



DEPARTMENT OF COMPUTER SCIENCE

CircuitFlow: A Domain Specific Language for Dataflow Programming

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Declaration

This dissertation is submitted to the University of Bristol in accordance with the requirements of the degree of MEng in the Faculty of Engineering. It has not been submitted for any other degree or diploma of any examining body. Except where specifically acknowledged, it is all the work of the Author.

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Contents

1	Introduction	1
2	Background	3
2.1	Dataflow Programming	3
2.1.1	The Benefits	4
2.1.2	Dataflow Diagrams	4
2.1.3	Kahn Process Networks (KPNs)	5
2.2	Domain Specific Languages (DSLs)	5
2.2.1	Deep Embeddings	5
2.2.2	Shallow Embeddings	6
2.3	Higher Order Functors	6
2.3.1	Monadic Catamorphism with IFunctors	8
2.4	Data types à la carte	8
2.5	Dependently Typed Programming	10
2.5.1	DataKinds Language Extension	10
2.5.2	Singletons	10
2.5.3	Type Families	11
2.5.4	Heterogeneous Lists	11
2.5.5	Summary	12
2.6	Existential Types	12
2.7	Phantom Type Parameters	13
2.8	Monoidal Resource Theories	13
2.8.1	Preorders	13
2.8.2	Symmetric Monoidal Preorders	14
2.8.3	Wiring Diagrams	14
3	The Language	17
3.1	Language Requirements	17
3.2	Tasks	17
3.2.1	Data Stores	17
3.2.2	Task Constructor	18
3.3	Chains, A Dalliance	18
3.3.1	Trees as Chains	19
3.3.2	Evaluation	20
3.4	Solution: Circuit	21
3.4.1	Constructors	21
3.4.2	Combined Data Stores	23
3.4.3	Multi-Input Tasks	24
3.4.4	mapC operator	25
3.4.5	Completeness	25
3.4.6	Evaluation	26
4	Implementation	27
4.1	Requirements	27
4.2	Circuit AST	27
4.2.1	IFunctor	27
4.2.2	Indexed Data Types à la Carte	28

4.3	Process Network	29
4.3.1	Network Typeclass	29
4.3.2	The Basic Network Representation	30
4.4	Translation to a Network	30
4.4.1	Indexed Monadic Catamorphism	30
4.4.2	BuildNetworkAlg	31
4.4.3	The Translation	33
4.5	UUIDS	37
4.6	Failure in the Process Network	37
4.6.1	Maybe Monad	37
4.6.2	Except Monad	37
4.7	Evaluation	37
5	Examples	39
5.1	Machine Learning (Audio Playlist Generation)	39
5.1.1	Building the pre-processing Circuit	39
5.1.2	Building the prediction Circuit	42
5.2	Build System (lhs2TeX)	43
5.2.1	Building the Circuit	43
5.2.2	Using the Circuit	44
5.3	Types saving the day	45
6	Critical Evaluation	49
6.1	Runtime comparison	49
6.1.1	Lazy evaluation problems	49
6.2	Use of Library	49
6.2.1	Other Libraries	49
6.3	Type safety	49
7	Conclusion	51

List of Figures

2.1	Luigi dependency graph [11]	3
2.2	Quartz composer [6]	4
2.3	An example dataflow and its imperative approach.	4
2.4	A sequence of node firings in a KPN	5
2.5	An example wiring diagram	14
3.1	A Pipe (a) and its corresponding dataflow diagram (b).	19
3.2	The constructors in the Circuit library alongside their graphical representation.	21
3.3	A graphical representation of a task with multiple dependencies	24
5.1	A dataflow diagram for playlist generation	39
5.2	A dataflow diagram for pre-processing the song data	40
5.3	The first layer (a) and its corresponding dataflow diagram (b).	41
5.4	The second layer (a) and its corresponding dataflow diagram (b).	41
5.5	The third layer (a) and its corresponding dataflow diagram (b).	42
5.6	An example config file for the lhs2TeX build system	45
5.7	A Broken Luigi Example	46
5.8	A Broken Circuit Example	47

Notation and Acronyms

DSL Domain Specific Language

EDSL Embedded DSL

FIFO First-In First-Out

KPN Kahn Process Network

GPL General Purpose Language

DPN Data Process Network

DAG Directed Acyclic Graph

AST Abstract Syntax Tree

PID Process Identifier

Acknowledgements

Change this to something meaningful

It is common practice (although totally optional) to acknowledge any third-party advice, contribution or influence you have found useful during your work. Examples include support from friends or family, the input of your Supervisor and/or Advisor, external organisations or persons who have supplied resources of some kind (e.g., funding, advice or time), and so on.

Chapter 1

Introduction

Write an introduction (do near the end)

Chapter 2

Background

2.1 Dataflow Programming

Dataflow programming is a paradigm that models applications as a directed graph. The nodes of the graph have inputs and outputs and are pure functions, therefore have no side effects. It is possible for a node to be a: source; sink; or processing node. A source is a read-only storage: it can be used to feed inputs into processes. A sink is a write-only storage: it can be used to store the outputs of processes. Processes will read from either a source or the output of another process, and then produce a result which is either passed to another process or saved in a sink. Edges connect these nodes together, and define the flow of information.

Example - Data Pipelines A common use of dataflow programming is in pipelines that process data. This paradigm is particularly helpful as it helps the developer to focus on each specific transformation on the data as a single component. Avoiding the need for long and laborious scripts that could be hard to maintain. One example of a data pipeline tool that makes use of dataflow programming is Luigi [22]. An example dataflow graph produced by the tool is shown in Figure 2.1

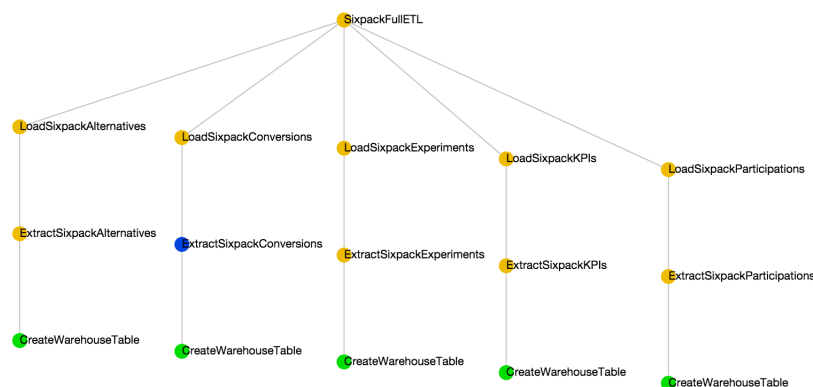


Figure 2.1: Luigi dependency graph [11]

Example - Quartz Composer Apple developed a tool included in XCode, named Quartz Composer, which is a node-based visual programming language [1]. As seen in Figure 2.2, it uses a visual approach to programming connecting nodes with edges. This allows for quick development of programs that process and render graphical data, without the user having to write a single line of code. This means that even non-programmers are able to use the tool.

Example - Spreadsheets A widely used example of dataflow programming is in spreadsheets. A cell in a spreadsheet can be thought of as a single node. It is possible to specify dependencies to other cells through the use of formulas. Whenever a cell is updated it sends its new value to those who depend on it, and so on. Work has also done to visualise spreadsheets using dataflow diagrams, to help debug ones that are complex [9].



Figure 2.2: Quartz composer [6]

2.1.1 The Benefits

Visual The dataflow paradigm uses graphs, which make programming visual. It allows the end-user programmer to see how data passes through the program, much easier than in an imperative approach. In many cases, dataflow programming languages use drag and drop blocks with a graphical user interface to build programs. For example, Tableau Prep [26], that makes programming more accessible to users who do not have programming skills.

Implicit Parallelism Moore's law states that the number of transistors on a computer chip doubles every two years [19]. This meant that the chips' processing speeds also increased in alignment with Moore's law. However, in recent years this is becoming harder for chip manufacturers to achieve [3]. Therefore, chip manufactures have had to turn to other approaches to increase the speed of new chips, such as multiple cores. It is this approach the dataflow programming can effectively make use of. Since each node in a dataflow is a pure function, it is possible to parallelise implicitly. No node can interact with another node, therefore there are no data dependencies outside of those encoded in the dataflow. Thus eliminating the ability for a deadlock to occur.

2.1.2 Dataflow Diagrams

Dataflow programs are typically viewed as a graph. An example dataflow graph along with its corresponding imperative approach, can be found in Figure 2.3. The nodes 100, X , and Y are sources as they are only read from. C is a sink as it is wrote to. The remaining nodes are all processes, as they have some number of inputs and compute a result.

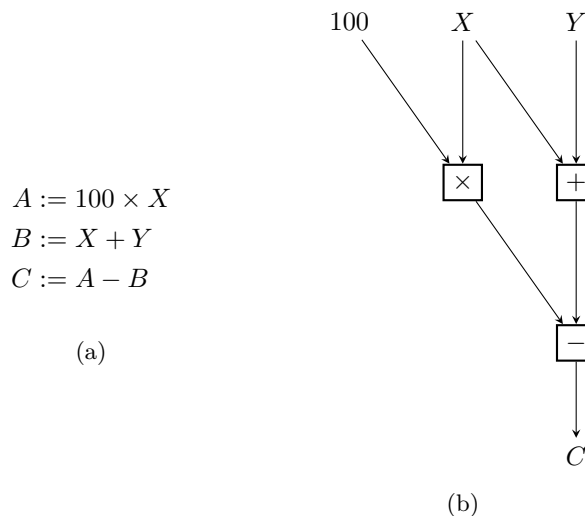


Figure 2.3: An example dataflow and its imperative approach.

In this diagram is possible to see how implicit parallelisation is possible. Both A and B can be calculated simultaneously, with C able to be evaluated after they are complete.

2.1.3 Kahn Process Networks (KPNs)

A method introduced by Gilles Kahn, Kahn Process Networks (KPNs) realised the concept of dataflow networks through the use of threads and unbounded First-In First-Out (FIFO) queues [13]. The FIFO queue is one where the items are output in the same order that they are added. A node in the dataflow becomes a thread in the process network. Each FIFO queue represents the edges connecting the nodes in a graph. The threads are then able to communicate through FIFO queues. The node can have multiple input queues and is able to read any number of values from them. It will then compute a result and add it to an output queue. Kahn imposed a restriction on a process in a KPNs that the thread is suspended if it attempts to fetch a value from an empty queue. The thread is not allowed to test for the presence of data in a queue.

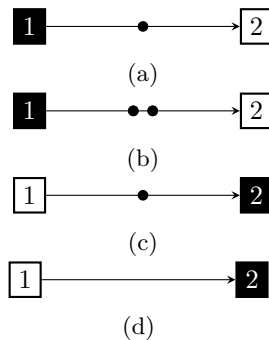


Figure 2.4: A sequence of node firings in a KPN

Parks described a variant of KPNs, called Data Process Networks (DPNs) [16]. They recognise that if functions have no side effects then they have no values to be shared between each firing. Therefore, a pool of threads can be used with a central scheduler instead.

2.2 Domain Specific Languages (DSLs)

A DSL is a programming language that has a specialised domain or use-case. This differs from a General Purpose Language (GPL), which can be applied across a larger set of domains, and are generally turing complete. HTML is an example of a DSL: it is good for describing the appearance of websites, however, it cannot be used for more generic purposes, such as adding two numbers together.

Approaches to Implementation DSLs are typically split into two categories: standalone and embedded. Standalone DSLs require their own compiler and typically their own syntax; HTML would be an example of a standalone DSL. Embedded DSLs (EDSLs) use an existing language as a host, therefore they use the syntax and compiler from the host. This means that they are easier to maintain and often quicker to develop than standalone DSLs. An EDSL, can be implemented using two differing techniques: deep and shallow embeddings.

2.2.1 Deep Embeddings

A deep embedding is when the terms of the DSL will construct an Abstract Syntax Tree (AST) as a host language datatype. Semantics can then be provided later on with evaluation functions. Consider the example of a minimal non-deterministic parser combinator library [29], which will be a running example for this chapter.

```
data Parserd (a :: Type) where
  Satisfyd :: (Char → Bool) → Parserd Char
  Ord      :: Parserd a → Parserd a → Parserd a
```

This can be used to build a parser that can parse the characters 'a' or 'b'.

```

aorbd :: Parserd Char
aorbd = Satisfyd (≡ 'a') `Ord` Satisfyd (≡ 'b')

```

However, this parser does not have any semantics, therefore this needs to be provided by the evaluation function `parse`.

```

parsed :: Parserd a → String → [(a, String)]
parsed (Satisfyd p) = λcase
  []      → []
  (t : ts') → [(t, ts') | p t]
parsed (Ord px py) = λts → parsed px ts ++ parsed py ts

```

The program can then be evaluated by the `parsed` function. For example, `parsed aorbd "a"` evaluates to `[('a', "")]`, and `parsed aorbd "c"` evaluates to `[]`.

A key benefit for deep embeddings is that the structure can be inspected, and then modified to optimise the user code: Parsley [28] makes use of such techniques to create optimised parsers. Another benefit, is that you can provide multiple interpretations, by specifying different evaluation functions. However, they also have drawbacks - it can be laborious to add a new constructor to the language. Since it requires that all functions that use the deep embedding be modified to add a case for the new constructor [24].

2.2.2 Shallow Embeddings

In contrast, a shallow approach is when the terms of the DSL are defined as first class components of the language. For example, a function in Haskell. Components can then be composed together and evaluated to provide the semantics of the language. Again a simple parser example can be considered.

```

newtype Parsers a = Parsers { parses :: String → [(a, String)] }
ors :: Parsers a → Parsers a → Parsers a
ors (Parsers px) (Parsers py) = Parsers (λts → px ts ++ py ts)
satisfys :: (Char → Bool) → Parsers Char
satisfys p = Parsers (λcase
  []      → []
  (t : ts') → [(t, ts') | p t])

```

The same `aorbs` parser can be constructed from these functions, avoiding the need for an intermediate AST.

```

aorbs :: Parsers Char
aorbs = satisfys (≡ 'a') `ors` satisfys (≡ 'b')

```

Using a shallow implementation has the benefit of being able add new ‘constructors’ to a DSL, without having to modify any other functions. Since each ‘constructor’, produces the desired result directly. However, this causes one of the main disadvantages of a shallow embedding - the structure cannot be inspected. This means that optimisations cannot be made to the structure before evaluating it.

