

Problem Name:

Performing intra and extra polation using Lagrange Interpolation Method.

Apparatus:

- Computing Device (e.g.; Computer)
- Programming Environment (MATLAB R2016b)

Method:

The Lagrange interpolation method based on two points is straightforward to implement due to its simplicity. With only two points, the calculation involves basic arithmetic operations, making it computationally efficient.

Algorithm:

1. Start
2. Read number of data (n)
3. Read data X_i and Y_i for $i=1$ to n
4. Read value of independent variables say x_p
whose corresponding value of dependent say y_p is to be determined.
5. Initialize: $y_p = 0$
6. For $i = 1$ to n
Set $p = 1$

For j =1 to n

 If $i \neq j$ then

 Calculate $p = p * (x_p - X_j)/(X_i - X_j)$

 End If

Next j

Calculate $y_p = y_p + p * Y_i$

Next i

6. Display value of y_p as interpolated value.

7. Stop

Code:

```
function y0= LagrangeInterpolation_1039(x, y, x0)
```

```
x= input('Enter x values: ');
```

```
y= input('Enter y values: ');
```

```
x0= input('Enter new x: ');
```

%x is the vector of abscissa

%y is the matching vector of ordinates

%x0 represents target to be interpolated

%y0 represents the solution from Lagrange Interpolation

```
y0=0;
```

```

n= length(x);
for j=1:n
    t=1;
    for i=1:n
        if i~=j
            t=t*(x0-x(i))/(x(j)-x(i));
        end
    end
    y0=y0+t*y(j);
end
end

```

Input:

Enter x values: [1; 2; 3; 4; 5; 6]

Enter y values: [3; 0; -1; 0; 3; 8]

Enter new x: 8

Output:

Editor - C:\Rim(1039)\LagrangeInterpolation_1039.m

LagrangeInterpolation_1039.m

```
1 function y0= LagrangeInterpolation_1039(~, ~, ~)
2 x= input('Enter x values: ');
3 y= input('Enter y values: ');
4 x0= input('Enter new x: ');
5
6 %x is the vector of abscissa
7 %y is the matching vector of ordinates
8 %x0 represents target to be interpolated
9 %y0 represents the solution from Lagrange Interpolation
10
11 y0=0;
12 n= length(x);
13 for j=1:n
14     t=1;
15     for i=1:n
16         if i~=j
17             t=t*(x0-x(i))/(x(j)-x(i));
18         end
19     end
20     y0=y0+t*y(j);
21 end
22 end
```

Command Window

>> LagrangeInterpolation_1039
Enter x values: [1;2;3;4;5;6]
Enter y values: [3;0;-1;0;3;8]
Enter new x: 8

ans =

24.0000

fx >> |

Discussion:

Lagrange interpolation is a powerful technique for approximating a function based on a set of data points. By constructing an interpolation polynomial through Lagrange basis polynomials, it provides a flexible approach to data interpolation. However, careful consideration is required to balance accuracy with computational complexity and numerical stability issues.