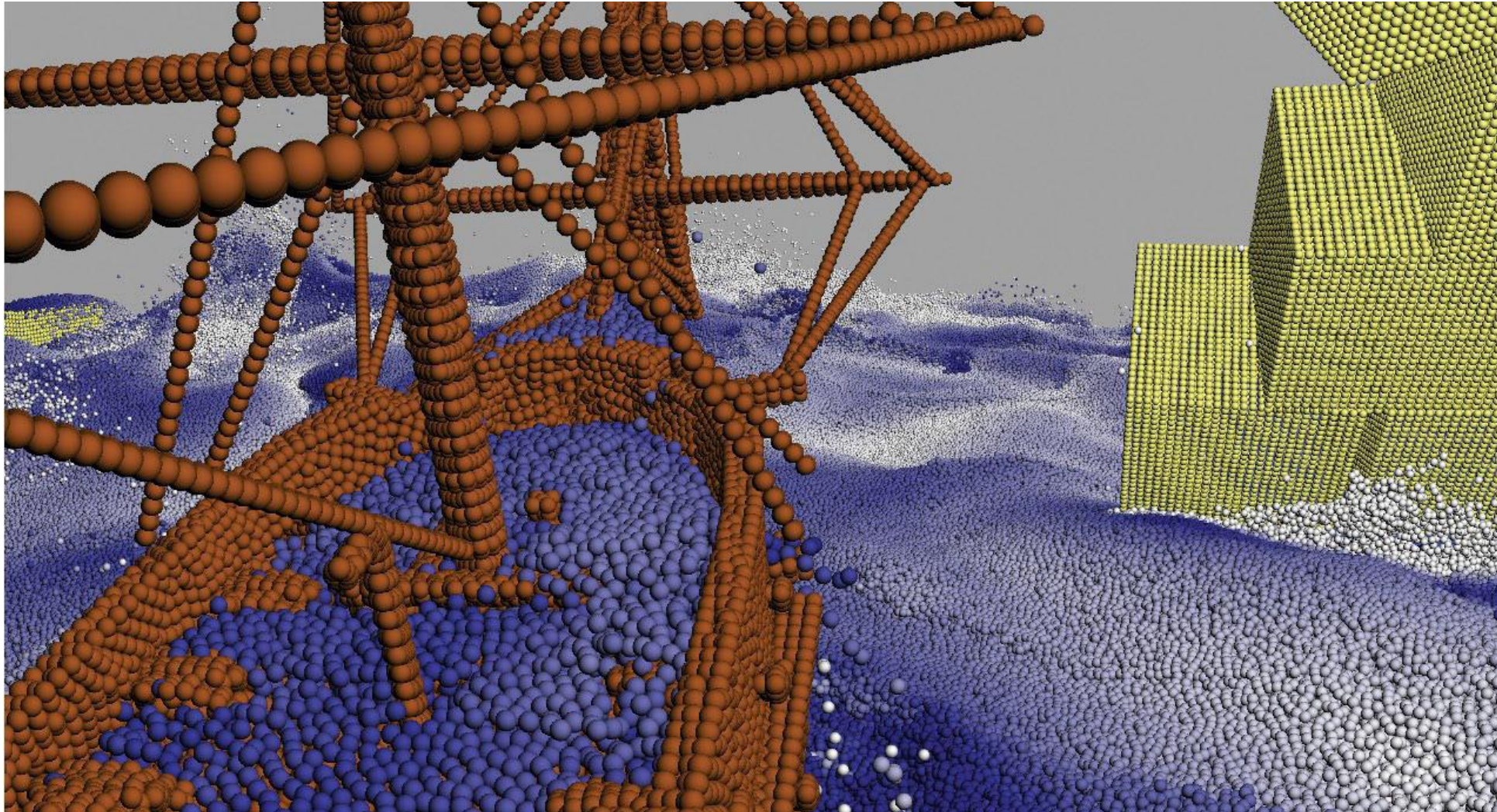
Set of parcels

$$x_i^t$$
$$v_i^t$$

Positions and  
velocities of  
parcels  $i$  over  
time  $t$



# Fluid and Solid Parcels



Akinci et al.,  
*ACM SIGGRAPH*,  
2012.

