

# 29

JUNE

Saturday

Week 26 | 181-185

2024

JUNE 2024						
30	1	2	3	4	5	6
9	10	11	12	13	14	15
16	17	18	19	20	21	22
23	24	25	26	27	28	29
S	M	T	W	T	F	S

MCQs

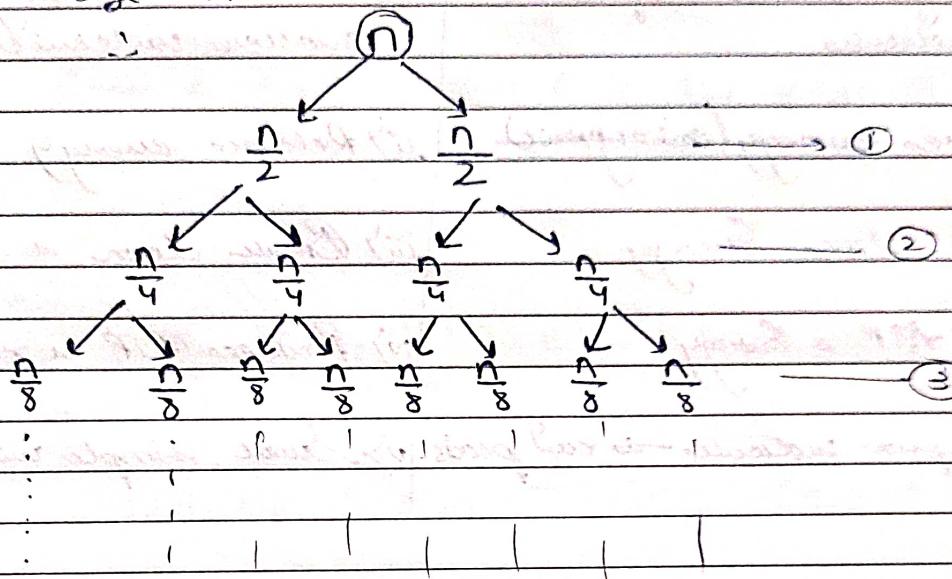
09.00

1)  $\Theta(\log n)$ 

10.00

Size =  $n$ 

1.00



2.00

3.00

$$\text{Base case } \frac{n}{2^k} = 1$$

$\frac{n}{2^k}$        $\frac{n}{2^k}$        $\vdots$        $\frac{n}{2^k}$        $\frac{n}{2^k}$        $\dots$        $= \frac{n}{2^k}$  after  $k^{th}$  iteration

4.00

5.00

Base case  $\frac{n}{2^k} = 1$

$$n = 2^k$$

Sunday 30

$$\log_2 n = k \log_2 2$$

$$k = \log_2 n$$

$\therefore$  Time Complexity =  $O(\log n)$

JULY 2024						
1	2	3	4	5	6	
7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29	30	31			
S	M	T	W	T	F	S

JULY  
Monday

01

2024 // 2027 1 123-153

09.00 2) c)  $O(1)$

$\because \text{low, mid, high} \rightarrow \text{The only variables used}$   
~~no extra variable is used to store.~~

~~no. of variables required does not depend on the size of the array.~~

3)  $O(n^2)$

$\hookrightarrow \text{① } 500$

$$500^2 = 250000 < 10^8$$

4) function Solve (array)

for i from 1 to length (array)  $\rightarrow n$

for j from 1 to length (array)  $\rightarrow n$   
print (array[i] + array[j])

length (array)  $\rightarrow n$

$$T(n) = O(n^2)$$

Time Complexity

Space Complexity =  $O(1)$

5) function Solve (array)

for i from 1 to length (array)  $\rightarrow n$

$$\text{if } \text{arr}[i] \% 2 = 0$$

prime (arr[i])

else

prime (arr[i] \* 2)

$$T.C = O(n)$$

$$S.C = O(1)$$

# 02

JULY

Tuesday

Week 27 | 184-182 // 2024

JULY						
1	2	3	4	5	6	7
8	9	10	11	12		
14	15	16	17	18	19	
21	22	23	24	25	26	27
28	29	30	31			
S	M	T	W	T	F	S

7) function solve (base, exp)

if exp == 0  
return 1

half = pow (base, floor(exp/2))

if exp % 2 == 0

return half \* half

else

return half \* half \* base

I.C = O(log n)

