

SYSC 4001A
Operating Systems

Assignment 3

Group Submission
Version 1

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Part 1

Part 2 Report

In shared memory, we store an array containing the rubric marks, an int that is the student number of the exam being marked, an array that is used to keep track of which questions has been marked, a boolean that indicates whether the current exam has finished being marked, and another boolean that indicates whether all the exams have been marked.

When running the program, a value is passed through the argv parameter to indicate the number of TAs marking the exams. This number is stored in the variable “numTA”. The parent process loops through a for loop numTA times, forking a child process each loop. It then waits for each child process to terminate before ending the program.

Each child process enters an infinite while loop. Inside the while loop they go through two for loop. In the first for loop, the process loops through each of the entries in the rubric marks array in shared memory, randomly deciding each loop whether to change the entry or not. If it does decide to change the entry, the process adjusts the entry in the array and updates the rubric.txt file. Semaphores are used to prevent other child processes from adjusting the rubric at the same time.

In the second for loop, the process loops through each of the entries in the marked array in shared memory. If an entry contains a 0, that indicated that the associated question has not been marked yet. As the process proceeds to mark the question, the associated entry in the array is updated to a 1, alerting other processes that this question is in the process of being marked/already marked.

Semaphores are used again to prevent multiple processes from claiming the same question at the same time.

When each process finishes checking all 5 questions, they enter a while loop until the exam has finished being marked. After that, the boolean value in shared memory “finishedExam”, is updated to end the while loop, allowing the processes to restart the loop. The next exam is loaded into shared memory, and the entire process repeats until exam 9999. After exam 9999 is finished being marked, the boolean value in shared memory “finished” is set to true, allowing the processes to reach a break statement, freeing them from the while loop and allowing them to exit.

Once all the child processes have been terminated, the parent process terminates the shared memory and semaphores, closes the rubric.txt file, and terminates.

Part 3

Q1:

i) 3 Frames Allocated

a) FIFO (First-In-First-Out)

- We can model the page reference string and allocated frames as the following timeline. In this scheme, a lower priority refers to its nearness to being replaced. So, an allocated frame with a priority of 1 will be replaced on the next page fault, while an allocated frame with a priority of 3 will be replaced only after 3 following page faults.

<p>1-3. The first 3 page lookups result in 3 page faults (since the page table is empty):</p> <ul style="list-style-type: none"> - Page Fault Count = 3 - Remaining Page Reference String: - 417, 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 713 649 811"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr> <td>415</td><td>1</td></tr> <tr> <td>305</td><td>2</td></tr> <tr> <td>502</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	415	1	305	2	502	3	<p>4. The page lookup 417 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="980 713 1286 811"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr> <td>417</td><td>3</td></tr> <tr> <td>305</td><td>1</td></tr> <tr> <td>502</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Priority	417	3	305	1	502	2
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Hit Ratio:

$$Hit\ Ratio: \frac{\# \text{ Page Lookup Hits}}{\text{Total } \# \text{ of Page Lookups}}$$

$$Hit\ Ratio: \frac{4}{20} (20\%)$$

b) LRU (Least Recently Used)

- Similarly to the FIFO implementation, we can model the page reference string and allocated frames as a timeline, however, the priority is changed by using a counter which increments on every page lookup and resets if a page is used during a lookup. The allocated frame with the highest number is selected as the victim to be replaced.

<p>1-3. The first 3 page lookups result in 3 page faults (since the page table is empty):</p> <ul style="list-style-type: none"> - Page Fault Count = 3 - Remaining Page Reference String: - 417, 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 1195 654 1290"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr> <td>415</td><td>2</td></tr> <tr> <td>305</td><td>1</td></tr> <tr> <td>502</td><td>0</td></tr> </tbody> </table>	Allocated Frames	Counter	415	2	305	1	502	0	<p>4. The page lookup 417 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="969 1195 1274 1290"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr> <td>417</td><td>0</td></tr> <tr> <td>305</td><td>2</td></tr> <tr> <td>502</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Counter	417	0	305	2	502	1
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<p>17. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 16 - Remaining Page Reference String: - 415, 520, 518 <table border="1" data-bbox="344 802 654 895"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr><td>305</td><td>1</td></tr> <tr><td>502</td><td>0</td></tr> <tr><td>417</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Counter	305	1	502	0	417	2	<p>18. The page lookup 415 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 17 - Remaining Page Reference String: - 520, 518 <table border="1" data-bbox="988 802 1282 895"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>1</td></tr> <tr><td>415</td><td>0</td></tr> </tbody> </table>	Allocated Frames	Counter	305	2	502	1	415	0
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502	0																
417	2																
Allocated Frames	Counter																
305	2																
502	1																
415	0																
<p>19. The page lookup 520 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 18 - Remaining Page Reference String: - 518 <table border="1" data-bbox="344 977 654 1070"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr><td>520</td><td>0</td></tr> <tr><td>502</td><td>2</td></tr> <tr><td>415</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Counter	520	0	502	2	415	1	<p>20. The page lookup 518 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 19 - Remaining Page Reference String: <table border="1" data-bbox="988 977 1282 1070"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr><td>520</td><td>1</td></tr> <tr><td>518</td><td>0</td></tr> <tr><td>415</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Counter	520	1	518	0	415	2
Allocated Frames	Counter																
520	0																
502	2																
415	1																
Allocated Frames	Counter																
520	1																
518	0																
415	2																

