L0(1)

October 22, 2020

1

$$Recall = \frac{TP}{TP + FN} = \frac{C(F_s F_r)}{C(F_s F_r) + C(L_s F_r)}$$

$$Precision = \frac{TP}{TP + FP * q} = \frac{C(F_s F_r)}{C(F_s F_r) + C(F_s L_r) * q}$$

()

```
[466]: import matplotlib.pyplot as plt import random import csv
```

,

```
[468]: data = data_mining('
                                .csv')
                    =',len(data))
[469]: print('
              = 29304
[470]: def recall_precision(data,cut_off=0.5,q=10):
               answer= [['TPR(recall)','precision','FPR']]
               for i in range(1,6):
                   TP = 0
                   FN = 0
                   TN = 0
                   FP = 0
                   for j in range(1,len(data)):
                        if (float(data[j][i])>=cut_off) and (str(data[j][6])=='F'):
                            TP+=1
                        elif (float(data[j][i])>=cut_off) and (str(data[j][6])=='G'):
                        elif (float(data[j][i]) < cut_off) and (str(data[j][6]) == 'G'):</pre>
                        elif (float(data[j][i]) < cut_off) and (str(data[j][6]) == 'F'):</pre>
                            FN+=1
                   try:
                        recall=TP/(TP+FN)
                   except ZeroDivisionError:
                        recall='0'
                   try:
                       precision=TP/(TP+FP*q)
                   except ZeroDivisionError:
                        precision='0'
                   try:
                       FPR=FP/(FP+TN)
                   except ZeroDivisionError:
                   answer.append([recall,precision,FPR])
               return answer
```

```
[477]: answer_d={}
  cut_off_mass = [i/100 for i in range(1,100)]
  for cut_off in cut_off_mass:
     answer_d[cut_off]=recall_precision(data,cut_off,q=10)
```

```
[478]: | for cut_off in [0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,0.95,0.99]:
           print('cut_off=',cut_off,'\n',answer_d[cut_off],'\n')
      cut off= 0.1
       [['TPR(recall)', 'precision', 'FPR'], [0.9791623470868754, 0.05749505402526252,
      0.8096532970768185], [1.0, 0.0480196738286306, 1.0], [0.9781256479369687,
      0.05705560426934357, 0.8154055326047168], [1.0, 0.0480196738286306, 1.0],
      [0.9810284055567075, 0.056132587508823543, 0.832087015635622]]
      cut_off= 0.2
       [['TPR(recall)', 'precision', 'FPR'], [0.8959154053493676, 0.05967737480319311,
      0.7120744653035611], [0.9831018038565208, 0.05624455080870447,
      0.832087015635622], [0.9569769852788721, 0.06560720961471489,
      0.6874967316843591], [1.0, 0.04802445533118254, 0.9998954138994928],
      [0.9634045200082936, 0.0621967298695562, 0.7327302201537416]]
      cut off= 0.3
       [['TPR(recall)', 'precision', 'FPR'], [0.7490151358075886, 0.05964419862137285,
      0.5956701354390002], [0.9197594857972217, 0.0654074696627888,
      0.6629189980651572], [0.9362430022807381, 0.07625537232650235,
      0.5720859697746169], [0.9478540327596932, 0.06592733067499261,
      0.6774041729854102], [0.9478540327596932, 0.06592733067499261,
