

ECE 509 (Spring 2024) – Final Exam

May 7, 2024

Name:

By writing my name, I affirm *on my honor* that I have neither received nor given any unauthorized assistance on this examination.

Read (and comply with) all of the following information before starting:

- The exam is open book, open notes, and open to any other material, provided it is in non-electronic format. However, an exception is made for paper-like e-ink devices such as the reMarkable tablet and e-ink Kindle. The use of electronic devices, including cell phones, smart watches, tablets, laptops, etc., is strictly forbidden during the exam, with the exception of the specified e-ink devices. Please ensure that you only have the permitted items on your desk before starting the exam.
- Show all work, clearly and in order, if you want to get full credit. In addition, *justify your answers* to ensure full credit. I reserve the right to take off points if I cannot see how you arrived at your answer (even if your final answer is correct).
- Pages are provided at the end of the answer book for rough work and additional space for answers. If your answer spills over into these pages or other unused pages in the exam booklet, please clearly indicate the relevant page numbers to facilitate correct marking.
- This exam has 10 questions, for a total of 85 points and 10 bonus points. You have 3 hours to complete it.
- Good luck!

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9. Consider the optimization problem:

$$\begin{array}{ll} \text{minimize} & e^{-x} \\ \text{subject to} & \frac{x^2}{y} \leq 0 \end{array}$$

with variables $x \in \mathbb{R}$ and $y \in \mathbb{R}$, and domain $\mathcal{D} = \{(x, y) \mid y > 0\}$.

- (4 points) Verify that this is a convex optimization problem. Find the optimal value.
- (4 points) Give the Lagrange dual problem, and find the optimal solution λ^* and optimal value d^* of the dual problem. What is the optimal duality gap?
- (2 points) Does Slater's condition hold for this problem? Justify your answer.

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—Scratch Pages—

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