



# Agent-based Systems

Paolo Turrini

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# Introduction

# Timetable

## CS404 - Agent Based Systems

Weeks: 16 (14 Jan 2019-20 Jan 2019)

	09:00	10:00	11:00	12:00	13:00	14:00	15:00	16:00	17:00	18:00
Mon						CS404L Agent Based Systems 15-24	140 MS.02 TURNING P			
Tue							CS404S Agent Based Systems 16-24	35 CS404S Agent Based Systems 16-24	35 MS.05 TURNING P	
Wed										
Thu									CS404L Agent Based Systems 15-24	140 WOODS-SCARLEN TURNING P
Fri							CS404L Agent Based Systems 15-24	140 MS.02 TURNING P		
Sat										
Sun										

# The module

**Labs** five in total, every other week, starting from the next

**Coursework** 50% of the mark (deadline early April)

**Exam** 50% of the mark

# Lectures

**Location** Available online. It changes.

**Description** Syllabus, notes and material on the course webpage

**Capture** **On** (but I would attend the lectures)

**Homepage** <https://warwick.ac.uk/fac/sci/dcs/teaching/modules/cs404/>

**Exercises** Questions on explained material

**Tutors** There will be at least one tutor each time

**Exams** Some exercises are previous exam papers of mine

**Solutions** Key exercises will come with model answers

**Tip 1:** go to the labs and do all the exercises.

**Tip 2:** write everything down, even when you think it's trivial.

- The coursework will be a Python-based implementation of a strategic agent, participating in an auction. The goal is to make money.
- You are going to be playing against one other.
- It's not a programming exercise, although it involves programming. The focus is on the strategic behaviour itself.
- There will be a coursework handout lecture (week 3), where everything will be explained in details, and a coursework hints lecture (week 10), to discuss some basics, in case you are lost.

- Questions on the material explained.
- Focus will be on precise applications of learnt techniques.
  - This means no questions like:  
“What’s your view on Artificial Intelligence?”
  - But rather:  
“This is the problem: calculate the solution”
- It won’t be a memory game.  
The goal is to reward the understanding of the subject.
- Everything I explain is examinable.



# Interaction

- This is a course on multi-agent interaction, and I like interaction.
- The vast majority of the slides will be available before the lecture, but some will not, because I want you to think on the spot.
- All the slides will be available after the lecture.
- Don't be scared of saying wrong things (before the exam).

# Questions

- 1 Ask them in class
- 2 Come and talk to me after the lectures
- 3 Office hour: Monday and Friday 15:00-16:00 (MSB227)
- 4 Send me an email ([p.turrini@warwick.ac.uk](mailto:p.turrini@warwick.ac.uk))

# Artificial Intelligence with many agents

**The toolbox for the design of interactive decision-makers**

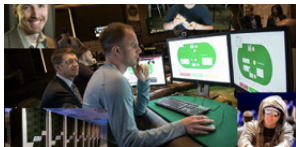
# Artificial Intelligence with many agents



AlphaGo  
Defeats the World Champion 4-1  
(March 2016)

**The toolbox for the design of interactive decision-makers**

# Artificial Intelligence with many agents



## Libratus

Wins 1.7M dollars from top players  
(January 2017)

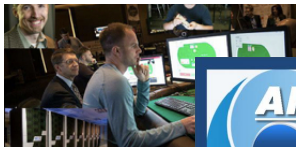


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# Artificial Intelligence with many agents



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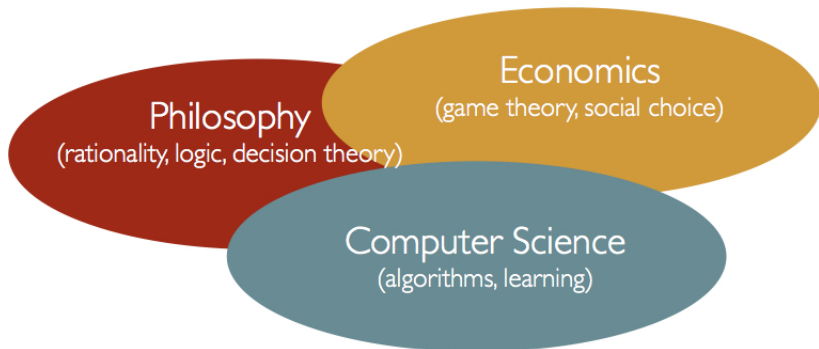