2.3 Higher Order Functors

It is possible to capture the shape of an abstract datatype as a `Functor`. The use of a `Functor` allows for the specification of where a datatype recurses. Consider an example on a small expression language:

```

data Expr = Add Expr Expr
          | Val Int

```

The recursion within the `Expr` datatype can be removed to form `ExprF`. The recursive steps can then be specified in the `Functor` instance.

```

data ExprF f = AddF f f
              | ValF Int

```

```
instance Functor ExprF where
  fmap f (AddF x y) = AddF (f x) (f y)
  fmap f (ValF x)   = ValF x
```

To regain a datatype that is isomorphic to the original datatype, the recursive knot need to be tied. This can be done with `Fix`, to get the fixed point of `ExprF`:

```
data Fix f = In (f (Fix f))
type Expr' = Fix ExprF
```

There is, however, one problem: a `Functor` expressing the a parser language is required to be typed. Parsers require the type of the tokens being parsed. For example, a parser reading tokens that make up an expression could have the type `Parser Expr`. A `Functor` does not retain this type information needed in a parser.

IFunctors Instead a type class called `IFunctor` [17] — also known as `HFunctor` [12] — can be used, which is able to maintain the type indices. This makes use of \leadsto , which represents a natural transformation [15] from `f` to `g`. `IFunctor` can be thought of as a functor transformer: it is able to change the structure of a functor, whilst preserving the values inside it. Whereas a functor changes the values inside a structure.

```
type ( $\leadsto$ ) f g =  $\forall a. f a \rightarrow g a$ 
class IFunctor iF where
  imap :: (f  $\leadsto$  g)  $\rightarrow$  iF f  $\leadsto$  iF g
```

The shape of `Parser` can be seen in `ParserF` where the `f` marks the recursive spots. The type `f` represents the type of the children of that node. In most cases this will be itself.

```
data ParserF (f :: *  $\rightarrow$  *) (a :: *) where
  SatisfyF :: (Char  $\rightarrow$  Bool)  $\rightarrow$  ParserF f Char
  OrF      :: f a  $\rightarrow$  f a  $\rightarrow$  ParserF f a
```

An `IFunctor` instance can be defined, which follow the same structure as a standard `Functor` instance.

```
instance IFunctor ParserF where
  imap _ (SatisfyF s) = SatisfyF s
  imap f (OrF px py) = OrF (f px) (f py)
```

`Fix` is used to get the fixed point of a `Functor`, to get the indexed fixed point `IFix` can be used.

```
newtype IFix iF a = In (iF (IFix iF) a)
```

The fixed point of `ParserF` is `Parserfixed`.

```
type Parserfixed = IFix ParserF
```

In a deep embedding, the **AST** can be traversed and modified to make optimisations, however, it may not be the best representation when evaluating it. This means that it might be transformed to a different representation. In the case of a parser, this could be a stack machine. Now that the recursion in the datatype has been generalised, it is possible to create a mechanism to perform this transformation. An indexed *catamorphism* is one such way to do this, it is a generalised way of folding an abstract datatype. The use of a catamorphism removes the recursion from any folding of the datatype. This means that the algebra can focus on one layer at a time. This also ensures that there is no re-computation of recursive calls, as this is all handled by the catamorphism. The commutative diagram below describes how to define a catamorphism, that folds an `IFix iF a` to a `f a`.

$$\begin{array}{ccc}
\text{iF (IFix iF) a} & \xrightarrow{\text{imap (icata alg)}} & \text{iF f a} \\
\text{inop} \uparrow \downarrow \text{In} & & \downarrow \text{alg} \\
\text{IFix iF a} & \xrightarrow{\text{icata alg}} & \text{f a}
\end{array}$$

`icata` is able to fold an `IFix iF a` and produce an item of type `f a`. It uses the algebra argument as a specification of how to transform a single layer of the datatype.

```
icata :: IFunctor iF => (iF f ~> f) -> IFix iF ~> f
icata alg (lIn x) = alg (imap (icata alg) x)
```

The resulting type of `icata` is `f a`, therefore the `f` has kind `* -> *`. This could be `IFix ParserF`, which would be a transformation to the same structure, possibly applying optimisations to the [AST](#).

2.3.1 Monadic Catamorphism with IFunctors

Using an indexed catamorphism, allows for principled recursion and makes it easier to define a fold over a data type, as any recursive step is abstracted from the user. However, there may be times when there is a need for monadic computations in the algebra. To be able to do this a monadic catamorphism is defined:

```
cataM :: (Traversable f, Monad m) => (forall a. f a -> m a) -> Fix f -> m a
cataM algM (lIn x) = algM <-< mapM (cataM algM) x
```

This catamorphism follows a similar pattern to a standard catamorphism, however, it does not have the `Functor` constraint. Instead it constrains `f` by `Traversable`: this type class still requires that `f` is a functor, it just provides additional functions such as a monadic map — `mapM :: Monad m => (a -> m b) -> fa -> m (fb)`. This allows the monadic catamorphism to be applied recursively on the data type being folded.

This technique can also be applied to indexed catamorphisms, however to do so an indexed monadic map has to be introduced. This will be included as part of the `IFunctor` type class.

```
class IFunctor iF where
  imap :: (f ~> g) -> iF f ~> iF g
  imapM :: Monad m => (forall a. f a -> m (g a)) -> iF f a -> m (iF g a)
```

`imapM` is the indexed equivalent of `mapM`, it performs a natural transformation, but is capable of also using monadic computation.

The new `IFunctor` instance for `ParserF` is defined as:

```
instance IFunctor ParserF where
  imap = ... -- already defined
  imapM _ (SatisfyF s) = return (SatisfyF s)
  imapM f (OrF px py) = do
    px' <- f px
    py' <- f py
    return (OrF px' py')
```

The definition for `imapM` on `ParserF` is intuitively the same, however just uses `do`-notation instead. Making use of `imapM`, `icataM` is defined to be:

```
icataM :: (IFunctor iF, Monad m) => (forall a. iF f a -> m (f a)) -> IFix iF a -> m (f a)
icataM algM (lIn x) = algM <-< imapM (icataM algM) x
```

`icataM`, has a similar structure to all other catamorphisms defined, however it takes a monadic algebra, that can be used to transform the structure of the input type.

2.4 Data types à la carte

When building a [DSL](#) one problem that becomes quickly prevalent, the so called *Expression Problem* [27]. The expression problem is a trade off between a deep and shallow embedding. In a deep embedding, it is easy to add multiple interpretations to the [DSL](#) - just add a new evaluation function. However, it is not easy to add a new constructor, since all functions will need to be modified to add a new case for the constructor. The opposite is true in a shallow embedding.

One possible attempt at fixing the expression problem is *Data types à la carte* [25]. It combines constructors using the co-product of their signatures. This technique makes use of standard functors, however, an approach using higher-order functors is described in *Compositional data types* [2].

This is defined as:

```
data (iF :+: iG) f a = L (iF f a) | R (iG f a)
```

It is also the case that if both f and g are `IFunctors` then so is the sum $f :+: g$.

```
instance (IFunctor iF, IFunctor iG)  $\Rightarrow$  IFunctor (iF :+: iG) where
  imap f (L x) = L (imap f x)
  imap f (R y) = R (imap f y)
```

For each constructor it is possible to define a new data type and a `Functor` instance specifying where it recurses. This allows for the modularisation of the parser example:

```
data SatisfyF2 f a where
  SatisfyF2 :: (Char  $\rightarrow$  Bool)  $\rightarrow$  SatisfyF2 f Char
data OrF2 f a where
  OrF2 :: f a  $\rightarrow$  f a  $\rightarrow$  OrF2 f a
instance IFunctor SatisfyF2 where
  imap f (SatisfyF2 g) = SatisfyF2 g
instance IFunctor OrF2 where
  imap f (OrF2 px py) = OrF2 (f px) (f py)
```

By using `IFix` to tie the recursive knot, the `IFix (SatisfyF2 :+: OrF2)` data type would be isomorphic to the original `Parserd` datatype found in Section 2.2.1.

One problem that now exists, however, is that it is now rather difficult to create expressions. Revisiting the simple example of a parser for 'a' or 'b'.

```
exampleParser :: IFix (SatisfyF2 :+: OrF2) Char
exampleParser = Iln (R (OrF2 (Iln (L (SatisfyF2 ( $\equiv$  'a'))))) (Iln (L (SatisfyF2 ( $\equiv$  'b'))))))
```

It would be beneficial if there was a way to add these `Ls` and `Rs` automatically. Fortunately, there is a method using injections. The `:<` type class captures the notion of subtypes between `IFunctors`.

```
class (IFunctor iF, IFunctor iG)  $\Rightarrow$  iF :<: iG where
  inj :: iF f a  $\rightarrow$  iG f a
instance IFunctor iF  $\Rightarrow$  iF :<: iF where
  inj = id
instance (IFunctor iF, IFunctor iG)  $\Rightarrow$  iF :<: (iF :+: iG) where
  inj = L
instance (IFunctor iF, IFunctor iG, IFunctor iH, iF :<: iG)  $\Rightarrow$  iF :<: (iH :+: iG) where
  inj = R  $\cdot$  inj
```

Using this type class, smart constructors are defined:

```
inject :: (iG :<: iF)  $\Rightarrow$  iG (IFix iF) a  $\rightarrow$  IFix iF a
inject = Iln  $\cdot$  inj
satisfy2 :: (SatisfyF2 :<: iF)  $\Rightarrow$  (Char  $\rightarrow$  Bool)  $\rightarrow$  IFix iF Char
satisfy2 f = inject (SatisfyF2 f)
or2 :: (OrF2 :<: iF)  $\Rightarrow$  IFix iF a  $\rightarrow$  IFix iF a  $\rightarrow$  IFix iF a
or2 px py = inject (OrF2 px py)
```

Expressions can now be built using the constructors, such as `satisfy2 (\equiv 'a') `or2` satisfy2 (\equiv 'b')`.

A modular algebra can now be defined that provides an interpretation of this datatype.

```
newtype Size a = Size { unSize :: Int } deriving Num
class IFunctor iF  $\Rightarrow$  SizeAlg iF where
  sizeAlg :: iF Size a  $\rightarrow$  Size a
instance (SizeAlg iF, SizeAlg iG)  $\Rightarrow$  SizeAlg (iF :+: iG) where
  sizeAlg (L x) = sizeAlg x
  sizeAlg (R y) = sizeAlg y
instance SizeAlg OrF2 where
  sizeAlg (OrF2 px py) = px + py
```

```

instance SizeAlg SatisfyF2 where
  sizeAlg (SatisfyF2 f) = 1
eval :: SizeAlg iF ⇒ IFix iF a → Size a
eval = icata sizeAlg

```

The main benefit of this approach is modularity. Each constructor is given by its interpretation in isolation and only for interpretations that make sense for it. Additionally, existing interpretations are not affected by the addition of new constructors, such as `ApF2`. This helps to solve the expression problem.

2.5 Dependently Typed Programming

Although Haskell does not officially support dependently typed programming, there are techniques available that together can be used to replicate some of the experience.

2.5.1 DataKinds Language Extension

Through the use of the DataKinds language extension [30], all data types can be promoted to also be kinds and their constructors to be type constructors. When constructors are promoted to type constructors, they are prefixed with a `'`. This allows for more interesting and restrictive types.

Consider the example of a vector that also maintains its length. Peano numbers can be used to keep track of the length, which prevents a negative length for a vector. This is where numbers are defined as zero or a number `n` incremented by 1.

```

data Nat = Zero
         | Succ Nat

```

A vector type can now be defined that makes use of the promoted `Nat` kind.

```

data Vec :: Type → Nat → Type where
  Nil  :: Vec a 'Zero
  Cons :: a → Vec a n → Vec a ('Succ n)

```

The use of DataKinds can enforce stronger types. For example a function can now require that a specific length of vector is given as an argument. With standard lists, this would not be possible, which could result in run-time errors when the incorrect length is used. For example, getting the head of a list. Getting the head of an empty list an error will be thrown. For a vector, a `safeHead` function can be defined that will not type check if the vector is empty.

```

safeHead :: Vec a ('Succ n) → a
safeHead (Cons x _) = x

```

2.5.2 Singletons

DataKinds are useful for adding extra information back into the types, but how can information be recovered from the types? For example, could a function that gets the length of a vector be defined?

```

vecLength :: Vec a n → Nat

```

This is enabled through the use of singletons [8]. A singleton in Haskell is a type that has just one inhabitant. That is that there is only one possible value for each type. They are written in such a way that pattern matching reveals the type parameter. For example, the corresponding singleton instance for `Nat` is `SNat`. The structure for `SNat` closely flows that of `Nat`.

```

data SNat (n :: Nat) where
  SZero :: SNat 'Zero
  SSucc :: SNat n → SNat ('Succ n)

```

A function that fetches the length of a vector can now be definable.

```

vecLength2 :: Vec a n → SNat n
vecLength2 Nil      = SZero
vecLength2 (Cons x xs) = SSucc (vecLength2 xs)

```

Recovering an SNat

talk

```
class IsNat (n :: Nat) where nat :: SNat n
instance IsNat 'Zero where
  nat = SZero
instance IsNat n => IsNat ('Succ n) where
  nat = SSucc nat
```

2.5.3 Type Families

Now consider the possible scenario of appending two vectors together. How would the type signature look? This leads to the problem where two type-level Nats need to be added together. This is where Type Families [21] become useful, they allow for the definition of functions on types. Consider the example of appending two vectors together, this would require type-level arithmetic — adding the lengths together.

```
vecAppend :: Vec a n -> Vec a m -> Vec a (n :+ m)
```

This requires a `:+` type family that can add two Nats together.

2.5.4 Heterogeneous Lists

Heterogeneous lists [14] are a way of having multiple types in the same list. Rather than be parameterised by a single type, they instead make use of a type list, which is the list type promoted through DataKinds to be a kind, with its elements being types. Each element in the type list aligns with the value at that position in the list, giving its type. A heterogeneous list is defined as:

```
data HList (xs :: [Type]) where
  HNil    :: HList '[]
  HCons :: x -> HList xs -> HList (x' : xs)
```

This data type has two constructors:

- `HNil` represents the empty list. The type parameter is the empty type list `'[]`
- `HCons` allows a new element to be added to the list. The type parameter is the type of the item inserted consed onto the front of the types of the tail of the list.

Functions on HLists

Length using singletons and type families, it is possible to get the length of a `HList` in a type-safe way. Firstly, a type family is defined that is able to return the length of a type list.

```
type family Length (l :: [k]) :: Nat where
  Length '[]      = 'Zero
  Length (e' : l) = 'Succ (Length l)
```

`Length` follows a similar definition to the `length :: [a] -> Int` function defined in the `Prelude`. The base case of `Length` defines the length to be `'Zero`. The recursive case increments the length by 1 for each item in the list, until it reaches the base case.

Now a function is defined that returns the length of a `HList`:

```
lengthH :: HList xs -> SNat (Length xs)
lengthH HNil      = SZero
lengthH (HCons _ xs) = SSucc (lengthH xs)
```

This follows the same structure as the `Length` type family, however instead, of working with types it uses singleton values.