# Parcel Movement for Fluids

Task



Governing equations

$$\frac{d\mathbf{v}_i^t}{dt} = \mathbf{a}_i^t = -\frac{1}{\rho_i^t} \nabla p_i^t + \nu \nabla^2 \mathbf{v}_i^t + \mathbf{g} \quad \frac{d\mathbf{x}_i^t}{dt} = \mathbf{v}_i^t$$
$$\frac{d\rho_i^t}{dt} = -\rho_i^t \nabla \cdot \mathbf{v}_i^t = 0$$

Numerics

$$\nabla p_i^t \approx \sum_j \frac{m_j}{\rho_j^t} p_j^t \nabla W_{ij}^t \quad \nabla^2 \mathbf{v}_i^t \approx \sum_j \dots$$
$$\mathbf{v}_i^{t+\Delta t} = \dots \quad \mathbf{x}_i^{t+\Delta t} = \dots$$



# Typical Steps of a Fluid Solver

- Neighbors  $j$  of  $i$
- Predicted velocity

$$\mathbf{v}_i^* = \mathbf{v}_i^t + \Delta t (\nu \nabla^2 \mathbf{v}_i^t + \mathbf{g})$$

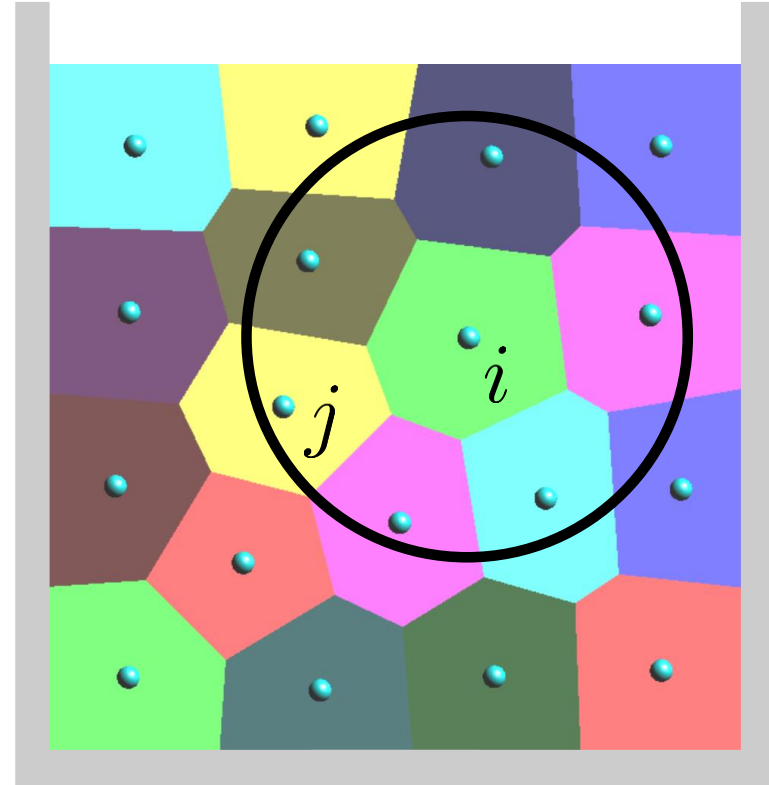
- Pressure

$$\nabla \cdot \mathbf{v}_i^* + \nabla \cdot \left( -\Delta t \frac{1}{\rho_i^t} \nabla p_i^t \right) = 0$$

- Velocity and position

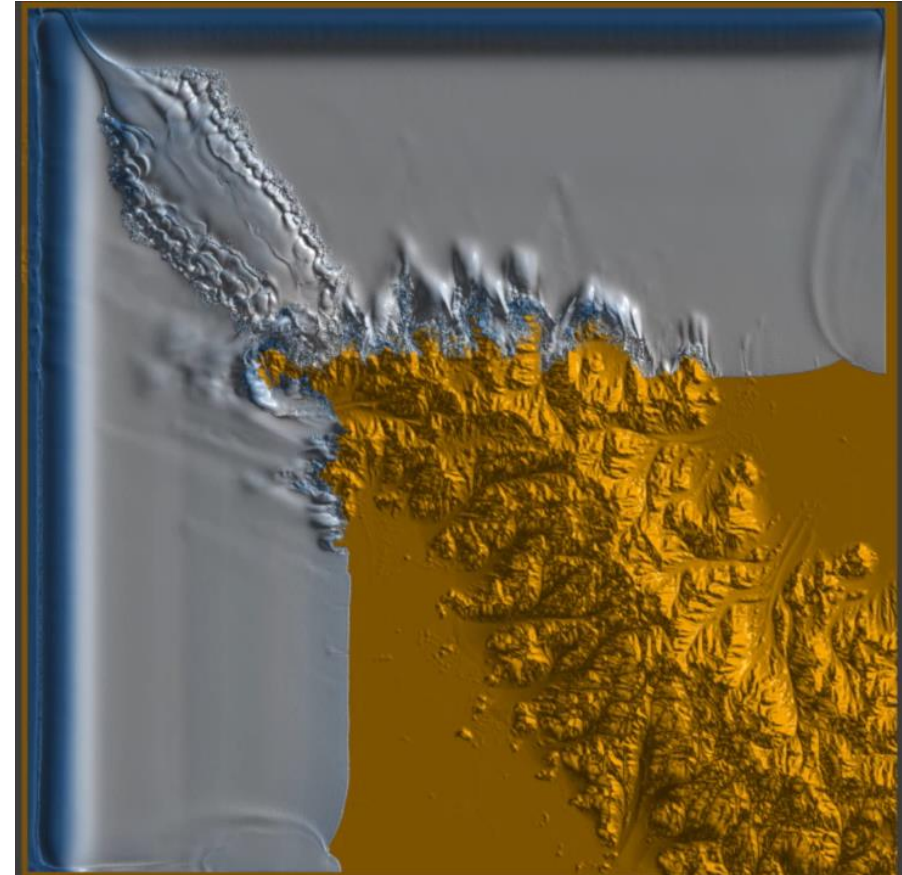
$$\mathbf{v}_i^{t+\Delta t} = \mathbf{v}_i^* - \Delta t \frac{1}{\rho_i^t} \nabla p_i^t$$

