Std Code Library(Qinhuangdao)

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一切的开始

Codeforces/XCPC

● 需要 C++17/C++20

```
#include <bits/stdc++.h>
   #define endl '\n'
   #define pll pair<ll, ll>
   #define tll tuple<ll, ll, ll>
5 #define vi vector<int>
   #define vl vector<ll>
   #define x first
   #define y second
   #define rep(i, j, k) for(int i = (j); i \le (k); i++)
   #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
   #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
11
   using namespace std;
   typedef long long ll;
13
   const ll maxn = 2e5 + 10;
   const ll mod = 998244353;
15
   const ll inf32 = 1e9;
16
   const ll inf64 = 1e18;
17
18
19
   void solve(){
20
21
22
   }
23
24
   int main(){
       ios;
25
        //freopen("sample.txt", "r", stdin);
26
        //freopen("resout.txt", "w", stdout);
27
       int t = 1;
28
29
        //cin >> t;
        while(t--){
30
31
            solve();
32
        return 0;
33
34
   }
35
```

int128

• 不要使用 cin/cout, 记得关同步流

```
typedef __int128 i128;
    i128 read()
4
    {
       i128 x = 0; bool f = 0;
5
       char c = getchar();
       while (c < '0' || c > '9')
           if (c == '-')
               f = 1;
           c = getchar();
11
12
       }
       while (c >= '0' && c <= '9')
13
14
           x = (x << 1) + (x << 3) + (c ^ 48);
15
           c = getchar();
16
17
       return f ? -x : x;
18
    }
19
20
    inline void write(i128 x)
21
22
       if (x < 0)
23
           putchar('-'), x = -x;
24
       if (x > 9)
25
```

```
write(x / 10);
27
       putchar(x % 10 + '0');
   }
28
```

数据结构

二维数点

```
● 逆序对
    #include <bits/stdc++.h>
    using namespace std;
    typedef long long ll;
    const int maxn = 500010;
    ll m;
    ll a[maxn], b[maxn], c[maxn];
    int lowbit(int x){return x & (-x);}
    void add(int x, ll y){
        for (int i = x; i <= m; i += lowbit(i)) c[i] += y;</pre>
    }
10
11
    ll sum(int x){
        ll res = 0;
12
13
        for (int i = x; i; i -= lowbit(i)) res += c[i];
        return res;
14
15
    }
    int main(){
16
        int n;
17
        cin >> n;
18
        for (int i = 1; i <= n; ++i){</pre>
19
            cin >> a[i];
20
            b[i] = a[i];
21
22
        sort(b + 1, b + n + 1);
        m = unique(b + 1, b + n + 1) - b - 1;
24
        ll ans = 0;
25
        for (int i = n; i; i--){
26
            int k = lower_bound(b + 1, b + m + 1, a[i]) - b;
27
28
            ans += sum(k - 1);
            add(k, 1);
29
        cout << ans;</pre>
31
        return 0;
32
33
   }
        • 园丁的烦恼 (矩阵内点的个数)
    #include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define pii pair<int, int>
    #define vi vector<int>
    #define vl vector<ll>
    #define rep(i, j, k) for(int i = (j); i <= (k); i++)
    #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
    #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
    using namespace std;
11
    typedef long long ll;
    const ll maxn = 1e7 + 10;
13
    const ll mod = 998244353;
14
    const ll inf = 0x3f3f3f3f;
15
16
    struct BIT{
17
        int tr[maxn];
18
19
        int lowbit(int x){return x & -x;}
        void add(int p, int x){
20
            for (; p < maxn; p += lowbit(p)) tr[p] += x;</pre>
21
22
23
        ll query(int p){
24
            ll sum = 0;
```

```
for (; p > 0; p -= lowbit(p))
25
26
                  sum += tr[p];
27
             return sum;
         }
28
    }Tr;
30
    void solve(){
31
         int n, m;
32
         cin >> n >> m;
33
34
         vector<pii> pos;
         vector<tuple<int, int, int, int>> q;
35
36
         vector<ll> ans(m + 1);
37
         rep(i, 1, n){
             int tx, ty;
38
39
             cin >> tx >> ty;
             tx++, ty++;
40
41
             pos.push_back({tx, ty});
42
43
         sort(pos.begin(), pos.end());
44
         rep(i, 1, m){
             int x1, y1, x2, y2;
45
46
             cin >> x1 >> y1 >> x2 >> y2;
             x1++, y1++, x2++, y2++;
47
             q.push_back(\{x1 - 1, y1 - 1, 1, i\});
             q.push_back(\{x1 - 1, y2, -1, i\});
49
50
             q.push_back(\{x2, y1 - 1, -1, i\});
51
             q.push_back({x2, y2, 1, i});
52
         sort(q.begin(), q.end());
53
         int cur = 0;
54
         for (auto [x, y, c, id] : q){
55
             while (cur < n && pos[cur].first <= x) Tr.add(pos[cur++].second, 1);</pre>
56
57
             ans[id] += c * Tr.query(y);
58
         }
         rep(i, 1, m) cout << ans[i] << endl;</pre>
59
    }
60
61
    int main(){
62
63
         //freopen("sample.txt", "r", stdin);
//freopen("resout.txt", "w", stdout);
64
65
         int t = 1;
66
         //cin >> t;
67
68
         while(t--){
             solve();
69
70
         return 0;
71
    }
```

● HH 的项链(区间元素种类)照常把 x 所在一维降掉后,发现 y 轴并没有明显的偏序关系。可以这样考虑,我们只计每个元素第一次在区间中出现时有贡献,设 pre[i] 表示位置 i 的元素前一次出现的位置,在整个序列中第一次出现时记为 0

```
#include <bits/stdc++.h>
1
   #define endl '\n'
   #define pll pair<ll, ll>
   #define tll tuple<ll, ll, ll>
   #define vi vector<int>
   #define vl vector<ll>
   #define rep(i, j, k) for(int i = (j); i \le (k); i++)
   #define per(i, j, k) for(int i = (j); i \ge (k); i--)
   #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
   using namespace std;
10
   typedef long long ll;
11
   const ll maxn = 1e6 + 10;
12
   const ll mod = 998244353;
13
14
   const ll inf = 0x3f3f3f3f3f;
15
   struct BIT{
       ll tr[maxn];
17
        int lowbit(int x){return x & -x;}
18
19
        void add(int p, ll x){
```

```
for (; p < maxn; p += lowbit(p)) tr[p] += x;</pre>
20
21
        ll query(int p){
22
23
            ll sum = 0;
24
            for (; p > 0; p -= lowbit(p))
                sum += tr[p];
25
            return sum;
26
        }
27
   }Tr;
28
29
    ll pre[maxn], ans[maxn];
30
31
    void solve(){
        int n, m;
32
        cin >> n;
33
34
        vector<pll> pos;
        vector<tuple<int, int, int, int>> q;
35
36
        for (int i = 3; i <= n + 2; ++i){
            int a;
37
38
            cin >> a;
            pos.push_back({i, pre[a] ? pre[a] : 2}), pre[a] = i;
39
40
41
        sort(pos.begin(), pos.end());
        cin >> m;
42
        for (int i = 1; i <= m; ++i){</pre>
43
            int l, r;
44
45
            cin >> l >> r;
            l += 2, r += 2;
46
            q.push_back({l - 1, 1, 1, i});
47
48
            q.push_back({l - 1, l - 1, -1, i});
            q.push_back({r, 1, -1, i});
49
            q.push_back({r, l - 1, 1, i});
50
51
        sort(q.begin(), q.end());
52
53
        int cur = 0;
        for (auto [x, y, c, id] : q)
54
55
            while (cur < n && pos[cur].first <= x)</pre>
56
                Tr.add(pos[cur++].second, 1);
57
58
            ans[id] += c * Tr.query(y);
59
60
        for (int i = 1; i <= m; i++) cout << ans[i] << endl;</pre>
   }
61
62
63
    int main(){
64
        ios;
        //freopen("sample.txt", "r", stdin);
65
        //freopen("resout.txt", "w", stdout);
66
        int t = 1;
        //cin >> t;
68
69
        while(t--){
70
            solve();
        }
71
        return 0;
   }
73
        ● 矩阵内权值之和
   #include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
   #define vi vector<int>
   #define vl vector<ll>
   #define rep(i, j, k) for(int i = (j); i <= (k); i++)
    #define per(i, j ,k) for(int i = (j); i >= (k); i--)
    #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
10
   using namespace std;
    typedef long long ll;
11
12
    const ll maxn = 3e5 + 10;
    const ll mod = 998244353;
13
    const ll inf = 0x3f3f3f3f3f;
14
15
```

```
struct BIT{
16
17
        ll tr[maxn];
        int lowbit(int x){return x & -x;}
18
19
        void add(int p, ll x){
            for (; p < maxn; p += lowbit(p)) tr[p] += x;</pre>
21
22
        ll query(int p){
            ll sum = 0;
23
            for (; p > 0; p -= lowbit(p))
24
25
                 sum += tr[p];
            return sum;
26
27
   }Tr;
28
29
    void solve(){
30
        int n, m;
31
32
        cin >> n >> m;
        vector<tuple<int, int, int>> pos;
33
34
        vector<tuple<int, int, int, int>> q;
        vector<ll> ans(m + 1);
35
        vector<int> yy;
36
        rep(i, 1, n){}
37
            int x, y, p;
38
             cin >> x >> y >> p;
            yy.push_back(y);
40
41
            pos.push_back({x, y, p});
42
        sort(pos.begin(), pos.end());
43
44
        rep(i, 1, m){
            int x1, y1, x2, y2;
45
            cin >> x1 >> y1 >> x2 >> y2;
46
            yy.push_back(y1 - 1), yy.push_back(y2);
47
            q.push_back({x1 - 1, y1 - 1, i});
48
49
            q.push_back({x2, y1 - 1, -1, i});
            q.push_back({x1 - 1, y2, -1, i});
50
51
            q.push_back({x2, y2, 1, i});
52
53
        sort(q.begin(), q.end());
54
        sort(yy.begin(), yy.end());
        yy.erase(unique(yy.begin(), yy.end()), yy.end());
55
56
        int cur = 0;
        for (auto [x, y, c, id] : q){
57
            y = lower_bound(yy.begin(), yy.end(), y) - yy.begin() + 1;
58
59
            while (cur < n){</pre>
                 auto [_x, _y, p] = pos[cur];
60
61
                 if (x > x) break;
                 _y = lower_bound(yy.begin(), yy.end(), _y) - yy.begin() + 1;
62
63
                 Tr.add(_y, p), ++cur;
64
65
            ans[id] += c * Tr.query(y);
66
        for (int i = 1; i <= m; ++i) cout << ans[i] << endl;</pre>
67
   }
69
70
    int main(){
71
        //freopen("sample.txt", "r", stdin);
72
        //freopen("resout.txt", "w", stdout);
73
        int t = 1;
74
        //cin >> t;
75
        while(t--){
76
77
            solve();
78
        }
        return 0;
79
   }
```