Take Another function that may be helpful with HLists is `take`. This will return the first `n` items from the list. If `n` is larger than the length of the list, then the whole list will be returned. Again, to be able to do this a new type family is needed – `Take`:

```
type family Take (n :: Nat) (l :: [k]) :: [k] where
  Take 'Zero    l      = '[]
  Take ('Succ n) '[]    = '[]
  Take ('Succ n) (e' : l) = e' : Take n l
```

The type family follows the same definition as the standard `take :: Int → [a] → [a]` as defined in the Prelude. Similar to the `lengthH` function, `takeH` follows the same structure as the type family:

```
takeH :: SNat n → HList xs → HList (Take n xs)
takeH SZero    l      = HNil
takeH (SSucc n) HNil   = HNil
takeH (SSucc n) (HCons x xs) = HCons x (takeH n xs)
```

Drop The final function used in this project on Hlists is one that can drop the first `n` elements. The `Drop` type family can be defined as:

```
type family Drop (n :: Nat) (l :: [k]) :: [k] where
  Drop 'Zero    l      = l
  Drop ('Succ _) '[]    = '[]
  Drop ('Succ n) (_' : l) = Drop n l
```

The `Drop` type family also closely follows the definition of `drop :: Int → [a] → [a]` from the Prelude, and its result is reflected in the values level just as with `lengthH` and `takeH`.

```
dropH :: SNat n → HList xs → HList (Drop n xs)
dropH SZero l = l
dropH (SSucc _) HNil = HNil
dropH (SSucc n) (HCons _ xs) = dropH n xs
```

```
type family (a :: Nat) :+ (b :: Nat) where
  a :+ 'Zero    = a
  a :+ 'Succ b = 'Succ (a :+ b)
```

2.5.5 Summary

Together these features allow for dependently typed programming constructs in Haskell:

- DataKinds allow for values to be promoted to types
- Singletons allow types to be demoted to values
- Type Families can be used to define functions that manipulate types.

2.6 Existential Types

Typically, when defining a data type in Haskell, every type variable that exists on the right hand side of the equals, must also be on the left hand side. For example, this is not allowed:

```
newtype Bad = Bad a
```

Existential types [18] are a way to allow this to happen, for example:

```
data Good = ∀a. Good a
```


One benefit of existential types is that the type variable no longer needs to be on the left hand side of the equals.

There is however, one problem with this approach, the variable will be a random unknown type. To avoid this problem constraints are typically added to the signature, so that there can be a set of functions that work with that variable. For example, the variable could have the `Show` constraint, so that we are able to use the `show` function with it:

```
data Showy =  $\forall a.$  Show a  $\Rightarrow$  Showy a
```

It would now be possible to build a list of items that can use the `show` function.

```
showList :: [Showy]
showList = [Showy 123, Showy "abc"]
```

This list can now store any value with a `Show` instance defined, by wrapping it in the `Showy` constructor.

2.7 Phantom Type Parameters

Phantom type parameters [4] could be considered the opposite of existential types. This is when a type variable only appears on the left hand side of the equals. The most basic example is `Const`, it has two type arguments, but only `a` is used on the right hand side:

```
newtype Const a b = Const a
```

Phantom type parameters can be used to store information in the types, which can act as further static constraints on the types. Consider an example revolving around locking doors: it should not be possible to lock a door that is open, first it has to be closed and then it can be locked. The state of the door can be represented by a data type that is promoted to a kind with the `DataKinds` extension. A door can be represented as a type with a phantom type variable, with kind `DoorState` that record the state of the door:

```
data DoorState = Open | Closed | Locked
data Door (state :: DoorState) where
  Door :: Door state
```

It would then be possible to define functions that can close and lock doors:

```
closeDoor :: Door 'Open  $\rightarrow$  Door 'Closed
lockDoor :: Door 'Closed  $\rightarrow$  Door 'Locked
```

The `closeDoor` function, enforces that only an open door can be given as input, similarly `lockDoor` prevents an open door from being locked.

2.8 Monoidal Resource Theories

Resource theories [5] are a branch of mathematics that allow for the reasoning of questions surrounding resources, for example:

- If I have some resources, can I make something?
- If I have some resources, how can I get what I want?

Resource theories provide a way to answer these questions.

2.8.1 Preorders

A preorder relation on a set X is denoted by \leq . The relation must obey two laws:

1. Reflexivity — $x \leq x$
2. Transitivity — if $x \leq y$ and $y \leq z$ then $x \leq z$.

A preorder is a pair (X, \leq) made up of a set and a preorder relation on that set.

2.8.2 Symmetric Monoidal Preorders

A symmetric monoidal structure (X, \leq, I, \otimes) on a preorder (X, \leq) has two additional components:

1. The monoidal unit — an element $I \in X$
2. The monoidal product — a function $\otimes : X \times X \rightarrow X$

To be a symmetric monoidal then the following laws must be satisfied:

1. Monotonicity — $\forall x_1, x_2, y_1, y_2 \in X$, if $x_1 \leq y_1$ and $x_2 \leq y_2$, then $x_1 \otimes x_2 \leq y_1 \otimes y_2$
2. Unitality — $\forall x \in X$, $I \otimes x = x$ and $x \otimes I = x$
3. Associativity — $\forall x, y, z \in X$, $(x \otimes y) \otimes z = x \otimes (y \otimes z)$
4. Symmetry — $\forall x, y \in X$, $x \otimes y = y \otimes x$

2.8.3 Wiring Diagrams

A wiring diagram is made up of: boxes that can have multiple inputs and outputs. The boxes can be arranged in series or in parallel. Figure 2.5, shows an example wiring diagram.

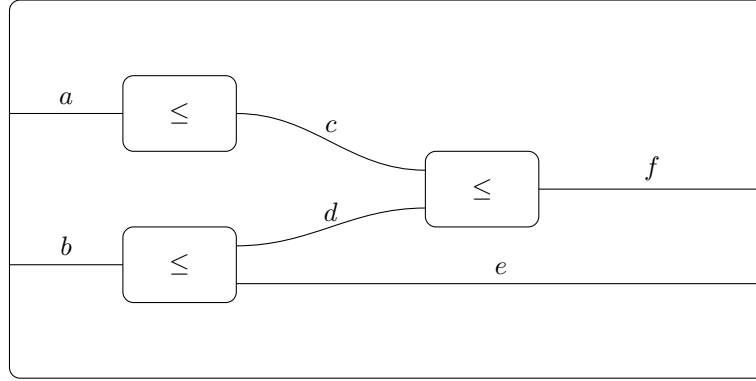


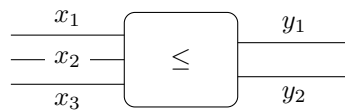
Figure 2.5: An example wiring diagram

A wiring diagram can be formalised as a symmetric monoidal preorder. Each element $x \in X$ can exist as the label on a wire. Two wires x and y , can be drawn in parallel:

$$\frac{x}{\frac{y}{}}$$

Two wires in parallel are considered to be the monoidal product $x \otimes y$. The monoidal unit is defined as a wire with the label I or no wire.

A box connects parallel wires on the left to parallel wires on the right. A wiring diagram is considered valid if the monoidal product of the left is less than the right.

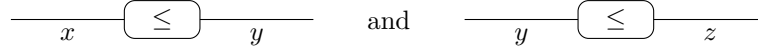


This example wiring diagram corresponds to the inequality $x_1 \otimes x_2 \otimes x_3 \leq y_1 \otimes y_2$.

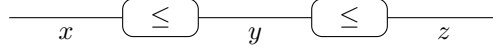
Reflexivity The reflexivity law states that $x \leq x$, this states that a diagram of one wire is valid.

$$\frac{x}{}$$

Transitivity The transitivity law says that if $x \leq y$ and $y \leq z$ then $x \leq z$. This corresponds to connecting two diagrams together in sequence. If both of the diagrams



are valid, then they can be joined together to obtain another valid diagram.



Monotonicity Monotonicity states that, if $x_1 \leq y_1$ and $x_2 \leq y_2$, then $x_1 \otimes x_2 \leq y_1 \otimes y_2$. This can be thought of as stacking two boxes on top of each other:



Unitality The unitality law states that $I \otimes x = x$ and $x \otimes I = x$, this means that a blank space can be ignored and that diagrams such as

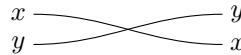


are valid.

Associativity The associativity law says that $(x \otimes y) \otimes z = x \otimes (y \otimes z)$, this states that diagrams can be built from either the top or bottom. In reality it is trivial to see how this is true with wires:



Symmetry The symmetry law states that $x \otimes y = y \otimes x$, this encodes the notion that a diagram is still valid even if the wires cross.

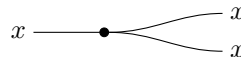


Discard Axiom There are times when there is no longer need to keep a value, it would be beneficial if it could be discarded. In a wiring diagram this is represented as:



This can be added as an additional axiom to the definition of a symmetric monoidal preorder: $\forall x \in X, x \leq I$

Copy Axiom The final axiom to add is the notion of copying a value: $\forall x \in X, x \leq x + x$. This can be represented in wiring diagram as a split wire:



Chapter 3

The Language

3.1 Language Requirements

For the design of the language to be considered a success, several criteria need to be met:

- **Describe any dataflow** — The combinators in the language should be able to describe any dataflow that the user needs.
- **Quickness to Learn** — The language should be quick and easy to learn. If it takes users too long to learn, they may never bother, meaning that the language will never be used.
- **Easy to write** — A user should be able to write programs easily. They should not have to spend time creating additional boilerplate code, where it is not necessary.
- **Easy to understand** — Any program written with this language should be easy to understand, so that users can review existing code and know what it will do.
- **Type-safe** — A feature missing in many dataflow tools is the lack of type checking. This causes problems later on in the development process with more debugging and testing needed. The language should be type-safe to avoid any run-time errors occurring where types do not match.

3.2 Tasks

Dataflow programming focuses on the transforming inputs to outputs. To be able to transform inputs this language will make use of tasks. They are responsible for reading from an input data source, completing some operation on the input, then finally writing to an output data sink. Tasks could take many different forms, for example they could be:

- A pure function — a function with type $a \rightarrow b$
- An external operation — interacting with some external system. For example, calling a terminal command.

A task could have a single input or multiple inputs, however, for now just a single input task will be considered. Multi-input tasks are explained further in Sub-Section [3.4.3](#)

3.2.1 Data Stores

Data stores are used to pass values between different tasks, this ensures that the input and output of tasks are closely controlled. They are used to represent different ways of storing values: one example could be a point to a CSV file. A data store can be defined as a type class, with two methods `fetch` and `save`:

Motivate further why a `DataStore` needs to exist — prevents the user from reading from a source incorrectly.

```

class DataStore f a where
  fetch :: f a → IO a
  save  :: f a → a → IO (f a)

```

A `DataStore` has two type parameters: where `f` is the type of `DataStore` being used and `a` is the type of the value stored inside it. The aptly named methods describe their intended function: `fetch` will fetch a value from a `DataStore`, and `save` will save a value. The `fetch` method takes a `DataStore` as input and will return the value stores inside. However, the `save` method may not be as self explanatory, since it has an extra `f a` argument. This argument can be thought of as a pointer to a `DataStore`: it contains the information needed to save. For example, in the case of a file store it could be the file name.

By implementing this as a type class, there can be many different implementations of a `DataStore`. The library comes with several pre-defined `DataStores`, such as a `VariableStore`. This can be thought of as an in memory storage between tasks.

```

data VariableStore a = Var a | Empty
instance DataStore VariableStore a where
  fetch (Var x) = return x
  save Empty x = return (Var x)

```

The `VariableStore` is the most basic example of a `DataStore`, a more complex example is a `FileStore`, which represents a pointer to a file:

```

newtype FileStore a = FileStore String
instance DataStore FileStore String where
  fetch (FileStore fname) = readFile fname
  save (FileStore fname) x = writeFile fname x >> return (FileStore fname)
instance DataStore FileStore [String] where
  fetch (FileStore fname) = readFile fname >> return . lines
  save (FileStore fname) x = writeFile fname (unlines x) >> return (FileStore fname)

```

The `FileStore` is only defined to store two different types: `String` and `[String]`. If a user attempts to store anything other than these two types then a compiler error will be thrown, for example:

```

ghci> save (FileStore "test.txt") (123 :: Int)
> No instance for (DataStore FileStore Int) arising from a use of ‘save’

```

Although a small set of `DataStores` are included in the library, the user is also able to add new instances of the type class with their own `DataStores`. Some example expansions, could be supporting writing to a database table, or a Hadoop file system.

3.2.2 Task Constructor

The type of a task details the inputs and outputs. A task is created via a constructor that takes two arguments: the function it represents and somewhere to store the output. This constructor makes use of GADTs syntax [20] so that constraints can be placed on the types used. It enforces that a `DataStore` must exist for the input and output types. This allows the task to make use of the `fetch` and `save` functions.

```

data Task (f :: Type → Type) (a :: Type) (g :: Type → Type) (b :: Type) where
  Task :: (DataStore f a, DataStore g b) ⇒ (f a → g b → IO (g b)) → g b → Task f a g b

```

When a `Task` is executed the stored function is executed, with the input being passed in as the first argument and the output “pointer” as the second argument. This returns an output `DataStore` that can be passed on to another `Task`.

3.3 Chains, A Dalliance

In a dataflow programming, one of the key aspects is the definition of dependencies between tasks in the flow. One possible approach to encoding this concept in the language, that was ultimately not up to scratch, is to make use of sequences of tasks — also referred to as chains. These chains compose tasks, based on their dependencies. A chain can be modelled with an abstract datatype:

```

data Chain (f :: Type → Type) (a :: Type) (g :: Type → Type) (b :: Type) where
  Chain :: Task f a g b → Chain f a g b
  Then :: Chain f a g b → Chain g b h c → Chain f a h c

```

free moniod? maybe yes it looks like what eddie did...

The `Chain` constructor wraps a `Task` in the `Chain` data type. This allows for them to be easily composed with other `Tasks`. Without this there would need to be an “empty” element, however, this could lead to the construction of a chain with no tasks. The `Then` constructor combines multiple chains to form a sequence of sequential tasks. To make this easier to use an operator `>>>` is defined that represents `Then`:

```

(>>>) :: Chain f a g b → Chain g b h c → Chain f a h c
(>>>) = Then

```

This can be now be used to join sequences of tasks together, for example:

```

task1 :: Task VariableStore Int      VariableStore String
task2 :: Task VariableStore String  FileStore      [String]
task3 :: Task FileStore      [String] VariableStore Int
sequence :: Chain VariableStore Int VariableStore Int
sequence = Chain task1 >>> Chain task2 >>> Chain task3

```

`sequence` will perform the three tasks in order, starting with `task1` and finishing with `task3`.