T(exp) = T(exp/2) + C

T.C = O(log exp)

T(exp) = T(exp/4) + C

(C) S.C = T(exp) + C

T(exp) = T(exp/2^u) + C

2^u = exp  
O(log exp)

8) func sumCal (n)

sum = 0

i = 1

while (i < n)

sum = sum + i → O(1)

i = i \* 2

return sum

AUGUST 2024						
4	5	6	7	8	9	10
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31
S	M	T	W	T	F	S

JULY

Wednesday

2024 // Week 27 | 185-181

03

iteration stops when after  $k^{\text{th}}$  iteration

$$i = 2^k$$

1st iteration  $i = 2$

2nd  $i = 1$

3rd  $i = 8$

$$2^k \geq n$$

$k^{\text{th}}$  iteration  $i = 2^k$

$$k = \log_2 n$$

$$O(\log n) \rightarrow T.C$$

$$O(1) \rightarrow S.C$$

9) func. solve(n)

if  $n == 0$  }  $O(1)$   
return 1

$$res = 1$$

$$i = 1 \rightarrow n$$

$$res = res * i$$

return res

$$T.C = O(n)$$

$$S.C = O(1)$$

10) func. solve(arr)

$$l = 0$$

$$r = \text{length}(arr) - 1$$

while ( $l \leq r$ )

$$\text{mid} = \text{floor}((l+r)/2);$$

if  $\text{arr}[\text{mid}] == \text{target}$

return mid

$$T.C = O(\log n)$$

$$S.C = O(1)$$

elif  $\text{arr}[\text{mid}] < \text{target}$

$$l = \text{mid} + 1$$

else

$$r = \text{mid} - 1$$

return -1

All that glitters is not gold

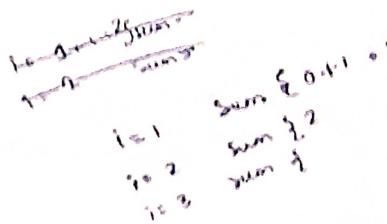
Remember

# 04

JULY

Thursday

Week 27 | 186-180 // 2024



JULY

	1	2	3	4	5	6
1	7	8	9	10	11	12
2	14	15	16	17	18	19
3	21	22	23	24	25	26
4	28	29	30	31		
S M T W T F						

11) func. `sum(n)`

if  $n \leq 1$

return 1

Sum = 0

for  $i = 1 \rightarrow n$

    Sum = Sum + sum(i-1)

return Sum

$\rightarrow O(1)$

$\rightarrow O(1)$

$\rightarrow O(n)$

T.C =  $O(n)$

S.C =

12) func. `sum(avr, n)`

$i = 1 \rightarrow k$

$\rightarrow n$

$j = 1 \rightarrow \text{length}(avr)$

$\rightarrow n$

point(avr[i])  $\rightarrow O(1)$

`length(avr)` on

T.C =  $O(k \times n)$

S.C =  $O(1)$

13) func. `Sum(avr)`

$i = 0$

while  $i < \text{length}(avr)$

$\rightarrow n$

$j = i + 1$

while  $j < \text{length}(avr)$

$\rightarrow n - 1$

    if  $avr[i] + avr[j] == \text{target}$   $\rightarrow O(1)$

        return true

$j = j + 1$

$i = i + 1$

    return false

AUGUST

2024

4	5	6	7	1	2	3
11	12	13	14	15	16	17
18	19	20	21	22	23	24
25	26	27	28	29	30	31

S M T W T F S

$$\text{for } i = 1 \text{ to } n-1$$

$$\{ 1, 2, \dots, n-1 \}$$

$$T(n) = \frac{n(n-1)}{2}$$

~~$$n \cdot ((n-1) + (n-2) + (n-3) + \dots + 3 + 2 + 1)$$

$$= n \cdot \frac{(n-1) + (n-2) + (n-3) + \dots}{2} + \dots$$

$$= n \cdot \frac{n(n+1)}{2} = \frac{n^2}{2} + \frac{n}{2}$$~~

JULY  
Friday

2024 // Week 27 | 187-179

05

$$T(n) = \frac{n^2}{2} + \frac{n}{2}$$

$$T.C = O(n^2)$$

$$S.C = O(1)$$

14) function Solve(n)

