

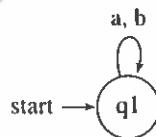
CMSC 303 Introduction to Theory of Computation

Deterministic Finite Automata Exercise

Key

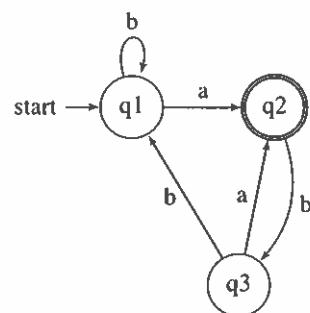
1. When given $\Sigma = \{a, b\}$, which of the following are DFA's? Explain why or why not.

(a)



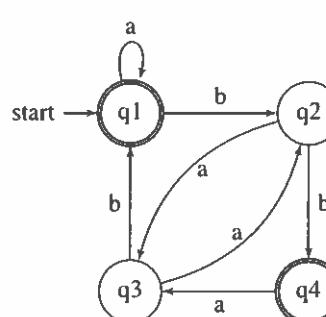
Yes. Have transitions for both alphabet symbols from every state.

(b)



No. State 2 does not have a transition for the symbol a.

2. Give the formal description of the DFA below:



$$Q = \{q_1, q_2, q_3, q_4\}$$

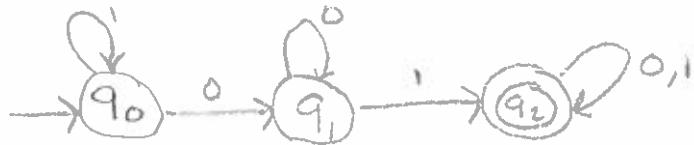
$$\Sigma = \{a, b\}$$

$$q_0 = q_1$$

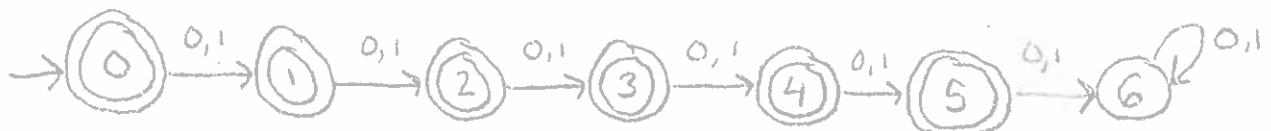
$$F = \{q_1, q_4\}$$

δ	a	b
q_1	q_1	q_2
q_2	q_3	q_4
q_3	q_2	q_1
q_4	q_3	q_4

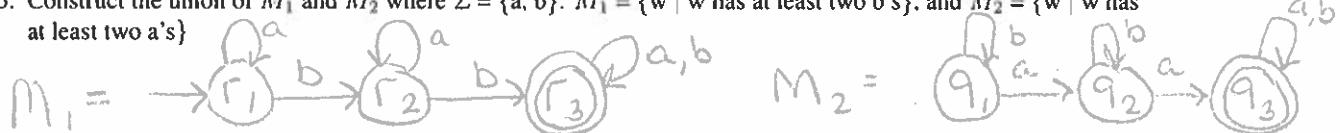
3. Construct the state diagram recognizing the following languages: $L = \{w \mid w \text{ contains the substring } 01\}$, $\Sigma = \{0, 1\}$



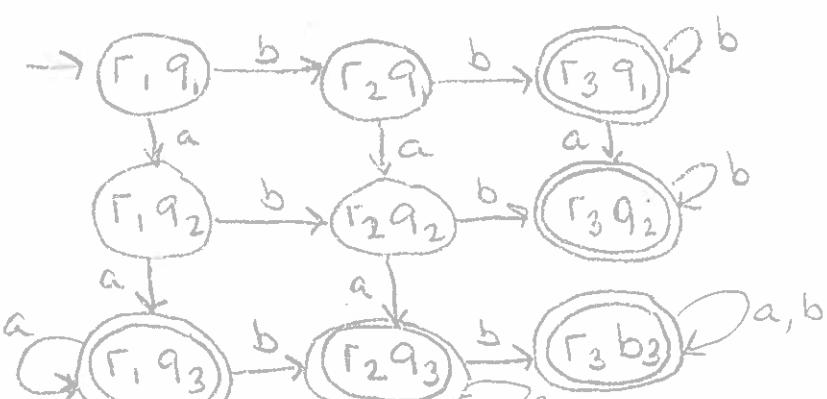
4. Construct the state diagram recognizing the following languages: $L = \{w \mid \text{length of } w \text{ is at most 5 symbols}\}$, $\Sigma = \{0, 1\}$



5. Construct the union of M_1 and M_2 where $\Sigma = \{a, b\}$. $M_1 = \{w \mid w \text{ has at least two } b\text{'s}\}$, and $M_2 = \{w \mid w \text{ has at least two } a\text{'s}\}$



$$M_1 \cup M_2$$



6. Construct the state diagram recognizing the following languages: $L = \{w \mid \text{every odd position of } w \text{ is 1}\}$, $\Sigma = \{0, 1\}$