3.3.1 Trees as Chains

Now that tasks can be performed in sequence, the next logical step will be to introduce the concept of branching out. This results in a tasks output being given to multiple tasks, rather than just 1.

To do this a new abstract datatype is required. This will be used to form a list of `Chains`, conventionally the `[]` type would be used, however this is not possible as each chain will have a different type. This means that existential types will need to be used.

```

data Pipe where
  Pipe :: ∀ f a g b. (DataStore f a, DataStore g b) ⇒ Chain f a g b → Pipe
  And :: Pipe → Pipe → Pipe

```

The `And` constructor can be used to combine multiple chains together. Figure 3.1 shows the previous sequence, with a new `task4` which also uses the input from `task2`.

```

task4 :: Task FileStore [String] VariableStore String
branchExample :: Pipe
branchExample = Pipe (Chain task1 >>> Chain task2 >>> Chain task3)
                  `And`
                  Pipe (Chain task2 >>> Chain task4)

```

(a)

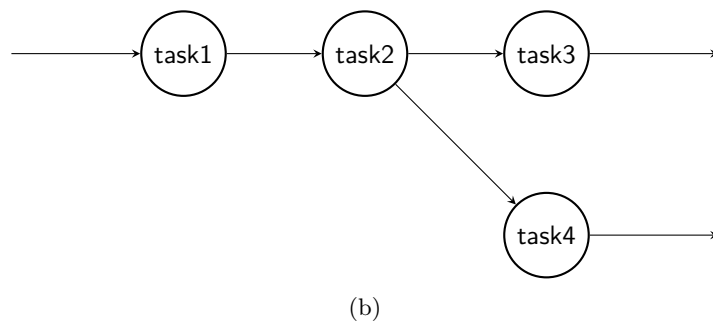


Figure 3.1: A `Pipe` (a) and its corresponding dataflow diagram (b).

However, there is a problem with this approach: to be able to form a network similar to that shown in Figure 3.1, the language will need to know where to join two Chains together. However, with the current definition of a Task, it is not possible to easily check the equivalence of two functions. Being able to check for equivalence will be key to defining a method to merge these chains together: it will need to match `task2` in the first chain with the `task2` in the second chain. Similarly, if a user wanted to use the same task multiple times, it would not be possible to differentiate between them. One approach to this would be to have unique identifiers for each task, such as PIDs.

Process Identifiers (PIDs) A Chain can be modified so that instead of storing a Task it instead stores a PID — a unique identifier for a task. However to do this a new PID data type is needed:

```
data PID (f :: Type → Type) (a :: Type) (g :: Type → Type) (b :: Type) where
  PID :: Int → PID f a g b
```

The PID data type has the same kind as a Task and makes use of phantom type parameters, to retain the same type information as a Task, whilst storing just an Int that can be used to identify it.

```
data Chain' (f :: Type → Type) (a :: Type) (g :: Type → Type) (b :: Type) where
  Chain' :: PID → f a g b → Chain' f a g b
  Then' :: Chain' f a g b → Chain' g b h c → Chain' f a h c
```

This new version of Chain named Chain', is almost identical in the way it behaves, however instead of storing a Task, it stores a PID.

This, however, leaves a key question, how do Tasks get mapped to PIDs. This can be done by employing the State monad. The state stores a map from PID to task and a counter for PIDs. As Tasks each have a different type a new wrapper datatype is required, making use of existential types, to close over the types, and produce values of apparently the same type. This is because a Map can only store one type. The Workflow monad is a type alias for the State monad, which stores the WorkflowState.

```
data TaskWrap = ∀ f a g b. TaskWrap (Task f a g b)
data WorkflowState = WorkflowState {
  pidCounter :: Int,
  tasks :: M.Map Int TaskWrap
}
type Workflow = State WorkflowState
```

An operation that is defined for the monad is `registerTask`. This takes a Task and returns a Chain that stores a PID inside it. Whenever a user would like to add a new task to the workflow, they register it. They can then use this returned value to construct multiple chains, which can now be joined easily by comparing the stored PID.

```
registerTask :: Task f a g b → Workflow (Chain' f a g b)
```

One benefit to this approach is that if the user would like to use a task again in a different place, they can simply register it again and use the new PID value.

3.3.2 Evaluation

☑ **Describe any Dataflow** This method would be capable of describing any dataflow, although in its current state, it can only support trees. The algorithm that would be used to join different chains together could be developed to allow them to rejoin onto another chain. This will allow for any Directed Acyclic Graph (DAG) to be defined.

☑ **Quickness to Learn** With only 4 different combinators (Chain, >>>, Pipe, And) and the Task constructor, this language should be simple to learn. There are only two main concepts the user needs to understand: how to join tasks into a chain and how to join chains together.

☑ **Easy to Write** Building chains is a very simple process, and allows the user to focus on the dependencies of one task. They do not need to be aware of the bigger picture. For example, adding a new `task5` that depends on `task2` in Figure 3.1. The user will just need to add one extra chain `task5 >>> task2`, which will have no effect on the existing chains.

try fix the
half if i
have time

☒ **Easy to Read** Although it is easy to write chains, this could lead to messy definitions with no structure. This will make it harder for a user to interpret an already defined collection of chains. Its possible that they will need to draw out some of the dependencies to further understand what is already defined.

☒ **Type-safe** Although a `Chain` can be well typed, the use of existential types to join chains together pose a problem. This causes the types to be ‘hidden’, this means that when executing these tasks, the types need to be recovered. This is possible through the use of `gcast` from the `Data.Typeable` library. However, this has to perform a reflection at run-time to compare the types. There is the possibility that the types could not matching and this would only be discovered at run-time. There is a mechanism to handle the failed match case, however, this does not fulfil the criteria of being fully type-safe.

Chains are not good enough Chains do not satisfy some of the key requirements that this library set out to solve, such as type safety. This could lead to crashes at run-time as the compiler is not able to fully verify that the system type-checks. Another approach could be to look to category theory, for ways to compose functions together in a type-safe way.

3.4 Solution: Circuit

This approach is inspired by monadic resource theory, which has a collection of mathematical operators for composing functions together. It uses parallel prefix circuits, described by Hinze [10], as a starting point for the design of the combinators. A set of constructors can be defined that are used to represent a **DAG**. The constructors seen in Figure 3.2 represent the behaviour of edges in the graph.

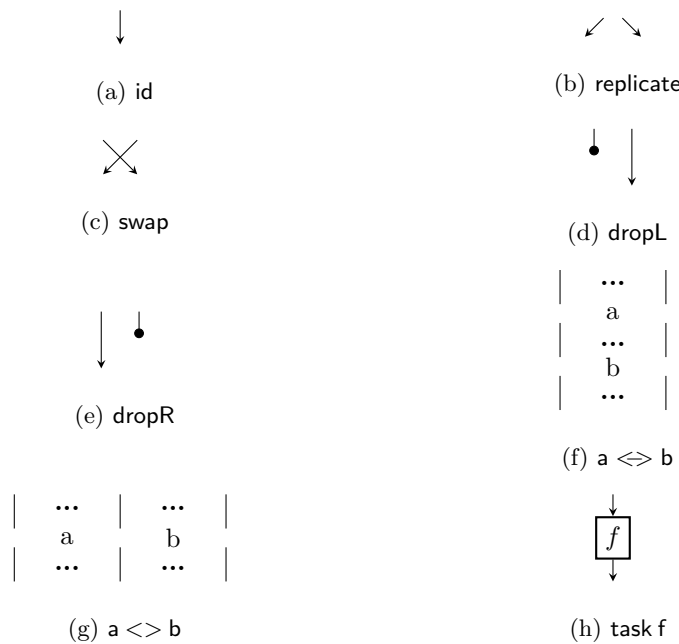


Figure 3.2: The constructors in the `Circuit` library alongside their graphical representation.

3.4.1 Constructors

Each of these constructors use strong types to ensure that they are combined correctly. A `Circuit` has 7 different type parameters:

```
Circuit (inputsStorageTypes :: [Type → Type]) (inputsTypes :: [Type]) (inputsApplied :: [Type])
        (outputsStorageTypes :: [Type → Type]) (outputsTypes :: [Type]) (outputsApplied :: [Type])
        (nInputs :: Nat)
```

A `Circuit` can be thought of as a list of inputs, which are processed and a resulting list of outputs are produced. To represent this it makes use of the `DataKinds` language extension [30], to use type-level lists

and natural numbers. Each parameter represents a certain piece of information needed to construct a circuit:

- `inputsStorageTypes` is a type-list of storage types, for example `'[VariableStore, CSVStore]` — these all have kind `* → *`.
- `inputsTypes` is a type-list of the types stored in the storage, for example `'[Int, [(String, Float)]]`.
- `inputsApplied` is a type-list of the storage types applied to the types stored, for example `'[VariableStore Int, CSVStore [(String, Float)]]`.
- `outputsStorageTypes`, `outputsTypes` and `outputsApplied` mirror the examples above, but for the outputs instead.
- `nInputs` is a type-level `Nat` that is the length of the input lists.

Although, to a human some of these types may seem irrelevant, GHC is not able to make all of the deductions itself, when type checking the code. It requires additional information, such as `inputsApplied` or `nInputs`.

In the language there are two different types of constructor, those that recurse and those that can be considered leaf nodes. The behaviour of both types of constructor is recorded within the types. For example, the `id` constructor has the type:

```
id :: DataStore '[f] '[a] ⇒ Circuit '[f] '[a] '[f a] '[f] '[a] '[f a] N1
```

It can be seen how the type information for this constructor states that it has 1 input value (`N1~SuccZero`) of type `f a` and it returns that same value. Each type parameter in `id` is a phantom type [4], since there are no values stored in the data type that use the type parameters. The rest of the constructors that are leaf nodes are: `replicate`, `swap`, `dropL`, and `dropR`:

```
replicate :: DataStore '[f] '[a] ⇒ Circuit '[f] '[a] '[f a] '[f, f] '[a, a] '[f a, f a] N1
swap      :: DataStore '[f, g] '[a, b] ⇒ Circuit '[f, g] '[a, b] '[f a, g b] '[g, f] '[b, a] '[g b, f a] N2
dropL     :: DataStore '[f, g] '[a, b] ⇒ Circuit '[f, g] '[a, b] '[f a, g b] '[g] '[b] '[g b] N2
dropR     :: DataStore '[f, g] '[a, b] ⇒ Circuit '[f, g] '[a, b] '[f a, g b] '[f] '[a] '[f a] N2
```

The `replicate` constructor states that a single input value of type `f a` should be input, and that value should then be duplicated and output. The `swap` constructor takes two values as input: `f a` and `g b`. It will then swap these values over, such that the output will now be: `g b` and `f a`. `dropL` will take two inputs: `f a` and `g b`. It will then drop the left argument and return just a `g b`. The `dropR` has the same behaviour as `dropL`, it just drops the right argument instead.

To be able to make use of the leaf nodes, they need to be combined in some way. To do this two new recursive constructors named ‘beside’ and ‘then’ will be used. However, before defining these constructors there are some tools that are required. This is due to the types no longer being concrete. For example, the input type list is no longer known: it can only be referred to as `fs` and `as`. This means it is much harder to specify the new type of the `Circuit`.

Apply Type Family It would not be possible to use a new type variable `xs` for the `inputsApplied` parameter. This is because it needs to be constrained so that it is equivalent to `fs` applied to `as`. To solve this a new closed type family [7] is created that is able to apply the two type lists together. This type family pairwise applies a list of types with kind `* → *` to a list of types with kind `*` to form a new list containing types of kind `*`. For example, `Apply '[f, g, h] '[a, b, c]~'[f a, g b, h c]`.

⚠: looks awful

```
type family Apply (fs :: [Type → Type]) (as :: [Type]) where
  Apply '[] '[] = '[]
  Apply (f' : fs) (a' : as) = f a' : Apply fs as
```

Append Type Family There will also be the need to append two type level lists together. Lists would need to be appended in this way, when combining inputs and outputs to form a larger circuit. For example, $'[a, b, c] :++' [d, e, f] \sim' [a, b, c, d, e, f]$. To do this an append type family [14] can be used:

```
type family (:++) (l1 :: [k]) (l2 :: [k]) :: [k] where
  (:++) '[]      l = l
  (:++) (e' : l) l' = e' : (l :++ l')
```

The $:++$ type family is defined in the same way as the standard $++$ function on value lists, however, it appends type lists together instead. This type family makes use of the language extension `PolyKinds` [30] to allow for the append to be polymorphic on the kind stored in the type list. This will avoid defining multiple versions to append `fs` with `gs`, and `as` with `bs`.

The ‘Then’ Constructor This constructor — denoted by $\langle\Rightarrow\rangle$ — is used to stack two circuits on top of each other. It is used to encapsulate the idea of dependencies, between different circuits. Through types it enforces that the output of the top circuit is the same as the input to the bottom circuit.

```
(⟨⇒⟩) :: (DataStore' fs as, DataStore' gs bs, DataStore' hs cs)
  ⇒ Circuit fs as (Apply fs as) gs bs (Apply gs bs) nfs
  ⇒ Circuit gs bs (Apply gs bs) hs cs (Apply hs cs) ngs
  ⇒ Circuit fs as (Apply fs as) hs cs (Apply hs cs) nfs
```

It employs a similar logic to function composition $(\cdot) :: (a \rightarrow b) \rightarrow (b \rightarrow c) \rightarrow (a \rightarrow c)$. The resulting type from this constructor uses the input types from the first argument `fs as (Apply fs as)`, and the output types from the second argument `hs cs (Apply hs cs)`. It then forces the constrain that the output type of the first argument and the input type of the second are the same — `gs bs (Apply gs bs)`.

The ‘Beside’ Constructor Denoted by $\langle\>\rangle$, the beside constructor is used to place two circuits side-by-side. The resulting `Circuit` has the types of left and right circuits appended together.

```
(⟨>⟩) :: (DataStore' fs as, DataStore' gs bs, DataStore' hs cs, DataStore' is ds)
  ⇒ Circuit fs as (Apply fs as) gs bs (Apply gs bs) nfs
  ⇒ Circuit hs cs (Apply hs cs) is ds (Apply is ds) nhs
  ⇒ Circuit (fs :++ hs) (as :++ cs) (Apply fs as :++ Apply hs cs)
    (gs :++ is) (bs :++ ds) (Apply gs bs :++ Apply is ds)
    (nfs :++ nhs)
```

This constructor works by making use of the $:++$ type family to append the input and output type list of the left constructor to those of the right constructor. It also makes use of the $:+$ type family — defined in Section 2.5.3 — to add the number of inputs from the left and right together.

