Recursive Objects

(Revisit) Lecture Quiz

__str__ and objects

Consider the following variable assignments. Which of the created variables can we call <u>str</u> on?

```
class Lamb:
    species_name = "Lamb"
    scientific_name = "Ovis aries"

def __init__(self, name):
    self.name = name

lamb = Lamb("Fleecey")  # 80%

grade = 79.5  # 80%

colors = ["red", "orange", "yellow"]  # 72%

translations = {"one": "uno", "two": "dos"} # 65%

is_fluffy = True  # 60%
```

__str__ and objects

Consider the following variable assignments. Which of the created variables can we call str on?

```
class Lamb:
    species name = "Lamb"
   scientific name = "Ovis aries"
   def __init__(self, name):
        self.name = name
                                           # 80%
lamb = Lamb("Fleecey")
print(Lamb. str (lamb))
grade = 79.5
                                           # 80%
print(float. str (grade))
colors = ["red", "orange", "yellow"]
                                           # 72%
print(list. str (colors))
translations = {"one": "uno", "two": "dos"} # 65%
print(dict. str (translations))
is fluffy = True
                                           # 60%
print(bool. str (is fluffy))
```

All of them! All of them inherit from object and thus have a __str__ method defined. Run type(var).__str__(var) to prove it to yourself.

Attribute access

Imagine we have a class Book with a class variable available formats, and an instance of that class named bookywook.

```
class Book:
    available_formats = ["Kindle", "paperback"]

def __init__(self, title):
    self.title = title

bookywook = Book("Where's Boo?")
```

Which line of code would retrieve the value of that attribute?

```
Book.__getattribute__(bookywook, "available_formats") # 61%

getattr(bookywook, "available_formats") # 60%

bookywook.available_formats # 51%

Book.available_formats # 20%

getattr(Book, "available_formats") # 19%
```

Attribute access

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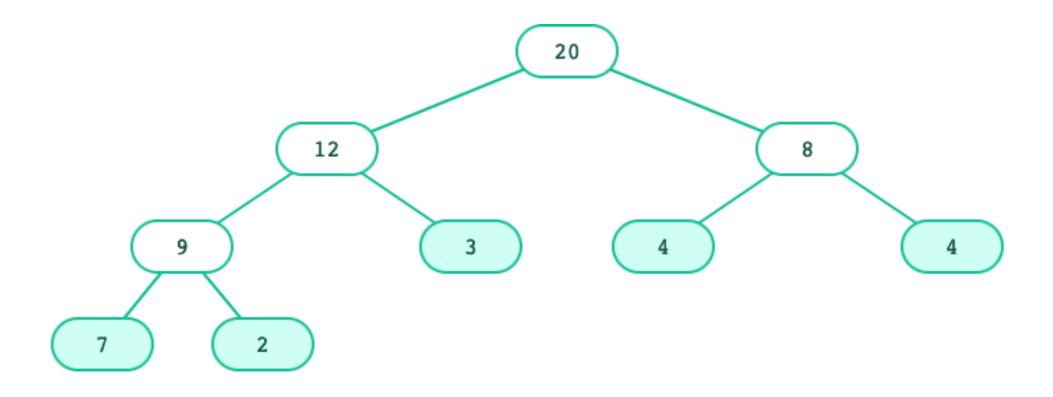
Book.available_formats # 20%

getattr(Book, "available_formats") # 19%
```

All of them retrieve the value!

Trees

Tree concepts



- A tree has a root label and a list of branches
- Each branch is itself a tree
- A tree with zero branches is called a leaf

Trees: Data abstraction

This is what we've been using:

<pre>tree(label, children)</pre>	Returns a tree with given LABEL at its root, whose children are CHILDREN	
label(tree)	Returns the label of root node of TREE	
branches(tree)	Returns the branches of TREE (each a tree).	
<pre>is_leaf(tree)</pre>	Returns true if TREE is a leaf node.	

Trees: Data abstraction

Using an implementation like this:

```
def tree(label, branches=[]):
    return [label] + list(branches)

def label(tree):
    return tree[0]

def branches(tree):
    return tree[1:]

def is_leaf(tree):
    return not branches(tree)
```

How could we represent trees as a Python class?

A Tree class

