





motion estimation. This is the estimation of the 20 motion field from fromes in an image sequence.
This uses the Generalian Spectial and temporal variation in pixel values this does not model real motion, just apparent motioner optical flow, It is just a relationship between variation in pixel values. the have an image Sequence I(x, y, E).
and we want to find the variation of pixel values between frames to find the motion. the can assume I(x,y, \(\) i's constant along-the trajectory. ie d (I(1, y, e)) = 0. me know & and y are functions of t.

hence me can use the Chain rule to
give atotal derivative. $\frac{\partial I}{\partial x}$ $\frac{\partial x}{\partial E}$ $\frac{\partial I}{\partial y}$ $\frac{\partial J}{\partial E}$ = 0.

Gradients motion (V_x, V_y) . (Ix, Ig, Ie) So Ix Vx + Ty Vy + IL = 0. the could model motion in the following way, The pixel value (x,y,t) will nove by dx, dy and It. T(x+dt, y+dt, t+dt) = I(x,y,t). T(xxxx) T(xxxde, yxde, Exdt)

the could use clinear approximation. $T(x+dx, y+dy, t+dt) \approx T(x,y,t) + \frac{\partial I}{\partial x}dx + \frac{\partial I}{\partial y}dy + \frac{\partial I}{\partial t}dt$ the can then divide this approximation $\frac{\partial I}{\partial x} \cdot \frac{\partial x}{\partial t} + \frac{\partial I}{\partial y} \cdot \frac{\partial y}{\partial t} + \frac{\partial I}{\partial t} = 0$ Again this gives us Gradients $\left(\frac{\partial I}{\partial x}, \frac{\partial I}{\partial y}, \frac{\partial I}{\partial t}\right) = \left(I_{x}, I_{y}, I_{t}\right)$ Motion $\left(\frac{\partial x}{\partial t}, \frac{\partial y}{\partial t}\right) = (V_{x_1}, V_y)$ with the Optical Flow Equation, 1 20 V2 1 24 Uy 1 It = 0 At one pixel the OFE is under constrained meaning it can only estimate normal flow. So we need to add extractonstrains. Forexample, assume a parametric form of motion field in regions, or have a constant velocity. we could assume it is linear and xandy,
ey Vie = ax+ by+(. Lets look of the constant velocity model: · For a region, find the velocity v= (Vs., Uy) E (Vx, Vy) = [(Ix Vx + Iy Vy + IL)] to Solve this we can take derivatives with Vx and Vy. Set them to zero and solve for Vx and Vy.

Lucas & Kornade Algorithm. Solve for V= (vx, Vy) given that: V2 ZIx + Vg Z InIy = - ZIEIx Vx \(\SI_2\Ty + Vy \(\SI_0 \) = - \(\SI_4\Ty \) we can deline

A=Z[Ix]y Iy'] b=-Z[Ix]y me con coloulate V, doring sheet?

V=[V] = A'b. Motion Segmentation Motion is a good way of identified different objects and inferding depths me can use motion to segment framesinto regions fore xample, o to extract foreground from backy round moving against to isolate individual objects. awhite wall at this isolate individual objects. But this is not straight forward! moving paixels giving us foreground and backgrow.

1. Motion on its own may be abiguous for segmentation, we also went colour, Shape, texture 2. What do we consider a homogeneous motion region. Single motion, se parametric variation? 3. Generalised Aperture Problem. Large regions are needed forgood motion estimates but they are more litely to contain complex motions. Bigger theorea the more stuff likely googon.

Overvieto 7 Multion Estimation Eg.L. & k. Block motion of fitting Final Mohion Segmentation < Detection of dominant parametric motion (ithing Block Motion Fitting 215-Motion estimates -> 30 Motion. Vx=ax+by+c Vs 2 dx + ey+f me can assume linear

Detect Dominant Mutions the can use k-means todelect clusters in the parameter space! I.e. group, similar moving things that we together.

These clusters are the dominant motions. Vic= axt by tc Vy=d>c+ey+f (a, b, c) run kneuns over and (d,e,f). Each cluster gives as a (ay, by, cy) Motion Segmentation motion to the closest dominant Parametric Motion Regions we con then update our parametric motions V= (a, b, c) and Un = (d, e, f) using the assigned motions pixel motions (ag 5 y (cy) -> (ay , by , cy) (dy, dey, (y) -> (dy, ey, fy). the last thing to do is link these regions between the traines.

Spatial and Temporal Gradients. we want to find Ix, Iyand It. heres how, frame E frame ++1 Ix = (Ix + Ix + Ix + Ix) /4 I, = B-A T = D - C T = F - E

T = H - 6 I = A - C I, - B - D T = E - G

T = F - H I = (Ie + It + It + Id) /4 II = E - A It = F - B I = G - C Id = H - D

Or alternatively we could ill ustrate this in a very complicated way... Frame E+1 France Ix, Ty, Ie Yep, good Luck with that one :