$$\mathbf{x}_i^{t+\Delta t} = \mathbf{x}_i^t + \Delta t \mathbf{v}_i^{t+\Delta t}$$



# Neighbor Search

- Huge numbers of neighbors have to be estimated
- Uniform grid
  - Sorted list
  - Compact hashing
  - 1 million samples: 20 ms
  - 1 billion samples: 30 s
- Minimized secondary data structures



Ihmsen et al.,  
*Computer Graphics Forum*, 2011.

# Pressure Computation

- Solving a pressure Poisson equation
  - Matrix-free
  - OpenMP, MPI
  - Up to 1 billion samples on desktop PCs

Ihmsen et al., *IEEE Transactions on Visualization and Graphics*, 2014.

$$\nabla \cdot \mathbf{v}_i^* + \nabla \cdot \left( -\Delta t \frac{1}{\rho_i^t} \nabla p_i^t \right) = 0$$

$\Downarrow$

$$\begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{pmatrix} \begin{pmatrix} p_1^t \\ p_2^t \\ \vdots \\ p_n^t \end{pmatrix} = \begin{pmatrix} s_1 \\ s_2 \\ \vdots \\ s_n \end{pmatrix}$$

# Applications



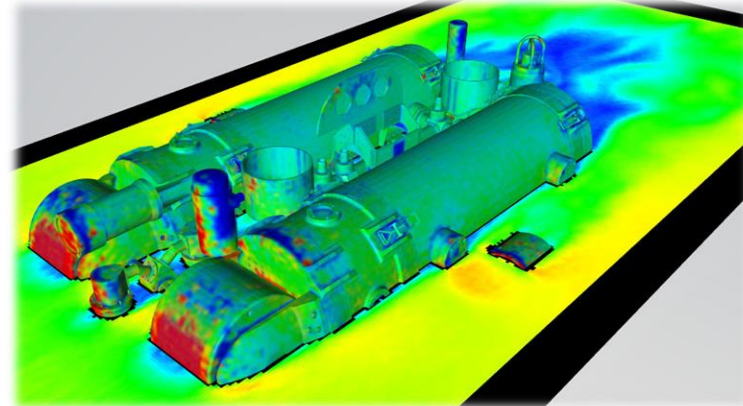
Pixar Animation Studios, Emeryville



FIFTY2 Technology, Freiburg



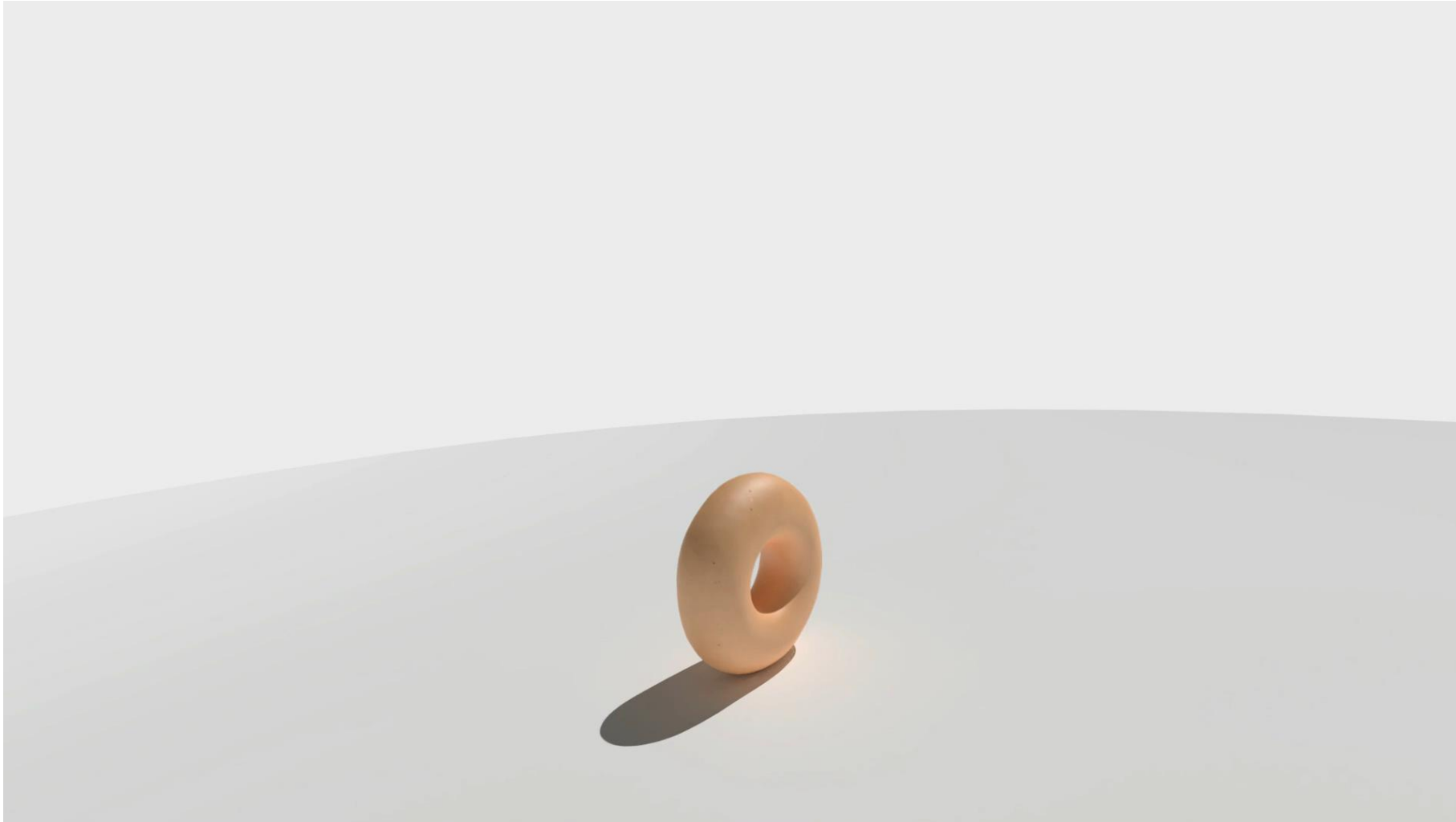
Studio Claudia Comte, Grancy / Berlin



Robotics Innovation Center DFKI, Bremen

# *Fluids Meet Art*

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Studio Claudia Comte  
Grancy / Berlin

Andreas Peer  
University of Freiburg

PreonLab  
FIFTY2 Technology

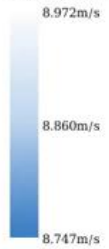