```
class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        self.branches = list(branches)

def is_leaf(self):
    return not self.branches
```

What's different? What's the same?

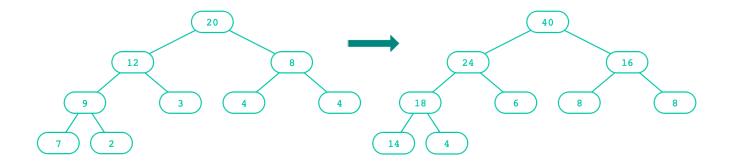
tree versus Tree

```
tree
t = tree(label, branches=[])
branches(t)
t.branches
label(t)
t.label
is_leaf(t)
t.is_leaf()
```

```
def fib_tree(n):
    if n == 0 or n == 1:
        return tree(n)
    else:
        left = fib_tree(n - 2)
        right = fib_tree(n - 1)
        fib_n = label(left) + label(right)
        return tree(fib_n, [left, right])
```

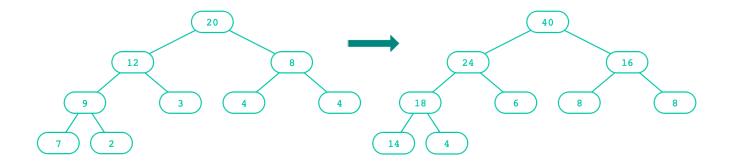
```
def fib_tree(n):
    if n == 0 or n == 1:
        return Tree(n)
    else:
        left = fib_tree(n - 2)
        right = fib_tree(n - 1)
        fib_n = left.label + right.label
        return Tree(fib_n, [left, right])
```

Doubling a Tree



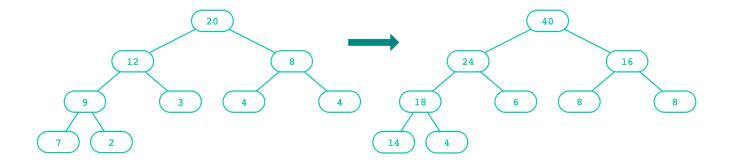
Is the Tree object mutable or immutable?
Is double(t) destructive or non-destructive?

Doubling a Tree



Is the Tree object mutable or immutable? Mutable! Is double(t) destructive or non-destructive?

Doubling a Tree



Is the <u>Tree</u> object mutable or immutable? Mutable!
Is <u>double(t)</u> destructive or non-destructive? Destructive!

A fancier Tree

This is what assignments actually use:

```
class Tree:
   def init (self, label, branches=[]):
        self.label = label
        for branch in branches:
            assert isinstance(branch, Tree)
       self.branches = list(branches)
   def is leaf(self):
        return not self.branches
   def repr (self):
       if self.branches:
           branch_str = ', ' + repr(self.branches)
       else:
           branch str = ''
       return 'Tree({0}{1})'.format(self.label, branch str)
   def str (self):
        return '\n'.join(self.indented())
   def indented(self):
       lines = []
        for b in self.branches:
            for line in b.indented():
               lines.append(' ' + line)
        return [str(self.label)] + lines
```

It's built in to code.cs61a.org, and remember, you can draw() any tree/Tree.

Linked lists

Why do we need a new list?

Python lists are implemented as a "dynamic array", which isn't optimal for all use cases.

figure Inserting an element is slow, especially near front of list:

"A"	"B"	"C"	"D"	"E"	"F"
0	1	2	3	4	5
3300	3301	3302	3303	3304	3305

What should we insert?

value: Z @ index: 3 Insert

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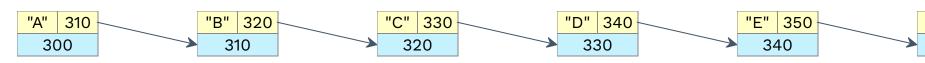
What should we insert?

value: Z @ index: 3 Insert

Plus inserting too many elements can require re-creating the entire list in memory, if it exceeds the pre-allocated memory.

Linked lists

A linked list is a chain of objects where each object holds a **value** and a **reference to the next link**. The list ends when the final reference is empty.

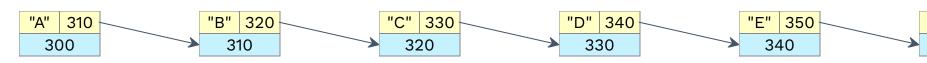


What should we insert?

value: Z @ index: 5 Insert

Linked lists

A linked list is a chain of objects where each object holds a **value** and a **reference to the next link**. The list ends when the final reference is empty.



What should we insert?

value: Z @ index: 5 Insert

Linked lists require more space but provide faster insertion.

A Link class