if  $n = 1$

return 1

if  $n \% 2 = 0$

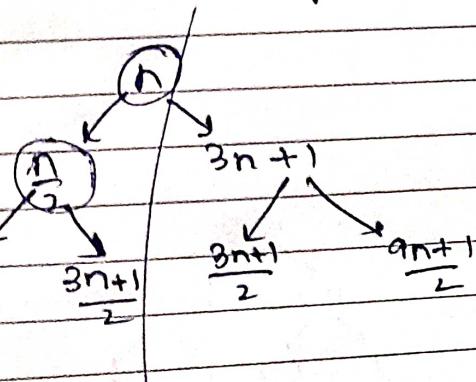
$$T.C = O(\log n)$$

$$S.C = O(1)$$

even  $\rightarrow$  solve( $\frac{n}{2}$ )

$\delta(\log n)$

odd  $\rightarrow (3 \times n + 1) \rightarrow O(n)$



15) func. Solve(arr)

for  $i = 1 \rightarrow n$

$j = 1 \rightarrow 9$

print(arr[j])

$i = 1 \quad j = \{1\}$   
 $i = 2 \quad j = \{1, 2\}$   
 $i = 3 \quad j = \{1, 2, 3\}$

$\vdots$   
 $i = n \quad j = \{1, 2, 3, \dots, n\}$

$$1 + 2 + 3 + \dots + n$$

$$n(n+1) = \frac{n^2 + n}{2}$$

$$T.C = O(n^2)$$

$$S.C = O(1)$$

06

JULY

Saturday

WED 27 JULY 2024

JULY 2024						
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				
S	M	T	W	T	F	S

16) func. solve (arr)

09:00 res = 0

i = 1 → n

O(n)

10:00 res = res + arr[i]

i = 1 → n

O(n)

res = res - arr[i]

return res.

T.C = O(n)

S.C = O(1)

17) func. solve (n)

if n &lt;= 1 return 1

O(1)

a = solve (n-1)

b = solve (n-1)

return a+b

$$T(n) = 2T(n-1) + O(1)$$

$$T(n-1) = 2T(n-2) + O(1)$$

$$T(n-2) = 2T(n-3) + O(1)$$

~~2^n =~~

$$\therefore 2^1 + 2^2 + 2^3 + \dots + 2^{n-1} = (n-(n-1))$$

$$\frac{2(2^n - 1)}{2-1}$$

$$i = (n-(n-1))$$

$$O(2^n) \rightarrow T.C$$

$$\therefore S.C \rightarrow O(n)$$

Sunday 07

2024										
AUGUST										
	1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20	21
22	23	24	25	26	27	28	29	30	31	
S	M	T	W	T	F	S				

JULY

Monday

2024 // Week 28 | 190-176

08

09.00 ~~18~~ func. solve( $m1, m2$ )

for  $i = 1 \rightarrow \text{length}(m1)$

for  $j = 1 \rightarrow \text{length}(m2[0])$

sum = 0

for  $k = 1 \rightarrow \text{length}(m1[0])$

sum = sum +  $m1[i][k] \times m2[k][j]$

res[i][j] = sum

return res.

$$\text{T.C} = O(\text{length}(m1) \times \text{length}(m2[0]) \times \text{length}(m1[0]))$$

$$\text{S.C} = O(\text{length}(m1) \times \text{length}(m2[0]))$$

resultant matrix dimensions

~~19~~ 19 func. solve(n)

$i = 1 \rightarrow n$

$j = 1 \rightarrow i$

$k = 1 \rightarrow j$

print(i, j, k)

$$\sum_{j=1}^i j = \frac{i(i+1)}{2}$$

$$\sum_{i=1}^n \frac{i^2}{2} = \frac{1}{2} \sum_{i=1}^n i^2 + \frac{1}{2} \sum_{i=1}^n i$$

$$\frac{1}{2} \frac{n(n+1)(2n+1)}{6} + \frac{n(n+1)}{4}$$

$$= O(n^3) \rightarrow \text{T.C}$$

Remember

# 09

JULY

Tuesday

Week 28 | 191-175 // 2024

JULY						
1	2	3	4	5	6	7
7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29	30	31			
S	M	T	W	T	F	S

$$S.C = O(1)$$

09.00

~~217~~ func. solve(n)  
~~if n == 0~~

10.00

return 0

return n + solve(n - 1)