# Fluids in Engineering

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Time: 0.0100s

PreonSolver\_1: Velocity



PreonLab  
FIFTY2 Technology

FORD F-150

Water wading

# Outline

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- Organization
- Our research
- Image generation
- Course topics

# Setup Aspects

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- Light
- Scene
  - Light sources, sensor / eye / camera
  - Geometry, materials / reflection properties
  - Participating media, e.g. haze, fog
- Dynamics
  - Simulation of fluids, elastic and rigid solids

# Rendering Aspects

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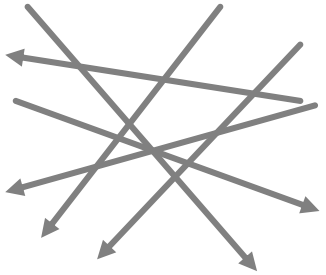
- What is visible by the sensor?
  - Rasterization
  - Ray Tracing
- Which color / intensity does it have?
  - Local evaluation of governing equations (Phong illumination model)
  - Global evaluation of governing equations for light interaction at surfaces (rendering equation) and in participating media (volume rendering equation)

# Light

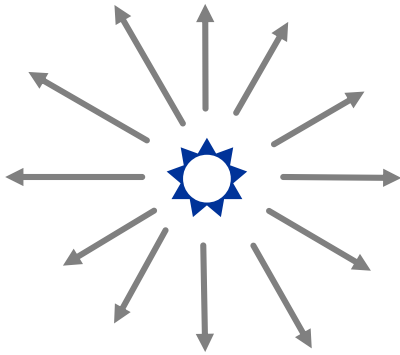
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- Modeled as energy parcels / photons that travel
  - Along geometric rays
  - At infinite speed
- Emitted by light sources
- Scattered / absorbed at surfaces
- Scattered / absorbed by participating media
- Absorbed / measured by sensors

