CALCULUS TRICKS AND TRAPS

Schrödinger's Cat

- 1. Is it true that if a function has a vertical asymptote, its derivative has a vertical asymptote at the same place?
- 2. Is it true that if a function is continuous on the interval (a, b) and its graph is a smooth curve (no sharp corners) on that interval, then the function is differentiable at any point on (a, b)?
- 3. Is it true that if a function is not monotone, then it does not have an inverse function?
- 4. If a function f is continuous for all real x and $\lim_{n\to\infty} f(n) = A$ for natural numbers n, then $\lim_{x\to\infty} f(x) = A$. True or false?
- 5. If a function is defined on \mathbb{R}^2 , it cannot be continuous at only one point. Discuss.
- 6. Discuss the following statement: If f(x,y) approaches zero, as a point approaches the origin along any algebraic curve $y=cx^{m/n}$, where $c\in\mathbb{R}$ and $m,n\in\mathbb{N}$ ($x\geq 0$ in case the exponential fraction is in lowest terms and n is even), then the limit of f(x,y) is zero at the origin.