```
class Link:
    empty = ()

def __init__(self, first, rest=empty):
    self.first = first
    self.rest = rest
```

How would we use that?

A Link class

```
class Link:
    empty = ()

def __init__(self, first, rest=empty):
    self.first = first
    self.rest = rest
```

How would we use that?

```
ll = Link("A", Link("B", Link("C")))
```



A fancier LinkedList

```
class Link:
   """A linked list."""
    empty = ()
    def init (self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
       self.first = first
       self.rest = rest
    def __repr__(self):
       if self.rest:
           rest_repr = ', ' + repr(self.rest)
       else:
            rest_repr = ''
       return 'Link(' + repr(self.first) + rest_repr + ')'
    def str (self):
        string = '<'
       while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
       return string + str(self.first) + '>'
```

It's built-in to code.cs61a.org and you can draw() any Link.

Creating linked lists

Creating a range

Similar to [x for x in range(3, 6)]

```
def range_link(start, end):
    """Return a Link containing consecutive integers
    from START to END, not including END.
    >>> range_link(3, 6)
    Link(3, Link(4, Link(5)))
    """
```



Creating a range

Similar to [x for x in range(3, 6)]

```
def range_link(start, end):
    """Return a Link containing consecutive integers
    from START to END, not including END.
    >>> range_link(3, 6)
    Link(3, Link(4, Link(5)))
    """
    if start >= end:
        return Link.empty
    return Link(start, range_link(start + 1, end))
```



Mapping a linked list

Similar to [f(x) for x in 1st]

```
def map_link(f, ll):
    """Return a Link that contains f(x) for each x in Link LL.
    >>> square = lambda x: x * x
    >>> map_link(square, range_link(3, 6))
    Link(9, Link(16, Link(25)))
    """
```



Mapping a linked list

Similar to [f(x) for x in 1st]

```
def map_link(f, ll):
    """Return a Link that contains f(x) for each x in Link LL.
    >>> square = lambda x: x * x
    >>> map_link(square, range_link(3, 6))
    Link(9, Link(16, Link(25)))
    """
    if ll is Link.empty:
        return Link.empty
    return Link(f(ll.first), map_link(f, ll.rest))
```



Filtering a linked list

Similar to [x for x in lst if f(x)]

```
def filter_link(f, ll):
    """Return a Link that contains only the elements x of Link LL
    for which f(x) is a true value.
    >> is_odd = lambda x: x % 2 == 1
    >> filter_link(is_odd, range_link(3, 6))
    Link(3, Link(5))
    """
```



Filtering a linked list

Similar to [x for x in lst if f(x)]

```
def filter_link(f, ll):
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    >> is_odd = lambda x: x % 2 == 1
    >> filter_link(is_odd, range_link(3, 6))
    Link(3, Link(5))
    """

if ll is Link.empty:
    return Link.empty
elif f(ll.first):
    return Link(ll.first, filter_link(f, ll.rest))
return filter_link(f, ll.rest)
```



Mutating linked lists

Linked lists can change

Attribute assignments can change first and rest attributes of a Link.

```
s = Link("A", Link("B", Link("C")))
s.first = "Hi"
s.rest.first = "Hola"
s.rest.rest.first = "Oi"
```



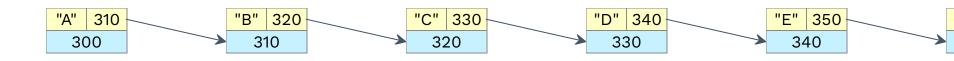
Beware infinite lists

The rest of a linked list can contain the linked list as a sub-list.