区间问题

莫队

● 区间取两个数相同概率

```
#include <algorithm>
    #include <cmath>
   #include <cstdio>
   using namespace std;
   const int N = 50005;
   int n, m, maxn;
    int c[N];
    long long sum;
    int cnt[N];
    long long ans1[N], ans2[N];
11
12
    struct query {
      int l, r, id;
13
14
      bool operator<(const query &x) const { // 重载 < 运算符
15
        if (l / maxn != x.l / maxn) return l < x.l;</pre>
16
17
        return (l / maxn) & 1 ? r < x.r : r > x.r;
18
      }
    } a[N];
19
20
21
    void add(int i) {
22
      sum += cnt[i];
      cnt[i]++;
23
24
25
    void del(int i) {
26
27
     cnt[i]--;
      sum -= cnt[i];
28
29
30
    long long gcd(long long a, long long b) { return b ? gcd(b, a % b) : a; }
31
32
    int main() {
33
      scanf("%d%d", &n, &m);
      maxn = sqrt(n);
35
      for (int i = 1; i <= n; i++) scanf("%d", &c[i]);</pre>
36
      for (int i = 0; i < m; i++) scanf("%d%d", &a[i].l, &a[i].r), a[i].id = i;</pre>
37
      sort(a, a + m);
38
      for (int i = 0, l = 1, r = 0; i < m; i++) { // 具体实现
        if (a[i].l == a[i].r) {
40
41
          ans1[a[i].id] = 0, ans2[a[i].id] = 1;
          continue;
42
43
        while (l > a[i].l) add(c[--l]);
44
45
        while (r < a[i].r) add(c[++r]);
46
        while (l < a[i].l) del(c[l++]);</pre>
        while (r > a[i].r) del(c[r--]);
47
        ans1[a[i].id] = sum;
48
        ans2[a[i].id] = (long long)(r - l + 1) \star (r - l) / 2;
49
50
      for (int i = 0; i < m; i++) {</pre>
51
        if (ans1[i] != 0) {
52
          long long g = gcd(ans1[i], ans2[i]);
54
          ans1[i] /= g, ans2[i] /= g;
55
        } else
          ans2[i] = 1;
56
        printf("%lld/%lld\n", ans1[i], ans2[i]);
57
58
      return 0;
59
```

CDQ

● 逆序对

```
#include <bits/stdc++.h>
1
    #define endl '\n'
2
   #define pll pair<ll, ll>
   #define tll tuple<ll, ll, ll>
   #define vi vector<int>
   #define vl vector<ll>
   #define x first
   #define y second
   #define rep(i, j, k) for(int i = (j); i <= (k); i++)
   #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
   #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
11
12
   using namespace std;
   typedef long long ll;
13
   const ll maxn = 2e5 + 10;
14
   const ll mod = 998244353;
15
    const ll inf = 0x3f3f3f3f;
16
    void solve(){
18
19
        int n;
        cin >> n;
20
        vi a(n + 1), temp(n + 1);
21
22
        ll ans = 0;
        rep(i, 1, n) cin >> a[i];
23
        function<void(int, int)> cdq = [&](int l, int r){
            if (l == r) return;
25
            int mid = l + r >> 1;
26
27
            cdq(l, mid);
            cdq(mid + 1, r);
28
            int p1 = l, p2 = mid + 1, idx = l;
            while (p1 <= mid && p2 <= r){</pre>
30
                if (a[p1] > a[p2]) temp[idx++] = a[p1++];
31
                else temp[idx++] = a[p2++], ans += p1 - l;
32
            }
33
34
            while (p1 <= mid) temp[idx++] = a[p1++];</pre>
            while (p2 \le r) temp[idx++] = a[p2++], ans += p1 - l;
35
            for (int i = l; i <= r; ++i) a[i] = temp[i];</pre>
36
        }:
37
38
        cdq(1, n);
39
        cout << ans << endl;</pre>
   }
40
41
    int main(){
42
43
        //freopen("sample.txt", "r", stdin);
44
        //freopen("resout.txt", "w", stdout);
45
46
        int t = 1;
        //cin >> t:
47
        while(t--){
49
            solve();
50
51
        return 0;
   }
52
       • 求最长不上升子序列和最长上升子序列
    #include<bits/stdc++.h>
   using namespace std;
    const int MAXN = 100005;
    int n, x, dp[MAXN], a[MAXN], ans;
    pair<int, int> temp[MAXN][20]; //val, pos
5
    bool cmp(const pair<int, int> &A, const pair<int, int> &B, const int &type) {
        return type ? A.first != B.first ? A.first > B.first : A.second < B.second : A.first != B.first ? A.first <
       B.first: A.second > B.second;
    }
9
10
11
    void mergeSort(int l, int r, int deep, const int &cmptype) {
        if (l == r) {
12
13
            temp[l][deep].first = a[l];
            temp[l][deep].second = l;
14
15
            return;
        }
```

```
int mid = (l + r) >> 1;
17
18
        mergeSort(l, mid, deep + 1, cmptype);
        mergeSort(mid + 1, r, deep + 1, cmptype);
19
        int p1 = l, p2 = mid + 1;
20
        while (p1 <= mid && p2 <= r) {
            if (cmp(temp[p1][deep + 1], temp[p2][deep + 1], cmptype)) {
22
                 temp[l++][deep] = temp[p1++][deep + 1];
23
            } else {
24
                temp[l++][deep] = temp[p2++][deep + 1];
25
27
28
        while (p1 <= mid) {</pre>
            temp[l++][deep] = temp[p1++][deep + 1];
29
30
        while (p2 <= r) {
31
            temp[l++][deep] = temp[p2++][deep + 1];
32
33
   }
34
35
    void cdqDivAlgorithm(int l, int r, int deep, const int &cmptype) {
36
37
        if (l == r) {
38
            dp[l] = max(dp[l], 1);
            ans = max(ans, dp[l]);
39
            return;
41
        int mid = (l + r) >> 1;
42
        cdqDivAlgorithm(l, mid, deep + 1, cmptype);
43
        int p1 = l, p2 = mid + 1, premax = 0;
44
45
        while (p1 <= mid && p2 <= r) {</pre>
            if (cmp(temp[p1][deep + 1], temp[p2][deep + 1], cmptype)) {
46
                premax = max(premax, dp[temp[p1++][deep + 1].second]);
47
            } else {
48
                dp[temp[p2][deep + 1].second] = max(premax + 1, dp[temp[p2][deep + 1].second]);
49
                p2++;
50
            }
51
52
        while (p2 <= r) {
53
54
            dp[temp[p2][deep + 1].second] = max(premax + 1, dp[temp[p2][deep + 1].second]);
55
            p2++;
56
57
        cdqDivAlgorithm(mid + 1, r, deep + 1, cmptype);
   }
58
59
60
    int main()
61
    {
62
        while (scanf("%d", &x) != EOF)a[++n] = x;
        mergeSort(1, n, \theta, 1);
63
64
        cdqDivAlgorithm(1, n, 0, 1);
        printf("%d\n", ans);
65
        memset(dp, 0, sizeof(dp));
66
67
        ans = 0;
        mergeSort(1, n, 0, 0);
68
        cdqDivAlgorithm(1, n, \Theta, \Theta);
        printf("%d\n", ans);
70
71
        return 0;
   }
72
       ● 求地毯覆盖(最多取多少个不相互覆盖)
   #include<bits/stdc++.h>
    using namespace std;
    const int MAXN = 1000005;
    int n, L[MAXN], R[MAXN], id[MAXN], dp[MAXN], ans;
    int temp[MAXN];
    void cdqDivAlgorithm(int l, int r) {
        if (l == r) {
            dp[id[l]] = max(1, dp[id[l]]);
            ans = max(ans, dp[id[l]]);
10
            return;
11
12
        int mid = (l + r) >> 1;
        cdqDivAlgorithm(l, mid);
13
```

```
int p1 = l, pl, p2 = mid + 1, premax = 0;
14
15
         while (p1 <= mid && p2 <= r) {
             if (R[id[p1]] <= L[id[p2]]) {</pre>
16
17
                 premax = max(premax, dp[id[p1++]]);
             } else {
                 dp[id[p2]] = max(premax + 1, dp[id[p2]]);
19
20
                  ++p2;
             }
21
22
         while (p2 <= r) {
23
             dp[id[p2]] = max(premax + 1, dp[id[p2]]);
24
25
             ++p2;
26
        cdqDivAlgorithm(mid + 1, r);
27
28
         p1 = l, pl = l, p2 = mid + 1;
         while (p1 <= mid && p2 <= r) {
29
             if (R[id[p1]] < R[id[p2]]) {</pre>
                 temp[pl++] = id[p1++];
31
32
             } else {
                 temp[pl++] = id[p2++];
33
34
35
        while (p1 <= mid) {</pre>
36
             temp[pl++] = id[p1++];
38
39
        while (p2 <= r) {
40
             temp[pl++] = id[p2++];
41
42
         for (int i = l; i <= r; ++i) {</pre>
             id[i] = temp[i];
43
44
45
    int main()
46
47
         scanf("%d", &n);
48
         for (int i = 1; i <= n; ++i) {
49
             scanf("%d %d", &L[i], &R[i]);
50
             id[i] = i;
51
52
         sort(id + 1, id + 1 + n, [](const int &A, const int &B) {
53
54
             return L[A] < L[B];</pre>
55
        cdqDivAlgorithm(1, n);
56
57
         printf("%d\n", ans);
        return 0;
58
59
    }
```