Hit Ratio:

$$Hit\ Ratio: \frac{\# \text{ Page Lookup Hits}}{\text{Total } \# \text{ of Page Lookups}}$$

$$Hit\ Ratio: \frac{1}{20} (5\%)$$

c) Optimal

- Similarly to the FIFO and LRU implementation, we can model the page reference string and allocated frames as a timeline, however, each allocated page keeps track of its distance to its next use in the page sequence. The one with the largest distance is used as the victim when a location is needed during a page fault.

<p>1-3. The first 3 page lookups result in 3 page faults (since the page table is empty):</p> <ul style="list-style-type: none"> - Page Fault Count = 3 - Remaining Page Reference String: - 417, 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 1740 654 1854"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>415</td><td>3</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	3	305	2	502	4	<p>4. The page lookup 417 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="988 1740 1282 1854"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>415</td><td>2</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>417</td><td>5</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	2	305	1	417	5
Allocated Frames	Distance Away																
415	3																
305	2																
502	4																
Allocated Frames	Distance Away																
415	2																
305	1																
417	5																

<p>5. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 276 649 375"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>415</td><td>1</td></tr> <tr> <td>305</td><td>5</td></tr> <tr> <td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	1	305	5	417	4	<p>6. The page lookup 415 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="987 276 1276 375"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>415</td><td>5</td></tr> <tr> <td>305</td><td>4</td></tr> <tr> <td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	5	305	4	417	3
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Allocated Frames	Distance Away																
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417	3																
<p>7. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: - 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 456 649 534"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>502</td><td>5</td></tr> <tr> <td>305</td><td>3</td></tr> <tr> <td>417</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Distance Away	502	5	305	3	417	2	<p>8. The page lookup 518 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 6 - Remaining Page Reference String: - 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="987 456 1276 534"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>6</td></tr> <tr> <td>305</td><td>2</td></tr> <tr> <td>417</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	6	305	2	417	1
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Allocated Frames	Distance Away																
518	6																
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417	1																
<p>9. The page lookup 417 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 6 - Remaining Page Reference String: - 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 635 649 734"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>5</td></tr> <tr> <td>305</td><td>1</td></tr> <tr> <td>417</td><td>6</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	5	305	1	417	6	<p>10. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 6 - Remaining Page Reference String: - 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="987 635 1276 734"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>4</td></tr> <tr> <td>305</td><td>6</td></tr> <tr> <td>417</td><td>5</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	4	305	6	417	5
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417	6																
Allocated Frames	Distance Away																
518	4																
305	6																
417	5																
<p>11. The page lookup 415 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: - 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 899 649 998"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>3</td></tr> <tr> <td>415</td><td>7</td></tr> <tr> <td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	3	415	7	417	4	<p>12. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 8 - Remaining Page Reference String: - 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="987 899 1276 998"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>2</td></tr> <tr> <td>502</td><td>5</td></tr> <tr> <td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	2	502	5	417	3
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Allocated Frames	Distance Away																
518	2																
502	5																
417	3																
<p>13. The page lookup 520 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: - 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="344 1058 649 1157"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>1</td></tr> <tr> <td>520</td><td>6</td></tr> <tr> <td>417</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	1	520	6	417	2	<p>14. The page lookup 518 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: - 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="987 1058 1276 1157"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>6</td></tr> <tr> <td>520</td><td>5</td></tr> <tr> <td>417</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	6	520	5	417	1
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520	6																
417	2																
Allocated Frames	Distance Away																
518	6																
520	5																
417	1																
<p>15. The page lookup 417 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: - 305, 502, 415, 520, 518 <table border="1" data-bbox="344 1237 649 1336"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>5</td></tr> <tr> <td>520</td><td>4</td></tr> <tr> <td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	5	520	4	417	Inf	<p>16. The page lookup 305 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 10 - Remaining Page Reference String: - 502, 415, 520, 518 <table border="1" data-bbox="987 1237 1276 1336"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>4</td></tr> <tr> <td>520</td><td>3</td></tr> <tr> <td>305</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	4	520	3	305	Inf
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Allocated Frames	Distance Away																
518	4																
520	3																
305	Inf																
<p>17. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 11 - Remaining Page Reference String: - 415, 520, 518 <table border="1" data-bbox="344 1417 649 1516"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>3</td></tr> <tr> <td>520</td><td>2</td></tr> <tr> <td>502</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	3	520	2	502	Inf	<p>18. The page lookup 415 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 12 - Remaining Page Reference String: - 520, 518 <table border="1" data-bbox="987 1417 1276 1516"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>2</td></tr> <tr> <td>520</td><td>1</td></tr> <tr> <td>415</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	2	520	1	415	Inf
Allocated Frames	Distance Away																
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502	Inf																
Allocated Frames	Distance Away																
518	2																
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415	Inf																
<p>19. The page lookup 520 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 12 - Remaining Page Reference String: - 518 <table border="1" data-bbox="344 1596 649 1679"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>1</td></tr> <tr> <td>520</td><td>Inf</td></tr> <tr> <td>415</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	1	520	Inf	415	Inf	<p>20. The page lookup 518 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 12 - Remaining Page Reference String: - 518 <table border="1" data-bbox="987 1596 1276 1679"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr> <td>518</td><td>Inf</td></tr> <tr> <td>520</td><td>Inf</td></tr> <tr> <td>415</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	518	Inf	520	Inf	415	Inf
Allocated Frames	Distance Away																
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415	Inf																