AlphaGo  
Defeats the World Champion 4-1  
(March 2016)

AlphaZero  
Defeats the best open source engine  
28-0, after 9 hours of self-training  
(December 2017)

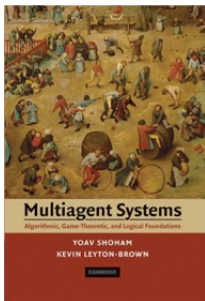
**The toolbox for the design of interactive decision-makers**

# Connections



**Important private investments:** Google DeepMind

# The starting kit



Y. Shoham and K. Leyton-Brown  
Multiagent Systems: Algorithmic,  
Game-Theoretic and Logical Foundations  
[www.masfoundations.org](http://www.masfoundations.org)

Helpful background basics


Discrete mathematics, probabilities, algorithms, logic.

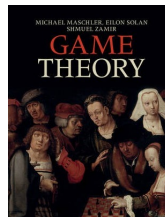


# Other important references

 M. Maschler, E. Solan and S. Zamir  
Game Theory

 Y. Shoham and K. Leyton-Brown  
Essentials of Game Theory

 S. Russel and P. Norvig  
Artificial intelligence: a modern approach



One of the most exciting books ever written

It's very useful to look at different ways of presenting the same topic!

# Acknowledgments

This course would not have been possible without:



Nathan Griffiths  
(the previous lecturer)



Ulle Endriss  
(and his material on game theory)



Mr (soon Dr) Alex Carver  
(He who created the coursework)

# Agents

An **agent** is a formal model of decision-maker which:

- lives in a world, made of states
- is goal-oriented (wants to achieve some states, or sequences of states)
- has a view-point on the world
- can take actions to change the world into a different state

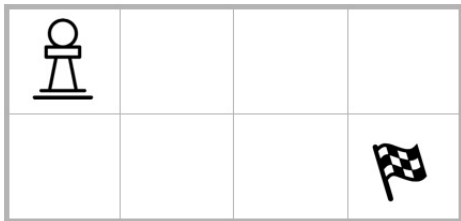
AlphaGo is an agent,


A Dyson vacuum cleaner is an agent,

James Bond is an agent.

An abstract comprehensive theory of (rational) decision-making

# One agent

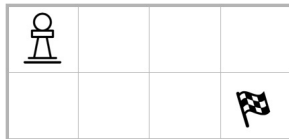


- *Up, Down, Left, Right*
- Wants to catch 
- Hitting the wall results in no movement

**Goal:** Devise a plan to reach the objective.

# Complications

- actions might not be fully controllable (uncertain actions, noisy environment etc)
- the agent might not know how states are connected
- the agent might not know their goal
- time might decrease the value of the goal
- the state space can be huge, and too difficult to fully calculate



**We can see this as a constrained optimisation problem:**

“What is the best course of actions I can take,  
**given** the information I have about the interaction?”

# Rationality



Robert J. Aumann  
Nobel Prize in Economics

*'A person's behaviour is **rational** if it is in their best interests, given their information.'*

**Agents** (not only humans) can be rational!

# Rational Agents



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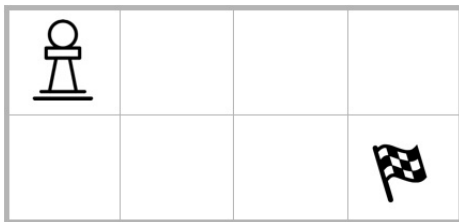
# Multi-agent Systems







A **multi-agent system** is any situation with more than one agent.

- their goals might be interdependent (one against the other, or they need one another to achieve them)
- each have view points on the world, the other agents, and view points about the other agents viewpoints!
- their choices are interdependent, too: the world state changes as a function of what **all** agents do.