• 动态凸包

第一行: 一个整数 N ,表示方案和询问的总数。接下来 N 行,每行开头一个单词 "Query" 或 "Project"。若单词为 Query,则后接一个整数 T,表示 Blue Mary 询问第 T 天的最大收益。若单词为 Project,则后接两个实数 S,P,表示该种设计方案第一天的收益 S,以及以后每天比上一天多出的收益 P。对于每一个 Query,输出一个整数,表示询问的答案,并精确到整百元 $1 <= N <= 100000 \ 1 <= T <= 50000 \ 0 < P < 100, | S | <= 10^6$

```
#include<bits/stdc++.h>
    using namespace std;
    const int MAXN = 100005;
    const double eps = 1e-6;
    int m, n, id[MAXN], qid[MAXN], type[MAXN], x[MAXN], temp[MAXN], top;
    double k[MAXN], b[MAXN], ans[MAXN];
    char op[55];
    inline bool cmp(const int &A, const int &B) {
          \textbf{return type[A] } != \textbf{type[B] } ? \textbf{type[A] } < \textbf{type[B] } : \textbf{type[A] } ? \textbf{x[A] } < \textbf{x[B] } : \textbf{k[A] } < \textbf{k[B] }; 
10
    inline int dcmp(double x) {
11
         return x > eps ? 1 : x < -eps ? -1 : 0;
12
13
    inline double getCross(const double &k1, const double &b1, const double &k2, const double &b2) {
14
15
         return (b2 - b1) / (k1 - k2);
    inline double getVal(const double &k, const double &b, const int &x)
17
```

```
18
    {
19
        return k * x + b;
    }
20
    pair<double, double>stk[MAXN];
21
    void stkClear() {
        top = 0;
23
        stk[++top] = make_pair(0, 0);
24
25
    void stkInsert(double k, double b) {
26
        if (dcmp(stk[top].first - k) == 0 && dcmp(stk[top].second - b) < 0)top--;</pre>
27
        if (dcmp(stk[top].first - k) == 0 && dcmp(stk[top].second - b) >= 0)return;
28
29
        while (top >= 2 && dcmp(getCross(stk[top].first, stk[top].second, stk[top - 1].first, stk[top - 1].second) -
        {\tt getCross(stk[top].first,\ stk[top].second,\ k,\ b))} \ > \ 0) {\tt top--};
        stk[++top] = make_pair(k, b);
30
31
    }
    double stkQuery(int x) {
32
33
        while (top >= 2 && dcmp(getVal(stk[top].first, stk[top].second, x) - getVal(stk[top - 1].first, stk[top -
        1].second, x)) < 0)--top;
34
        return getVal(stk[top].first, stk[top].second, x);
    }
35
    void cdqDivAlgorithm(int l, int r) {
36
37
        if (l == r)return;
        int mid = (l + r) >> 1;
38
        cdqDivAlgorithm(l, mid);
39
        cdqDivAlgorithm(mid + 1, r);
40
        stkClear();
41
        for (int i = l; i <= mid && !type[id[i]]; ++i) {</pre>
42
             stkInsert(k[id[i]], b[id[i]]);
43
44
        for (int i = r; i > mid && type[id[i]]; --i) {
45
             ans[qid[id[i]]] = max(ans[qid[id[i]]], stkQuery(x[id[i]]));
46
47
        int p1 = l, pl = l, p2 = mid + 1;
48
49
        while (p1 <= mid && p2 <= r) {
             if (cmp(id[p1], id[p2])) {
50
                 temp[pl++] = id[p1++];
51
             } else {
52
                 temp[pl++] = id[p2++];
53
54
             }
55
        while (p1 <= mid) {</pre>
56
             temp[pl++] = id[p1++];
57
58
        while (p2 <= r) {
59
             temp[pl++] = id[p2++];
60
61
        for (int i = l; i <= r; ++i) {</pre>
62
63
             id[i] = temp[i];
64
    }
65
66
    int main() {
        scanf("%d", &n);
67
        for (int i = 1; i <= n; ++i) {
             id[i] = i;
69
             scanf("%s", op);
if (*op == 'P') {
70
71
                 type[i] = 0;
72
                 scanf("%lf %lf", &b[i], &k[i]);
74
                 b[i] -= k[i];
75
76
             else {
77
                 type[i] = 1;
78
                 qid[i] = ++m;
                 scanf("%d", &x[i]);
79
80
81
82
        cdqDivAlgorithm(1, n);
        for (int i = 1; i <= m; ++i) {</pre>
83
             printf("%d\n", (int)ans[i] / 100);
84
85
        return 0:
86
```

87 }

树上问题

树剖

● 2018ICPC 青岛网络赛 (多测时候用来剖的)

```
#include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define vi vector<int>
    #define vl vector<ll>
    #define x first
    #define y second
    #define rep(i, j, k) for(int i = (j); i \le (k); i++)
    #define per(i, j, k) for(int i = (j); i \ge (k); i--)
    \textit{\#define ios ios::sync\_with\_stdio(false), cin.tie(0), cout.tie(0)}
11
    using namespace std;
    typedef long long ll;
13
14
    const ll maxn = 1e5 + 10;
    const ll mod = 998244353;
15
16
    const ll inf = 0x3f3f3f3f3f;
17
    void solve()
18
19
        int n, m, q, k, cnt = 0;
20
        cin >> n >> m >> q;
21
        vi red(n + 1);
22
        vector<vector<pll>>> G(n + 1);
23
24
        vl dis(n + 1), dep(n + 1), v(n + 1);
        vi dfn(n + 1), idx(n + 1);
25
        vi son(n + 1, -1), sz(n + 1), fa(n + 1), top(n + 1);
26
        function<void(int, int)> dfs1 = [&](int u, int f) {
27
            son[u] = -1;
28
29
            sz[u] = 1;
            if(!red[u])
30
31
                 red[u] = red[f];
            for(auto [v, w] : G[u]) {
32
                 if(v == f)
33
                     continue;
                 dep[v] = dep[u] + 1;
35
                 dis[v] = dis[u] + w;
                 fa[v] = u;
37
                 dfs1(v, u);
38
39
                 sz[u] += sz[v];
                 if(son[u] == -1 \mid \mid sz[v] > sz[son[u]])
40
41
                     son[u] = v;
            }
42
43
        function<void(int, int)> dfs2 = [&](int u, int t) {
44
45
            top[u] = t;
            dfn[u] = ++cnt;
46
            idx[cnt] = u;
47
            if(son[u] == -1)
                 return;
49
             dfs2(son[u], t);
50
51
             for(auto [v, w] : G[u])
                 if(v != son[u] && v != fa[u])
52
53
                     dfs2(v, v);
        };
54
        auto lca = [&](int u, int v) {
55
56
            while(top[u] != top[v]) {
                 if(dep[top[u]] > dep[top[v]])
57
58
                     u = fa[top[u]];
59
                 else
                     v = fa[top[v]];
            }
61
```

```
return dep[u] > dep[v] ? v : u;
62
63
         };
         for(int i = 1, x; i <= m; ++i)</pre>
64
             cin >> x, red[x] = x;
65
         for(int i = 1; i < n; ++i) {</pre>
              int u, v, w;
67
68
              cin >> u >> v >> w;
              G[u].push_back({v, w});
69
              G[v].push_back({u, w});
70
71
         dfs1(1, 0);
72
73
         dfs2(1, 1);
         for(int i = 1; i <= n; ++i)</pre>
74
             v[i] = dis[i] - dis[red[i]];
75
         while(q--) {
76
              cin >> k;
77
78
              vector<int> p(k + 1);
              auto check = [&](ll st) {
79
                  vector<int> q;
                  for(int i = 1; i <= k; ++i)</pre>
81
                       if(v[p[i]] > st)
82
83
                           q.push_back(p[i]);
                  if(q.size() == 0)
84
                       return true;
                  int mnd = n + 1, mxd = 0;
86
                  for(int i = 0; i < q.size(); ++i) {</pre>
87
                       mnd = min(mnd, dfn[q[i]]);
88
                       mxd = max(mxd, dfn[q[i]]);
89
                  int ca = lca(idx[mnd], idx[mxd]);
91
                  for(int i = 0; i < q.size(); ++i)</pre>
92
                       if(dis[q[i]] - dis[ca] > st)
93
94
                           return false;
95
                  return true;
              };
96
97
              ll mx = 0;
              for(int i = 1; i <= k; ++i) {</pre>
98
                  cin >> p[i];
99
100
                  mx = max(mx, v[p[i]]);
101
              11 1 = 0, r = mx;
102
              while(l < r) {</pre>
103
                  ll mid = (l + r) >> 1;
104
105
                  if(check(mid))
                       r = mid;
106
107
                  else
                       l = mid + 1;
108
109
              cout << l << endl;</pre>
110
111
112
    }
113
114
     int main()
115
     {
116
         ios;
         // freopen("sample.txt", "r", stdin);
117
         // freopen("resout.txt", "w", stdout);
118
119
         int t = 1;
         cin >> t;
120
         while(t--) {
121
122
              solve();
         }
123
124
         return 0;
    }
125
126
```