Hit Ratio:

$$\text{Hit Ratio: } \frac{\# \text{ Page Lookup Hits}}{\text{Total # of Page Lookups}}$$

$$\text{Hit Ratio: } \frac{8}{20} (40\%)$$

ii) 4 Frames Allocated

a) FIFO

<p>1-4. The first 4 page lookups result in 4 page faults (since the page table is empty):</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: <p>- 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="349 397 649 508"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>3</td></tr> <tr><td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Priority	415	1	305	2	502	3	417	4	<p>5. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: <p>- 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="992 397 1292 508"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>3</td></tr> <tr><td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Priority	415	1	305	2	502	3	417	4
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<p>6. The page lookup 415 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: <p>- 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="349 597 649 709"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>3</td></tr> <tr><td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Priority	415	1	305	2	502	3	417	4	<p>7. The page lookup 502 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: <p>- 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="992 597 1292 709"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>3</td></tr> <tr><td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Priority	415	1	305	2	502	3	417	4
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<p>8. The page lookup 518 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: <p>- 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="349 798 649 910"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>4</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>502</td><td>2</td></tr> <tr><td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	518	4	305	1	502	2	417	3	<p>9. The page lookup 417 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: <p>305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="992 798 1292 910"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>4</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>502</td><td>2</td></tr> <tr><td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	518	4	305	1	502	2	417	3
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<p>10. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: <p>- 415, 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="349 998 649 1110"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>4</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>502</td><td>2</td></tr> <tr><td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	518	4	305	1	502	2	417	3	<p>11. The page lookup 415 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 6 - Remaining Page Reference String: <p>- 502, 520, 518, 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="992 998 1292 1110"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>3</td></tr> <tr><td>415</td><td>4</td></tr> <tr><td>502</td><td>1</td></tr> <tr><td>417</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Priority	518	3	415	4	502	1	417	2
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<p>14. The page lookup 518 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: <p>- 417, 305, 502, 415, 520, 518</p> <table border="1" data-bbox="349 1400 649 1512"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>2</td></tr> <tr><td>415</td><td>3</td></tr> <tr><td>520</td><td>4</td></tr> <tr><td>417</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Priority	518	2	415	3	520	4	417	1	<p>15. The page lookup 417 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: <p>- 305, 502, 415, 520, 518</p> <table border="1" data-bbox="992 1400 1292 1512"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>2</td></tr> <tr><td>415</td><td>3</td></tr> <tr><td>520</td><td>4</td></tr> <tr><td>417</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Priority	518	2	415	3	520	4	417	1
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417	1																				
<p>16. The page lookup 305 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 8 - Remaining Page Reference String: <p>- 502, 415, 520, 518</p> <table border="1" data-bbox="349 1600 649 1712"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>518</td><td>1</td></tr> <tr><td>415</td><td>2</td></tr> <tr><td>520</td><td>3</td></tr> <tr><td>305</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Priority	518	1	415	2	520	3	305	4	<p>17. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: <p>- 415, 520, 518</p> <table border="1" data-bbox="992 1600 1292 1712"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>502</td><td>4</td></tr> <tr><td>415</td><td>1</td></tr> <tr><td>520</td><td>2</td></tr> <tr><td>305</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	502	4	415	1	520	2	305	3
Allocated Frames	Priority																				
518	1																				
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305	4																				
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305	3																				
<p>18. The page lookup 415 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: <p>- 520, 518</p> <table border="1" data-bbox="349 1801 649 1900"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>502</td><td>4</td></tr> <tr><td>415</td><td>1</td></tr> <tr><td>520</td><td>2</td></tr> <tr><td>305</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	502	4	415	1	520	2	305	3	<p>19. The page lookup 520 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: <p>- 518</p> <table border="1" data-bbox="992 1801 1292 1900"> <thead> <tr> <th>Allocated Frames</th><th>Priority</th></tr> </thead> <tbody> <tr><td>502</td><td>4</td></tr> <tr><td>415</td><td>1</td></tr> <tr><td>520</td><td>2</td></tr> <tr><td>305</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Priority	502	4	415	1	520	2	305	3
Allocated Frames	Priority																				
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520	2																				
305	3																				
Allocated Frames	Priority																				
502	4																				
415	1																				
520	2																				
305	3																				