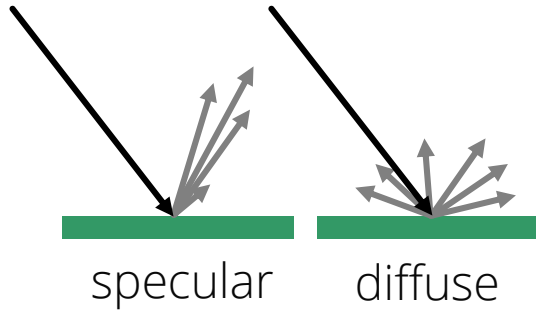
# Light



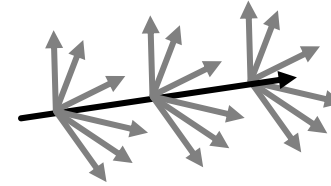
Light travels  
along rays



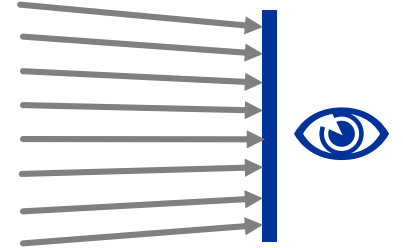
Light is  
generated  
at light  
sources



Incoming light  
is scattered  
and absorbed  
at surfaces



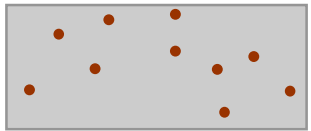
Participating  
media scatters  
and absorbs  
light



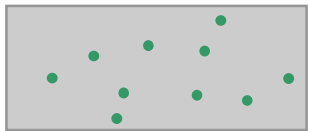
Sensors  
absorb  
light

# Color

- Photons are characterized by a wavelength within the visible spectrum
- Distribution of wavelengths  $\Rightarrow$  spectrum  $\Rightarrow$  color



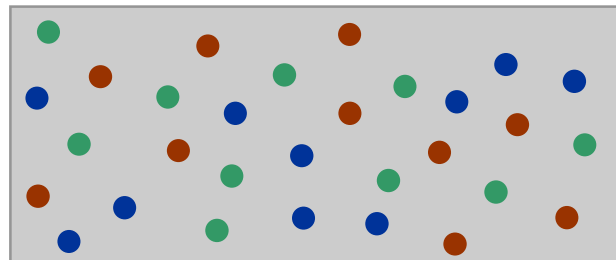
$\Phi_\lambda(\lambda_1)$



$\Phi_\lambda(\lambda_2)$



$\Phi_\lambda(\lambda_3)$



$$\Phi = \int_{\text{VisibleSpectrum}} \Phi_\lambda(\lambda) d\lambda$$

$$\approx \sum_i \Phi_\lambda(\lambda_i) \Delta\lambda_i$$

$$\approx \Phi_{\text{red}} \Delta\lambda + \Phi_{\text{green}} \Delta\lambda + \Phi_{\text{blue}} \Delta\lambda$$

$\Phi_\lambda(\lambda)$ : number of photons per time with a wavelength in a range  $\Delta\lambda_i$  around  $\lambda_i$ .