3.4.2 Combined Data Stores

A keen eyed reader may notice that all of these constructors have not been using the original `DataStore` type class. Instead they have all used the `DataStore'` type class. This is a special case of a `DataStore`, allowing for constructors to also be defined over type lists, not just a single type. Combined data stores make it easier for tasks to fetch from multiple inputs. Users will just have to call a single `fetch'` function, rather than multiple. However, since tasks can only have one output, there is no need for a `save'` function, that would be able to save to multiple data stores.

To be able to define `DataStore'`, heterogeneous lists [14] are needed — specifically two different forms. `HList'` stores values of type `f a` and is parameterised by two type lists `fs` and `as`. `IOList` stores items of type `IO a` and is parameterised by a type list `as`. Using an `IOList` makes it easier to define a function that produces a list of IO computations. Their definitions are:

```
data HList' (fs :: [Type → Type]) (as :: [Type]) where
  HCons' :: f a → HList' fs as → HList' (f' : fs) (a' : as)
  HNil'  :: HList' '[] '[]
data IOList (xs :: [Type]) where
  IOCons :: IO x → IOList xs → IOList (x' : xs)
  IONil  :: IOList '[]
```

Now that there is a mechanism to represent a list of different types, it is possible to define `DataStore'`:

```
class DataStore' (fs :: [Type → Type]) (as :: [Type]) where
  fetch' :: HList' fs as → IOList as
```

To save the user of the cumbersome task of having to define an instance of `DataStore'` for every possible combination of data stores, the instance is derived from the previous `DataStore` type class. This means that a user does not need to create any instances of `DataStore'`. They can instead focus on each single case, with the knowledge that they will automatically be able to combine them with other data stores.

```
instance {-# OVERLAPPING #-} (DataStore f a) ⇒ DataStore' '[f]' '[a] where
  fetch' (HCons' x HNil') = IOCons (fetch x) IONil
instance (DataStore f a, DataStore' fs as) ⇒ DataStore' (f' : fs) (a' : as) where
  fetch' (HCons' x xs) = IOCons (fetch x) (fetch' xs)
```

One of these instances makes use of the `{-# OVERLAPPING #-}` pragma. In most cases the base case instance that would be defined is `DataStore' '[]' '[]`. However, it does not make sense to have an empty data store. Therefore, the base case is selected to be a list with one element `DataStore' '[f]' '[a]`. This leads to a problem: GHC is unable to decide which instance to use. It could use either the `DataStore' '[f]' '[a]` or the `DataStore' (f' : '[]) (a' : '[])` instance. The overlapping pragma tells GHC, that if it encounters this scenario, it should choose the one with the pragma.

3.4.3 Multi-Input Tasks

With a `Circuit`, it is possible to represent a **DAG**. This means that a node in the graph can now have multiple dependencies, as seen in Figure 3.3.

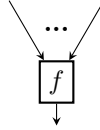


Figure 3.3: A graphical representation of a task with multiple dependencies

To support this, a modification is made to the `task` constructor: rather than have an input value type of `f a`, it can now have an input value type of `HList' fs as`. The function executed in the task can now use `fetch'` to fetch all inputs with one function call.

```
task :: (DataStore' fs as, DataStore g b)
      ⇒ (HList' fs as → g b → IO (g b))
      → g b
      → Circuit fs as (Apply fs as) '[g]' '[b]' '[g b]' (Length fs)
```

Now that the length of the inputs is unknown, in order to specify the `nInputs` type parameter, the `Length` type family defined in Section 2.5.4 must be used. This will return a type-level `Nat`, which is the length of the input array `fs`.

Smart Constructors There could be many times that the flexibility provided by defining your own tasks from scratch could cause a large amount of boiler plate code. For example, there may be times that a user already has pre-defined function and would like to convert it to a task. Therefore there are also two smart constructors that they are able to use:

```
multiInputTask :: (DataStore' fs as, DataStore g b)
                ⇒ (HList as → b)
                → g b
                → Circuit fs as (Apply fs as) '[g]' '[b]' '[g b]' (Length fs)
functionTask :: (DataStore f a, DataStore g b)
              ⇒ (a → b)
```

```

→ g b
→ Circuit '[f] '[a] '[f a] '[g] '[b] '[g b] N1

```

The first allows for a simple function with multiple inputs to be defined. With the fetching and saving handled by the smart constructor. The second allows for a simple $a \rightarrow b$ function to be turned into a Task.

3.4.4 mapC operator

Currently a circuit has a static design — once it has been created it cannot change. There are times when this could be a flaw in the language. For example, when there is a dynamic number of inputs. This could be combated with more smart constructors to generate more complex circuits, with the pre-existing constructors. Another approach would be to add new constructors that allow for more dynamic circuits, such as `mapC`. This new constructor is used to map a circuit on a single input containing a list of items. The input is fed into the inner circuit, accumulated back into a list, and then output.

```

mapC :: (DataStore '[f] '[[a]], DataStore g [b])
⇒ Circuit '[VariableStore] '[a] '[VariableStore a] '[VariableStore] '[b] '[VariableStore b] N1
→ g [b]
→ Circuit '[f]          '[[a]] '[f [a]]          '[g]          '[[b]] '[g [b]]          N1

```

This example can be thought of a production line ($[a] \rightarrow [b]$). The circuit given as an argument describes how to produce one item ($a \rightarrow b$). The `mapC` can then be provided with a pallet (or a list) of resources to build multiple items ($[a]$), it will then return a pallet of made items ($[b]$).

3.4.5 Completeness

The constructors in this library make up a symmetric monoidal preorder. For simplicity only the `inputsApplied` and `outputsApplied` type parameters will be used to formalise a `Circuit` — all other type parameters are only required to aid GHC in compilation.

A preorder is defined over tasks and `DataStores`. The preorder relation \leq , can be used to describe the dependencies in the `DataStores`, with a task being able to transform `DataStores` into new `DataStores`. The relation is defined over the set X , which describes the set of all possible `DataStores`.

The monoidal product \otimes can be thought of as the concatenation of multiple `DataStores` into type-lists. For example the monoidal product of $(f\ a) \otimes (g\ b) = '[f\ a] :++ '[g\ b] \sim '[f\ a, g\ b]$. The monoidal unit, is tricky to define as it has no real meaning within a `Circuit`, however it could be considered the empty `DataStore`: `'[]`.

The axioms are then satisfied as follows:

1. Reflexivity — this is the `id :: Circuit '[f a] '[f a]` constructor, it represents a straight line with the same input and output.
2. Transitivity — this is the `<=> :: Circuit x y → Circuit y z → Circuit x z` constructor, it allows for circuits to be placed in sequence.
3. Monotonicity — this is the `<> :: Circuit x1 y1 → Circuit x2 y2 → Circuit (x1 :++ x2) (y1 :++ y2)` constructor. This can place circuits next to each other.
4. Unitality — given the monoidal unit `'[]` and a `DataStore xs`, then the rules hold true: `'[] :++ xs ~ xs` and `xs :++ '[] ~ xs`.
5. Associativity — given three `DataStores`: `xs`, `ys`, `zs`. Since concatenation of lists is associative then this rule holds: `(xs :++ ys) :++ zs ~ xs :++ (ys :++ zs)`.
6. Symmetry — this is the `swap :: Circuit '[f a, g b] '[g b, f a]` constructor, it allows for values to swap over.
7. Delete Axiom — this is satisfied by the `dropL :: Circuit '[f a, g b] '[g b]` and `dropR :: Circuit '[f a, g b] '[f a]`. Although this does not directly fit with the axiom, it also has to ensure the constraint on a circuit that there must always be 1 output value.
8. Copy Axiom — this is the `replicate :: Circuit '[f a] '[f a, f a]` constructor. It allows for a `DataStore` to be duplicated.

By satisfying all the axioms a `Circuit` is a symmetric monoidal preorder.

3.4.6 Evaluation

☑ **Describe any Dataflow** It is possible to represent a **DAG** with the constructors in this library. Its completeness has been formalised as a symmetric monoidal preorder.

☑ **Quickness to Learn** The language uses combinators that also have a visual representation, this makes it easy to quickly understand how they all work. A user can then also benefit from the familiarity of using the host language Haskell.

☑ **Easy to Write** Building a circuit is a more difficult task: to be able to define it the user needs to have an understanding of the shape of the dataflow diagram. Once the user has a sketch for the dataflow they would like to create, translating to a circuit is a much simpler job. This creates more upfront work for the user, however, it is offset by the additional benefits that a circuit brings.

☑ **Easy to Read** Due to the graphical nature of the constructors, it is relatively simple to build up a picture of how an existing circuit works. The user is able to infer the shape of the dataflow diagram easily by working their way down a circuit from top to bottom, and visualising how different tasks are connected. It could also be possible to pretty print a circuit to recreate the dataflow diagram — although this has not been implemented.

☑ **Type-safe** One key benefit that a **Circuit** brings is that constructing them uses strong types. Each constructor encodes its behaviour within the types. This allows the GHC type checker to validate a **Circuit** at compile-time, to ensure that each task is receiving the correct values. This avoids the possibility of crashes at run-time, where types do not match correctly. There is, however, a consequence of this type-safety: the user now needs to add some explicit types on a **Circuit** to help the type checker.

Chapter 4

Implementation

4.1 Requirements

The implementation of the network itself has several requirements that are separate from the language design:

- **Type-safe** — This is a continuation of the previous requirement for the language. It is also important that once the user has built a well-typed `Circuit`, that the code also continues to be executed in a well-typed environment, to ensure that all inputs and outputs are correctly typed.
- **Parallel** — One of the key benefits that comes from dataflow programming is implicit parallelisation. With this `DSL` being tailored towards data pipelines, which could be computationally expensive, it should be able to benefit from parallel execution.
- **Competitive Speed** — This library should be able to execute dataflows in a competitive time, with other libraries that already exist.
- **Failure Tolerance** — It is important that if one invocation of a task crashes, it does not crash the whole program. This implementation should be able to gracefully handle errors and propagate them through the circuit.
- **Usable** — The implementation of the library should not break any of the usability of the language design.
- **Maintainable** — It should be easy to maintain the library and add new constructors in the future.

4.2 Circuit AST

The constructors for the language are actually *smart constructors*. They provide a more elegant way to build an `AST`, which represents the circuit. They give the ability to gain the benefits of extensibility and modularity, usually found in a shallow embedding, while still having a fixed core `AST` that can be used for interpretation.

4.2.1 IFunctor

To build the fixed core `AST` for a `Circuit`, indexed functors — also known as `IFunctor` — are used. `IFunctors` are, however, only defined to take a single type index — a `Circuit` needs 7. To do this `IFunctor7` can be defined:

```
class IFunctor7 iF where
  imap7 :: (∀ a b c d e f g. f' a b c d e f g → g' a b c d e f g) → iF f' a b c d e f g → iF g' a b c d e f g
```

`IFunctor7` follows a similar structure to a standard `IFunctor`, it just has 7 type indices instead. This indexed functor can be used to mark the recursive points of the data types used to construct the `Circuit AST`.

However, any data type that is converted to use an `IFunctor7`, will need a way to tie the recursive knot. A new type called `IFix7` can be used, it will follow a similar pattern to `IFix`, but with 7 type indicies.

```
newtype IFix7 iF a b c d e f g = IIn7 (iF (IFix7 iF) a b c d e f g)
```

4.2.2 Indexed Data Types à la Carte

To build the **AST**, the data types à la carte [25] approach is taken. This allows for a modular approach, making the library more extendable later on. To be able to use this approach, it needs to be modified to support the 7 type indicies — a through to g:

```
data (iF :+: iG) (f' :: i → j → k → l → m → n → o → Type)
    (a :: i) (b :: j) (c :: k) (d :: l) (e :: m) (f :: n) (g :: o) where
    L :: iF f' a b c d e f g → (iF :+: iG) f' a b c d e f g
    R :: iG f' a b c d e f g → (iF :+: iG) f' a b c d e f g
infixr :+:
```

As mentioned in Section 2.4, using the `:+:` operator comes with problem of many L's and R's, when trying to create the **AST** structure. To avoid this, the `:<:` operator can also be extended to work with `IFunctor7`. The definition follows closely to the original definition, with some minor modifications to the types and constraints.

```
class (IFunctor7 iF, IFunctor7 iG) ⇒ iF :<: iG where
    inj :: iF f' a b c d e f g → iG f' a b c d e f g
instance IFunctor7 iF ⇒ iF :<: iF where
    inj = id
instance (IFunctor7 iF, IFunctor7 iG) ⇒ iF :<: (iF :+: iG) where
    inj = L
instance (IFunctor7 iF, IFunctor7 iG, IFunctor7 iH, iF :<: iG) ⇒ iF :<: (iH :+: iG) where
    inj = R · inj
```

Defining a constructor Data types for each constructor can be defined individually. The `Then` constructor is used as an example, however, the process can be applied to all constructors in the language.

```
data Then (iF :: [Type → Type] → [Type] → [Type]
          → [Type → Type] → [Type] → [Type] → Nat → Type)
    (inputsS :: [Type → Type]) (inputsT :: [Type]) (inputsA :: [Type])
    (outputsS :: [Type → Type]) (outputsT :: [Type]) (outputsA :: [Type])
    (ninputs :: Nat) where
    Then :: (DataStore' fs as, DataStore' gs bs, DataStore' hs cs)
        ⇒ iF fs as (Apply fs as) gs bs (Apply gs bs) nfs
        → iF gs bs (Apply gs bs) hs cs (Apply hs cs) ngs
        → Then iF fs as (Apply fs as) hs cs (Apply hs cs) nfs
```

Each `iF` denotes the recursive points in the data type, with the subsequent type arguments mirroring those seen in Section 3.4.1. A corresponding `IFunctor7` instance formalises the points of recursion, by showing how to transform the structure inside it.

```
instance IFunctor7 Then where
    imap7 f (Then x y) = Then (f x) (f y)
```

The smart constructor, that injects the L's and R's automatically can be defined for `Then` as:


```
(<>) :: (Then :-: iF, DataStore' fs as, DataStore' gs bs, DataStore' hs cs)
  => IFix7 iF fs as (Apply fs as) gs bs (Apply gs bs) nfs
  → IFix7 iF gs bs (Apply gs bs) hs cs (Apply hs cs) nfs
  → IFix7 iF fs as (Apply fs as) hs cs (Apply hs cs) nfs
(<>) l r = lln7 (inj (Then l r))
infixr 4 <>
```

The constructor adds one extra constraint, to the constructor defined in Section 3.4.1 — `Then :-: iF`. This allows the smart constructor to produce an node in the **AST** for any sum of data types, that includes the `Then` data type.