20. The page lookup 518 **does** cause a page fault.

- Page Fault Count = 10
- Remaining Page Reference String:

Allocated Frames	Priority
502	3
518	4
520	1
305	2

Hit Ratio:

$$\text{Hit Ratio: } \frac{\# \text{ Page Lookup Hits}}{\text{Total # of Page Lookups}}$$

$$\text{Hit Ratio: } \frac{10}{20} (50\%)$$

b) LRU

- 1-4. The first 4 page lookups result in 4 page faults (since the page table is empty):

- Page Fault Count = 4
- Remaining Page Reference String:

- 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
415	3
305	2
502	1
417	0

5. The page lookup 305 **does not** cause a page fault.

- Page Fault Count = 4
- Remaining Page Reference String:

- 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
415	4
305	0
502	2
417	1

6. The page lookup 415 **does not** cause a page fault.

- Page Fault Count = 4
- Remaining Page Reference String:

- 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
415	0
305	1
502	3
417	2

7. The page lookup 502 **does not** cause a page fault.

- Page Fault Count = 4
- Remaining Page Reference String:

- 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
415	1
305	2
502	0
417	3

8. The page lookup 518 **does** cause a page fault.

- Page Fault Count = 5
- Remaining Page Reference String:

- 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
415	2
305	3
502	1
518	0

9. The page lookup 417 **does** cause a page fault.

- Page Fault Count = 6
- Remaining Page Reference String:

- 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
415	3
417	0
502	2
518	1

10. The page lookup 305 **does** cause a page fault.

- Page Fault Count = 7
- Remaining Page Reference String:

- 415, 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
305	0
417	1
502	3
518	2

11. The page lookup 415 **does** cause a page fault.

- Page Fault Count = 8
- Remaining Page Reference String:

- 502, 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
305	1
417	2
415	0
518	3

12. The page lookup 502 **does** cause a page fault.

- Page Fault Count = 9
- Remaining Page Reference String:

- 520, 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
305	2
417	3
502	0
518	4

13. The page lookup 520 **does** cause a page fault.

- Page Fault Count = 10
- Remaining Page Reference String:

- 518, 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
305	3
417	4
502	1
520	0

14. The page lookup 518 **does** cause a page fault.

- Page Fault Count = 11
- Remaining Page Reference String:

- 417, 305, 502, 415, 520, 518

Allocated Frames	Counter
305	4
518	0
502	2
520	1

15. The page lookup 417 **does** cause a page fault.

- Page Fault Count = 12
- Remaining Page Reference String:

- 305, 502, 415, 520, 518

Allocated Frames	Counter
417	0
518	1
502	3
520	2

<p>16. The page lookup 305 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 13 - Remaining Page Reference String: - 502, 415, 520, 518 <table border="1" data-bbox="349 283 654 397"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr><td>417</td><td>1</td></tr> <tr><td>518</td><td>2</td></tr> <tr><td>305</td><td>0</td></tr> <tr><td>520</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Counter	417	1	518	2	305	0	520	3	<p>17. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 14 - Remaining Page Reference String: - 415, 520, 518 <table border="1" data-bbox="971 283 1276 397"> <thead> <tr> <th>Allocated Frames</th><th>Counter</th></tr> </thead> <tbody> <tr><td>417</td><td>2</td></tr> <tr><td>518</td><td>3</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>502</td><td>0</td></tr> </tbody> </table>	Allocated Frames	Counter	417	2	518	3	305	1	502	0
Allocated Frames	Counter																				
417	1																				
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Allocated Frames	Counter																				
417	2																				
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305	1																				
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<p>18. The page lookup 415 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 15 - Remaining Page Reference String: - 520, 518 <table border="1" data-bbox="349 483 654 597"> <thead> <tr> <th>Allocated Frames</th> <th>Counter</th> </tr> </thead> <tbody> <tr><td>417</td><td>3</td></tr> <tr><td>415</td><td>0</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>502</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Counter	417	3	415	0	305	2	502	1	<p>19. The page lookup 520 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 16 - Remaining Page Reference String: - 518 <table border="1" data-bbox="971 483 1276 597"> <thead> <tr> <th>Allocated Frames</th> <th>Counter</th> </tr> </thead> <tbody> <tr><td>520</td><td>0</td></tr> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>3</td></tr> <tr><td>502</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Counter	520	0	415	1	305	3	502	2
Allocated Frames	Counter																				
417	3																				
415	0																				
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Allocated Frames	Counter																				
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415	1																				
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502	2																				
<p>20. The page lookup 518 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 17 - Remaining Page Reference String: <table border="1" data-bbox="349 663 654 768"> <thead> <tr> <th>Allocated Frames</th> <th>Counter</th> </tr> </thead> <tbody> <tr><td>520</td><td>1</td></tr> <tr><td>415</td><td>2</td></tr> <tr><td>518</td><td>0</td></tr> <tr><td>502</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Counter	520	1	415	2	518	0	502	3											
Allocated Frames	Counter																				
520	1																				
415	2																				
518	0																				
502	3																				