- 树上操作
- 1. 节点 x 加上 a
- 2. 节点 x 的子树中所有点的点权加 a
- 3. 询问某个点 x 到根节点

```
#include <bits/stdc++.h>
1
    #define endl '\n'
2
   #define pll pair<ll, ll>
   #define tll tuple<ll, ll, ll>
   #define vi vector<int>
   #define vl vector<ll>
   #define x first
   #define y second
   #define rep(i, j, k) for(int i = (j); i <= (k); i++)
   #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
   #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
11
12
   using namespace std;
   typedef long long ll;
13
    const ll maxn = 2e5 + 10;
14
   const ll mod = 998244353;
15
    const ll inf = 0x3f3f3f3f3f;
16
17
    const int N = 1e5 + 10, M = N * 2;
18
19
   int n, m;
   // w 为节点权值
20
   int h[N], w[N], e[M], ne[M], idx;
21
    // id[x] 为节点 x 的新编号, nw[x] 是新编号为 x 的节点的权值
   int id[N], nw[N], cnt;
23
   // dep 为深度, sz 为子树大小, top[x] 是 x 所在重链的头结点,
   // fa[x] 为 x 父亲, son[x] 为 x 的重儿子
25
    int dep[N], sz[N], top[N], fa[N], son[N];
26
27
    struct Tree {
        int l, r;
28
        ll sum, add;
   } tr[N << 2];
30
31
    void add(int a, int b) {
32
        e[idx] = b, ne[idx] = h[a], h[a] = idx++;
33
34
35
    // 第一次 dfs, 求节点深度、父亲、子树大小和重儿子
36
    void dfs1(int u, int from, int depth) {
37
        dep[u] = depth, fa[u] = from, sz[u] = 1;
38
39
        for (int i = h[u]; ~i; i = ne[i]) {
            int v = e[i];
40
41
            if (v == from) continue;
            dfs1(v, u, depth + 1);
42
            sz[u] += sz[v];
43
44
            if (sz[son[u]] < sz[v]) son[u] = v;</pre>
45
        }
46
   }
47
   // 第二次 dfs, t 为 u 重链头结点
    void dfs2(int u, int t) {
49
50
        id[u] = ++cnt, nw[cnt] = w[u], top[u] = t;
51
        // 到叶子了,直接返回
        if (!son[u]) return;
52
        // 先遍历重儿子
        dfs2(son[u], t);
54
55
        // 遍历轻儿子
        for (int i = h[u]; ~i; i = ne[i]) {
56
            int v = e[i];
57
            if (v == fa[u] || v == son[u]) continue;
59
            dfs2(v, v);
60
   }
61
62
    void pushup(int u) {
        tr[u].sum = tr[u << 1].sum + tr[u << 1 | 1].sum;
64
65
66
67
    void pushdown(int u) {
        auto &root = tr[u], &left = tr[u << 1], &right = tr[u << 1 | 1];</pre>
68
        if (root.add) {
69
            left.sum += root.add * (left.r - left.l + 1);
70
            left.add += root.add;
71
```

```
right.sum += root.add * (right.r - right.l + 1);
72
73
             right.add += root.add;
             root.add = 0;
74
75
         }
    }
77
     void build(int u, int l, int r) {
78
         tr[u] = \{l, r, nw[l], 0\};
79
         if (l == r) return;
80
81
         int mid = l + r >> 1;
         build(u << 1, l, mid), build(u << 1 \mid 1, mid + 1, r);
82
83
         pushup(u);
    }
84
85
     void update(int u, int l, int r, ll k) {
86
         if (l <= tr[u].l && tr[u].r <= r) {</pre>
87
             tr[u].add += k;
88
             tr[u].sum += k * (tr[u].r - tr[u].l + 1);
89
             return;
         }
91
92
         pushdown(u);
93
         int mid = tr[u].l + tr[u].r >> 1;
         if (l <= mid) update(u << 1, l, r, k);</pre>
94
         if (r > mid) update(u << 1 | 1, l, r, k);</pre>
         pushup(u);
96
97
    }
98
     ll query(int u, int l, int r) {
99
100
         if (l <= tr[u].l && tr[u].r <= r) return tr[u].sum;</pre>
         pushdown(u);
101
         int mid = tr[u].l + tr[u].r >> 1;
102
         ll res = 0;
103
         if (l <= mid) res += query(u << 1, l, r);
104
105
         if (r > mid) res += query(u << 1 | 1, l, r);</pre>
         return res;
106
107
108
     void update_path(int u, int v, ll k) {
109
110
         while (top[u] != top[v]) {
             if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
111
             // u 的重链头更深, 并且 u 重链头在 dfs 序里下标更小, 直接更新 u 重链头到 u 这段区间
112
             update(1, id[top[u]], id[u], k);
113
             // u 跳到重链头上面
114
115
             u = fa[top[u]];
116
117
         if (dep[u] < dep[v]) swap(u, v);</pre>
         update(1, id[v], id[u], k);
118
119
    }
120
     ll query_path(int u, int v) {
121
122
         ll res = 0;
         while (top[u] != top[v]) {
123
             if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
124
             res += query(1, id[top[u]], id[u]);
125
             u = fa[top[u]];
126
127
         if (dep[u] < dep[v]) swap(u, v);</pre>
128
129
         res += query(1, id[v], id[u]);
         return res;
130
131
    }
132
     void update_tree(int u, ll k) {
133
134
         update(1, id[u], id[u] + sz[u] - 1, k);
    }
135
136
    ll query_tree(int u) {
137
         return query(1, id[u], id[u] + sz[u] - 1);
138
139
    }
140
     void solve() {
141
         int n, q;
142
```

```
memset(h, -1, sizeof h);
143
144
         cin >> n >> q;
         int cnt = 0;
145
         for (int i = 1; i <= n; ++i) cin >> w[i];
146
147
         for (int i = 1; i <= n - 1; ++i) {
             int u, v;
148
             cin >> u >> v;
149
             add(u, v);
150
             add(v, u);
151
152
        dfs1(1, 1, 0);
153
154
         dfs2(1, 1);
155
        build(1, 1, n);
         while (q--) {
156
157
             int t, u;
             ll k;
158
159
             cin >> t >> u;
             if (t == 1) {
160
161
                 cin >> k;
                 update_path(u, u, k);
162
             } else if (t == 2) {
163
164
                 cin >> k;
                 update_tree(u, k);
165
             } else cout << query_path(1, u) << endl;</pre>
        }
167
    }
168
169
    int main() {
170
171
        ios;
         //freopen("sample.txt", "r", stdin);
172
         //freopen("resout.txt", "w", stdout);
173
         int t = 1;
174
         //cin >> t;
175
176
         while (t--) {
            solve();
177
178
        return 0:
179
    }
180
        • 树上路径
       1. 将以 u 为根的子树内节点 (包括 u) 的权值加 val
       2. 将 (u, v) 路径上的节点权值加 val
       3. 询问 (u, v) 路径上节点的权值两两相乘的和
#include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define vi vector<int>
    #define vl vector<ll>
    #define int ll
    #define x first
    #define y second
    #define rep(i, j, k) for(int i = (j); i \le (k); i++)
    #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
11
    #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
12
13
    using namespace std;
    typedef long long ll;
14
    const ll mod = 1e9 + 7;
    const ll inf = 0x3f3f3f3f3f;
16
    const int N = 1e5 + 10, M = N * 2;
18
    int n, m;
19
    int h[N], a[N], e[M], ne[M], idx;
    int id[N], cnt, rnk[N];
21
    int dep[N], sz[N], top[N], fa[N], son[N];
    ll inv2;
23
24
    void add(int u, int v) {
25
        e[idx] = v, ne[idx] = h[u], h[u] = idx++;
26
```

```
27
28
    ll qmi(ll x, ll k) {
        ll res = 1;
29
        while (k) {
30
31
            if (k & 1) res = res * x % mod;
            x = x * x % mod;
32
            k >>= 1;
33
        }
34
        return res;
35
36
    struct Segment {
37
38
        struct Node {
39
            int l, r;
            ll sum, psum, add;
40
41
        } tr[N * 4];
        void pushup(int u) {
42
43
             tr[u].sum = (tr[u << 1].sum + tr[u << 1 | 1].sum) % mod;
             tr[u].psum = (tr[u << 1].psum + tr[u << 1 | 1].psum) % mod;</pre>
44
45
46
47
        void pushdown(Node& u, Node& l, Node& r) {
48
            if (u.add) {
                 ll x = u.add;
49
                 l.psum = (l.psum + 2 * l.sum * x % mod + (ll)x * x % mod * (l.r - l.l + 1) % mod) % mod;
                 r.psum = (r.psum + 2 * r.sum * x % mod + (ll)x * x % mod * (r.r - r.l + 1) % mod) % mod;
51
52
                 l.sum = (l.sum + (ll)x * (l.r - l.l + 1) % mod) % mod;
                 r.sum = (r.sum + (ll)x * (r.r - r.l + 1) % mod) % mod;
53
                 l.add = (l.add + x) \% mod;
54
                 r.add = (r.add + x) \% mod;
                 u.add = 0;
56
            }
57
58
            return;
59
        }
60
        void pushdown(int u) {
            pushdown(tr[u], tr[u << 1], tr[u << 1 \mid 1]);
61
62
        void build(int u, int l, int r) {
63
            tr[u] = {l, r};
64
65
            if (l == r) {
                 tr[u].sum = a[rnk[l]];
66
67
                 tr[u].psum = (ll)a[rnk[l]] * a[rnk[l]] % mod;
68
                 return;
69
70
            int mid = (l + r) >> 1;
            build(u << 1, l, mid);</pre>
71
72
            build(u << 1 | 1, mid + 1, r);
            pushup(u);
73
            return;
75
        void update(int u, int l, int r, ll x) {
76
77
            if (l <= tr[u].l && tr[u].r <= r) {</pre>
               tr[u].psum = (tr[u].psum + 2 * tr[u].sum * x % mod + (ll)x * x % mod * (tr[u].r - tr[u].l + 1) % mod) % mod;
78
                 tr[u].sum = (tr[u].sum + (ll)(tr[u].r - tr[u].l + 1) * x % mod) % mod;
                 tr[u].add = (tr[u].add + x) \% mod;
80
81
                 return;
82
            pushdown(u);
83
            int mid = (tr[u].l + tr[u].r) >> 1;
            if (l <= mid) update(u << 1, l, r, x);
85
            if (mid < r) update(u << 1 | 1, l, r, x);</pre>
86
87
            pushup(u);
            return;
88
89
        ll query_sum(int u, int l, int r) {
90
91
             if (l <= tr[u].l && tr[u].r <= r) return tr[u].sum;</pre>
            pushdown(u);
92
93
             int mid = (tr[u].l + tr[u].r) >> 1;
            ll res = 0;
            if (l <= mid) res = (res + query_sum(u << 1, l, r)) % mod;
95
            if (mid < r) res = (res + query_sum(u << 1 | 1, 1, r)) % mod;</pre>
            return res:
97
```

```
98
99
         ll query_psum(int u, int l, int r) {
              \textbf{if} \ (\texttt{l} \ \Leftarrow \ \texttt{tr[u].l} \ \&\& \ \texttt{tr[u].r} \ \Leftarrow \ \texttt{r)} \ \textbf{return} \ \texttt{tr[u].psum;}
100
              pushdown(u);
101
              int mid = (tr[u].l + tr[u].r) >> 1;
              ll res = 0:
103
              if (l <= mid) res = (res + query_psum(u << 1, l, r)) % mod;</pre>
104
              if (mid < r) res = (res + query_psum(u << 1 \mid 1, 1, r)) % mod;
105
              return res;
106
107
    } Tr;
108
109
110
     //Tree
     void dfs1(int u, int from, int depth) {
111
         dep[u] = depth, fa[u] = from, sz[u] = 1;
112
         for (int i = h[u]; ~i; i = ne[i]) {
113
114
              int v = e[i];
              if (v == from) continue;
115
116
              dfs1(v, u, depth + 1);
117
              sz[u] += sz[v];
              if (sz[son[u]] < sz[v]) son[u] = v;</pre>
118
119
    }
120
     void dfs2(int u, int t) {
121
         id[u] = ++cnt, top[u] = t;
122
         rnk[cnt] = u;
123
124
         if (!son[u]) return;
         dfs2(son[u], t);
125
         for (int i = h[u]; ~i; i = ne[i]) {
126
              int v = e[i];
127
              if (v == fa[u] || v == son[u]) continue;
128
129
              dfs2(v, v);
         }
130
131
     void update_path(int u, int v, ll k) {//更新路径
132
         while (top[u] != top[v]) {
133
              if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
134
              Tr.update(1, id[top[u]], id[u], k);
135
136
              u = fa[top[u]];
137
138
         if (dep[u] < dep[v]) swap(u, v);</pre>
         Tr.update(1, id[v], id[u], k);
139
140
141
     ll query_path(int u, int v) {
         ll res_sum = 0, res_psum = 0;
142
143
         while (top[u] != top[v]) {
              if (dep[top[u]] < dep[top[v]]) swap(u, v);</pre>
144
145
              res_sum = (res_sum + Tr.query_sum(1, id[top[u]], id[u])) % mod;
              res_psum = (res_psum + Tr.query_psum(1, id[top[u]], id[u])) % mod;
146
              u = fa[top[u]];
147
148
         if (dep[u] < dep[v]) swap(u, v);</pre>
149
         res_sum = (res_sum + Tr.query_sum(1, id[v], id[u])) % mod;
         res\_psum = (res\_psum + Tr.query\_psum(1, id[v], id[u])) \% mod;
151
         return (res_sum * res_sum % mod - res_psum + mod) % mod * inv2 % mod;
152
153
    }
     //Tree
154
155
     void solve() {
156
         inv2 = qmi(2, mod - 2);
157
158
         cin >> n >> m;
         for (int i = 1; i <= n; ++i) cin >> a[i];
159
         memset(h, -1, sizeof h);
160
         for (int i = 1; i <= n - 1; ++i) {
161
              int u, v;
162
              cin >> u >> v:
163
              add(u, v);
164
165
              add(v, u);
166
167
         dfs1(1, 0, 1);
         dfs2(1, 1);
168
```

```
170
        while (m--) {
171
             int op;
172
173
             cin >> op;
             ll u, v, k;
174
             if (op == 1) {
175
                 cin >> u >> k;
176
                 Tr.update(1, id[u], id[u] + sz[u] - 1, k);
177
178
             } else if (op == 2) {
                 cin >> u >> v >> k;
179
180
                 update_path(u, v, k);
181
             } else {
                 cin >> u >> v;
182
                 cout << query_path(u, v) << endl;</pre>
183
             }
184
185
    }
186
187
    signed main() {
188
        ios;
189
         //freopen("sample.txt", "r", stdin);
190
         //freopen("resout.txt", "w", stdout);
191
        int t = 1;
192
        //cin >> t;
193
        while (t--) {
194
195
             solve();
196
197
        return 0;
    }
198
    dsu
        • 树上数颜色
    #include <bits/stdc++.h>
    using namespace std;
    const int N = 2e5 + 5;
    int n;
    // g[u]: 存储与 u 相邻的结点
    vector<int> g[N];
10
    // sz: 子树大小
11
    // big: 重儿子
12
    // col: 结点颜色
    // L[u]: 结点 u 的 DFS 序
14
    // R[u]: 结点 u 子树中结点的 DFS 序的最大值
    // Node[i]: DFS 序为 i 的结点
    // ans: 存答案
17
    // cnt[i]: 颜色为 i 的结点个数
    // totColor: 目前出现过的颜色个数
19
    int sz[N], big[N], col[N], L[N], R[N], Node[N], totdfn;
    int ans[N], cnt[N], totColor;
21
22
23
    void add(int u) {
      if (cnt[col[u]] == 0) ++totColor;
24
25
      cnt[col[u]]++;
    }
26
27
    void del(int u) {
      cnt[col[u]]--;
29
      if (cnt[col[u]] == 0) --totColor;
30
31
32
    int getAns() { return totColor; }
33
34
35
    void dfs0(int u, int p) {
      L[u] = ++totdfn;
```

