EXERCISE - 5.3

APPLICATIONS OF NORMAL DISTRIBUTION

- 1. The heights of boys at particular age follows a normal distribution with mean 150.3 cm and variance 25 cm. Find the probability that a boy picked at random from this age group
 - a. less than 153 cm,
 - **b.** more than 158 cm
 - c. between 150 cm and 158 cm.

(*Ans* : 0.7054, 0.0618, 0.4621)

- 2. The masses of packages from a particular machine are normally distributed with a mean of 200 g and a standard deviation of 2 g. Find the probability that a randomly selected package from the machine weighs
 - a. less than 197 g,
 - **b.** more than 200.6 g
 - **c.** between 198.5 g and 199.5 g

(*Ans* : 0.0668, 0.4013, 0.1747)

- **3.** The average number of calories in a 1.5-ounce chocolate bar is 225. Suppose that the distribution of calories is approximately normal with s 10. Find the probability that a randomly selected chocolate bar will have
 - **a.** Less than 200 calories
 - **b.** more than 215 calories
 - c. Between 200 and 220 calories

(Ans: 0.0062, 0.3023)

- **4.** The average credit card debt for college seniors is \$3262. If the debt is normally distributed with a standard deviation of \$1100, find these probabilities.
 - **a.** That the senior owes at least \$1000
 - **b.** That the senior owes more than \$4000
 - c. That the senior owes between \$3000 and \$4000

(*Ans*: 0.9803, 0.2514, 0.3434)

- 5. The average monthly mortgage payment including principal and interest is \$982 in the United States. If the standard deviation is approximately \$180 and the mortgage payments are approximately normally distributed, find the probability that a randomly selected monthly payment is
 - **a.** More than \$1000
 - **b.** More than \$1475
 - **c.** Between \$800 and \$1150

(*Ans* : 0.4602, 0.0031, 0.6676)

- **6.** According to the Federal Highway Administration's 2003 highway statistics the distribution of ages for licensed drivers has a mean of 44.5 years and a standard deviation of 17.1 years. Assuming the distribution of ages is normally distributed, what percentage of the drivers are:
 - **a.** Younger than 25 years of age
 - **b.** Older than 21 years of age
 - **c.** Between the ages of 45 and 65

(*Ans*: 0.1271, 0.9153, 0.373)

- **7.** According to the American College Test (ACT), results from the 2004 ACT testing found that students had a mean reading score of 21.3 with a standard deviation of 6.0. Assuming that the scores are normally distributed:
 - **a.** Find the probability that a randomly selected student has a reading ACT score less than 20.
 - **b.** Find the probability that a randomly selected student has a reading ACT score between 18 and 24.
 - **c.** Find the probability that a randomly selected student has a reading ACT score greater than 30

(*Ans*: 0.4142, 0.3825, 0.0735)

- **8.** In a survey of South African CEOs, the annual incomes were normally distributed, with a mean of \$7.14 million and a standard deviation of \$0.5 million. Find the probability that a randomly selected CEO has an annual income that is
 - a. less than \$6.5 million,
 - **b.** more than 8 million.
 - **c.** between \$7 million and \$7.5 million.

(*Ans*: 0.1003, 0.0427, 0.3745)

- **9.** In a recent year, the MCAT scores for the critical analysis and reasoning skills portion of the test were normally distributed, with a mean of 124.9 and a standard deviation of 3.0. Find the probability that a randomly selected medical student who took the MCAT has a critical analysis and reasoning skills score that is
 - **a.** less than 120,
 - **b.** more than 130.
 - **c.** between 122 and 128

(*Ans*: 0.0512, 0.0446, 0.6824)

- **10.** The ages of prime ministers of Sri Lanka, when they were first sworn to office, are normally distributed with a mean of 58.21 years and a standard deviation of 11.56 years. Find the probability that the age of a randomly selected prime minister of Sri Lanka when he was sworn to office was
 - **a.** less than 50 years,
 - **b.** more than 70 years.
 - **c.** between 55 and 60 years.

(*Ans*: 0.2388, 0.1539, 0.1709)