

1. Derive the general heat conduction equation in cylindrical coordinates systems.
2. Consider a long rectangular bar of length a in the x -direction and width b in the y -direction. The temperatures of the surfaces at $x = 0$, $y = 0$, and $x = a$ are all equal to T_1 , while the temperature of the surface at $y = b$ is equal to T_2 . Assuming constant thermal conductivity and steady state heat conduction with no heat generation, (a) determine the general relation for temperature distribution inside the rectangular bar; (b) draw isotherms in the bar if ($b = 1.5a$).
3. Consider a water pipe of length $L = 17$ m, inner radius $r_1 = 15$ cm, outer radius $r_2 = 20$ cm, and thermal conductivity $k = 14$ W/m·K. Heat is generated in the pipe material uniformly by a 25-kW electric resistance heater. The inner and outer surfaces of the pipe are at $T_1 = 60^\circ\text{C}$ and $T_2 = 80^\circ\text{C}$, respectively. Obtain a general relation for temperature distribution inside the pipe under steady conditions and determine the temperature at the center plane of the pipe.
4. Heat is generated uniformly at a rate of 4.2×10^6 W/m³ in a spherical ball ($k = 45$ W/m·K) of diameter 24 cm. The ball is exposed to iced-water at 0°C with a heat transfer coefficient of 1200 W/m²·K. (a) express the differential equation and the boundary conditions for steady one-dimensional heat conduction through the spherical ball, (b) obtain a relation for the variation of temperature in the ball by solving the differential equation, and (c) Determine the temperatures at the center and the surface of the ball.
5. Watch Chap. 3 videos for undergraduate lectures on steady heat conduction and find answers to Chap. 3 review questions. Written answers are not required. Please be prepared to answer the review questions in the next lecture.