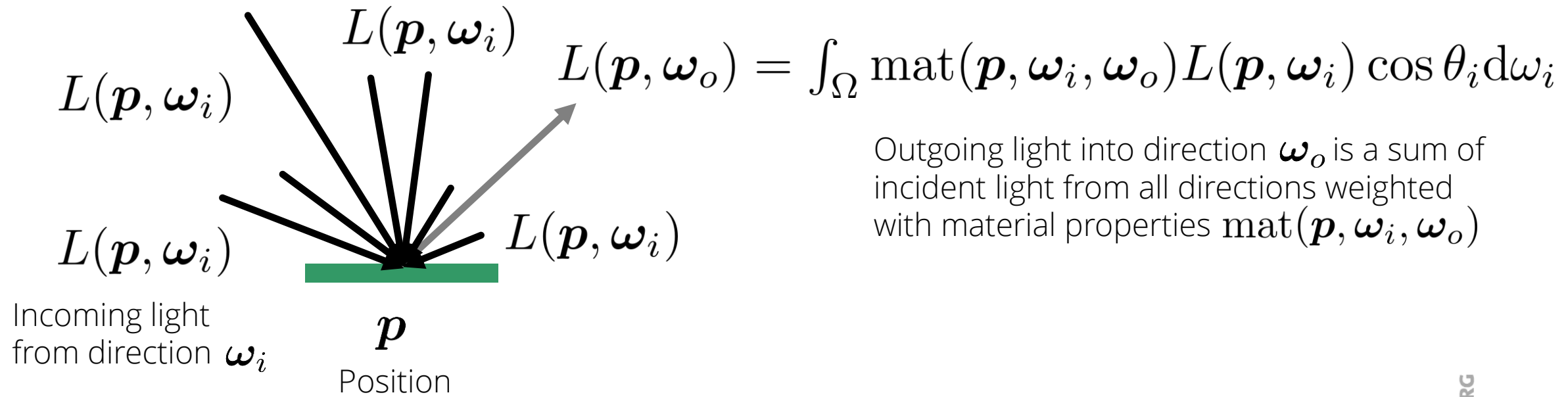
# *Governing Equations*

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- Light is affected by surfaces and by participating media
- Processes described by governing equations
  - Rendering equation
  - Volume rendering equation

# Light at Surfaces

- Governing equation for reflected light at surfaces into a particular direction given incident light from all directions



# Light in Volumes

- Governing equations for light changes along rays through participating media, e.g. haze or fog

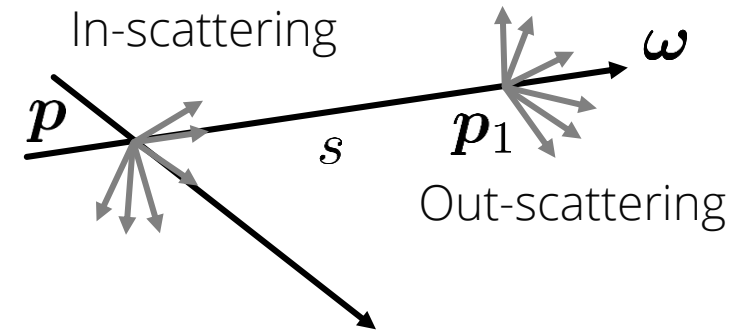
- Setting 
$$L(\mathbf{p}_1, \boldsymbol{\omega}) = L(\mathbf{p}, \boldsymbol{\omega}) + s \frac{dL}{ds}$$

- Absorption 
$$\frac{dL}{ds} = -\kappa L(\mathbf{p}, \boldsymbol{\omega})$$

- Emission 
$$\frac{dL}{ds} = L_e(\mathbf{p}, \boldsymbol{\omega})$$

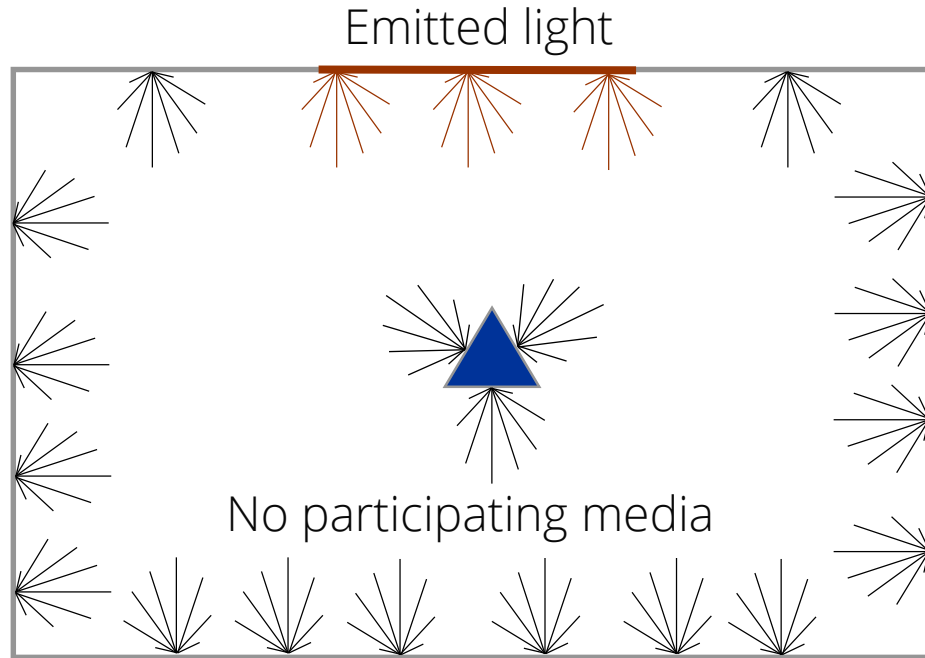
- Out-scattering 
$$\frac{dL}{ds} = -\sigma L(\mathbf{p}, \boldsymbol{\omega})$$