Tr.build(1, 1, n);

169

```
Node[totdfn] = u;
37
38
      sz[u] = 1;
      for (int v : g[u])
39
        if (v != p) {
40
41
          dfs0(v, u);
          sz[u] += sz[v];
42
          if (!big[u] || sz[big[u]] < sz[v]) big[u] = v;</pre>
43
44
      R[u] = totdfn;
45
46
    }
47
48
    void dfs1(int u, int p, bool keep) {
      // 计算轻儿子的答案
49
      for (int v : g[u])
50
        if (v != p && v != big[u]) {
51
          dfs1(v, u, false);
52
53
      // 计算重儿子答案并保留计算过程中的数据(用于继承)
54
      if (big[u]) {
       dfs1(big[u], u, true);
56
57
58
      for (int v : g[u])
        if (v != p && v != big[u]) {
59
          // 子树结点的 DFS 序构成一段连续区间, 可以直接遍历
          for (int i = L[v]; i <= R[v]; i++) {
61
62
            add(Node[i]);
63
        }
64
65
      add(u);
      ans[u] = getAns();
66
      if (keep == false) {
67
        for (int i = L[u]; i <= R[u]; i++) {</pre>
68
          del(Node[i]);
69
70
        }
      }
71
72
73
74
    int main() {
75
      scanf("%d", &n);
      for (int i = 1; i <= n; i++) scanf("%d", &col[i]);</pre>
76
77
      for (int i = 1; i < n; i++) {
        int u, v;
78
        scanf("%d%d", &u, &v);
79
80
        g[u].push_back(v);
        g[v].push_back(u);
81
82
      dfs0(1, 0);
83
      dfs1(1, 0, false);
      for (int i = 1; i <= n; i++) printf("%d%c", ans[i], " \n"[i == n]);</pre>
85
86
87
   }
       • 子树权值不大于 k 的数量
    #include <bits/stdc++.h>
1
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define vi vector<int>
    #define vl vector<ll>
    #define x first
   #define y second
   #define rep(i, j, k) for(int i = (j); i \le (k); i++)
   #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
   #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
11
    using namespace std;
    typedef long long ll;
13
    const ll N = 1e6 + 10;
15
    const ll mod = 998244353;
    const ll inf = 0x3f3f3f3f;
16
17
    int tr[N];
    int h[N], to[2 * N], ne[2 * N], cnt;
```

```
int sz[N], dep[N], fa[N], son[N];
19
20
    int top[N], dfn, L[N], R[N], idx[N], skp;
    int a[N], sum, ans[N];
21
    int n, m;
22
    vector<pll> q[N];
24
    int lowbit(int x) {return x & -x;}
25
    void add(int p, int k){for (int i = p; i < N; i += lowbit(i)) tr[i] += k;}</pre>
    int query(int p){int res = 0; for (int i = p; i; i -= lowbit(i)) res += tr[i]; return res;}
27
28
    void addedge(int u, int v){
29
30
        to[++cnt] = v;
        ne[cnt] = h[u];
31
        h[u] = cnt;
32
    }
33
34
35
    void dfs1(int u, int f){
        sz[u] = 1;
36
        dep[u] = dep[f] + 1;
37
        fa[u] = f;
38
39
        for (int i = h[u]; i; i = ne[i]){
40
             int v = to[i];
             if (v == f) continue;
41
             dfs1(v, u);
42
             sz[u] += sz[v];
43
             if (!son[u] || sz[son[u]] < sz[v]) son[u] = v;</pre>
44
45
    }
46
47
    void dfs2(int u, int t){
48
        L[u] = ++dfn;
49
        idx[dfn] = u;
50
        top[u] = t;
51
52
        if (son[u]) dfs2(son[u], t);
        for (int i = h[u]; i; i = ne[i]){
53
54
             int v = to[i];
             if (v != fa[u] && v != son[u])
55
56
                 dfs2(v, v);
57
        R[u] = dfn;
58
59
60
    void get(int u, int op){
61
62
        for (int i = L[u]; i <= R[u]; ++i){</pre>
             if (idx[i] == skp){i = R[idx[i]]; continue;}
63
64
             add(a[idx[i]], op);
65
        if (op == -1) return;
        for (auto x : q[u]) ans[x.second] = query(x.first);
67
68
    }
69
    void dsu(int u){
70
        for (int i = h[u]; i; i = ne[i]){
71
             int v = to[i];
72
73
             if (v == fa[u] || v == son[u]) continue;
74
             dsu(v);
75
        if (son[u]) {dsu(son[u]), skp = son[u];}
77
        get(u, 1);
        if (u == top[u]){
78
             skp = 0;
79
80
             get(u, -1);
81
        }
    }
82
83
    void solve() {
84
        cin >> n:
85
        rep(i, 1, n) cin >> a[i];
        int u, v;
        for (int i = 1; i <= n - 1; ++i){
87
88
             cin >> u >> v;
            addedge(u, v);
89
```

```
addedge(v, u);
90
91
         }
         cin >> m;
92
93
         int x, k;
         rep(i, 1, m){
              cin >> x >> k;
95
              q[x].push_back({k, i});
96
97
         dfs1(1, 0);
98
99
         dfs2(1, 1);
         dsu(1);
100
101
         for (int i = 1; i <= m; ++i) cout << ans[i] << endl;</pre>
102
    }
103
     int main() {
104
         ios;
105
         //freopen("sample.txt", "r", stdin);
106
         //freopen("resout.txt", "w", stdout);
107
108
         int t = 1;
         //cin >> t;
109
         while (t--) {
110
111
              solve();
112
         return 0;
    }
114
```