# More than one agent

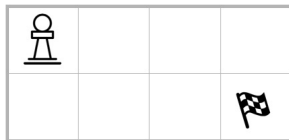


-  moves
-  moves too!
-  wants to catch 
-  wants to catch 

Complex strategic behaviour

# More complications

- turn-taking or simultaneous actions?
- cooperation or competition?
- difference in view-points, are agents playing the same game?
- many agents, and many games played at the same time



## A complex constrained optimisation problem:

“What is the best action I can take, **given** the information I have about the environment and the opponents, and the information I have about the information they have about me, and the information I have about the information they have about the ... (too long to write) ...?”

# Week 1, Lecture 2: Strategies

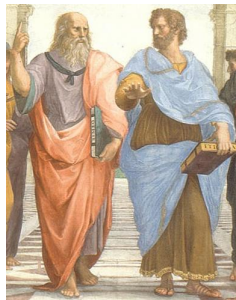
- A formal definition of the world:
  - states
  - transitions
  - actions
  - winning conditions
- Strategies, as opposed to actions.
- Results on 'simple' games: Chess and Zermelo's theorem.



The very basics of strategic behaviour in multi-agent interaction.

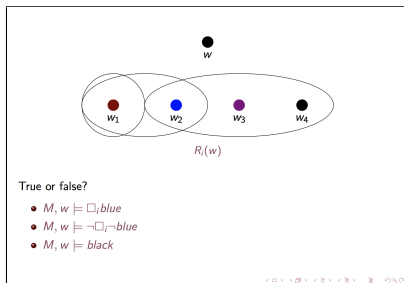
# Week 1, Lecture 3: Knowledge

- What it means “to know” something:
  - a mathematical definition of knowledge
  - properties of knowledge
- What it means to know something, “together”:
  - general knowledge
  - distributed knowledge
  - common knowledge
- Knowing that versus knowing how



# Week 2: Logic

- Agents that can reason
  - What are inferences?
  - Why are they useful?
- Modelling reasoning in logic
  - Restricting the language
  - Expressivity and complexity
- Modal logic
  - Worlds and possible worlds
  - Connection with set theory



# Week 2: Logic

- How to reason with knowledge:
  - epistemic logic
- How to reason with strategies:
  - coalition logic
- How to reason with goals and preferences:
  - preference logic

$$K_i\varphi \rightarrow K_iK_i\varphi$$

"if I know something, then I know that I know it"

Expressing complex strategic reasoning within one simple language

# Week 3: Expected Utility

- Logical languages:
  - succinct
  - elegant correspondences
- But, sometimes, we need a more fine-grained structure
- From formulas to numbers

A **probability space** or **probability model** is a sample space  $\Omega$  with an assignment  $P(w)$  for every  $w \in \Omega$  s.t.

$$0 \leq P(w) \leq 1$$

$$\sum_w P(w) = 1$$

## Week 3: Expected Utility

- Probabilistic beliefs:
  - conditional probability
  - Bayesian reasoning
- utility and preferences
  - von Neumann-Morgenstern Representation Theorem
- Rationality as expected utility

Lottery  $A = [p, A_1; (1 - p), A_2]$

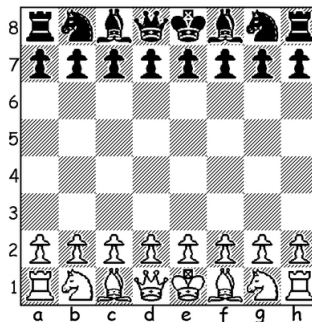


The mathematics of rational behaviour



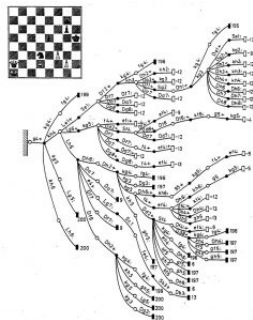
# Week 4: Games

- Rational players
- Interdependent actions
- Conflict



# Week 4: Games

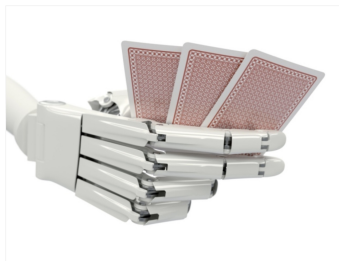
- Strategic games:
  - equilibria
  - expected utility in games
- Extensive games:
  - backwards induction
  - relation to strategic games
  - imperfect and incomplete information