Hit Ratio:

$$\text{Hit Ratio: } \frac{\# \text{ Page Lookup Hits}}{\text{Total } \# \text{ of Page Lookups}}$$

$$\text{Hit Ratio: } \frac{3}{20} (15\%)$$

c) Optimal

<p>1-4. The first 4 page lookups result in 4 page faults (since the page table is empty):</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 305, 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 1151 654 1265"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>415</td><td>2</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>502</td><td>3</td></tr> <tr><td>417</td><td>5</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	2	305	1	502	3	417	5	<p>5. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 415, 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="971 1151 1276 1265"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>5</td></tr> <tr><td>502</td><td>2</td></tr> <tr><td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	1	305	5	502	2	417	4
Allocated Frames	Distance Away																				
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<p>6. The page lookup 415 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 502, 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 1330 654 1465"> <thead> <tr> <th>Allocated Frames</th> <th>Distance Away</th> </tr> </thead> <tbody> <tr><td>415</td><td>5</td></tr> <tr><td>305</td><td>4</td></tr> <tr><td>502</td><td>1</td></tr> <tr><td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	5	305	4	502	1	417	3	<p>7. The page lookup 502 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 4 - Remaining Page Reference String: - 518, 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="971 1330 1276 1465"> <thead> <tr> <th>Allocated Frames</th> <th>Distance Away</th> </tr> </thead> <tbody> <tr><td>415</td><td>4</td></tr> <tr><td>305</td><td>3</td></tr> <tr><td>502</td><td>5</td></tr> <tr><td>417</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	4	305	3	502	5	417	2
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<p>8. The page lookup 518 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: - 417, 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 1531 654 1666"> <thead> <tr> <th>Allocated Frames</th> <th>Distance Away</th> </tr> </thead> <tbody> <tr><td>415</td><td>3</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>518</td><td>6</td></tr> <tr><td>417</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	3	305	2	518	6	417	1	<p>9. The page lookup 417 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: - 305, 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="971 1531 1276 1666"> <thead> <tr> <th>Allocated Frames</th> <th>Distance Away</th> </tr> </thead> <tbody> <tr><td>415</td><td>2</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>518</td><td>5</td></tr> <tr><td>417</td><td>6</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	2	305	1	518	5	417	6
Allocated Frames	Distance Away																				
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<p>10. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: - 415, 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 1731 654 1894"> <thead> <tr> <th>Allocated Frames</th> <th>Distance Away</th> </tr> </thead> <tbody> <tr><td>415</td><td>1</td></tr> <tr><td>305</td><td>6</td></tr> <tr><td>518</td><td>4</td></tr> <tr><td>417</td><td>5</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	1	305	6	518	4	417	5	<p>11. The page lookup 415 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 5 - Remaining Page Reference String: - 502, 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="971 1731 1276 1894"> <thead> <tr> <th>Allocated Frames</th> <th>Distance Away</th> </tr> </thead> <tbody> <tr><td>415</td><td>7</td></tr> <tr><td>305</td><td>5</td></tr> <tr><td>518</td><td>3</td></tr> <tr><td>417</td><td>4</td></tr> </tbody> </table>	Allocated Frames	Distance Away	415	7	305	5	518	3	417	4
Allocated Frames	Distance Away																				
415	1																				
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415	7																				
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518	3																				
417	4																				

