Problem Name:

Finding the root of non-linear equations using Bisection and False Position Method.

Apparatus:

- Computing Device (e.g., Computer)
- Programming Environment (MATLAB R2016b)

Method:

Closed type methods offer numerical solutions for root finding within specified intervals. The Bisection Method starts with an interval, calculates the midpoint, evaluates the function, and iteratively narrows down the interval. Meanwhile, the Regula Falsi Method employs linear interpolation to estimate the root, updates the interval, and refines the approximation through iterative steps. Both methods systematically converge to the root, providing effective solutions for non-linear equations.

Algorithm:

- Bisection Method Algorithm
 - 1. start
 - 2. Define function f(x)
 - 3. Choose initial guesses x0 and x1 such that f(x0) f(x1) < 0
 - 4. Choose pre-specified tolerable error e.
 - 5. Calculate new approximated root as $x^2 = (x^0 + x^1)/2$
 - 6. Calculate f(x0) f(x2)
 - a. if f(x0) f(x2) < 0 then x0 = x0 and x1 = x2

- b. if f(x0) f(x2) > 0 then x0 = x2 and x1 = x1
- c. if f(x0) f(x2) = 0 then goto (8)
- 7. if |f(x2)| > e then goto (5) otherwise goto (8)
- 8. Display x2 as root.
- 9. Stop

• False Position Method Algorithm

- 1. start
- 2. Define function f(x)
- 3. Choose initial guesses x0 and x1 such that f(x0) f(x1) < 0
- 4. Choose pre-specified tolerable error e.
- 5. Calculate new approximated root as:

$$x2 = x0 - ((x0-x1) * f(x0))/(f(x0) - f(x1))$$

- 6. Calculate f(x0) f(x2)
 - a. if f(x0) f(x2) < 0 then x0 = x0 and x1 = x2
 - b. if f(x0) f(x2) > 0 then x0 = x2 and x1 = x1
 - c. if f(x0) f(x2) = 0 then goto (8)
- 7. if |f(x2)| > e then goto (5) otherwise goto (8)
- 8. Display x2 as root.
- 9. Stop

Code:

Bisection Method Code-

```
%Clearing Screen
clc
% Setting x as symbolic variable
syms x;
% Input Section
y = input('Enter non-linear equations: ');
a = input('Enter first guess: ');
b = input('Enter second guess: ');
e = input('Tolerable error: ');
% Finding Functional Value
fa = eval(subs(y,x,a));
fb = eval(subs(y,x,b));
% Implementing Bisection Method
if fa*fb > 0
  disp('Given initial values do not bracket the root.');
end
while(fa*fb>0)
```

```
a = a+1;
  b = b+1;
  fa = eval(subs(y,x,a));
  fb = eval(subs(y,x,b));
end
  c = (a+b)/2;
  fc = eval(subs(y,x,c));
  fprintf('\n\n\t\t\t\t\t\t\t\t\t\t);
  while abs(fc)>e
  fprintf('%f\t%f\t%f\t%f\n',a,b,c,fc);
  if fa*fc < 0
    b = c;
  else
    a = c;
   end
  c = (a+b)/2;
   fc = eval(subs(y,x,c));
 end
 fprintf('\nRoot is: \%f\n', c);
```

False Position Method Code-

```
% Clearing Screen
clc
% Setting x as symbolic variable
syms x;
% Input Section
y = input('Enter non-linear equations: ');
a = input('Enter first guess: ');
b = input('Enter second guess: ');
e = input('Tolerable error: ');
% Finding Functional Value
fa = eval(subs(y,x,a));
fb = eval(subs(y,x,b));
% Implementing Bisection Method
if fa*fb > 0
  disp('Given initial values do not bracket the root.');
else
  c = a - (a-b) * fa/(fa-fb);
  fc = eval(subs(y,x,c));
  fprintf('\n\na\t\t\t\t\t\t\t\t\t\t\tf(c)\n');
```

```
while abs(fc)>e
    fprintf('%f\t%f\t%f\t%f\n',a,b,c,fc);
    if fa*fc< 0
        b = c;
        fb = eval(subs(y,x,b));
    else
        a = c;
        fa = eval(subs(y,x,a));
    end
        c = a - (a-b) * fa/(fa-fb);
        fc = eval(subs(y,x,c));
    end
    fprintf('\nRoot is: %f\n', c);
end</pre>
```