The mathematics of rational behaviour in interaction

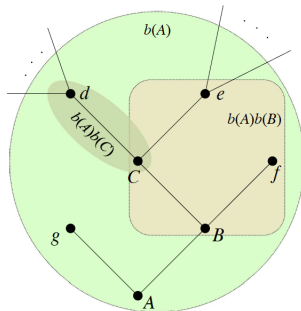
# Week 5: Knowing the game

- What do we need to know in order to play rationally?
- We might not be able to fully assess the consequences of our own decisions
- Exploiting the opponents weaknesses and the team-mates' strengths



# Week 5: Knowing the game

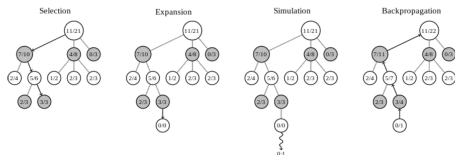
- Common knowledge of rationality and backwards induction (Aumann's Theorem)
- Strategic reasoning in games with limited foresight (like in chess)
- Bluffing, risk, and counterfactual regret minimization (like in poker)



Procedures for complex strategic thinking  
(in games that matter to AI)

# Week 6: MDPs and Learning

- Complicating further:
  - discounting
  - patience
  - stochastic actions
- Trial and error:
  - self-play
  - learning from experience

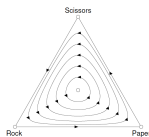


# Week 6: MDPs and Learning

- Markov Decision Processes (modelling and optimisation)
- Reinforcement Learning (basics)
- Multi-agent Reinforcement Learning (and connection with repeated games)

## Rock-Paper-Scissors

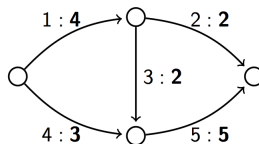
	R	P	S
R	0	-1	+1
P	+1	0	-1
S	-1	+1	0



Modelling rationality with partial observation, in interaction

# Week 7: Cooperation

- Agents working together
- Collective decision-making
- Competing within fair rules



# Week 7: Cooperation

$$\begin{array}{lll} v(\{1\}) = 0 & v(\{1, 2\}) = 7 & v(N) = 10 \\ v(\{2\}) = 0 & v(\{1, 3\}) = 6 & \\ v(\{3\}) = 0 & v(\{2, 3\}) = 5 & \end{array}$$

- Cooperative Games  
(intuitions and models)
- Solution Concepts  
(Stability)

The mathematics of cooperative behaviour



## Week 8: Social Choice

- Voting (intuitions, models)
- Different rules and interrelations
- What are good voting rules?

$$\triangle \succ_1 \bigcirc \succ_1 \square$$

$$\square \succ_2 \triangle \succ_2 \bigcirc$$

$$\bigcirc \succ_3 \square \succ_3 \triangle$$

---

?

## Week 8: Social Choice

	<i>A</i>	<i>B</i>	<i>C</i>
Judge 1:	yes	yes	yes
Judge 2:	no	yes	no
Judge 3:	yes	no	no
Majority:	yes	yes	no

*A*: witness is reliable

*B*: if witness is reliable then guilty

*C*: guilty

note that  $A \wedge B \rightarrow C$

- Desirable properties (and corresponding rules)
- Putting them together (impossibility theorems)
- Logic-based voting (judgment aggregation)

Designing procedures for collective decision-making

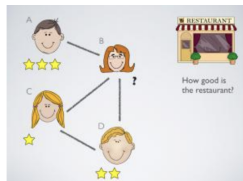
# Week 9: Social Agents

- How to divide resources fairly?
- How to form coalitions fairly?
- How to design fair evaluation systems?



# Week 9: Social Agents

- Fair division (intuitions, protocols)
- Matching (Gale-Shapley Algorithm)
- Social Networks (and online rating)



Designing cooperation and competition, together

# Week 10: Recap

- Coursework hints for those who are hopelessly lost
- Review 1 (your input matters!)
- Review 2 (same here)

# What we have seen

- The course plan
- Agents: first definition
- Agents and multi-agent systems
- Rationality

# Coming next

- Modelling actions, plays and wins
- Strategies