<p>12. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 6 - Remaining Page Reference String: - 520, 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 283 654 392"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>502</td><td>5</td></tr> <tr><td>305</td><td>4</td></tr> <tr><td>518</td><td>2</td></tr> <tr><td>417</td><td>3</td></tr> </tbody> </table>	Allocated Frames	Distance Away	502	5	305	4	518	2	417	3	<p>13. The page lookup 520 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: - 518, 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="992 283 1281 392"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>6</td></tr> <tr><td>305</td><td>3</td></tr> <tr><td>518</td><td>1</td></tr> <tr><td>417</td><td>2</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	6	305	3	518	1	417	2
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<p>14. The page lookup 518 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: - 417, 305, 502, 415, 520, 518 <table border="1" data-bbox="349 479 654 589"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>5</td></tr> <tr><td>305</td><td>2</td></tr> <tr><td>518</td><td>6</td></tr> <tr><td>417</td><td>1</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	5	305	2	518	6	417	1	<p>15. The page lookup 417 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: - 305, 502, 415, 520, 518 <table border="1" data-bbox="992 479 1281 589"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>4</td></tr> <tr><td>305</td><td>1</td></tr> <tr><td>518</td><td>5</td></tr> <tr><td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	4	305	1	518	5	417	Inf
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<p>16. The page lookup 305 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 7 - Remaining Page Reference String: - 502, 415, 520, 518 <table border="1" data-bbox="349 675 654 785"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>3</td></tr> <tr><td>305</td><td>Inf</td></tr> <tr><td>518</td><td>4</td></tr> <tr><td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	3	305	Inf	518	4	417	Inf	<p>17. The page lookup 502 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 8 - Remaining Page Reference String: - 415, 520, 518 <table border="1" data-bbox="992 675 1281 785"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>2</td></tr> <tr><td>502</td><td>Inf</td></tr> <tr><td>518</td><td>3</td></tr> <tr><td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	2	502	Inf	518	3	417	Inf
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<p>18. The page lookup 415 does cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: - 520, 518 <table border="1" data-bbox="349 872 654 982"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>1</td></tr> <tr><td>415</td><td>Inf</td></tr> <tr><td>518</td><td>2</td></tr> <tr><td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	1	415	Inf	518	2	417	Inf	<p>19. The page lookup 520 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: - 518 <table border="1" data-bbox="992 872 1281 982"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>Inf</td></tr> <tr><td>415</td><td>Inf</td></tr> <tr><td>518</td><td>1</td></tr> <tr><td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	Inf	415	Inf	518	1	417	Inf
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<p>20. The page lookup 518 does not cause a page fault.</p> <ul style="list-style-type: none"> - Page Fault Count = 9 - Remaining Page Reference String: <table border="1" data-bbox="349 1047 654 1165"> <thead> <tr> <th>Allocated Frames</th><th>Distance Away</th></tr> </thead> <tbody> <tr><td>520</td><td>Inf</td></tr> <tr><td>415</td><td>Inf</td></tr> <tr><td>518</td><td>Inf</td></tr> <tr><td>417</td><td>Inf</td></tr> </tbody> </table>	Allocated Frames	Distance Away	520	Inf	415	Inf	518	Inf	417	Inf											
Allocated Frames	Distance Away																				
520	Inf																				
415	Inf																				
518	Inf																				
417	Inf																				

Hit Ratio:

$$\text{Hit Ratio: } \frac{\# \text{ Page Lookup Hits}}{\text{Total } \# \text{ of Page Lookups}}$$

$$\text{Hit Ratio: } \frac{11}{20} (55\%)$$

iii) Conclusion, and questions

- From this one experiment, the FIFO algorithm performed better with a 20% hit rate compared to LRU's 5% hit rate. However, this disparity is mostly set by this example's sequence and not truly indicative of the real-world comparison. At a page table size of 3, the performance is heavily reliant on the peculiar sequence since it doesn't allow the algorithms to truly show their differences. When moving to a 4-frame sized table, the FIFO algorithm still beats out LRU at a 50% hit rate compared to a 15% hit rate. The LRU should normally outperform FIFO in real-world sequences, where it is common to access pages near each other giving LRU the edge over FIFO. In some cases, FIFO can exhibit Belady's Anomaly where LRU will never. If we include the optimal algorithm in the comparison, it will always match or beat other algorithms since it guarantees the minimal amount of page faults. However, in real systems, it is impractical to implement since it requires knowledge of future events. This is only possible in very specific situations where everything is preplanned. Comparing the LRU and FIFO algorithms, FIFO can sometimes outperform LRU where a page

sequence contains a pseudorandom cyclical behavior a size slightly bigger than the page table. The bias created by LRU can cause the incorrect page to be removed where the order of FIFO reduces the fault rate. However, in sequences where common pages are used (locality) frequently, LRU will outperform FIFO by a wide margin.