- In-scattering 
$$\frac{dL}{ds} = L_j(\mathbf{p}, \boldsymbol{\omega})$$

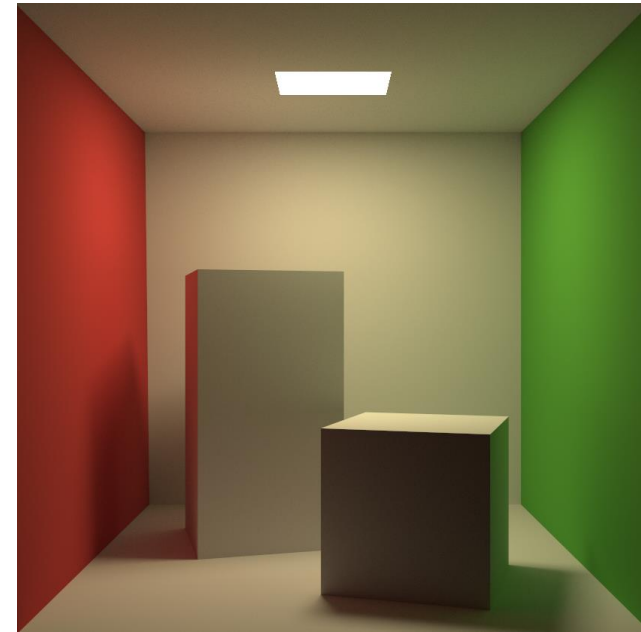


# Light Transport

- Governing equations enable the computation of light at all points in space into all direction



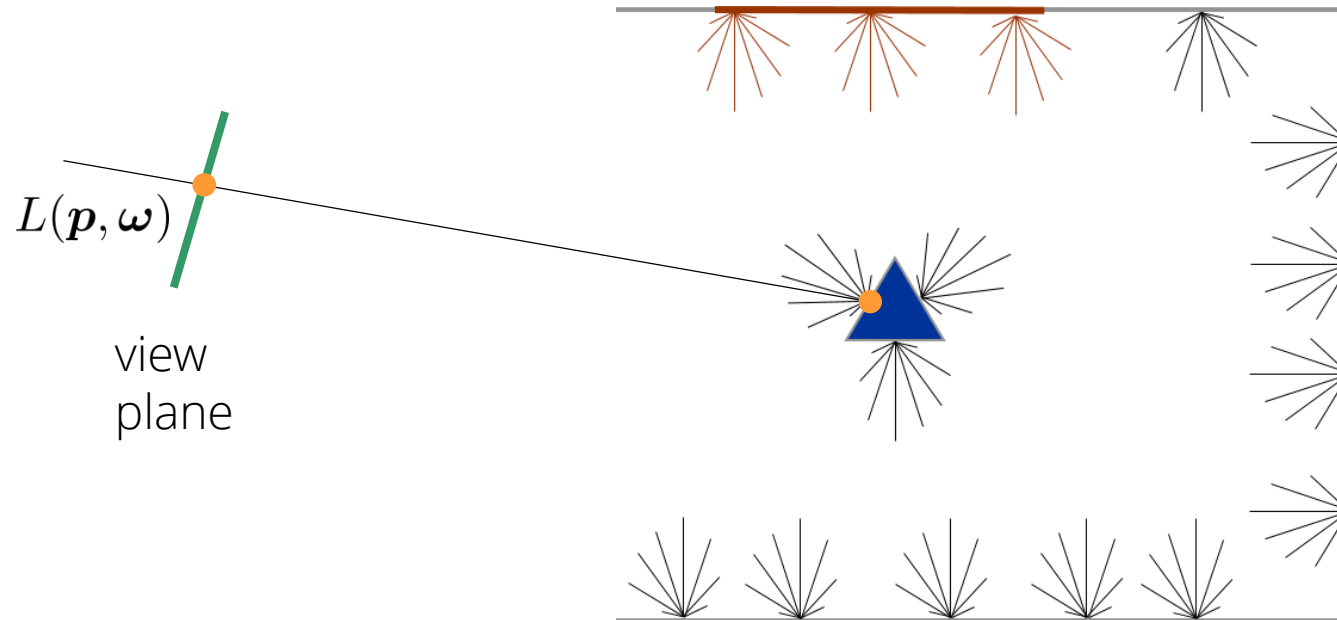
Reflected light due to material properties



Cornell box

# Rendering

- At an arbitrarily placed and oriented sensor
  - Cast rays into the scene
  - Lookup light that is transported along these rays





# Rendering Algorithms

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- Approximately solve the light transport in a scene
- Radiosity
  - Computes reflected light at all surface points into all directions
  - Simplifications: No participating media, diffuse surfaces, equal reflected light per finite-size surface patch, e.g. triangle
  - Linear system with unknown reflected light per surface patch