      0.6774041729854102]]
      cut_off= 0.4
       [['TPR(recall)', 'precision', 'FPR'], [0.5844909807173958, 0.06205970412116943,
      0.445589081211107], [0.8557951482479784, 0.07109943585547565,
      0.5639805469853056], [0.9002695417789758, 0.09108071824131565,
      0.4531715734978821], [0.8178519593613933, 0.0786548220819749,
      0.4832400773937144], [0.9172714078374455, 0.07184267363874047,
      0.597761857449145]]
      cut off= 0.5
       [['TPR(recall)', 'precision', 'FPR'], [0.2737922454903587, 0.03400677302635815,
      0.39230246300266697], [0.7220609579100146, 0.07834205050334626,
      0.4284892537781729], [0.8440804478540328, 0.11899681389026921,
      0.31522250692882914], [0.5566037735849056, 0.07542955085067225,
      0.34414056371908175], [0.8680281982168775, 0.07673696076544499,
      0.5268001882549809]]
      cut_off= 0.6
       [['TPR(recall)', 'precision', 'FPR'], [0.262699564586357, 0.03709885219020848,
      0.34393139151806723], [0.6425461331121709, 0.07631313255682239,
      0.39230246300266697], [0.7660170018660585, 1.0, 0.0], [0.04281567489114659,
      0.05725772910023569, 0.03555927417246248], [0.8178519593613933,
      0.0786626648984435, 0.48318778434346077]]
```

```
cut off= 0.7
       [['TPR(recall)', 'precision', 'FPR'], [0.0011403690648973668,
      0.18032786885245902, 0.0002614652512681065], [0.5578478125647937,
      0.07562788998046409, 0.34393139151806723], [0.6660792038150529, 1.0, 0.0],
      [0.04271200497615592, 0.05720633157456262, 0.03550698112220886],
      [0.7133526850507983, 0.07766278032979312, 0.4273388066725932]]
      cut_off= 0.8
       [['TPR(recall)', 'precision', 'FPR'], [0.0, '0', 0.0], [0.0025917478747667427,
      0.3333333333333333, 0.0002614652512681065], [0.5757827078581795, 1.0, 0.0],
      [0.04250466514617458, 0.0569444444444444, 0.03550698112220886],
      [0.6376736471076093, 0.07577829520395216, 0.39230246300266697]]
      cut off= 0.9
       [['TPR(recall)', 'precision', 'FPR'], [0.0, '0', 0.0], [0.0, '0', 0.0],
      [0.29421521874352063, 1.0, 0.0], [0.04250466514617458, 0.057103064066852366,
      0.035402395021701616], [0.5562927638399336, 0.07543297345928925,
      0.34393139151806723]]
      cut off= 0.95
       [['TPR(recall)', 'precision', 'FPR'], [0.0, '0', 0.0], [0.0, '0', 0.0], [0.0,
       '0', 0.0], [0.04105328633630521, 0.05852793378657996, 0.03331067301155676],
      [0.4713871034625752, 0.0749007527962179, 0.29367777022433716]]
      cut_off= 0.99
       [['TPR(recall)', 'precision', 'FPR'], [0.0, '0', 0.0], [0.0, '0', 0.0], [0.0,
      '0', 0.0], [0.016794526228488493, 0.07706945765937202, 0.010144851749202531],
      [0.295355587808418, 0.09169912131063118, 0.14757098781571928]]
      #
            2
                              Recall = \frac{TP}{TP + FN} = \frac{S(F_s F_r)}{S(F_s F_r) + S(L_s F_r)}
                          Precision = \frac{TP}{TP + FP * a} = \frac{S(F_s F_r)}{S(F_s F_r) + S(F_s I_r) * a}
        S()-
[479]: def recall_precision_money(data,cut_off=0.5,q=10):
```