Input:

• For Bisection Method

Enter non-linear equations: sin(x)+cos(x)+exp(x)-8

Enter first guess: 2

Enter second guess: 3

Tolerable error: 0.00001

• For Regula Falsi Method

Enter non-linear equations: sin(x)+cos(x)+exp(x)-8

Enter first guess: 2

Enter second guess: 3

Tolerable error: 0.00001

Output:

• For Bisection Method

```
BisectionMethod.m × +

    Command Window

/MATLAB Drive/MATLAB Reports/BisectionMethod.m
                                                                                 Enter non-linear equations:
         %Clearing Screen
1
                                                                                 sin(x)+cos(x)+exp(x)-8
 2
                                                                                 Enter first guess:
 3
          % Setting x as symbolic variable
                                                                                 Enter second guess:
 4
          syms x;
                                                                                 Tolerable error:
 6
                                                                                 0.00001
 7
          % Input Section
 8
 9
          y = input('Enter non-linear equations: ');
                                                                                                        b
                                                                                                                                                         f(c)
          a = input('Enter first guess: ');
10
                                                                                2.000000
                                                                                                3.000000
                                                                                                                2.500000
                                                                                                                                3,979822
11
          b = input('Enter second guess: ');
                                                                                 2.000000
                                                                                                2.500000
                                                                                                                2.250000
                                                                                                                                 1.637635
          e = input('Tolerable error: ');
12
                                                                                 2.000000
                                                                                                2.250000
                                                                                                                 2.125000
                                                                                                                                 0.696951
13
                                                                                 2.000000
                                                                                                2.125000
                                                                                                                 2.062500
                                                                                                                                 0.275011
14
          % Finding Functional Value
                                                                                 2.000000
                                                                                                2.062500
                                                                                                                2.031250
                                                                                                                                 0.075106
15
          fa = eval(subs(y,x,a));
                                                                                 2.000000
                                                                                                2.031250
                                                                                                                2.015625
                                                                                                                                 -0.022202
16
          fb = eval(subs(y,x,b));
                                                                                 2.015625
                                                                                                2.031250
                                                                                                                 2.023438
                                                                                                                                 0.026235
17
                                                                                 2.015625
                                                                                                2.023438
                                                                                                                2.019531
                                                                                                                                 0.001963
18
          % Implementing Bisection Method
                                                                                 2.015625
                                                                                                2.019531
                                                                                                                2.017578
                                                                                                                                 -0.010133
                                                                                 2.017578
                                                                                                                 2.018555
                                                                                                                                 -0.004089
19
                                                                                                2.019531
20
          if fa*fb > 0
                                                                                 2.018555
                                                                                                2.019531
                                                                                                                 2.019043
                                                                                                                                 -0.001064
                                                                                 2.019043
                                                                                                2.019531
                                                                                                                2.019287
                                                                                                                                 0.000449
21
             disp('Given initial values do not bracket the root.');
                                                                                 2.019043
                                                                                                2.019287
                                                                                                                 2.019165
                                                                                                                                 -0.000307
22
                                                                                 2.019165
                                                                                                 2.019287
                                                                                                                 2.019226
                                                                                                                                 0.000071
23
                                                                                                                 2.019196
                                                                                                                                 -0.000118
                                                                                 2.019165
                                                                                                2.019226
24
     日
          while(fa*fb>0)
                                                                                 2.019196
                                                                                                2.019226
                                                                                                                 2.019211
                                                                                                                                 -0.000024
25
             a = a+1;
                                                                                 2.019211
                                                                                                2.019226
                                                                                                                 2.019218
                                                                                                                                 0.000024
26
             b = b+1;
27
             fa = eval(subs(y,x,a));
                                                                                 Root is: 2.019215
             fb = eval(subs(y,x,b));
28
                                                                                 >>
29
30
31
             c = (a+b)/2;
32
              fc = eval(subs(y,x,c));
              fprintf('\n\na\t\t\t\t\t\t\t\t\t\t\t\t);
33
             while abs(fc)>e
34
35
              fprintf('%f\t%f\t%f\t%f\n',a,b,c,fc);
36
              if fa*fc < 0
37
                 b = c;
38
39
               else
40
                 a = c;
41
42
               end
43
44
               c = (a+b)/2;
45
               fc = eval(subs(y,x,c));
                                                                                 - Code Issues
46
47
                                                                                  Open Files ▼
48
           fprintf('\nRoot is: %f\n', c);
```