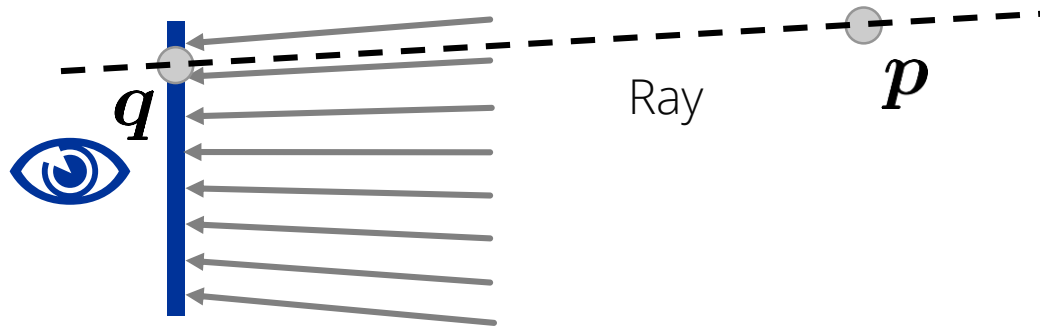
# Rendering Algorithms

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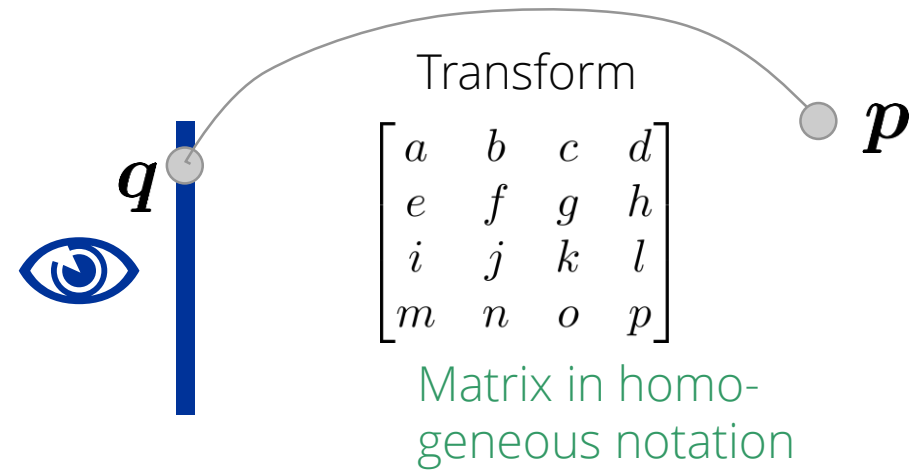
- Ray Tracing, Rasterization
  - Compute visible surfaces  
(What is visible by the sensor?)
  - Have to be combined with shading algorithms  
(Which color does it have?)
    - Phong illumination model
    - Monte-Carlo Ray Tracing

# Ray Tracing and Rasterization

- Solve the visibility problem



Ray Tracers compute ray-scene intersections to estimate  $q$  from  $p$ .



Rasterizers apply transformations to  $p$  in order to estimate  $q$ .  $p$  is projected onto the sensor plane.

# Shading

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- Solve  $L(\mathbf{p}, \omega_o) = \int_{\Omega} \text{mat}(\mathbf{p}, \omega_i, \omega_o) L(\mathbf{p}, \omega_i) \cos \theta_i d\omega_i$  at a surface point  $\mathbf{p}$  with, e.g., Monte-Carlo raytracing
  - Accumulate all illumination onto  $\mathbf{p}$  weighted with material properties  $\text{mat} \Rightarrow$  reflected light towards sensor point  $\mathbf{q}$
- Phong illumination model
  - Simplified setting
  - Considers light, sensor and normal direction and material properties

# *Challenges for Realistic Images*

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- Rendering
  - Computing the entire light transport
  - Understanding simplifications introduced by practical concepts
- Modeling
  - Detailed geometry and material properties
  - Properties of participating media
  - Realistic light sources
- Simulation



# Outline

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- Organization
- Our research
- Image generation
- Course topics

# Course Curriculum

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1. Introduction
  - Modeling, rendering, simulation
  - Concepts, challenges, applications
2. Visibility with Ray Tracing
3. Shading
4. Homogeneous coordinates
  - Prerequisite for projection
5. Visibility with projection

# Course Curriculum

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6. Rasterization
  - Concepts for vertex and fragment processing
7. Curves and surfaces
8. Particle fluids
9. Summary and outlook
  - Test exam
  - Radiosity, Monte Carlo ray tracing, simulation

# *Summary*

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