answer=[['TPR(recall_m)','precision_m','FPT_m']]

for i in range(1,6):
 TP = 0
 FN = 0
 TN = 0
 FP = 0

```
for j in range(1,len(data)):
                if data[j][0] != '':
                    sum = float(data[j][0])
                if (float(data[j][i])>=cut_off) and (str(data[j][6])=='F'):
                elif (float(data[j][i])>=cut_off) and (str(data[j][6])=='G'):
                    FP+=sum
                elif (not(float(data[j][i])>=cut_off)) and_u
\hookrightarrow (str(data[j][6])=='G'):
                elif (not(float(data[j][i])>=cut_off)) and_u
\hookrightarrow (str(data[j][6])=='F'):
                    FN+=sum
           try:
                recall=TP/(TP+FN)
           except ZeroDivisionError:
                recall='0'
           try:
                precision=TP/(TP+FP*q)
           except ZeroDivisionError:
                precision='0'
           try:
                FPR=FP/(FP+TN)
           except ZeroDivisionError:
                FPR='0'
           answer.append([recall,precision,FPR])
       return answer
```

```
[480]: answer_m_d= {}
    cut_off_mass_m = [i/100 for i in range(1,100)]
    for cut_off in cut_off_mass_m:
        answer_m_d[cut_off] = recall_precision_money(data,cut_off,q=10)

[481]: for cut_off in [0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,0.95,0.99]:
        print('cut_off=',cut_off,'\n',answer_m_d[cut_off],'\n')

cut_off= 0.1
    [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.9611527195431848,
    0.0517687399162424, 0.7568764547592146], [1.0, 0.041219717940729914, 1.0],
    [0.9606739435808853, 0.05089141572953319, 0.7702528290603144], [1.0,
    0.041219717940729914, 1.0], [0.9638613317244922, 0.0483850722323333175,
    0.8149863439192119]]

cut_off= 0.2
```

```
[['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.81678517285839,
0.06041458963137132, 0.5461201512219054], [0.9656096581162038,
0.04846858300111809, 0.8149863439192119], [0.9238082226019778,
0.06695580078097256, 0.5534542846049282], [1.0, 0.041220055811897124,
0.9999914508396527], [0.9302527728191226, 0.06213056802034052,
0.6037038589862197]]
cut off= 0.3
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.6189048533047601,
0.05964233841460968, 0.4195156963721876], [0.8516494433240163,
0.0648191696490183, 0.5282492890893146], [0.8749234169356489,
0.08348051857226926, 0.4129643145696993], [0.8916700362364741,
0.07034261582601017, 0.5066342002374059, [0.8916700362364741,
0.07034261582601017, 0.5066342002374059]]
cut_off= 0.4
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.34471347110995054,
0.05187538762728368, 0.27086210111327846], [0.7598642724511975,
0.07666833017248294, 0.3934265589358551, [0.7919630260554712,
0.10285594827974293, 0.29697753463835047], [0.6903488899476272,
0.09138489486672956, 0.29509380238843735], [0.8407028104446791,
0.08110716642605337, 0.4094812839858981]]
cut_off= 0.5
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.1348273674362985,
0.02403058062238027, 0.23541597068415349], [0.5465374534411631,
0.08320895524603808, 0.2588845565861145], [0.717569574592336,
0.14478836285667895, 0.1822174153515674], [0.312259479151668,
0.06253526150189806, 0.20124797715517181], [0.745196034918961,
0.08780303385911312, 0.3328400344648049]]
cut_off= 0.6
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.11307674671142583,
0.023596050277863323, 0.20116361963201562], [0.434196753188775,
0.07346780833548236, 0.23541597068415349], [0.6084096745609308, 1.0, 0.0],
[0.03787087552239329, 0.035698721221001234, 0.0439796076495234],
[0.6903488899476272, 0.0913868193621236, 0.2950869630601596]]
cut_off= 0.7
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.0018586225324483995,
0.24380738731218699, 0.0002478350289716023], [0.31318994719993015,
0.06273456555005226, 0.20116361963201562, [0.4490645715358533, 1.0, 0.0],
[0.037858944194215455, 0.03569657442302823, 0.04396849374107192],
[0.5262536972468168, 0.08070921920869327, 0.25769787696192775]]
cut off= 0.8
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.0, '0', 0.0],
[0.011966000378888007, 0.6748746307900155, 0.0002478350289716023],
```

