Practice Test

Convex Optimization, 10-725

Name:

Andrew ID:

Each question is either in true/false format, or multiple choice. For multiple choice, just choose the single best option. In each case, make sure to fill in the box according to the answer you choose (true or false, or the multiple choice option) completely. All questions are worth 1 point.

1.	The only functions that are both convex and concave are affine functions. ☐ True ☐ False
2.	The least squares loss $f(\beta) = \ y - X\beta\ _2^2$ is always strongly convex. \Box True \Box False
3.	Suppose we are minimizing a generic twice differentiable function f over \mathbb{R}^n (its Hessian is assumed to be dense at each $x \in \mathbb{R}^n$). Both DFP and BFGS improve over the cost of Newton's method, per iteration, by a factor of: \square a. $O(n)$; \square b. $O(n^2)$; \square c. $O(\sqrt{n})$; \square d. they have the same cost per iteration.
4.	The augmented Lagrangian parameter ρ in ADMM is really a theoretical formality, and the choice of ρ does not have any practical implications. \Box True \Box False
5.	For a convex optimization problem with criterion f , a necessary and sufficient condition for a feasible point x^* to be optimal is that $g^T(x-x^*) \geq 0$ for some $g \in \partial f(x^*)$, and all feasible x . \Box True \Box False
6.	In the barrier method, at any point $x(t)$ along the central path we can always construct points $u(t)$, $v(t)$ that are feasible for the dual of the original optimization problem. \Box True \Box False
7.	In any optimization problem, the criterion $f(x)$ can always be replaced by $e^{f(x)}$ without changing the solution. \Box True \Box False
8.	In general, the minimizations over the two blocks of primal variables in ADMM can be done in parallel. \Box True \Box False
9.	A Cholesky decomposition is well-defined for: □ a. any nonsingular matrix; □ b. any positive semidefinite matrix; □ c. any positive definite matrix; □ d. any matrix.

10.	For the problem $\min_{x,y} \ f(x) + g(y),$
	where f,g are convex and f is strictly convex, the x -component of the solution must be unique. That is, if (x,y) and (\tilde{x},\tilde{y}) are both solutions, then we must have $x=\tilde{x}$. \Box True \Box False
11.	For a generic convex function, coordinatewise optimality implies global optimality. \Box True \Box False
12.	A conic hull of points is a convex set. ☐ True ☐ False
13.	For a strongly convex function f on \mathbb{R} , we cannot have $f(x) \to -\infty$ as $x \to \infty$. \Box True \Box False
14.	For a strictly convex and twice differentiable function f , which is the following is true? \square a. $dom(f)$ is convex; \square b. $-f$ is strictly concave; \square c. $\nabla^2 f(x) \succ 0$ at all x ; \square d. both (a) and (b); \square e. all of (a), (b), (c).
15.	The SVM problem satisfies strong duality. □ True □ False
16.	An advantage of the barrier method over the primal-dual interior point method is that: □ a. the barrier method generally converges faster; □ b. the barrier method yields dual feasible points throughout; □ c. the barrier method yields primal feasible points throughout; □ d. the barrier method maintains complementary slackness throughout.
17.	The polyhedron $\{x:Ax\leq b\}$ is always convex, regardless of A . \Box True \Box False
18.	Stochastic gradient descent generally converges more rapidly to a high accuracy solution than does its nonstochastic counterpart. \Box True \Box False
19.	A nonconvex optimization problem always has multiple local minima. \Box True \Box False
20.	Stochastic gradient descent on a strongly convex function with a Lipschitz gradient, converges (with suitable step sizes) at the rate:
21.	A convex function must be defined on all of \mathbb{R}^n . \Box True \Box False

-22	If f has convex sublevel sets, $\{x: f(x) \leq \alpha\}$, for all $\alpha \in \mathbb{R}$, then f is convex. \square True \square False
23.	The surrogate duality gap in the primal-dual interior-point method is a bonafide duality gap when both the primal and dual residuals are zero. \Box True \Box False
24.	The SR1 update ensures that the approximated Hessian remains positive definite. \Box True \Box False
25.	In the barrier method, if there are m inequality constraints, then the suboptimality gap at a point $x(t)$ on the central path is bounded above by: \square a. m/t ; \square b. t/m ; \square c. $\sqrt{t/m}$; \square d. there is no general closed-form inolving t,m .
26.	The conjugate of $f(x) = x^2$ is: \Box a. $f^*(y) = y^2$; \Box b. $f^*(y) = y^2/2$; \Box c. $f^*(y) = 2y^2$; \Box d. $f^*(y) = y^2/4$.
27.	For minimizing a convex, differentiable function f , whose gradient is Lipschitz, gradient descent achieves the optimal rate among first-order methods. \Box True \Box False
28.	For minimizing the least squares loss $\ y - X\beta\ _2^2$, the coordinate descent updates are equivalent to the Gauss-Seidel updates for solving the linear system $X^T X \beta = X^T y$. \Box True \Box False
29.	If f_1, f_2 are convex and differentiable, then subgradients of the function $f = \max\{f_1, f_2\}$ at a point x such that $f_1(x) = f_2(x)$ are: \square a. only $\nabla f_1(x)$ and $\nabla_2 f(x)$; \square b. all convex combinations of $\nabla f_1(x)$ and $\nabla f_2(x)$; \square c. all linear combinations of $\nabla f_1(x)$ and $\nabla f_2(x)$; \square d. none of the above.
30.	Projection onto the feasible set in a linear program can always be done in closed-form. \Box True \Box False
31.	The Frank-Wolfe method is affine invariant. ☐ True ☐ False
32.	Both DFP and BFGS converge at the same (local) rate as Newton's method, under the same set of assumptions. \Box True \Box False
33.	When comparing QR and Cholesky decompositions to solve a least squares problem, generally speaking, it holds that: \Box a. QR is cheaper, Cholesky is more stable;

	 □ b. QR is cheaper and more stable; □ c. QR is more stable, Cholesky is cheaper; □ d. none of the above.
	In coordinate descent, after minimizing over coordinate i , either the new value or the old value for this coordinate can be used for the minimization over coordinate $i+1$; either choice will result in a convergent algorithm. \Box True False
35.	Newton's method is affine invariant. ☐ True ☐ False