• 子树查询类问题

现在将会问你 m 个问题。对于每个问题,它将会给你三个参数 x,l,r 表示询问以 x 为根的子树中,节点深度在该子树中不小于 l 且不大于 r 的所有节点。你需要告诉智乃酱三个信息,所有符合条件节点的最小值,最大值,以及它们的和。

```
#include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
   #define vi vector<int>
    #define vl vector<ll>
    #define x first
    #define y second
    #define rep(i, j, k) for(int i = (j); i \le (k); i++)
    #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
    \textit{\#define ios ios::sync\_with\_stdio(false), cin.tie(0), cout.tie(0)}
11
    using namespace std;
    typedef long long ll;
13
    const ll maxn = 1e5 + 10;
14
    const ll mod = 998244353;
    const ll inf32 = 1e9;
16
    const ll inf64 = 2e18;
18
    int tot, h[maxn], len[maxn], L[maxn], R[maxn], fa[maxn], son[maxn], dfn, n, m, x, l, r, u, v;
20
    ll val[maxn];
21
22
    struct node {
        ll Sum, Max, Min;
23
24
    } ans[maxn];
25
26
    struct qnode {
        int id;
27
        int l, r;
28
        qnode(int _id = 0, int _l = 0, int _r = 0) {id = _id, l = _l, r = _r;}
    };
30
31
32
    struct edges {
        int to, next;
33
34
    e[2 * maxn];
    vector<qnode> lis[maxn];
35
36
37
    struct tnode
38
    {
        ll Sum, Max, Min;
39
        int l, r;
40
```

```
};
41
42
    tnode operator + (const tnode &a, const tnode &b)
43
    {
44
         tnode c;
45
         c.l = a.l;
         c.r = b.r;
46
47
         c.Sum = a.Sum + b.Sum;
         c.Max = max(a.Max, b.Max);
48
         c.Min = min(a.Min, b.Min);
49
50
         return c;
    }
51
52
53
    struct Segment_Tree
54
         tnode t[4 * maxn];
55
         int mp[maxn];
56
57
         void update (int root)
58
             int ch = root << 1;
             t[root] = t[ch] + t[ch + 1];
60
61
         void buildt(int root, int l, int r)
62
63
             t[root].l = l;
             t[root].r = r;
65
             if (l != r)
66
67
                 int mid = (l + r) >> 1;
68
                 int ch = root << 1;
                 buildt(ch, l, mid);
70
                 buildt(ch + 1, mid + 1, r);
71
                 update(root);
72
             }
73
74
             else
             {
75
                 mp[l] = root;
76
                 t[root].Max = -inf64;
77
                 t[root].Min = inf64;
78
79
                 t[root].Sum = 0;
             }
80
81
         }
         void change(int pos, long long delta, long long nmax, long long nmin)
82
83
             int root = mp[pos];
84
85
             t[root].Sum += delta;
86
             t[root].Max = max(t[root].Max, nmax);
             t[root].Min = min(t[root].Min, nmin);
87
             while (root >>= 1)update(root);
         }
89
90
         tnode getdata(int pos)
91
             return t[mp[pos]];
92
         tnode getseg(int root, int l, int r)
94
95
             if (t[root].l == l && t[root].r == r)
96
97
             {
                 return t[root];
99
             int mid = (t[root].l + t[root].r) >> 1;
100
             int ch = root << 1;</pre>
101
             if (r <= mid)return getseg(ch, l, r);</pre>
102
103
             else if (l > mid)return getseg(ch + 1, l, r);
             else return getseg(ch, l, mid) + getseg(ch + 1, mid + 1, r);
104
105
106
    };
107
    Segment_Tree ST;
108
    void add_edge(int u, int to)
109
110
         e[++tot].to = to;
111
```

```
e[tot].next = h[u];
112
113
         h[u] = tot;
114
         return;
    }
115
116
117
     void dfs1(int x, int father)
118
119
     {
         fa[x] = father;
120
         for (int i = h[x]; i; i = e[i].next)
121
122
123
              if (e[i].to != father)
124
                  dfs1(e[i].to, x);
125
                  if (!son[x] || len[son[x]] < len[e[i].to])son[x] = e[i].to;</pre>
126
127
128
         len[x] = len[son[x]] + 1;
129
130
    }
131
132
     void dfs2(int x)
133
     {
134
         L[x] = ++dfn;
135
         R[x] = L[x] + len[x] - 1;
136
         if (son[x])dfs2(son[x]);
137
         for (int i = h[x]; i; i = e[i].next)
138
139
140
              if (e[i].to != fa[x] && e[i].to != son[x])
141
              {
                  dfs2(e[i].to);
142
143
         }
144
145
         return;
    }
146
147
     void dfs(int x)
148
     {
149
         if (son[x])
150
151
152
              dfs(son[x]);
153
         for (int i = h[x]; i; i = e[i].next)
154
155
              if (e[i].to != fa[x] && e[i].to != son[x])
156
157
              {
                  dfs(e[i].to);
158
159
                  for (int j = L[e[i].to], k = 1; j <= R[e[i].to]; ++j, ++k)</pre>
160
                       tnode temp = ST.getdata(j);
161
162
                       ST.change(L[x] + k, temp.Sum, temp.Max, temp.Min);
                  }
163
              }
165
         ST.change(L[x], val[x], val[x]);
166
         for (auto &i : lis[x])
167
         {
168
              tnode temp = ST.getseg(1, L[x] + i.l, L[x] + i.r);
169
170
              ans[i.id].Sum = temp.Sum;
              ans[i.id].Max = temp.Max;
171
              ans[i.id].Min = temp.Min;
172
         }
173
174
         return;
    }
175
176
     void solve() {
177
178
         cin >> n;
         for (int i = 1; i <= n; ++i) cin >> val[i];
179
         for (int i = 1; i <= n - 1; ++i) {
180
              cin >> u >> v;
181
              add_edge(u, v);
182
```

```
add_edge(v, u);
183
184
         dfs1(1, 0);
185
         dfs2(1);
186
187
         ST.buildt(1, 1, n);
         cin >> m;
188
         for (int i = 1; i <= m; ++i) {</pre>
189
             cin >> x >> l >> r;
190
             lis[x].push_back(qnode(i, l, r));
191
192
         dfs(1);
193
194
         for (int i = 1; i <= m; ++i)</pre>
195
             cout << ans[i].Min << " " << ans[i].Max << " " << ans[i].Sum << endl;</pre>
196
         }
197
    }
198
199
     int main() {
200
201
         //freopen("sample.txt", "r", stdin);
202
         //freopen("resout.txt", "w", stdout);
203
204
         int t = 1;
         //cin >> t:
205
         while (t--) {
             solve();
207
         }
208
209
         return 0;
    }
210
         小Q与树
    u \sum v \sum \min(a[u], a[v]) * dis(u, v)
    #include <bits/stdc++.h>
 1
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define vi vector<int>
    #define vl vector<ll>
    #define int ll
    #define rep(i, j, k) for(int i = (j); i <= (k); i++)
    #define per(i, j ,k) for(int i = (j); i \ge (k); i--)
    \textit{\#define ios ios::sync\_with\_stdio(false), cin.tie(0), cout.tie(0)}
10
    using namespace std;
11
12
     typedef long long ll;
    const ll maxn = 2e5 + 10;
13
     const ll mod = 998244353;
     const ll inf = 0x3f3f3f3f3;
15
16
     int n, h[maxn], to[maxn << 1], nxt[maxn << 1], cnt = 0;</pre>
17
     int sz[maxn], son[maxn], dep[maxn], L[maxn], R[maxn], f[maxn], idx[maxn], top[maxn], dfn = 0;
18
     ll sum[maxn], ans = 0;
     struct node {
20
21
         int x, id;
22
    } a[maxn];
23
     void add(int u, int v) {
         to[++cnt] = v;
25
26
         nxt[cnt] = h[u];
         h[u] = cnt;
27
28
    }
29
     void dfs1(int u, int fa) {
30
31
         f[u] = fa;
         dep[u] = dep[fa] + 1;
32
         sz[u] = 1;
33
         for (int i = h[u]; i; i = nxt[i]) {
34
35
              int v = to[i];
36
             if (v == fa) continue;
             dfs1(v, u);
37
             sz[u] += sz[v];
```

```
if (sz[v] > sz[son[u]])
39
40
                  son[u] = v;
         }
41
42
    }
    void dfs2(int u, int t) {
44
45
         top[u] = t;
         L[u] = ++dfn;
46
         idx[dfn] = u;
47
48
         if (son[u]) dfs2(son[u], t);
         for (int i = h[u]; i; i = nxt[i]) {
49
50
             int v = to[i];
             if (v == f[u] || v == son[u]) continue;
51
             dfs2(v, v);
52
53
         R[u] = dfn;
54
55
56
     struct Segment {
57
         struct Node {
58
             int l, r;
59
60
             int sum, add;
         } tr[maxn * 4];
61
         void pushup(int u) {
             tr[u].sum = tr[u << 1].sum + tr[u << 1 | 1].sum;
63
64
         void pushdown(int u) {
65
             if (tr[u].add) {
66
67
                  int x = tr[u].add;
                  tr[u << 1].sum += (tr[u << 1].r - tr[u << 1].l + 1) * x;
68
                  tr[u << 1 \mid 1].sum += (tr[u << 1 \mid 1].r - tr[u << 1 \mid 1].l + 1) * x;
69
70
                  tr[u << 1].add += x;
                  tr[u << 1 | 1].add += x;
71
                  tr[u].add = 0;
             }
73
74
             return;
75
         void build(int u, int l, int r) {
76
77
             tr[u] = {l, r};
             if (l == r) return;
78
79
             int mid = (l + r) >> 1;
             build(u << 1, l, mid);</pre>
80
             build(u << 1 | 1, mid + 1, r);
81
82
             return;
83
84
         void modify(int u, int l, int r, int x) {
             if (l <= tr[u].l && tr[u].r <= r) {</pre>
85
                  tr[u].add += x;
                  tr[u].sum += (tr[u].r - tr[u].l + 1) * x;
87
88
                  return;
89
             }
             pushdown(u);
90
             int mid = (tr[u].l + tr[u].r) >> 1;
             if (l <= mid) modify(u << 1, l, r, x);
92
             if (mid < r) modify(u << 1 | 1, l, r, x);
93
94
             pushup(u);
             return;
95
97
         int query(int u, int l, int r) {
             if (l <= tr[u].l && tr[u].r <= r) return tr[u].sum;</pre>
98
             pushdown(u);
99
             int mid = (tr[u].l + tr[u].r) >> 1;
100
101
             int res = 0;
             if (l <= mid) res += query(u << 1, l, r);</pre>
102
103
             if (mid < r) res += query(u << 1 | 1, l, r);</pre>
104
             return res:
105
106
    } Tr;
107
     void tree_add(int x, int y) {
         while (top[x] != top[y]) {
109
```

```
if (dep[top[x]] < dep[top[y]]) swap(x, y);</pre>
110
111
             Tr.modify(1, L[top[x]], L[x], 1);
             x = f[top[x]];
112
         }
113
         if (dep[x] < dep[y]) swap(x, y);</pre>
114
         Tr.modify(1, L[y], L[x], 1);
115
         return;
116
    }
117
118
119
     int tree_sum(int x, int y) {
         int res = 0;
120
121
         while (top[x] != top[y]) {
122
             if (dep[top[x]] < dep[top[y]]) swap(x, y);</pre>
             res += Tr.query(1, L[top[x]], L[x]);
123
             x = f[top[x]];
124
125
126
         if (dep[x] < dep[y]) swap(x, y);
         res += Tr.query(1, L[y], L[x]);
127
128
         return res;
    }
129
130
131
     void solve() {
         cin >> n;
132
         rep(i, 1, n) {
133
             cin >> a[i].x;
134
             a[i].id = i;
135
136
         sort(a + 1, a + n + 1, [\&](node p, node q) {return p.x > q.x;});
137
138
         rep(i, 1, n - 1) {
             int u, v;
139
             cin >> u >> v;
140
             add(u, v);
141
             add(v, u);
142
143
         dfs1(1, 0);
144
         dfs2(1, 1);
145
         Tr.build(1, 1, n);
146
         rep(i, 1, n) sum[i] = sum[i - 1] + dep[a[i].id];
147
148
         rep(i, 1, n){
             int x = a[i].id;
149
             ans = (ans + (ll)dep[x] * (i - 1) * a[i].x % mod + sum[i - 1] * a[i].x % mod - 2ll * a[i].x * tree\_sum(1, x) % \\
150
         mod + mod) % mod;
             tree_add(1, x);
151
152
         }
         cout << ans * 2ll % mod << endl;</pre>
153
154
     signed main() {
155
156
         //freopen("sample.txt", "r", stdin);
157
         //freopen("resout.txt", "w", stdout);
158
159
         int t = 1;
         //cin >> t:
160
         while (t--) {
             solve();
162
         }
163
164
         return 0;
    }
165
     计算几何
     二维几何: 点与向量
    #define y1 yy1
    #define nxt(i) ((i + 1) % s.size())
    typedef double LD;
    const LD PI = 3.14159265358979323846;
    const LD eps = 1E-10;
    int sgn(LD x) { return fabs(x) < eps ? 0 : (x > 0 ? 1 : -1); }
```