Representing a Circuit Once each constructor has been defined then they can be combined together to form the `CircuitF` type, which can be used to represent a circuit.

```
type CircuitF = Id :+: Replicate :+: Then :+: Beside :+: Swap :+: DropL :+: DropR :+: Task :+: Map
```

The fixed-point of the `CircuitF` datatype can be defined with `IFix7`:

```
type Circuit = IFix7 CircuitF
```

4.3 Process Network

Now that it is possible to build a `Circuit`, which can be considered a specification for how to execute a set of tasks, there needs to be a mechanism in place to execute the specification. The standard implementation of a process network will use a Kahn Process Network (**KPN**). This means that each task in a circuit will run on its own separate thread, with inputs being passed between them on unbounded channels.

4.3.1 Network Typeclass

To allow for different process networks, a typeclass will be used to specify all the functions that every network should have. The `Network` typeclass is defined as:

```
class Network n where
  startNetwork :: Circuit inputsS inputsT inputsA outputsS outputsT outputsA nInputs
    → IO (n inputsS inputsT inputsA outputsS outputsT outputsA)
  stopNetwork :: n inputsS inputsT inputsA outputsS outputsT outputsA
    → IO ()
  write :: HList' inputsS inputsT
    → n inputsS inputsT inputsA outputsS outputsT outputsA
    → IO ()
  read :: n inputsS inputsT inputsA outputsS outputsT outputsA
    → IO (HList' outputsS outputsT)
```

This type class requires that a network has 4 different functions:

- `startNetwork` is responsible for converting the circuit into the underlying representation for a process network: it will be discussed in more detail in Section 4.4.
- `stopNetwork` is for cleaning up the network after it is no longer needed. For example, this could be stopping the threads running. This could be particularly important if embedding a circuit into a larger program, where unused threads could be left hanging.
- `write` should take some input values and add them into the network, so that they can be processed.
- `read` should retrieve some output values from the network.

Examples of how to use a network are included in Chapter 5.

4.3.2 The Basic Network Representation

An implementation of the `Network` typeclass is a `BasicNetwork`. This implementation makes use of a special case of heterogeneous list. A `PipeList` is used to represent a heterogeneous list of channels. This allows the `BasicNetwork` to store multiple channels in the same list without the need for existential types — one of the problems previously encountered with chains in Section 3.3.

```
data PipeList (fs :: [Type → Type]) (as :: [Type]) (xs :: [Type]) where
  PipeCons :: Chan (f a) → PipeList fs as xs → PipeList (f' : fs) (a' : as) (f a' : xs)
  PipeNil   :: PipeList '[] '[] '[]
```

Making use of `PipeLists`, the `BasicNetwork` data type can be defined. This definition makes use of record syntax, this allows for named fields, with accessors automatically generated.

```
data BasicNetwork (inputsS :: [Type → Type]) (inputsT :: [Type]) (inputsA :: [Type])
  (outputsS :: [Type → Type]) (outputsT :: [Type]) (outputsA :: [Type]) where
  BasicNetwork :: {
    threads :: [ThreadId],
    inputs  :: PipeList inputsS inputsT inputsA,
    outputs :: PipeList outputsS outputsT outputsA }
    → BasicNetwork inputsS inputsT inputsA outputsS outputsT outputsA
```

The `BasicNetwork` has three fields:

- `threads` is a list of `ThreadId`s, this allows for the threads to be managed after their creation.
- `inputs` is a `PipeList` containing the channels that the initial input into the network.
- `outputs` is a `PipeList` that stores channels, which the output of the network can be read from.

The `Network` type instance for a `BasicNetwork` is relatively trivial to implement: if given a function to transform a `Circuit` to it.

```
instance Network BasicNetwork where
  startNetwork = buildBasicNetwork -- Definition to come...
  stopNetwork n = forM_ (threads n) killThread
  write uuid xs n = writePipes xs (inputs n)
  read n          = readPipes (outputs n)
```

The `writePipes` function will input a list of values into each of the respective pipes. The `readPipes` function will make a blocking call to each channel to read an output from it. This function will block till an output is read from every output channel.

add a definition of these

4.4 Translation to a Network

There is now a representation for a `Circuit` that the user will build, and a representation used to execute the `Circuit`. However, there is no mechanism to convert between them. This can be achieved by folding the circuit data type into a network. This fold, however, will need to create threads and channels, both of which IO actions. The current definition for the fold `icata7` is not able perform monadic computation inside the algebra. To solve this `unsafePerformIO` could be used, however, for this to be safe the IO computation needs to have no side-effects. This fold will violate this rule, therefore, the only other way to support this is to modify the catamorphism to support monadic computation.

4.4.1 Indexed Monadic Catamorphism

An indexed monadic catamorphism, found in Section 2.3.1, can be used to perform this fold: it will allow for monadic computation within the algebra. However, `icataM` needs to be modified to support the 7 type indices needed. The first step is to define a monadic `imap` that supports the needed number of type indices. This will be added by extending the `IFunctor7` instance to also include a function named `imapM7`.

```

class IFunctor7 iF where
  imap7 :: (∀ a b c d e f g. f' a b c d e f g → g' a b c d e f g) → iF f' a b c d e f g → iF g' a b c d e f g
  imapM7 :: Monad m ⇒ (∀ a b c d e f g. f' a b c d e f g → m (g' a b c d e f g))
    → iF f' a b c d e f g
    → m (iF g' a b c d e f g)

```

The definition for this new function `imapM7` for each instance closely follows the non-monadic version, however, now has a monadic function to map on the input. Here is the definition of the new `IFunctor7` instance for `Beside`:

```

instance IFunctor7 Beside where
  imap7 f (Beside l r) = Beside (f l) (f r)
  imapM7 f (Beside l r) = do
    l' ← f l
    r' ← f r
    return (Beside l' r')

```

The definition is intuitively the same, just using `do`-notation instead.

Now that there is a indexed monadic map, it is possible to define the a monadic catamorphism for an `IFunctor7`:

```

icataM7 :: (IFunctor7 iF, Monad m)
  ⇒ (∀ a b c d e f g. iF f' a b c d e f g → m (f' a b c d e f g))
  → IFix7 iF a b c d e f g
  → m (f' a b c d e f g)
icataM7 algM (lln7 x) = algM ≡≡ imapM7 (icataM7 algM) x

```

`icataM7` is almost identical to `icataM`, however, it makes use of `imapM7` instead of `imapM`.

4.4.2 BuildNetworkAlg

To use `icataM7` to fold a `Circuit` into a `BasicNetwork`, an algebra is required. However, a standard algebra will not be able to complete this transformation. Consider this example `Circuit` with two tasks executed in sequence.

```

example = task1
        <>
        task2

```

In a standard algebra both sides of the `Then` constructor would be evaluated independently. In this case it would produce two disjoint networks, both with their own input and output channels. The algebra for `Then`, would then need to join the output channels of `task1` with the input channels of `task2`. However, it is not possible to join channels together. Instead, the output channels from `task1` need to be accessible when creating `task2`. This is referred to as a *context-sensitive* or *accumulating* fold. An accumulating fold forms series of nested functions, that collapse to give a final value once the base case has been applied. A simple example of an accumulating fold could be, implementing `foldl` in terms of `foldr`.

```

foldl :: (b → a → b) → b → [a] → b
foldl f b as = foldr (λ a g x → g (f x a)) id as b

```

A simple example of `foldl` can be considered.

```

foldl (+) 0 [1,2]
≡
(λ x → (λ x → id (x + 2)) (x + 1)) 0

```

To be able to have an accumulating fold, inside an indexed catamorphism a carrier data type is required to wrap up this function. This carrier, which shall be named `AccuN`, contains a function that when given a network that has been accumulated up to that point, then it is able to produce a network including the next layer in a circuit. The type of the layer being folded will be `Circuit a b c d e f g`.

this clear enough?
maybe a diagram showing the layer and all the

```
newtype AccuN n asS asT asA a b c d e f g = AccuN
  { unAccuN :: n asS asT asA a b c → IO (n asS asT asA d e f) }
```

This newtype has 3 additional type parameters at the beginning, namely: `asS`, `asT`, `asA`. They represent the input types to the initial circuit. Since the accumulating fold will work layer by layer from the top downwards, these types will remain constant and never change throughout the fold.

Classy Algebra An algebra type class can now be defined. This will ensure that the approach remains with modular: a new instance can be made when adding a new constructor to the language.

```
class (Network n, IFunctor7 iF) ⇒ BuildNetworkAlg n iF where
  buildNetworkAlg :: iF ( AccuN n asS asT asA ) bsS bsT bsA csS csT csA nbs
    → IO ((AccuN n asS asT asA) bsS bsT bsA csS csT csA nbs)
```

This algebra type class is parameterised by `n` and `iF`. The `n` is constrained to have a `Network` instance, this allows the same algebra to be used for defining folds for multiple network types. The `iF` is the `IFunctor7` that this instance is being defined for, an example is `Then` or `Id`. This algebra uses the `N` data type to perform an accumulating fold. The input to the algebra is an `IFunctor7` with the inner elements containing values of type `AccuN`. The function can be retrieved from inside `AccuN` to perform steps that are dependent on the previous, for example, in the `Then` constructor.

To be able to define the algebra on sums of `IFunctor7`s, without having a nest of `L`s and `R`s to pattern match, an instance for the sum of two data types is defined:

```
instance (BuildNetworkAlg n iF, BuildNetworkAlg n iG) ⇒ BuildNetworkAlg n (iF :+: iG) where
  buildNetworkAlg (L x) = buildNetworkAlg x
  buildNetworkAlg (R y) = buildNetworkAlg y
```

This instance enforces that there must also be an instance for the left and right hand side of the sum. It will then be able to automatically recurse through the `L`s and `R`s, to get to the types that have been summed.

The Initial Network Before being able to define the actual translation, there is one more base to cover. This is an accumulating fold that depends on the previous layer to be able to define the current one. However, what happens on the first layer? There is no previous `Network` to use. The initial network should have matching input and output types, this means that the input channels should be the same as the output channels.

To generate the `PipeList` of channels that will be stored in the initial network a new type class is defined:

```
class InitialPipes (inputsS :: [Type → Type]) (inputsT :: [Type]) (inputsA :: [Type]) where
  initialPipes :: IO (PipeList inputsS inputsT inputsA)
```

This type class is able to construct an `initialPipes` based on the type required, in the initial network. To be able to construct this value two instances are defined:

```
instance InitialPipes '[] '[] '[] where
  initialPipes = return PipeNil

instance InitialPipes fs as xs ⇒ InitialPipes (f' : fs) (a' : as) (f a' : xs) where
  initialPipes = do
    c ← newChan :: IO (Chan (f a))
    PipeCons c <$> (initialPipes :: IO (PipeList fs as xs))
```

The first instance deals with the base case: when the type lists are empty, an empty `PipeList` is created. The later more interesting case deals with a cons in the type lists. Here a new channel is created with the same type as the type removed from the front of the type list. The channel is then consed to the front of a `PipeList` with the remaining list generated by a recursive call.

Now that there is a method for creating a `PipeList` that matches a type-list, the initial network is defined:

```
initialNetwork
  :: ∀inputsS inputsT inputsA
  . (InitialPipes inputsS inputsT inputsA)
  ⇒ IO (BasicNetwork inputsS inputsT inputsA inputsS inputsT inputsA)
initialNetwork = do
  ps ← initialPipes :: IO (PipeList inputsS inputsT inputsA)
  return $ BasicNetwork [] ps ps
```

This creates a network that has matching input and output types. To do so a `PipeList` of the initial channels is created, which is then used as both the inputs and outputs of the network.

4.4.3 The Translation

Now that the algebra type class, and the initial input to the accumulating fold is defined, each instance of the type class are defined.

Basic Constructors There are several constructors that just manipulate the output `PipeList`, these constructors are `Id`, `Replicate`, `Swap`, `DropL`, and `DropR`. The `Swap` constructor takes two inputs and then swaps them over:

```
instance BuildNetworkAlg BasicNetwork Swap where
  buildNetworkAlg Swap = return $ AccuN
    (λn → do
      output ← swapOutput (outputs n)
      return $ BasicNetwork (threads n) (inputs n) output
    )
  where
    swapOutput :: PipeList '[f, g] '[a, b] '[f a, g b]
      → IO (PipeList '[g, f] '[b, a] '[g b, f a])
    swapOutput (PipeCons c1 (PipeCons c2 PipeNil)) =
      return $ PipeCons c2 (PipeCons c1 PipeNil)
```

The instance for `Swap`, defines a function wrapped by `AccuN`, that takes the current accumulated network, up to this point. It then is able to transform the outputs and build a new `BasicNetwork`. To transform the networks it makes use of a function named `swapOutput`, which unpacks the `PipeList` and swaps the two channels `c1` and `c2` over.

Another basic constructor is `Replicate`: the purpose of this constructor is to duplicate the input to produce two outputs. The instance for `Replicate` is defined as:

```
instance BuildNetworkAlg BasicNetwork Replicate where
  buildNetworkAlg Replicate = return $ AccuN
    (λn → do
      output ← dupOutput (outputs n)
      return $ BasicNetwork (threads n) (inputs n) output
    )
  where
    dupOutput :: PipeList '[f] '[a] '[f a]
      → IO (PipeList '[f, f] '[a, a] '[f a, f a])
    dupOutput (PipeCons c PipeNil) = do
      c' ← dupChan c
      return $ PipeCons c (PipeCons c' PipeNil)
```

This instance follows a similar pattern to the `Swap` instance — defining a function which retrieves the accumulated network, then manipulates the outputs. However, the `dupOutput` function also has to make use of an operation on the channel — `dupChan`. This will create a new channel that will mirror the inputs of the original channel.

All other basic constructors will follow this pattern:

- `Id`, will return the same outputs as the accumulated network.
- `DropL`, will drop the *first* item in the output `PipeList` of the accumulated network.
- `DropR`, will drop the *last* item in the output `PipeList` of the accumulated network.

Task In a `BasicNetwork` a task will run as a separate thread, to do this `forkIO :: IO () → IO ThreadId` will be used. Using this function requires some `IO ()` computation to run, this will be defined by `taskExecutor`:

```
taskExecutor
  :: Task iF inputsS inputsT inputsA outputS outputT outputsA ninputs
  → PipeList inputsS inputsT inputsA
  → PipeList outputS outputT outputA
  → IO ()
taskExecutor (Task f outStore) inPipes outPipes = forever
  (do
    taskInput) ← readPipes inPipes
    r ← f taskInputs outStore
    writePipes (HCons' r HNil') outPipes
  )
```

The `taskExecutor` has three arguments:

- The `Task` to be executed on the thread.
- A `PipeList` which has channels containing the input values.
- A `PipeList` to output the results of the `Task`.