For False Position Method

```
    Command Window

RegulaFalsiMethod.m × BisectionMethod.m × +
/MATLAB Drive/MATLAB Reports/RegulaFalsiMethod.m
                                                                                 Enter non-linear equations:
 1
          % Clearing Screen
                                                                              sin(x)+cos(x)+exp(x)-8
 2
                                                                                 Enter first guess:
 3
 4
          % Setting x as symbolic variable
                                                                                 Enter second guess:
 5
                                                                                 Tolerable error:
 6
                                                                                 0.00001
 7
         % Input Section
 8
         y = input('Enter non-linear equations: ');
          a = input('Enter first guess: ');
 9
                                                                                                                                                          f(c)
         b = input('Enter second guess: ');
10
                                                                                 2.000000
                                                                                                 3.000000
                                                                                                                 2.010374
                                                                                                                                 -0.054516
          e = input('Tolerable error: ');
11
                                                                                                                 2.015152
                                                                                                                                 -0.025119
                                                                                 2.010374
                                                                                                 3.000000
12
                                                                                 2.015152
                                                                                                 3.000000
                                                                                                                 2.017349
                                                                                                                                 -0.011551
13
         % Finding Functional Value
                                                                                                                 2.018358
                                                                                                                                 -0.005306
                                                                                 2.017349
                                                                                                 3.000000
14
          fa = eval(subs(y,x,a));
                                                                                 2.018358
                                                                                                 3.000000
                                                                                                                 2.018821
                                                                                                                                 -0.002437
15
          fb = eval(subs(y,x,b));
                                                                                 2.018821
                                                                                                 3.000000
                                                                                                                 2.019034
                                                                                                                                 -0.001119
16
                                                                                 2.019034
                                                                                                 3.000000
                                                                                                                 2.019132
                                                                                                                                 -0.000514
17
         % Implementing Bisection Method
                                                                                                                 2.019177
                                                                                                                                 -0.000236
                                                                                 2.019132
                                                                                                 3.000000
          if fa*fb > 0
18
                                                                                 2.019177
                                                                                                 3.000000
                                                                                                                 2.019197
                                                                                                                                 -0.000108
              disp('Given initial values do not bracket the root.');
19
                                                                                                                 2.019207
                                                                                                                                 -0.000050
                                                                                 2.019197
                                                                                                 3.000000
                                                                                                 3.000000
                                                                                                                 2.019211
                                                                                                                                 -0.000023
                                                                                 2.019207
20
                                                                                 2.019211
                                                                                                 3.000000
                                                                                                                 2.019213
                                                                                                                                 -0.000010
21
             c = a - (a-b) * fa/(fa-fb);
22
             fc = eval(subs(y,x,c));
                                                                                 Root is: 2.019214
23
              fprintf('\n\na\t\t\t\t\t\t\t\t\t\t\t\f(c)\n');
24
             while abs(fc)>e
                  fprintf('%f\t%f\t%f\t%f\n',a,b,c,fc);
25
                  if fa*fc< 0
26
27
                      b =c;
                      fb = eval(subs(y,x,b));
28
29
                  else
30
                      fa = eval(subs(y,x,a));
31
32
33
                  c = a - (a-b) * fa/(fa-fb);
34
                  fc = eval(subs(y,x,c));
35
36
              fprintf('\nRoot is: %f\n', c);
37
```

Discussion:

In this report, the problem involved the implementation of the Bisection and Regula Falsi (False Position) methods for root finding in non-linear equations.

Throughout the coding process, certain challenges surfaced, particularly in handling input parameters. Additionally, working with MATLAB for the first time posed a learning curve, adding an extra layer of complexity to the implementation. Despite these initial hurdles, the report systematically evaluates the performance of closed type methods, emphasizing aspects like convergence rates, accuracy, and stability. The choice between Bisection and Regula Falsi is further explored, considering factors such as function smoothness and the initial guess for the root. The algorithms and code presented here not only address the core problem but also highlight the learning experiences encountered during the coding phase.