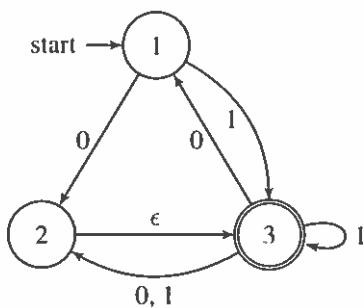


CMSC 303 Introduction to Theory of Computation
 Nondeterministic Finite Automata and Regular Expressions
 Exercise

1. Formally describe this NFA:

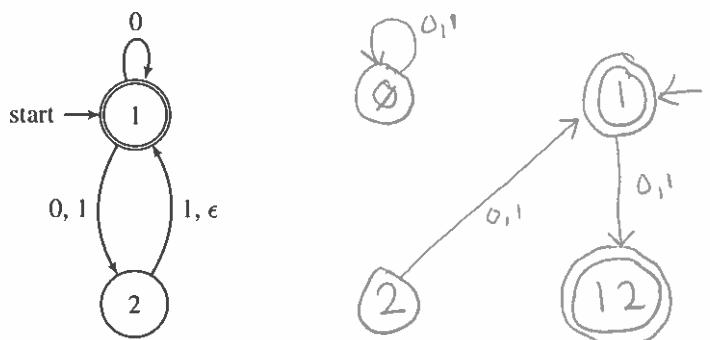


$$\begin{aligned}
 Q &= \{1, 2, 3\} \\
 \Sigma &= \{0, 1\} \\
 \Sigma_\epsilon &= \{0, 1, \epsilon\} \\
 q_0 &= 1 \\
 F &= \{3\}
 \end{aligned}$$

δ	0	1	ϵ
1	$\{2, 3\}$	$\{3\}$	\emptyset
2	\emptyset	\emptyset	$\{3\}$
3	$\{1, 2\}$	$\{2, 3\}$	\emptyset

2. Convert the NFA below into a DFA.

$$\begin{aligned}
 |Q| &= 2 \\
 2^{|Q|} &= 2^2 = 4 \\
 Q' &= \{\emptyset, 1, 2, 12\} \\
 q'_0 &= \emptyset \\
 F &= \{1, 12\}
 \end{aligned}$$



Note: At state 2 on input of 0,
 You can slide to 1 and then
 stay at 1.

3. Create the regular expression to represent the language $R = \{w \mid w \in \{0, 1\}^* \text{ and contains the string } 001 \text{ as a substring}\}$.

$$\Sigma^* 001 \Sigma^*$$

4. Create the regular expression to represent the language $R = \{w \mid w \in \{0, 1\}^* \text{ and starts with a } 1 \text{ and has even length}\}$.

$$1 \Sigma (\Sigma^2)^*$$

5. Convert the NFA below into a DFA.

$$|Q|=3$$

$$2^{|Q|} = 2^3 = 8$$

$$Q' = \{\emptyset, 1, 2, 3, 12, 13, 23, 123\}$$

$$q_0' = 1$$

$$F = \{3, 13, 23, 123\}$$