struct L;
struct P;

```
typedef P V;
10
    struct P {
11
        LD x, y;
        explicit P(LD x = 0, LD y = 0): x(x), y(y) {}
12
        explicit P(const L& l);
    };
14
    struct L {
15
        P s, t;
16
        L() {}
17
        L(P s, P t): s(s), t(t) {}
18
    };
19
20
    P operator + (const P& a, const P& b) { return P(a.x + b.x, a.y + b.y); }
21
    P operator - (const P& a, const P& b) { return P(a.x - b.x, a.y - b.y); }
22
    P operator * (const P& a, LD k) { return P(a.x * k, a.y * k); }
23
    P operator / (const P& a, LD k) { return P(a.x / k, a.y / k); }
24
    inline bool operator < (const P& a, const P& b) {</pre>
        return sgn(a.x - b.x) < 0 \mid | (sgn(a.x - b.x) == 0 && sgn(a.y - b.y) < 0);
26
27
    bool operator == (const P& a, const P& b) { return !sgn(a.x - b.x) & !sgn(a.y - b.y); }
28
    P::P(const L& l) { *this = l.t - l.s; }
29
    ostream &operator << (ostream &os, const P &p) {
        return (os << "(" << p.x << "," << p.y << ")");
31
32
    istream &operator >> (istream &is, P &p) {
33
34
        return (is >> p.x >> p.y);
35
36
    LD dist(const P& p) { return sqrt(p.x * p.x + p.y * p.y); }
    LD dot(const V& a, const V& b) { return a.x * b.x + a.y * b.y; }
38
    LD det(const V& a, const V& b) { return a.x * b.y - a.y * b.x; }
39
    LD cross(const P& s, const P& t, const P& o = P()) { return det(s - o, t - o); }
40
```

字符串

KMP

KMP 模板

```
#include <bits/stdc++.h>
    using namespace std;
    const int N = 1e6 + 10;
    vector<int> prefix_function(string s)
8
        int n = (int)s.length();
9
10
        vector<int> pi(n);
        for (int i = 2; i < n; i++)</pre>
11
12
            pi[i] = pi[i - 1];
13
            while (pi[i] && s[i] != s[pi[i] + 1])
14
15
                pi[i] = pi[pi[i]];
            pi[i] += (s[i] == s[pi[i] + 1]);
16
17
18
        return pi:
    }
19
20
21
    int main(void)
22
        ios::sync_with_stdio(false), cin.tie(0), cout.tie(0);
23
        string s1, s2;
24
25
        cin >> s1 >> s2;
        s1 = " " + s1;
26
        s2 = " " + s2;
27
        auto nxt = prefix_function(s2);
28
        for (int i = 1, j = 0; i < s1.size(); i++)</pre>
        {
```

```
while (j && s1[i] != s2[j + 1])
31
32
                 j = nxt[j];
             if (s1[i] == s2[j + 1])
33
                 j++;
34
             if (j == s2.size() - 1)
             {
36
37
                 cout << i - j + 1 << "\n";
                 j = nxt[j];
38
39
40
         for (int i = 1; i < s2.size(); i++)</pre>
41
42
             cout << nxt[i] << " ";
43
        return 0;
44
   }
45
```

● carpet(二维 KMP) 有一个 n*m 的地毯, aij 表示地毯每格的元素, bij 表示地毯每格的价格, 要求选取一块价格最大值最小的地毯, 并且这块地毯无限铺开之后, 原地毯是其子矩阵

```
#include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define x first
    #define y second
   #define int ll
   #define rep(i, j, k) for (int i = (j); i \le (k); i++)
    #define per(i, j, k) for (int i = (j); i \ge (k); i--)
    #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
10
11
    using namespace std;
    typedef long long ll;
12
    const ll maxn = 1e6 + 10;
    const ll mod = 998244353;
14
    const ll inf = 0x3f3f3f3f;
15
    vector<int> prefix_function(string s)
17
18
        int n = (int)s.length();
19
        vector<int> pi(n);
20
        for (int i = 2; i < n; i++)</pre>
21
22
23
             pi[i] = pi[i - 1];
             while (pi[i] && s[i] != s[pi[i] + 1])
24
25
                pi[i] = pi[pi[i]];
            pi[i] += (s[i] == s[pi[i] + 1]);
26
27
        return pi;
28
    }
29
    int get_length(vector<string> s)
31
32
        int len = s[1].size() - 1;
33
        int ret = len;
34
35
        vector<int> cnt(len + 1);
        for (int i = 1; i < s.size(); ++i)</pre>
36
37
             string tmp = s[i];
38
             auto nxt = prefix_function(tmp);
39
             int j = len;
40
             while (j)
41
42
                 cnt[len - nxt[j]]++;
43
                 j = nxt[j];
44
            }
45
46
47
        for (int i = 1; i <= len; ++i)</pre>
            if (cnt[i] == s.size() - 1)
48
49
             {
                 ret = i;
50
                 break;
51
             }
52
```

```
return ret;
53
54
    }
55
    void solve()
56
57
         int n, m;
58
59
         cin >> n >> m;
         vector<string> s1(n + 1);
60
         for (int i = 1; i <= n; ++i)</pre>
61
             cin >> s1[i], s1[i] = " " + s1[i];
         vector<string> s2(m + 1);
63
64
         for (int i = 1; i <= m; ++i)</pre>
65
             string tmp = " ";
66
              for (int j = 1; j <= n; ++j)</pre>
67
                  tmp += s1[j][i];
68
69
             s2[i] = tmp;
70
71
         vector<vector<int>>> a(n + 1, vector<int>(m + 1, 0));
         for (int i = 1; i <= n; ++i)
72
             for (int j = 1; j \le m; ++j)
73
74
                  cin >> a[i][j];
         int p = get_length(s1), q = get_length(s2);
75
         ll ans = 1e9;
77
         deque<int> dq;
         auto b = a;
78
         for (int i = 1; i <= n; ++i){</pre>
79
             while (dq.size()) dq.pop_back();
80
             for (int j = 1; j <= m; ++j){</pre>
                  while (dq.size() \&\& j - dq.front() + 1 > p) dq.pop_front();
82
                  while (dq.size() && a[i][dq.back()] <= a[i][j]) dq.pop_back();</pre>
83
84
                  dq.push_back(j);
                  b[i][j] = a[i][dq.front()];
85
87
         for (int j = 1; j <= m; ++j){</pre>
88
             while (dq.size()) dq.pop_back();
89
             for (int i = 1; i <= n; ++i){</pre>
                  while (dq.size() \&\& i - dq.front() + 1 > q) dq.pop_front();
                  while (dq.size() && b[dq.back()][j] <= b[i][j]) dq.pop_back();</pre>
92
93
                  dq.push_back(i);
                  if (i >= q && j >= p)
94
                       ans = min(ans, 1ll * b[dq.front()][j]);
95
96
             }
97
98
         ans = ans * (p + 1) * (q + 1);
         cout << ans << endl;</pre>
99
100
101
    signed main()
102
103
104
         // freopen("sample.txt", "r", stdin);
105
         // freopen("resout.txt", "w", stdout);
106
         int t = 1;
107
         // cin >> t;
108
         while (t--)
109
             solve();
111
112
113
         return 0;
114
```