A `taskExecutor` will, read a value from each of input channels, execute the task with those inputs, and then write the output to the output channels. This computation is then repeated forever, using the aptly named function `forever`.

Making use of the `taskExecutor`, the algebra instance for `Task` is defined as:

```
instance BuildNetworkAlg BasicNetwork Task where
  buildNetworkAlg (Task t out) = return $ AccuN
    (λn → do
      c ← newChan
      let output = PipeCons c PipeNil
      threadId ← forkIO (taskExecutor (Task t out) (outputs n) output)
      return $ BasicNetwork (threadId : threads n) (inputs n) output
    )
```

This instance first creates a new output channel, this will be given to the task to send its outputs on. It then forks a new thread with the computation generated by `taskExecutor`. The executor is given the output values of the accumulated network and the output channel, just created. The resulting network has the same inputs, but now adds a new thread id to the list and the outputs set to be the output channels from the task.

Then The `Then` constructor is responsible for connecting circuits in sequence. When converting this to a network, this will involve making use of the accumulated network value to generate the next layer. The instance is defined as:

```
instance BuildNetworkAlg BasicNetwork Then where
  buildNetworkAlg (Then (AccuN fx) (AccuN fy)) = return $ N
    (λn → do
      nx ← fx n
      fy nx
    )
```

This instance has an interesting definition: firstly it takes the accumulated network `n` as input. It then uses the function `fx`, with the input `n` to generate a network for the top half of the `Then` constructor.

Finally, it takes the returned network `nx`, from the top half of the constructor, and generates a network using the function `fy` representing the bottom half of the constructor.

Beside The **Beside** constructor places two circuits side by side. This is the most difficult algebra to define as the accumulated network needs to be split in half to pass to the two recursive sides of **Beside**. An instance of the algebra is defined as:

```
instance BuildNetworkAlg BasicNetwork Beside where
  buildNetworkAlg = beside
```

This requires a `beside` function, however to define this function some extra tools are required. The first is `takeP`, which will take the first `n` elements from a `PipeList`:

```
takeP :: SNat n → PipeList fs as xs → PipeList (Take n fs) (Take n as) (Take n xs)
takeP SZero _ = PipeNil
takeP (SSucc _) PipeNil = PipeNil
takeP (SSucc n) (PipeCons x xs) = PipeCons x (takeP n xs)
```

This makes use of the `Take` type family to take `n` elements from each of the type lists: `fs`, `as`, and `xs`. It follows the same structure as the `take :: Int → [a] → [a]` defined in the `Prelude`.

The next function is `dropP`, it drops `n` elements from a `PipeList`:

```
dropP :: SNat n → PipeList fs as xs → PipeList (Drop n fs) (Drop n as) (Drop n xs)
dropP SZero l = l
dropP (SSucc _) PipeNil = PipeNil
dropP (SSucc n) (PipeCons _ xs) = dropP n xs
```

This function again follows the same structure as `drop :: Int → [a] → [a]` defined in the `Prelude`. Both `takeP` and `dropP` are used to split the outputs of a network after `n` elements. This requires the knowledge of what `n` is at the value level, however `n` is only stored at the type level as the argument `ninputs`. To be able to recover this value the `IsNat` type class, as defined in Section ?? is used. The `recoverNInputs` function is able to direct the `IsNat` type class to the correct type argument, and produces an `SNat` with the same value as that stored in the type.

```
recoverNInputs :: (Length bsS ~ Length bsT, Length bsT ~ Length bsA, Length bsA ~ Length bsS,
                  ninputs ~ Length bsS, IsNat ninputs, Network n)
  ⇒ (N n asS asT asA) bsS bsT bsA csS csT csA (ninputs :: Nat)
  → SNat (Length bsS)
circuitInputs _ = nat
```

After splitting a network and generating two new networks, the outputs will need to be joined together again: this will require the appending of two `PipeLists`. To do this an `AppendP` type class is defined:

```
class AppendP fs as xs gs bs ys where
  appendP :: PipeList fs as xs → PipeList gs bs ys → PipeList (fs :++ gs) (as :++ bs) (xs :++ ys)
```

This type class has one function `appendP`, it is able to append two `PipeLists` together. It makes use of the `:++` type family to append the type lists together. The instances for this type class are made up of two cases: the base case and a recursive case.

```
instance AppendP '[] '[] '[] gs bs ys where
  appendP PipeNil ys = ys
instance (AppendP fs as xs gs bs ys) ⇒ AppendP (f' : fs) (a' : as) (f a' : xs) gs bs ys where
  appendP (PipeCons x xs) ys = PipeCons x (appendP xs ys)
```

The base case corresponds to having an empty list on the left, with some other list on the right. Here the list on the right is returned. The recursive case, simply takes 1 element from the left hand side and conses it onto the from of a recursive call, with the rest of the left hand side.

It is now possible to define the `beside` function. The result is calculated in 4 steps, with helper functions for each step:

1. Get the number of inputs (`ninputs`) on the left hand side of the `Beside` constructor. This will give the information needed to split the inputted accumulated network `n`.
2. Split the network into a left and right hand side. This will retain the same input type to the network, as there is no information on how to split that. Only the output `PipeList` will be split into two parts.
3. Translate the both the left and right network. This will perform the recursive step and generate two new networks with the networks from the left and right added to the accumulated network `n`.
4. Join the networks back together. Now that the left and right hand side of this layer has been added to the accumulated network, the two sides need to be joined back together to get a single network that can be returned.

This is very long, but I cant really break it up because it needed the scoped type variables from `beside`

```

beside :: ∀asS asT asA bsS bsT bsA csS csT csA (nbs :: Nat)
  . Beside (AccuN BasicNetwork asS asT asA) bsS bsT bsA csS csT csA nbs
  → IO ((AccuN BasicNetwork asS asT asA) bsS bsT bsA csS csT csA nbs)
beside (Beside l r) = return $ AccuN
  (λn → do
    let ninputs = circuitInputs l
    (nL, nR) ← splitNetwork ninputs n
    (newL, newR) ← translate ninputs (nL, nR) (l, r)
    joinNetwork (newL, newR)
  )
where
  splitNetwork :: SNat nbsL
    → BasicNetwork asS asT asA bsS bsT bsA
    → IO (BasicNetwork asS asT asA (Take nbsL bsS) (Take nbsL bsT) (Take nbsL bsA),
      BasicNetwork asS asT asA (Drop nbsL bsS) (Drop nbsL bsT) (Drop nbsL bsA))
  splitNetwork nbs n = return
    (BasicNetwork (threads n) (inputs n) (takeP nbs (outputs n)),
     BasicNetwork (threads n) (inputs n) (dropP nbs (outputs n)))
  translate :: SNat nbsL
    → (BasicNetwork asS asT asA (Take nbsL bsS) (Take nbsL bsT) (Take nbsL bsA),
      BasicNetwork asS asT asA (Drop nbsL bsS) (Drop nbsL bsT) (Drop nbsL bsA))
    → ((AccuN BasicNetwork asS asT asA)
      (Take nbsL bsS) (Take nbsL bsT) (Take nbsL bsA) csLS csLT csLA nbsL,
      (AccuN BasicNetwork asS asT asA)
      (Drop nbsL bsS) (Drop nbsL bsT) (Drop nbsL bsA) csRS csRT csRA nbsR)
    → IO (BasicNetwork asS asT asA csLS csLT csLA,
      BasicNetwork asS asT asA csRS csRT csRA)
  translate _ (nL, nR) (N cL, N cR) = do
    nL' ← cL nL
    nR' ← cR nR
    return (nL', nR')
  joinNetwork :: (AppendP csLS csLT csLA csRS csRT csRA)
    ⇒ (BasicNetwork asS asT asA csLS csLT csLA, BasicNetwork asS asT asA csRS csRT csRA)
    → IO (BasicNetwork asS asT asA (csLS :++ csRS) (csLT :++ csRT) (csLA :++ csRA))
  joinNetwork (nL, nR) = return
    $ BasicNetwork (nub (threads nL ++ threads nR)) (inputs nL) (outputs nL `appendP` outputs nR)

```

The `splitNetwork` function creates two new `BasicNetwork`s. To split the output values, `takeP`, and `dropP` are used. `translate` performs the recursive step in the accumulating fold, which produces two new networks that include this layer. `joinNetwork` takes the two new networks and appends the outputs with `appendP`. It also has to append the thread ids from both sides, however, this will now include duplicates as threads were not split in `splitNetwork`. To combat this `nub` is used, which returns a list containing all the unique values in the original.

4.5 UUIDS

When inputting multiple values into a `Network` problems can occur.

Why are they needed?

How are they added?

4.6 Failure in the Process Network

Why?

4.6.1 Maybe Monad

No error messages

4.6.2 Except Monad

based on `Either`

Propagation

4.7 Evaluation

Chapter 5

Examples

5.1 Machine Learning (Audio Playlist Generation)

A use case for CircuitFlow is when building data pipelines. Here there are many tasks that can only be executed when other data files have been produced. A data pipeline will also benefit from being parallel to improve run-times. CircuitFlow can help to build a parallel data pipeline, without the user having to worry about how to combine all their data manipulations together, in a way that will not run into concurrency problems.

Consider the example where an audio streaming service would like to create a playlist full of new songs to listen to. This could require a machine learning model that can predict your songs based on the top 10 artists and songs that you have listened to over the last 3 months. However, each of the months data is stored in different files that need aggregating together, before they can be input into the model.

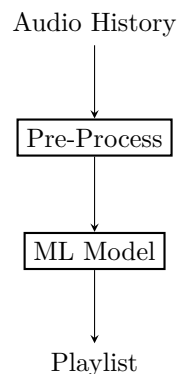


Figure 5.1: A dataflow diagram for playlist generation

5.1.1 Building the pre-processing Circuit

This circuit will need to have 3 different inputs — each months listening history. It will also have 2 outputs: the top 10 songs and artists. To begin with a dataflow diagram can be constructed — seen in Figure 5.2. This will model all the dependencies between each of the pre-processing tasks.

To write this in CircuitFlow, the first step is to create all the tasks that will be used. Both the `AggSongs` and `AggArtists` tasks will require three inputs, which will be CSVs. This means that it is possible to make use of the pre-defined data store: `NamedCSVStore`. The type instances that are required to parse the CSV will be omitted, as they are not relevant to the discussion.

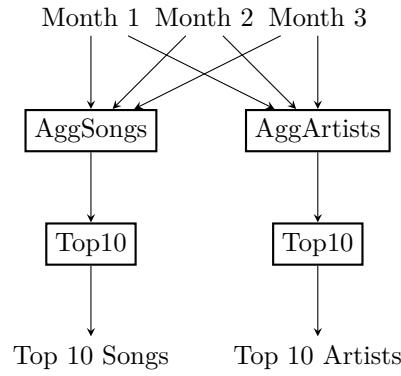


Figure 5.2: A dataflow diagram for pre-processing the song data

```

aggSongsTask :: Circuit
  '[NamedCSVStore,      NamedCSVStore,      NamedCSVStore]
  '[      [Listen],      [Listen],      [Listen]]
  '[NamedCSVStore [Listen], NamedCSVStore [Listen], NamedCSVStore [Listen]]
  '[VariableStore]
  '[      [TrackCount]]
  '[VariableStore [TrackCount]]
  N3
aggSongsTask = multiInputTask f Empty
where
  f :: HList '[[Listen], [Listen], [Listen]] → [TrackCount]
  f (HCons month1 (HCons month2 (HCons month3 HNil))) =
    (map (uncurry TrackCount) · reverse · count_ · map track) (month1 ++ month2 ++ month3)

```

This task applies a composition of functions:

1. Firstly, the track is extracted from the `Listen` data type using the function `track :: Listen → Track`.
2. Next, a list of unique tracks are extracted, along with the number of appearances they made in the original list. This makes use of a special variant `count_ :: [a] → [(a, Int)]`, which will also sort the list in ascending order.
3. This list is then flipped to descending order with `reverse :: [a] → [a]`.
4. Finally, a `TrackCount` value is made from the previous tuple `uncurry TrackCount :: (Track, Int) → TrackCount`.

```

aggArtistsTask :: Circuit
  '[NamedCSVStore,      NamedCSVStore,      NamedCSVStore]
  '[      [Listen],      [Listen],      [Listen]]
  '[NamedCSVStore [Listen], NamedCSVStore [Listen], NamedCSVStore [Listen]]
  '[VariableStore]
  '[      [ArtistCount]]
  '[VariableStore [ArtistCount]]
  N3
aggArtistsTask = multiInputTask f Empty
where
  f :: HList '[[Listen], [Listen], [Listen]] → [ArtistCount]
  f (HCons month1 (HCons month2 (HCons month3 HNil))) =
    (map (uncurry ArtistCount) · reverse · count_ · map (artist · track)) (day1 ++ day2 ++ day3)

```

The `aggArtistsTask` is constructed in a similar way to the `aggSongsTask`, however, it extracts the artist from the track before aggregating the data.

The final task to define is `Top10`, however, this task is used multiple times. Therefore, it would be beneficial if the type was polymorphic so that it can receive and input of both `[ArtistCount]` and `[TrackCount]`. This is possible to do:

```
top10Task :: (ToNamedRecord a, FromNamedRecord a, DefaultOrdered a)
  => FilePath
  -> Circuit '[VariableStore] '[a] '[VariableStore [a]]
            '[NamedCSVStore] '[a] '[NamedCSVStore [a]]
            N1
top10Task filename = functionTask (take 10) (NamedCSVStore filename)
```

The `top10Task` takes an input list and then returns the first 10 from the list.

Now that all of the tasks have been defined, they need to be combined into a circuit. The dataflow diagram seen in Figure 5.2, will prove to be helpful. The first obvious problem is how to create a circuit that can achieve the top part of the diagram, transforming the inputs so that they can be passed into two tasks. This can be dealt with in layers: using the diagrams associated with each constructor, it is possible to convert a layer into a composition of Circuits. The first layer, seen in Figure 5.3 will be responsible for duplicating each of the three inputs.

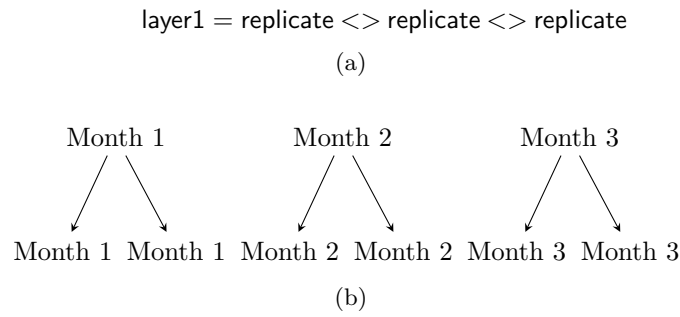


Figure 5.3: The first layer (a) and its corresponding dataflow diagram (b).