```
s = Link("A", Link("B", Link("C")))
t = s.rest
t.rest = s

s.first
s.rest.rest.rest.rest.first
```

Adding to front of linked list

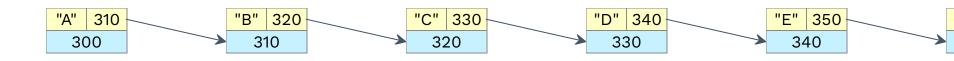


Insert

```
def insert_front(linked_list, new_val):
    """Inserts NEW_VAL in front of LINKED_LIST,
    returning new linked list.

>>> ll = Link(1, Link(3, Link(5)))
    >>> insert_front(ll, 0)
    Link(0, Link(1, Link(3, Link(5))))
    """
```

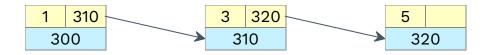
Adding to front of linked list



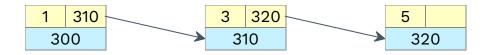
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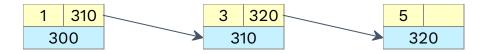
>>> ll = Link(1, Link(3, Link(5)))
    >>> insert_front(ll, 0)
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    """
    return Link(new_val, linked_list)
```



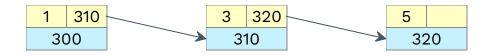
```
def add(ordered_list, new_val):
    """Add NEW_VAL to ORDERED_LIST, returning modified ORDERED_LIST.
    >> s = Link(1, Link(3, Link(5)))
    >> add(s, 0)
    Link(0, Link(1, Link(3, Link(5))))
    >> add(s, 3)
    Link(0, Link(1, Link(3, Link(5))))
    >> add(s, 4)
    Link(0, Link(1, Link(3, Link(4, Link(5)))))
    >> add(s, 6)
    Link(0, Link(1, Link(3, Link(4, Link(5, Link(6))))))
    """
    if new_val < ordered_list.first:
    elif new_val > ordered_list.first and ordered_list.rest is Link.empty:
        return ordered_list
```



```
def add(ordered list, new val):
    """Add NEW VAL to ORDERED LIST, returning modified ORDERED LIST.
   >>> s = Link(1, Link(3, Link(5)))
   >>> add(s, 0)
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   Link(0, Link(1, Link(3, Link(4, Link(5, Link(6))))))
    if new val < ordered list.first:</pre>
        original first = ordered list.first
        ordered list.first = new val
        ordered list.rest = Link(original first, ordered list.rest)
   elif new val > ordered list.first and ordered list.rest is Link.empty:
    elif new val > ordered list.first:
    return ordered list
```



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   elif new val > ordered list.first and ordered list.rest is Link.empty:
        ordered list.rest = Link(new val)
    elif new val > ordered list.first:
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        original first = ordered list.first
        ordered list.first = new val
        ordered list.rest = Link(original first, ordered list.rest)
   elif new val > ordered list.first and ordered list.rest is Link.empty:
        ordered list.rest = Link(new val)
    elif new val > ordered list.first:
        add(ordered list.rest, new val)
    return ordered list
```

Showdown: Python list vs. Link

The challenge:

- Store all the half-a-million words in "War and Peace"
- Insert a word at the beginning.

Version	10,000 runs	100,000 runs
Python list		
Link		

Try it yourself on your local machine (Legit Python!): warandpeace.py

Showdown: Python list vs. Link

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- Store all the half-a-million words in "War and Peace"
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Version	10,000 runs	100,000 runs
Python list	2.6 seconds	37 seconds
Link		

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- Insert a word at the beginning.

Version	10,000 runs	100,000 runs	
Python list	2.6 seconds	37 seconds	
Link	0.01 seconds	0.1	

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Recursive objects

Why are Tree and Link considered recursive objects?

Recursive objects

Why are Tree and Link considered recursive objects?

Each type of object contains references to the same type of object.

- An instance of Tree can contain additional instances of Tree, in the branches variable.
- An instance of Link can contain an additional instance of Link, in the rest variable.

Both classes lend themselves to recursive algorithms. Generally:

- For Tree: The base case is when is_leaf() is true; the recursive call is on the branches.
- For Link: The base case is when the rest is empty; the recursive call is on the rest.