

Vector Autoregression (VAR) models, particularly regarding stationarity requirements:

1. Basic Differences:
  - VAR models are used for stationary time series
  - VECM models are specifically designed for non-stationary series that are cointegrated
2. Stationarity Requirements: For VAR:
  - All variables must be stationary at the same level
  - Usually requires differencing of variables until they become stationary
  - Works with  $I(0)$  variables (already stationary)

For VECM:

- Variables should be non-stationary in levels but have same order of integration
  - Typically uses  $I(1)$  variables that are cointegrated
  - No need to difference variables as VECM captures long-run relationships
3. Long-run Relationships:
    - VAR doesn't capture long-run equilibrium relationships
    - VECM includes an error correction term that captures long-run equilibrium adjustments
  4. When to Use Each: Use VAR when:
    - Variables are already stationary
    - No cointegration exists between variables

Use VECM when:

- Variables are non-stationary but cointegrated
- You want to analyze both short-run dynamics and long-run relationships

So, regarding your specific question about stationarity levels:

- For VAR: Yes, variables must be stationary at the same level
- For VECM: Variables must be integrated of the same order (usually  $I(1)$ ) but are not stationary in their levels

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So, regarding your specific question about stationarity levels:

- For VAR: Yes, variables must be stationary at the same level
  - For VECM: Variables must be integrated of the same order (usually  $I(1)$ ) but are not stationary in their levels
  - Both series need first differencing to become stationary
  - Their levels show trending behavior
  - If cointegrated, they share a long-run equilibrium relationship
  - VECM captures both:
    - Long-run relationship (levels)
    - Short-run dynamics (differences)
5. Testing Process:
1. First, test for unit roots in levels
  2. Confirm variables are  $I(1)$
  3. Test for cointegration
  4. If cointegrated, proceed with VECM
  6. Key Point: The magic of VECM is that it can work with non-stationary data directly because:
    - It models the long-run relationship between non-stationary variables
    - The error correction term ensures the system returns to equilibrium
    - The differences handle short-run dynamics