11.00

$$T.C = O(n)$$

$$S.C = O(n)$$

12.00

~~22~~ func. solve(arr)  
i = 1 → length(arr)

01.00

j = 1 → length(arr)

if arr[i] &lt; arr[j]

swap(arr[i], arr[j])

02.00

$$T.C = O(n^2)$$

$$S.C = O(1)$$

03.00

~~23~~ func. solve(n)  
for i = 1 → n

04.00

j = 1 → n

if i == j

print(i, j)

05.00

$$T.C = O(n^2)$$

$$S.C = O(1)$$

06.00

AUGUST 2024						
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				
S	M	T	W	T	F	S

JULY

Wednesday

10

2024 // mon - sun

24) func. some (arr)

for  $i = 1 \rightarrow \frac{n}{2} \rightarrow O(n)$ 

swap (arr[i], arr[n-i])

$$T.C = O(n)$$

$$S.C = O(1)$$

11.00 25) func. Solve [matrix]

 $T. = []$  $i = 1 \rightarrow n \rightarrow$  rows

row = []

 $j = 1 \rightarrow n[0] \rightarrow$ 

row.append (matrix[i][j])

T.append (row)

return T

$$T.C = O(nxm)$$

$$S.C = O(nxm)$$

03.00 26) func. some (arr)

$$T.C = O(n)$$

$$S.C = O(1)$$

C = 0

 $i = 1 \rightarrow n$ 

if : arr[i] &gt; 0

C = C + 1

return C

06.00

JULY 2024						
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7	8	9	10	11	12	13
14	15	16	17	18	19	20
21	22	23	24	25	26	27
28	29	30	31			
S	M	T	W	T	F	S

11

JULY

Thursday

Week 28 | 193-173 2024

27) func. solve(arr)

09.00 res = []

i = 1 → n

if not res.contains(arr[i])

res.append(arr[i])

return res.

11.00 T.C = O(n)

S.C = O(n)

12.00 28) func. solve(n)

i = 1

(i < n)

i = 1 \* 2

S.C = O(1)

02.00

$2^k \geq n$

$2^k > n$

$\log n = k$

O(log n) → T.C

03.00 29) func. solve(arr)

i = 1 → n

j = i

(j > 0 ∧ arr[j-1] > arr[j])

swap (arr[i], arr[j-1])

j = j - 1

04.00 i = 1, j = 1

i = 2, j = 2, 1

i = 3, j = 3, 2, 1

S.C = O(1)

05.00

i = 1, j = 1, n-1, ..., 3, 2, 1

T.C

Remember

$(n) + (n-1) + (n-2) + \dots + 3 + 2 + 1$

$$= \frac{n(n+1)}{2} = \frac{n^2 + n}{2} = O(n^2)$$

AUGUST		2024				
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31	S	M	T	W

JULY  
Friday

2024 // Week 28 | 194-172

12

30) func. Solve  $(a_{uv}, u)$

$$09.00 \quad i = 1 \rightarrow n - k \rightarrow n - u$$

$$\text{mani} = a_{uv}[i]$$

for  $j = i+1 \rightarrow i+u \rightarrow n \text{ times}$

$$\text{if } (a_{uv}[j] > \text{mani})$$

$$\text{mani} = a_{uv}[j]$$

return (mani)

11.00

$$O((n-u) \times u)$$

$$O(nu - u^2)$$

$$n > u$$

12.00

$$\therefore O(nu) \rightarrow T.C$$

$$S.C = O(1)$$

01.00

17) ③  $O(n!)$

02.00

27) ④  $O(n)$

03.00

37)  $O(n \times 2^{n-1}) = \cancel{O(n)} \times O(2^n \times n)$

04.00

$$O(2^n)$$

~~$O(n \times 2^n)$~~

05.00

06.00