杂项

线性基

• 线性基模板 (总异或最大值)

```
ll p[64];
1
2
    void insert(ll x){
        for (int i = 63; ~i; --i){
            if (!(x >> i)) continue;
            if (!p[i]){
                p[i] = x;
                break;
            }
            x ^= p[i];
10
        }
   }
11
        • 区间线性基 (区间异或最大值, 强制在线)
    #include<bits/stdc++.h>
   #define M 500009
    using namespace std;
3
    int read() {
        int f = 1, re = 0; char ch;
        for (ch = getchar(); !isdigit(ch) && ch != '-'; ch = getchar());
        if (ch == '-') {f = -1, ch = getchar();}
        for (; isdigit(ch); ch = getchar()) re = (re << 3) + (re << 1) + ch - '0';</pre>
        return re * f;
10
    int pos[M][32], p[M][32], t, n, m, lastans;
    void insert(int val, int num, int po) {
12
13
        for (int i = 30; i >= 0; i--) {
            if (val & (1ll << i)) {</pre>
14
                 if (!p[num][i]) {p[num][i] = val, pos[num][i] = po; return;}
15
                 else if (pos[num][i] < po) {</pre>
                     swap(val, p[num][i]);
17
                     swap(po, pos[num][i]);
18
                } val ^= p[num][i];
19
            }
20
21
        } return;
   }
22
23
    int query(int l, int r) {
        int ans = 0;
24
        for (int i = 30; i >= 0; i--)
25
            if (pos[r][i] >= l \&\& (p[r][i]^ans) > ans) ans ^= p[r][i];
26
27
        return ans;
28
    signed main() {
29
        t = read();
30
        while (t--) {
31
32
            n = read(), m = read(); lastans = 0;
33
            memset(p, 0, sizeof(p));
            memset(pos, 0, sizeof(pos));
34
35
            for (int i = 1; i <= n; i++) {
                 int x = read();
36
                 for (int j = 0; j <= 30; j++)
37
                     p[i][j] = p[i - 1][j], pos[i][j] = pos[i - 1][j];
38
                 insert(x, i, i);
39
            for (int i = 1; i <= m; i++) {</pre>
41
                 int opt = read();
42
                if (opt) {
43
44
                     int x = read()^lastans; n++;
45
                     for (int j = 0; j <= 30; j++)
                         p[n][j] = p[n - 1][j], pos[n][j] = pos[n - 1][j];
46
47
                     insert(x, n, n);
                }
48
49
                else {
                     int l = (read()^lastans) % n + 1;
50
                     int r = (read()^lastans) % n + 1;
51
                     if (l > r) swap(l, r);
52
                     printf("%d\n", lastans = query(l, r));
53
54
55
            }
56
        } return 0;
57
   }
```

● 区间问题 (异或和, 区间内是否存在异或和为 x)

```
#include <bits/stdc++.h>
1
    #define ll long long
    using namespace std;
    constexpr ll maxn = 4e5 + 5;
    int pos[65];
    ll p[65], t, n, m;
    bool ans[maxn];
    void insert(ll val, int P)
8
         for (int i = 59; i >= 0; i--)
10
11
             if (val & (1ll << i))</pre>
12
             {
13
14
                 if (!p[i])
15
                 {
                      p[i] = val, pos[i] = P;
16
17
                      return;
                 }
18
19
                 else if (pos[i] < P)</pre>
                 {
20
21
                      swap(val, p[i]);
                      swap(P, pos[i]);
22
23
                 val ^= p[i];
24
             }
25
26
        return;
27
    }
28
    bool query(int l, ll val)
29
30
    {
         for (int i = 59; i >= 0; i--)
31
32
             if (val & (1ll << i))</pre>
33
34
                 if (!p[i])
35
36
                      return false;
                 if (pos[i] < l)
37
38
                      return false;
                 val ^= p[i];
39
40
             }
41
        return true;
42
43
    signed main()
44
45
    {
         ios::sync_with_stdio(false);
46
47
        cin.tie(nullptr);
48
        cin >> n >> m;
        vector<ll> a(n + 1);
49
         vector<tuple<int, int, ll, int>> q(m);
50
51
         for (int i = 1; i <= n; i++)</pre>
             cin >> a[i];
52
        for (int i = 0; i < m; i++)</pre>
53
54
55
             auto &[l, r, val, id] = q[i];
             cin >> l >> r >> val, id = i;
56
        }
57
58
         sort(q.begin(), q.end(), [&](auto x, auto y)
59
             {
60
             auto &[l1,r1,val1,id1] = x;
             auto &[l2,r2,val2,id2] = y;
61
             return (r1==r2)?(l1<l2):(r1<r2); });</pre>
        int R = 0;
63
         for (int i = 0; i < m; i++)</pre>
64
65
             auto &[l, r, val, id] = q[i];
66
67
             while (R < r)</pre>
                 insert(a[R + 1], R + 1),R++;
68
             ans[id] = query(l, val);
69
        }
70
```

```
for (int i = 0; i < m; i++)
{
      cout << (ans[i] ? "Yes\n" : "No\n");
}

return 0;
}</pre>
```

Tarjan

缩点

```
//Tarjan 缩点 (删去一个点, 有多少点对不能互通)
   #include <bits/stdc++.h>
    #define endl '\n'
    #define pll pair<ll, ll>
    #define tll tuple<ll, ll, ll>
    #define x first
    #define y second
    #define int ll
    #define rep(i, j, k) for (int i = (j); i \le (k); i++)
    #define per(i, j, k) for (int i = (j); i \ge (k); i--)
   #define ios ios::sync_with_stdio(false), cin.tie(0), cout.tie(0)
    using namespace std;
12
13
    typedef long long ll;
    typedef __int128 i128;
14
    const ll maxn = 1e6 + 10;
15
    const ll mod = 998244353;
    const ll inf = 0x3f3f3f3f;
17
    ll n, m;
19
    ll head[maxn], nxt[maxn], to[maxn], tot = 1;
20
    ll dfn[maxn], low[maxn];
    bool vis[maxn];
22
23
    ll cnt;
    ll deg[maxn];
24
    ll ans[maxn];
25
    ll sz[maxn];
26
27
28
    void addedge(int u, int v)
    {
29
        nxt[++tot] = head[u];
        to[head[u] = tot] = v;
31
        nxt[++tot] = head[v];
32
33
        to[head[v] = tot] = u;
    }
34
35
    void tarjan(int u, int lst)
36
37
    {
38
        dfn[u] = low[u] = ++cnt;
        ll sum = 0;
39
40
        sz[u] = 1;
        for (int i = head[u]; i; i = nxt[i])
41
42
            if (i != (lst ^ 1))
43
44
            {
                int v = to[i];
45
                if (!dfn[v])
46
47
                     tarjan(v, i);
48
                     sz[u] += sz[v];
49
                     low[u] = min(low[u], low[v]);
50
                     if (low[v] >= dfn[u])
51
52
                         // 找到新的双连通分量
53
                         ans[u] += 1ll * sz[v] * (n - sz[v]);
54
                         sum += sz[v];
55
                         ++deg[u];
56
57
                         if (deg[u] > 1 || u != 1)
                             vis[u] = 1;
58
```

```
}
59
                  }
60
                  else
61
                       low[u] = min(low[u], dfn[v]);
62
              }
64
         if (vis[u])
65
66
             ans[u] += 1ll * (n - (sum + 1)) * (sum + 1) + n - 1;
67
         }else
68
             ans[u] = 2 * (n - 1);
69
    }
70
    void solve()
71
72
    {
73
         cin >> n >> m;
74
         for (int i = 1; i <= m; ++i)</pre>
75
              int u, v;
76
              cin >> u >> v;
77
              addedge(u, v);
78
         }
79
         tarjan(1, -1);
80
         for (int i = 1; i <= n; ++i)</pre>
81
              if (vis[i])
83
84
              {
                  cout << ans[i] << endl;</pre>
85
              }
86
87
              else
88
              {
89
                  cout << 2ll * (n - 1) << endl;
90
91
         }
    }
92
93
     signed main()
94
95
     {
96
         //freopen("sample.txt", "r", stdin);
97
98
         //freopen("res.txt", "w", stdout);
         int t = 1;
99
         // cin >> t;
100
         while (t--)
101
102
              solve();
103
         }
104
105
         return 0;
    }
107
```