Scanning down the dataflow diagram the next layer to deal with is the two swaps that occur: month 1 and 2, and month 2 and 3. This can be seen in Figure 5.4

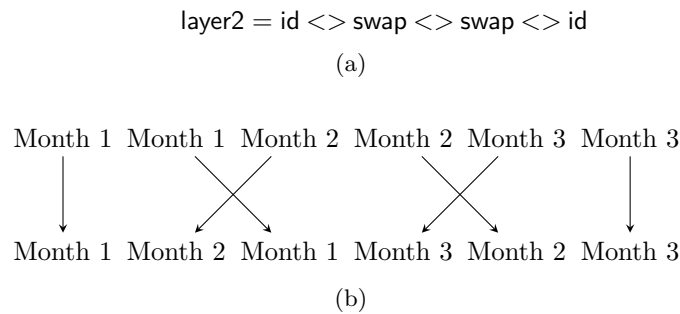


Figure 5.4: The second layer (a) and its corresponding dataflow diagram (b).

The final layer, seen in Figure 5.5, will swap month 1 with month 3.

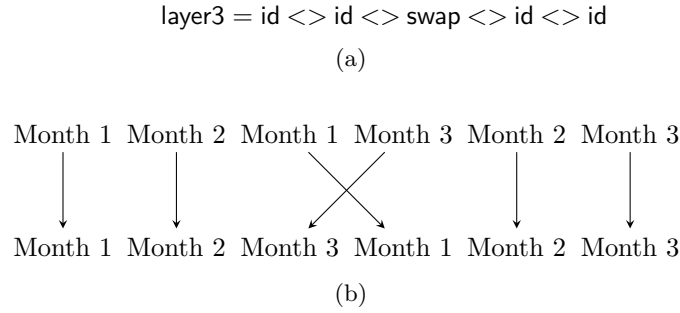


Figure 5.5: The third layer (a) and its corresponding dataflow diagram (b).

These layers can be stacked on top of each other to provide a full transformation:

```
organiseInputs = layer1
                  <>
                  layer2
                  <>
                  layer3
```

The tasks can now be combined with this transformation to provide the full circuit:

```
preProcPipeline :: Circuit
  '[NamedCSVStore,      NamedCSVStore,      NamedCSVStore]
  '[      [Listen],      [Listen],      [Listen]]
  '[NamedCSVStore [Listen], NamedCSVStore [Listen], NamedCSVStore [Listen]]
  '[NamedCSVStore, NamedCSVStore]
  '[      [ArtistCount],      [TrackCount]]
  '[NamedCSVStore [ArtistCount], NamedCSVStore [TrackCount]]
  N3
preProcPipeline = organiseInputs
                  <>
                  aggSongsTask      <> aggArtistsTask
                  <>
                  top10Task "top10Artists.csv" <> top10Task "top10Artists.csv"
```

Again it can be seen how this structure of tasks directly correlates with the dataflow diagram previously seen in Figure 5.2. This helps to make it easier when designing circuits as it can be constructed visually level by level.

5.1.2 Building the prediction Circuit

Now that there is a pipeline to pre-process the data for the model, a new playlist can be created. Again it is possible to build a circuit that combines with the pre-processing circuit.

The audio company train models for each user and store them in a cloud storage service. This would be a good use-case for creating a new **DataStore** — called a **ModelStore**. Say that there are two types defined **ModelStore** and **NewSongPlaylist**: a new **DataStore** instance can be defined for each different model. Here is the **NewSongsPlaylist** as an example:

```
instance DataStore ModelStore NewSongsPlaylist where
  -- Fetch from cloud storage and load into the program
  fetch (ModelStore NewSongsPlaylist) = ...
  save (ModelStore NewSongsPlaylist) _ = ...
```

`fetch` is used to download a trained model from the cloud store. `save` will be used when training a new model, it will allow the model to be saved for use in the future.

With this `DataStore` a new task can be defined that will, take a users top 10 songs and artists, and a model as input. It will then output a list of songs to create a playlist.

```

predictTask :: Circuit
  '[NamedCSVStore,           NamedCSVStore, ,           ModelStore]
  '[           [ArtistCount],           [TrackCount],           NewSongsPlayList]
  '[NamedCSVStore [ArtistCount], NamedCSVStore [TrackCount], ModelStore NewSongsPlayList]
  '[NamedCSVStore]
  '[           [Track]]
  '[NamedCSVStore [Track]]
  N3
predictTask = multiInputTask f (NamesCSVStore "newSongsPlaylist.csv")
  where
    f :: HList '[ [ArtistCount], [TrackCount], NewSongsPlayList ] → [Track]
    f (HCons topArtists (HCons topSongs (HCons model HNil))) =
      predict model topArtists topSongs

```

The `predictTask` can now be combined with the pre-processing circuit to create a circuit that is able to create a new playlist from listening history.

```

createPlaylist = preProcPipeline <> id
                <>
                predictTask

```

The `createPlaylist`, circuit can now be converted into a `Network` and used on user data to generate new playlists, based on their top songs. `preProcPipeline` will be revisited in Chapter 6, to act as a benchmark to compare the performance of the `CircuitFlow` library.

5.2 Build System (lhs2TeX)

Another use case for a task based dependency system is a build system. For example, a Makefile is a way of specifying the target files from some source files, with a command that can be used to generate the target file. `CircuitFlow`: could also be used to model such a system.

Consider this dissertation, which is made using `LATEX`. This project is made up of multiple sub-files, each written in a literate Haskell format. Each of these files needs to be pre-processed by the `lhs2TeX` command to produce the `.tex` source file. Once each of these files has been generated, then the `LATEX`project can be built into a PDF file.

5.2.1 Building the Circuit

The Circuit defined here makes use of the `mapC` operator. To do so a `Circuit` is defined that is able to build a single `.tex` file from a `.lhs`. This has to make use of the standard `task` constructor:

```

buildLhsTask :: Circuit '[VariableStore] '[String] '[VariableStore String]
               '[VariableStore] '[String] '[VariableStore String]
               N1
buildLhsTask = task f Empty
  where
    f :: UUID
      → HList '[VariableStore] '[String]
      → VariableStore String
      → ExceptT SomeException IO (VariableStore String)
    f _ (HCons' (Var flnName) HNil') _ = do
      let fOutName = flnName <.> ".tex"
      lift (callCommand ("lhs2tex -o " ++ fOutName ++ " " ++ flnName))
      return (Var fOutName)

```

This Circuit makes use of the `callCommand` function from the `System.Process` library. This allows the task to execute external commands, that may not necessarily be defined in Haskell. A similar Circuit can

be defined that will compile the `.tex` files and produce a PDF.

```

buildTexTask :: String → Circuit '[VariableStore] '[[String]] '[VariableStore [String]]
                                   '[VariableStore] '[String] '[VariableStore String]
                                   N1
buildTexTask name = task f Empty
where
  f :: UUID
    → HList '[VariableStore] '[String]
    → VariableStore String
    → ExceptT SomeException IO (VariableStore String)
  f mainFileName (HCons' (Var _) HNil') _ = do
    lift
      (callCommand
        ("texfot -no-stderr latexmk -interaction=nonstopmode -pdf "
          ++ "-no-shell-escape -bibtex -jobname="
          ++ name
          ++ " "
          ++ mainFileName
        )
      )
    return (Var "dissertation.pdf")

```

The `buildTexTask` also demonstrates how it is possible to pass a global parameter into a task. This can allow tasks to be made in a more reusable way. Saving a user from defining multiple variations of the same task.

These two tasks can now be combined into a `Circuit`. This `Circuit` can be interpreted as inputting a list of `.lhs` files, which are sequentially compiled to `.tex` files by the `mapC` operator. These files are *then* built by the `buildTexTask` to produce a PDF file as output.

```

buildDiss :: String → Circuit '[VariableStore] '[[String]] '[VariableStore [String]]
                                   '[VariableStore] '[String] '[VariableStore String]
                                   N1
buildDiss name = mapC buildLhsTask Empty
                ⇔
                buildTexTask name

```

`mapC` takes two arguments, the inner circuit to execute and a pointer to the location it should store its results. In this case the output data store is a `VariableStore`, therefore, the pointer to this location is just an `Empty` variable.

5.2.2 Using the Circuit

To use this `Circuit`, a `Config` data type is used to store the information needed within the system to build the project:

```

data Config = Config
  { mainFile    :: FilePath
  , outputName :: String
  , lhsFiles    :: [FilePath]
  }
deriving (Generic, FromJSON, Show)

```

This data type uses record syntax to have name fields:

- `mainFile` is the name of the root file that should be used for compilation.
- `outputName` is the desired name for the output PDF file.
- `lhsFiles` are all the literate haskell files required to build the \LaTeX document.

The `Config` data type also derives the `Generic` and `FromJSON` instance. This allows it to be used in conjunction with a YAML file to specify these parameters. The config can be loaded with:

```
loadConfig :: IO Config
loadConfig = loadYamlSettings ["dissertation.tex-build"] [] ignoreEnv
```

An example config file can be seen in Figure 5.6.

```
mainFile: dissertation.lhs
outputName: dissertation
lhsFiles: [dissertation.lhs
           , chapters/introduction.lhs
           , chapters/background.lhs
           , chapters/the-language.lhs
           , chapters/implementation.lhs
           , chapters/evaluation.lhs
           , chapters/examples.lhs]
```

Figure 5.6: An example config file for the `lhs2TeX` build system

To be able to use the system a `main` function is defined, which will serve as the entry point to the executable:

```
main :: IO ()
main = do
  config <- loadConfig
  n <- startNetwork (buildDiss (outputName config)) :: IO
    (BasicNetwork '[VariableStore] '[String] '[VariableStore [String]]
      '[VariableStore] '[String] '[VariableStore String])
  write (mainFile config -<. > "tex") (HCons' (Var (lhsFiles config)) HNil) n
  _ <- read n
  stopNetwork n
```

The `main` function in the build system has 5 steps:

1. The config file is loaded.
2. A network is started based on the `buildDiss` circuit. The type of network to be started has to be annotated, so that the type system knows which `Network` instance to use.
3. The build job is input into the network, with the input values being a list of `.lhs` files to compile.
4. A call is made to the blocking function `read`, although the outputs are not needed, the call to `read` is. This prevents the program ending before the network has complete processing values.
5. Finally, the network is destroyed.

This dissertation makes use of this build system to be able include literate Haskell files.

5.3 Types saving the day

Consider an example shown in the docs for Luigi [23], that is made up of two tasks. The first generates a list of words and saves it to a file and second counts the number of letters in each of those words. The counting letters task is dependent on the words being generated.

Figure 5.7, shows an implementation of such a system, in the Python library called Luigi. However, this implementation has a very subtle bug! `GenerateWords` writes the words to a file separated by new lines, but `CountLetters` reads that same file as a comma-separated list. This shows a key flaw in this system, it is up to the programmer to ensure that they write the outputs correctly, and then that they read that same file in the same way. This error, would not even cause a run-time error, instead, it will just produce the incorrect result. For a developer this is extremely unhelpful, it means more of time is used writing tests — something that no one enjoys.

```

import luigi

class GenerateWords(luigi.Task):
    def output(self):
        return luigi.LocalTarget('words.txt')

    def run(self):
        # write a dummy list of words to output file
        words = ['apple', 'banana', 'grapefruit']

        with self.output().open('w') as f:
            for word in words:
                f.write('{word}\n'.format(word=word))

class CountLetters(luigi.Task):
    def requires(self):
        return GenerateWords()

    def output(self):
        return luigi.LocalTarget('letter_counts.txt')

    def run(self):
        # read in file as list
        with self.input().open('r') as infile:
            words = infile.read().split(',')

        # write each word to output file with its corresponding letter count
        with self.output().open('w') as outfile:
            for word in words:
                outfile.write('{word}:{letter_count}\n'.format(
                    word=word,
                    letter_count=len(word)
                ))

```

Figure 5.7: A Broken Luigi Example

The Fix Why not eliminate the need for all of this with `DataStores` and types. As previously mentioned in Section 3.2.1, a `DataStore` can be used to abstract the reading and writing of many different sources. This will help to ensure correctness of this step, by eliminating any possible duplicated code. Instead, just having the `fetch` and `save` methods to test.

The second greater benefit, is to use `DataStores` in combination with the type system. Each constructor for a `Circuit` will, enforce that the types of a `DataStore` align correctly. It would not be possible to feed the output of one task, with the type `FileStore[String]` into a task that expects a `CommaSepFile[String]`. The same example as before can be seen in Figure 5.8. In this example it will fail to compile, giving the error:

```
> Couldn't match type 'CommaSepFile' with 'FileStore'
```

This will benefit the user as it reduces the feedback loop of knowing if the program will succeed. Previously the whole data pipeline had to be run, whereas now this information can be informed to the user at compile-time.

```
generateWords :: Circuit '[VariableStore] '[(())] '[VariableStore ()]
                  '[FileStore] '[[String]] '[FileStore [String]]
                  N1
generateWords = functionTask (const ["apple", "banana", "grapefruit"]) (FileStore "fruit.txt")

countLetters :: Circuit '[CommaSepFile] '[[String]] '[CommaSepFile [String]]
                  '[FileStore] '[[String]] '[FileStore [String]]
                  N1
countLetters = functionTask (map f) (FileStore "count.txt")
  where
    f word = (concat [word, ":", show (length word)])

circuit :: Circuit '[VariableStore] '[(())] '[VariableStore ()]
                  '[FileStore] '[[String]] '[FileStore [String]]
                  N1
circuit = generateWords <=> countLetters
```

Figure 5.8: A Broken Circuit Example

Chapter 6

Critical Evaluation

6.1 Runtime comparison

6.1.1 Lazy evaluation problems

6.2 Use of Library

Something about how DataStores prevent the need for `luigi.ExternalTask` at the beginning.

6.2.1 Other Libraries

How does it compare?

Luigi Object-orientated approach Python library

Funflow Uses arrows to compose flows sequentially.

6.3 Type safety

Chapter 7

Conclusion

Todo list

Change this to something meaningful	ix
Write an introduction (do near the end)	1
talk	11
Motivate further why a <code>DataStore</code> needs to exist — prevents the user from reading from a source incorrectly.	17
free moniod? maybe yes it looks like what eddie did...	19
try fix the half if i have time	20
'': looks awful	22
add a definition of these	30
this clear enough? maybe a diagram showing the layer and all the types	31
Sketchy :s	32
This is very long, but I cant really break it up because it needed the scoped type variables from beside	36

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