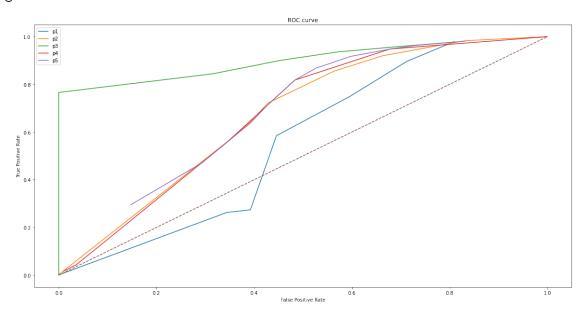
```
[0.34316834999218326, 1.0, 0.0], [0.03783766665896499, 0.03567722795078604,
0.04396849374107192], [0.4204670946216958, 0.07131035777768041,
0.23541597068415349]]
cut off= 0.9
 [['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.0, '0', 0.0], [0.0, '0', 0.0],
[0.13999321541806564, 1.0, 0.0], [0.03783766665896499, 0.03572926360440266,
0.04390208945464508], [0.31222627028823974, 0.06255360788775319,
0.20116361963201562]]
cut_off= 0.95
 [['TPR(recall m)', 'precision m', 'FPT m'], [0.0, '0', 0.0], [0.0, '0', 0.0],
[0.0, '0', 0.0], [0.035015859779824444, 0.03528871987344086,
0.04115401093319049], [0.24647270069535948, 0.061620736996022635,
0.16136385444766513]]
cut_off= 0.99
[['TPR(recall_m)', 'precision_m', 'FPT_m'], [0.0, '0', 0.0], [0.0, '0', 0.0],
[0.0, '0', 0.0], [0.010699098823644799, 0.03276641468416771,
0.013577992535037667], [0.14091886376653923, 0.06613375958093261,
0.08554931138239481]]
```

3

0.1 ROC 1

```
[482]: FPR=[[]for i in range(5)]
      TPR=[[]for i in range(5)]
      for i in range(1,6):
          for cut off in [0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,0.95,0.99]:
              FPR[i-1].append(float(answer_d[cut_off][i][2]))
               TPR[i-1].append(float(answer_d[cut_off][i][0]))
      plt.gcf().clear()
      plt.figure(figsize=(20,10))
      plt.title('ROC curve')
      plt.plot(FPR[0], TPR[0], label='p1')
      plt.plot(FPR[1], TPR[1], label='p2')
      plt.plot(FPR[2], TPR[2], label='p3')
      plt.plot(FPR[3], TPR[3], label='p4')
      plt.plot(FPR[4], TPR[4], label='p5')
      plt.plot([0, 1], [0, 1], '--')
      plt.ylabel('True Positive Rate')
      plt.xlabel('False Positive Rate')
      plt.legend()
      plt.show()
```