Q2

a)

- Since the page table is itself stored in physical memory, an initial lookup in main memory is required to find the corresponding physical address of the logical address. Then, a second lookup with the newly found logical address is completed. So, the lookup time without a TLB would be 240ns ($2 * 120\text{ns}$).

b)

- Assuming the TLB search happens sequentially to the physical memory lookup (the page lookup in the TLB and page table are not done at the same time), the Effective Access Time (EAT) can be calculated using the following equation, where t is the lookup time for the physical memory, ε is the lookup time for the TLB, and α is the hit ratio for the TLB:

$$EAT = (1 - \alpha) * (t + \varepsilon) + \alpha * \varepsilon + t$$

$$EAT = 2t + \varepsilon - \alpha * t$$

(Slightly different initial equation compared to the slides but identical final equation. The $(1 - \alpha) * (t + \varepsilon)$ term is the case where there is a TLB miss. Inversely, the $\alpha * \varepsilon$ term is when there is a TLB hit. The additional t is the required lookup time when the physical address is acquired.)

Using that equation, the EAT can be calculated using the following values: $\alpha = .95$, $\varepsilon = 20$, and $t = 120$.

$$EAT = 2t + \varepsilon - \alpha * t$$

$$EAT = 2(120) + 20 - 0.95 * 120$$

$$EAT = 146\text{ns}$$

In conclusion, with the addition of the TLB, the effective memory access time would be 146ns.

c)

- Generally, adding a TLB improves performance by drastically reducing the lookup time on pages that are frequently searched for. In real systems there could be specific pages that are required often, and reducing those lookup times can dramatically improve the effective access time. However, if the page look ups don't require fetching reoccurring pages, the TLB becomes pure overhead. If we take the example from part b of this question, having a hit rate lower than 50% would result in the EAT being worse than not having the TLB.

Q3:

Consider a system with a paged logical address space composed of 128 pages of 4 Kbytes each, mapped into a 512 Kbytes physical memory space. Answer the following questions and justify your answers.

- (a) What is the format and size (in bits) of the processor's logical address?

Page Number:

$$\log_2(128) = 7$$

Page Number is 7 bits

Page Offset:

$$4 \text{ Kbytes} = 4096 \text{ bytes}$$

$$\log_2(4096) = 12$$

Page Offset is 12 bits

The logical address has a size of 19 bits. 7 bits for the page number and 12 bits for the page offset.

- (b) What is the required length (number of entries) and width (size of each entry in bits, disregarding control bits) of the page table?

Number of entries in the page table is the same as number of pages: 128

Width of each entry in page table:

Number of frames:

$$\frac{512 \text{ kB}}{4 \text{ kB}} = 128$$

(Space on physical memory divided by page size gives 128 frames)

$$\log_2(128) = 7$$

Each entry has a width of 7 bits.

- (c) What is the effect on the page table width if now the physical memory space is reduced by half (from 512 Kbytes to 256 Kbytes)? Assume that the number of page entries and page size remain the same.

By halving the amount of physical memory space, the number of frames also gets halved.

$$\frac{256 \text{ kB}}{4 \text{ kB}} = 64$$

Since the number of frames has been halved, the number of bits in the page table width reduces by 1.

$$\log_2 64 = 6$$

Q4:

Explain, in detail, the sequence of operations and file system data structure accesses that occur when a process executes the lseek(fd, offset, SEEK_END) system call. Consider a system using a hierarchical directory structure and assume the file described by the file descriptor (fd) is not currently open by any other process.

When lseek is called, the open file table is accessed to check for fd. If fd is located within the open file table, the system accesses the file's inode and the current position pointer from the fd entry in the table. From the inode, it retrieves the size of the file. The offset value is then added to the size value, creating a new offset value for the current position pointer. The current position pointer is then set to this new offset. Finally, the lseek syscall returns the new position of the pointer to the process.

Q5:

- (a) Consider a file system that uses inodes to represent files. Disk blocks are 8Kb in size, and a pointer to a disk block requires 4 bytes. This file system has 12 direct disk blocks, as well as single, double, and triple indirect disk blocks. What is the maximum size of a file that can be stored in this file system?

Size of direct disk blocks:

$$12 \cdot 8 kB = 96 kB$$

Number of pointers in an indirect block:

$$\frac{8192 \text{ bytes}}{4 \text{ bytes}} = 2048$$

Single indirect disk blocks size:

$$2048^1 = 2048$$

$$2048 \cdot 8 Kb = 16384 kB$$

Double indirect disk blocks size:

$$2048^2 = 4194304$$

$$4194304 \cdot 8 Kb = 33554432 kB$$

Triple indirect disk blocks size:

$$2048^3 = 8589934592$$

$$8589934592 \cdot 8 kB = 68719476736 kB$$

$$96 kB + 16384 kB + 33554432 kB + 68719476736 kB = 68753047648 kB$$

The maximum size of a file that can be stored is 68753047648 kB or about 70.4 TB.

