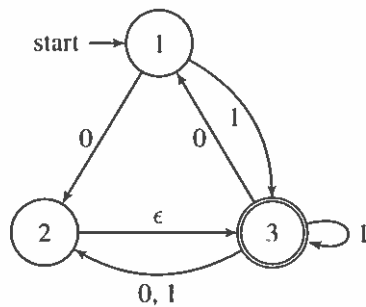


# CMSC 303 Introduction to Theory of Computation

## Nondeterministic Finite Automata and Regular Expressions

### Exercise

1. Formally describe this NFA:



$$Q = \{1, 2, 3\}$$

$$\Sigma = \{0, 1\}$$

$$\Sigma_{\epsilon} = \{0, 1, \epsilon\}$$

$$q_0 = 1$$

$$F = \{3\}$$

$q$	0	1	$\epsilon$
1	$\{2\}$	$\{3\}$	$\emptyset$
2	$\emptyset$	$\emptyset$	$\{3\}$
3	$\{1, 2\}$	$\{2, 3\}$	$\emptyset$

2. Convert the NFA below into a DFA.

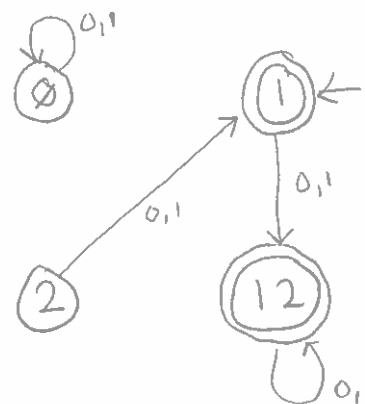
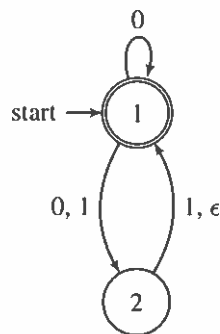
$$|Q| = 2$$

$$2^{|Q|} = 2^2 = 4$$

$$Q' = \{\emptyset, 1, 2, 12\}$$

$$q'_0 = 1$$

$$F = \{1, 12\}$$



Note: At state 2 on input of 0, You can slide to 1 and then stay at 1.

3. Create the regular expression to represent the language  $R = \{w \mid w \in \{0, 1\}^* \text{ and contains the string } 001 \text{ as a substring}\}$ .

$$\Sigma^* 001 \Sigma^*$$

4. Create the regular expression to represent the language  $R = \{w \mid w \in \{0, 1\}^* \text{ and starts with a 1 and has even length}\}$ .

$$1 \Sigma (\Sigma^2)^*$$

5. Convert the NFA below into a DFA.

$$|Q| = 3$$

$$2^{|Q|} = 2^3 = 8$$

$$Q' = \{\emptyset, 1, 2, 3, 12, 13, 23, 123\}$$

$$q_0' = 1$$

$$F = \{3, 13, 23, 123\}$$