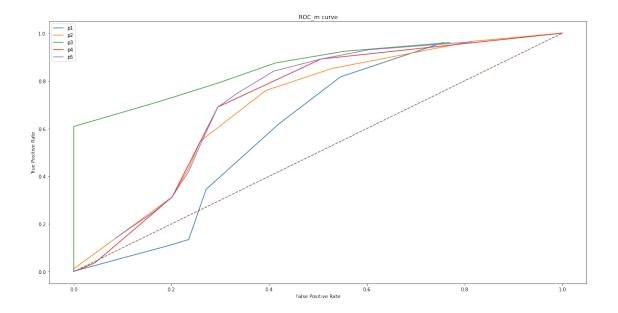
<Figure size 432x288 with 0 Axes>



$0.2 \quad ROC_m \quad 2$

```
[483]: FPR_m=[[]for i in range(5)]
       TPR_m=[[]for i in range(5)]
       for i in range(1,6):
           for cut_off in [0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,0.95,0.99]:
               FPR_m[i-1].append(float(answer_m_d[cut_off][i][2]))
               TPR_m[i-1].append(float(answer_m_d[cut_off][i][0]))
       plt.gcf().clear()
       plt.figure(figsize=(20,10))
       plt.title('ROC_m curve')
       plt.plot(FPR_m[0], TPR_m[0], label='p1')
      plt.plot(FPR_m[1], TPR_m[1], label='p2')
       plt.plot(FPR_m[2], TPR_m[2], label='p3')
       plt.plot(FPR_m[3], TPR_m[3], label='p4')
       plt.plot(FPR_m[4], TPR_m[4], label='p5')
       plt.plot([0, 1], [0, 1], '--')
       plt.ylabel('True Positive Rate')
       plt.xlabel('False Positive Rate')
       plt.legend()
       plt.show()
```

<Figure size 432x288 with 0 Axes>

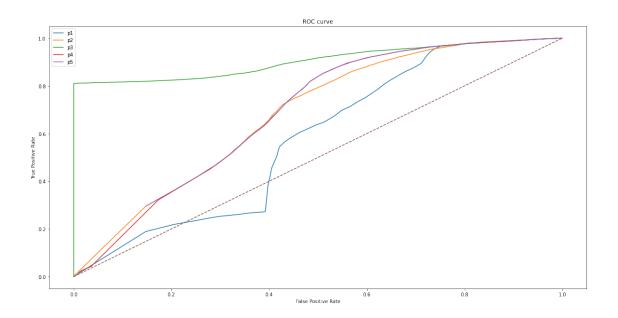


4

0.3 ROC 1

```
[484]: FPR=[[]for i in range(5)]
       TPR=[[]for i in range(5)]
       cut_off_mass = [i/100 for i in range(1,100)]
       for i in range(1,6):
           for cut_off in cut_off_mass:
               FPR[i-1].append(float(answer_d[cut_off][i][2]))
               TPR[i-1].append(float(answer_d[cut_off][i][0]))
       plt.gcf().clear()
       plt.figure(figsize=(20,10))
       plt.title('ROC curve')
       plt.plot(FPR[0], TPR[0], label='p1')
       plt.plot(FPR[1], TPR[1], label='p2')
       plt.plot(FPR[2], TPR[2], label='p3')
      plt.plot(FPR[3], TPR[3], label='p4')
       plt.plot(FPR[4], TPR[4], label='p5')
       plt.plot([0, 1], [0, 1], '--')
       plt.ylabel('True Positive Rate')
       plt.xlabel('False Positive Rate')
       plt.legend()
       plt.show()
```

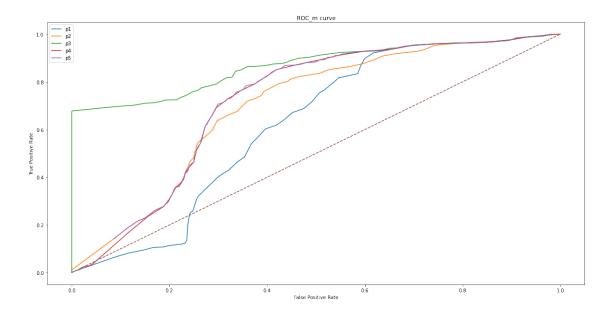
<Figure size 432x288 with 0 Axes>



$0.4 \quad ROC_m \quad 2$

```
[485]: FPR_m=[[]for i in range(5)]
       TPR_m=[[]for i in range(5)]
       cut_off_mass_m = [i/100 for i in range(1,100)]
       for i in range(1,6):
           for cut_off in cut_off_mass_m:
               FPR_m[i-1].append(float(answer_m_d[cut_off][i][2]))
               TPR_m[i-1].append(float(answer_m_d[cut_off][i][0]))
       plt.gcf().clear()
       plt.figure(figsize=(20,10))
       plt.title('ROC_m curve')
       plt.plot(FPR_m[0], TPR_m[0], label='p1')
       plt.plot(FPR_m[1], TPR_m[1], label='p2')
      plt.plot(FPR_m[2], TPR_m[2], label='p3')
       plt.plot(FPR_m[3], TPR_m[3], label='p4')
      plt.plot(FPR_m[4], TPR_m[4], label='p5')
       plt.plot([0, 1], [0, 1], '--')
       plt.ylabel('True Positive Rate')
       plt.xlabel('False Positive Rate')
       plt.legend()
       plt.show()
```