- (b) Explain what you can do in case (a) if you need to store a file that is larger than the maximum size computed. Give an example showing how you can define a larger file, and what the size of that file would be.

If we need to store a file that is larger than the maximum size computed (about 70.4 TB), we could define an inode that also contains a quadruple indirect disk block.

Quadruple indirect disk blocks size:

$$\begin{aligned}2048^4 &= 1.759218604e13 \\1.759218604e13 \cdot 8 kB &= 1.407374884e14 kB\end{aligned}$$

Adding a quadruple indirect disk block would increase the file size by about $1.407374884e14$ kB or 144115 TB, increasing the maximum size of the file to about 144185 TB or about 144 PB.

SYSC 4001 – Assignment Part 1 – Report

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Repository Links:

Part 1:

https://github.com/RigelLB/SYSC4001_A3_P1

Part 2:

https://github.com/AbdullahKhan28CU/SYSC4001_A3P2

Simulator Results:

To preface this report, midway through doing the test cases and analyzing them, I have noticed that my choice of test for the respective cases of I/O bound, CPU bound, and similar bursts are not ideal for a real test, however, I ran out of time to modify the whole report and test to fix this issue, so, the rest of this report is based on the tests previously made. I also realize that the python script I used to gather the metrics may be slightly faulty as some of the values collected look “off”.

The metrics for the throughput, average wait time, average turnaround time, and average response time were collected as follows.

$$\text{Throughput: } \frac{\# \text{ processes}}{\text{Total Time}}$$

Average Wait Time: Sum of time spent in the READY state

Average Turnaround Time: The time spent between the NEW state to the TERMINATED state

Average Response Time: The time spent between the NEW state to the first RUNNING state.

All the values were then summed for all the test cases in the same category is divided by the number of respective test cases. The different algorithms result in the following data table:

EP							
Test #	I/O Bound	CPU Bound	Similar I/O and CPU Burst	Throughput	Average Wait Time	Average TurnaroundTime	Average Response Time
			16	0.007	277	447	199
			6	0.007	288	458	233
				0.007	282.5	452.5	216
			11	0.008	125	245.67	125
			3	0.007	50	200	50
			4	0.007	45	200	2.5
			8	0.004	100	350	100
				0.0065	80	248.9175	69.375
			10	0.007	32.5	240	2.5
			5	0.007	110	278.33	15
				0.007	71.25	259.165	8.75
RR							
Test #	I/O Bound	CPU Bound	Similar I/O and CPU Burst	Throughput	Average Wait Time	Average TurnaroundTime	Average Response Time
			16	0.007	261	431	75
			6	0.007	261	431	75
				0.007	261	431	75
			11	0.008	135.33	240	2.5
			3	0.007	50	200	50
			4	0.007	45	200	2.5
			8	0.004	200	450	38.33
				0.0065	107.5825	272.5	23.3325
			10	0.007	32.5	240	2.5
			5	0.007	115	283.33	21.67
				0.007	73.75	261.665	12.085
EP_RR							
Test #	I/O Bound	CPU Bound	Similar I/O and CPU Burst	Throughput	Average Wait Time	Average TurnaroundTime	Average Response Time
			16	0.007	265	435	187
			6	0.007	306	476	227
				0.007	285.5	455.5	207
			11	0.008	135.33	256	71.67
			3	0.007	50	200	50
			4	0.007	82.5	237.5	2.5
			8	0.004	200	450	0
				0.0065	116.9575	285.875	31.0425
			10	0.006	77.5	285	2.5
			5	0.008	143.33	237.5	1.67
				0.007	110.415	261.25	2.085

The different colors are used to separate different groups of tests from each other. For example, the first set of green values are the collective averages of the Similar I/O and CPU Burst test group using the External Priorities algorithm.

From the collected data, the waiting time for similar IO/CPU bursts are similar, with the slight edge to the round robin algorithm. In terms of response times, the round-robin algorithm beats out the two other algorithms by a wide margin. In theory, the response time for the external priority algorithm should be worse than the two other algorithms since processes run until completion before handing over the CPU, which we do see in the simulation results. The hybrid external priority w/ the round-robin timeout should have slightly better response times since it gives up the CPU with higher priority processes when they arrive and are forced out by the quantum timer, which we do see in the data. In general, RR will be very good at reducing the waiting time and response time in I/O bound situations since it gives the opportunity to all processes to use the CPU equally. However, in this simulation it is not observed. This could be due to the test cases and the relatively large quantum. Since most of the processes don't have CPU processing times that are very large, they will very rarely be handled by the round robin style timeout. In practice, however, the hybrid approach can be very powerful and outshine the other algorithm in most cases. The ability to attribute priorities can be very important since some processes will be more important than others. The downsides such as the response time can be attributed somewhat by modifying the quantum to obtain the best performance.