

1	2	3	4	Σ (7)

Assignment 5

(Handed in 16. November 2015)

Theoretical Assignment - *Comparison with at most l mismatches*

General we are now only looking at the worst case scenario, which means uniform distributed mismatches in an alignment. Also we only look at $k \geq 1$, as $k = 0$ is in our application not a useful result. Assume two sequences of length t with l mismatches.

Then both sequences contain l tuples of length $\lfloor \frac{t}{l+1} \rfloor$ and one tuple which has a length of maximal $\lfloor \frac{t}{l+1} \rfloor$. Where $k = \lfloor \frac{t}{l+1} \rfloor$ is the maximal tuple length, possible in sequences.

So both sequences share $l + 1$ k -tuples and for each $k \leq \lfloor \frac{t}{l+1} \rfloor$ they share $(l + 1) * \lfloor \frac{\lfloor \frac{t}{l+1} \rfloor}{k} \rfloor$ k -tuples.

Theoretical Assignment - *Linear programming by hand*

The feasible region of this linear program is shown in figure 1, where the red line is constraint 1, green line is constraint 2, constraint 3 is drawn as a blue line and the yellow line is constraint 4.

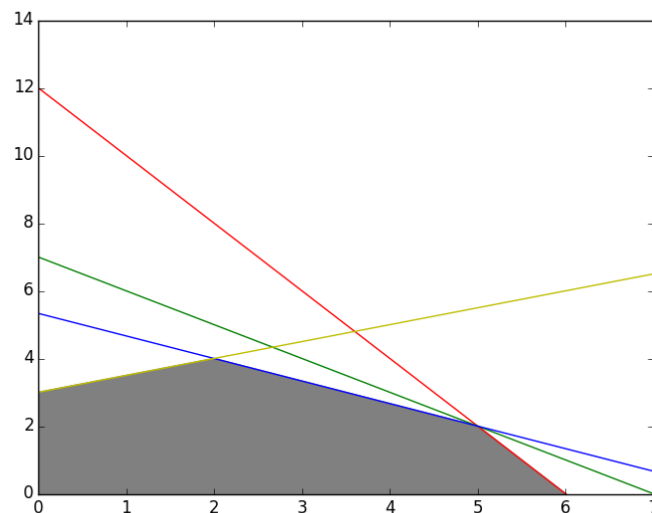


Figure 1: feasible region of linear program (grey area)

solution if $t=s=1$

The constraint for the algorithm are as following if t and s value is 1 now:

$$max : 1 * x_1 + 1 * x_2 \quad (1)$$

$$2 * x_1 + x_2 \leq 12 \quad (2)$$

$$2 * x_1 + 3 * x_2 \leq 7 \quad (3)$$

$$-1 * x_1 + 2 * x_2 \leq 16 \quad (4)$$

$$x_1, x_2 \geq 0 \quad (5)$$

In the next step we started to compute each line of the tuple. Starting with constraint 3. All possible tuples respectively to constraint 3 from the assignment are:

$$temp1 = \{(0, 7); (1, 6); (2, 5); (3, 4); (4, 3); (5, 2); (6, 1); (7, 0)\}$$

Next the constraint 2 was applied to temp1:

$$temp2 = \{(0, 7); (1, 6); (2, 5); (3, 4); (4, 3); (5, 2); \}$$

Again the next constraint (constraint 4) was applied:

$$temp3 = \{(5, 2)\}$$

The constraint (4) is checked and the remaining tuple from the last step is valid:

$$temp4 = \{(5, 2)\}$$

Last but not least the last constraint is tested (constraint 5)) and the result is: $r = \{(5, 2)\}$

So the final result for the Algorithm with $s=t=1$ is the Dupel: (5,2).

How to make unsolveable?

To get a not solveable algorithm for example the following constraint could be added:

$$x_1 + x_2 \geq 7 \quad (6)$$

How to get infinite solutions with t and s?

how to get the points? ?

$$P1=(0,3) \ P2=(2,4) \ P3=(1,3) \ P4=(6,0)$$

Theoretical Assignment - *Bonus: Carillo-Lipman bound*