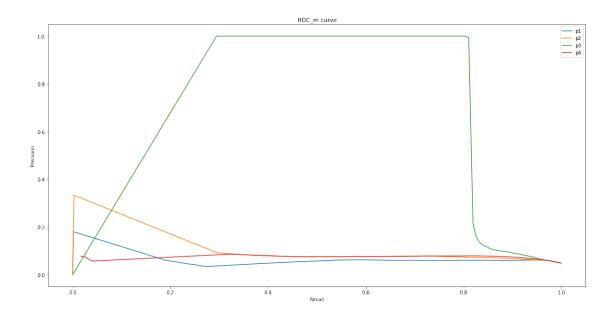
<Figure size 432x288 with 0 Axes>



5 ##Precision-recall

```
[486]: recall=[[]for i in range(5)]
       precs=[[]for i in range(5)]
       cut_off_mass = [i/100 for i in range(1,100)]
       for i in range(1,6):
           for cut_off in cut_off_mass_m:
               recall[i-1].append(float(answer_d[cut_off][i][0]))
               precs[i-1].append(float(answer_d[cut_off][i][1]))
       plt.gcf().clear()
       plt.figure(figsize=(20,10))
       plt.title('ROC_m curve')
       plt.plot(recall[0], precs[0], label='p1')
       plt.plot(recall[1], precs[1], label='p2')
       plt.plot(recall[2], precs[2], label='p3')
       plt.plot(recall[3], precs[3], label='p4')
       plt.ylabel('Precision')
       plt.xlabel('Recall')
       plt.legend()
       plt.show()
```

<Figure size 432x288 with 0 Axes>



```
6
      #
[487]:
                   5
          File "<ipython-input-487-d7631523e207>", line 1
       SyntaxError: invalid syntax
[488]: with open('data.csv', 'w') as file:
           writer = csv.writer(file,delimiter=';',lineterminator='\n')
           writer.writerows(data)
       cut_off_mass = [i/100 for i in range(1,100)]
       with open('answer_d.csv', 'w') as file:
           writer = csv.writer(file,delimiter=';',lineterminator='\n')
           for cut_off in cut_off_mass:
               tmp = [[cut_off]]
               writer.writerows(tmp)
               writer.writerows(answer_d[cut_off])
       with open('ROC.csv', 'w') as file:
           writer = csv.writer(file,delimiter=';',lineterminator='\n')
           writer.writerows([['X_FPR']])
           writer.writerows(FPR)
           writer.writerows([['Y_TPR']])
```

```
writer.writerows(TPR)

with open('ROC_M.csv', 'w') as file:
    writer = csv.writer(file,delimiter=';',lineterminator='\n')
    writer.writerows([['X_FPR_M']])
    writer.writerows(FPR_m)
    writer.writerows([['Y_TPR_M']])
    writer.writerows(TPR_m)

with open('Precision-recall', 'w') as file:
    writer = csv.writer(file,delimiter=';',lineterminator='\n')
    writer.writerows([['X_recall']])
    writer.writerows(recall)
    writer.writerows([['Y_precision']])
    writer.writerows(precs)
```

