

$$\text{Var}(AE) = A \text{Var}(E) A^T$$

$E$  is assumed to follow multivariate norm. dist. with mean vector 0 + covariance matrix  $\sigma^2 I$

$$\hat{\beta} = (X^T X)^{-1} X^T y \quad \text{derivation: sub } y = X\beta + E$$

$$\text{Var}(\hat{\beta}) = (X^T X)^{-1} \sigma^2 \quad \hat{\beta} = (X^T X)^{-1} X^T (X\beta + E)$$

$$\hat{\sigma}^2 = \frac{1}{N-p-1} \sum_{i=1}^N (y_i - \hat{y}_i)^2 = (X^T X)^{-1} X^T X \beta + \cancel{X^T X} \beta - \cancel{X^T X} \beta + (X^T X)^{-1} X^T E$$

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta = \beta + (X^T X)^{-1} X^T E$$

$$Z_j = \frac{\hat{\beta}_j}{\hat{\sigma} \sqrt{v_j}} \quad v_j = j^{\text{th}} \text{ diagonal of the cov-var matrix } X X^T$$

Since  $\beta$  is a constant vector, its variance is 0, so we only need to consider the other term

avg reduction in RSS per addit. param

let  $A = (X^T X)^{-1} X^T$  for eqn. above

$$\text{Var}(\hat{\beta}) = \text{Var}((X^T X)^{-1} X^T E)$$

$$= (X^T X)^{-1} X^T \text{Var}(E) [X^T X]^{-1}$$

$$= (X^T X)^{-1} X^T \text{Var}(E) X (X^T X)^{-1}$$

$$F = \frac{(RSS_0 - RSS_1) / (p_1 - p_0)}{RSS_1 / (N - p_1 - 1)}$$

$RSS_0 =$  RSS of model with fewer parameters

$p_0 + 1$ , a subset of larger model

$RSS_1 =$  RSS of larger model with  $p_1 + 1$  params

sub  $\text{Var}(E) = \sigma^2 I$

$$\text{Var}(\hat{\beta}) = (X^T X)^{-1} X^T \sigma^2 I X (X^T X)^{-1}$$

$$= (X^T X)^{-1} \sigma^2$$