7

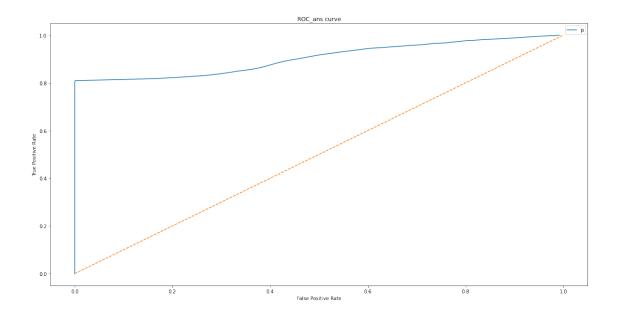
$$p = \frac{A * p1 + B * p2 + C * p3}{A + B + C}$$

```
[489]: data_ans = [['AMOUNT', 'p_fraud', 'CLASS']]
a = 0
b = 0.01
c = 0.99
for i in range(1,len(data)):
    p = (a*float(data[i][1])+b*float(data[i][2])+c*float(data[i][3]))/(a+b+c)
    data_ans.append([data[i][0],p,data[i][6]])
```

```
except ZeroDivisionError:
                       recall='0'
                   try:
                       precision=TP/(TP+FP*q)
                   except ZeroDivisionError:
                       precision='0'
                   try:
                       FPR=FP/(FP+TN)
                   except ZeroDivisionError:
                       FPR='0'
                   answer.append([recall,precision,FPR])
               return answer
[491]: answer ans={}
       cut off mass = [i/100 \text{ for } i \text{ in } range(1,100)]
       for cut_off in cut_off_mass:
           answer_ans[cut_off] = recall_precision_ans(data_ans,cut_off,q=10)
[492]: for cut_off in [0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,0.95,0.99]:
           print('cut_off=',cut_off,'\n',answer_ans[cut_off],'\n')
      cut_off= 0.1
       [['TPR(recall) ans', 'precision ans', 'FPR ans'], [0.9782293178519593,
      0.05696485275829178, 0.8168697380118183]]
      cut_off= 0.2
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.9573916649388348,
      0.06551271592239208, 0.6888563509909533]]
      cut off= 0.3
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.9367613518556914,
      0.07615291262135922, 0.5732364168801967]]
      cut off= 0.4
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.899232842629069,
      0.0910904813912459, 0.4525963499450923]]
      cut_off= 0.5
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.8431474186191167,
      0.11865544256889836, 0.31590231658212625]]
      cut_off= 0.6
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.7629069044163383, 1.0,
      0.0]]
```

```
cut_off= 0.7
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.6635911258552768, 1.0,
      0.0]]
      cut_off= 0.8
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.5745386688782915, 1.0,
      0.0]]
      cut off= 0.9
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.18401409910843874, 1.0,
      0.0]]
      cut_off= 0.95
       [['TPR(recall) ans', 'precision ans', 'FPR ans'], [0.0, '0', 0.0]]
      cut_off= 0.99
       [['TPR(recall)_ans', 'precision_ans', 'FPR_ans'], [0.0, '0', 0.0]]
[493]: FPR_ans=[]
       TPR_ans=[]
       cut_off_mas = [i/100 for i in range(1,100)]
       for i in [1]:
           for cut_off in cut_off_mass:
               FPR_ans.append(float(answer_ans[cut_off][i][2]))
               TPR_ans.append(float(answer_ans[cut_off][i][0]))
       plt.gcf().clear()
       plt.figure(figsize=(20,10))
       plt.title('ROC_ans curve')
       plt.plot(FPR_ans, TPR_ans, label='p')
       plt.plot([0, 1], [0, 1], '--')
      plt.ylabel('True Positive Rate')
       plt.xlabel('False Positive Rate')
       plt.legend()
      plt.show()
```

<Figure size 432x288 with 0 Axes>



$$G = 2AUC - 1$$

```
[494]: G = 0
AUC = 0
for i in range(0,len(cut_off_mass)-1):
    AUC += abs(FPR_ans[i]-FPR_ans[i+1])*(TPR_ans[i]+ TPR_ans[i+1])/2
G = 2*AUC-1
print('AUC=',AUC)
print('G=',G)
```

```
AUC= 0.8956699625022073
G= 0.7913399250044146
```