



Master in Computer Vision *Barcelona*

Module: M4 3D Vision
Lecture: **4.9b 3D sensors**
Lecturer: Josep R. Casas



Motto and fundamental questions

Motto:

Computer Vision = “Teaching computers to see”



Antonio Torralba (MIT)

Talk@CVC 20th Anniversary, Barcelona July 9th, 2015

*Exciting time for CV: new architectures, DBs, productivization, future
Fundamental problems: **reconstruct 3D world**, recognize...*

Questions around this:

*Q1: Is “**projective vision**” a natural way to capture the 3D world?*

*Q2: Do we need **photometry** to get **geometry**?*

*Q3: Does **3D vision** mean the same than **3D geometry**?*

*Q4: Does 2D/3D matter for “**Teaching computers to see**”?*

Introduction to 3D Sensors and Range Data

3D vision has been introduced from the concepts of:

- **Projective transformations**
perspective projection, *projectivities* (3D, plane-to-plane, n -dimensional spaces, homography, invariants...)
- **Multiple-View geometry**
reconstruct real world scenes from several images (projections) or from a moving camera (SfM)

...Ok. That's the natural way into the field of 3D vision as, for visual perception, humans come equipped with:

- Two '**projective**' sensors
- Multi-view (**stereoscopic**) vision (and FVV: 'free viewpoint view')

*Q1: Is “**projective vision**” a natural way to capture the 3D world?*

Introduction to 3D Sensors and Range Data (cont)

■ 2D vs 3D

“2D imaging

...projects 3D scenes onto a planar surface (retina, sensor)...

...so that the depth (Z) dimension is lost”

- *Are there imaging sensors not projecting onto a plane?*
- *How can depth (range) be perceived directly?*
- *What would be the main advantage of capturing 3D **directly**?*

*Q2: Do we need to measure **photometry** to get **geometry**?*

Introduction to 3D Sensors and Range Data (cont)

■ Distance measurement methods...

Range sensors (scanners!)

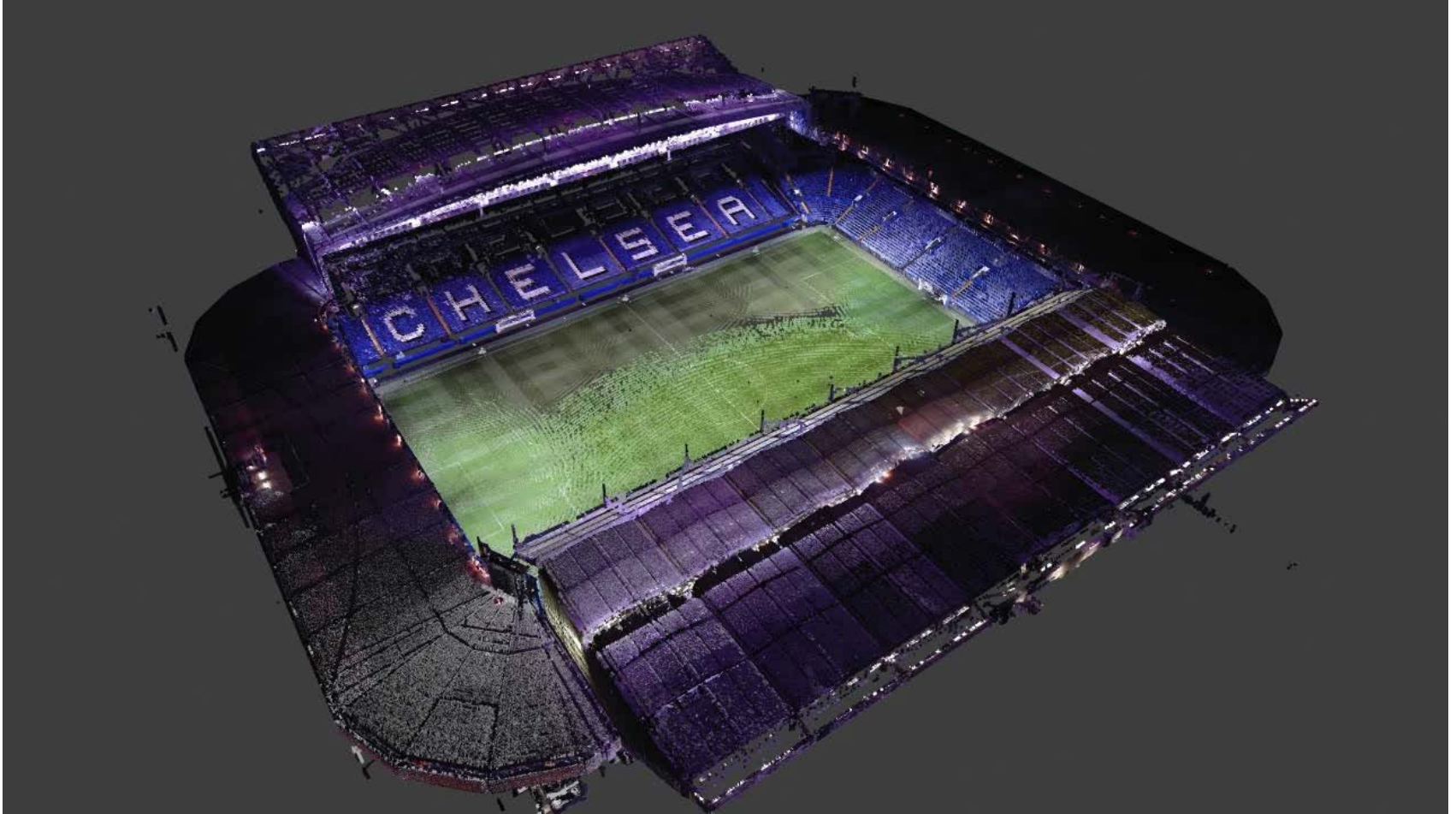
- 3D scanners and Lidar systems
- Light coding systems (e.g. Kinect™)
- TOF cameras (e.g. Kinect™ v2)

...and then

- *Will this result in a complete view... like a CAD design?*
- *Panoramic / Surround view?*
- *Free viewpoint?*

Q3: Does 3D vision mean the same than 3D geometry?

Example of 3D capture



Lidar capture of the Stamford Bridge (cf. [FascinatE project](#))

Example of 3D processing



AR magic mirror using Kinect (cf. T. Blum, N. Navab, TUM)

3D/range/scan sensors vs Multiple View

Advantages 3D/range/scan

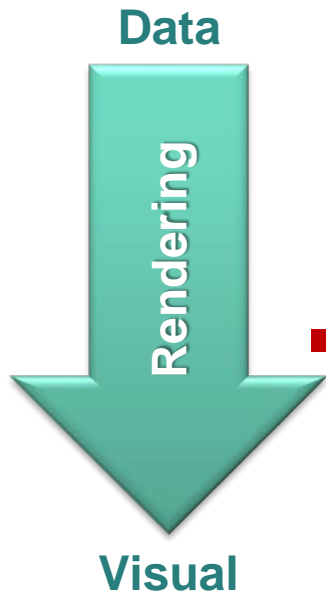
- ...
-
-
-
- Direct measure of 3D geometry
- Independent of photometry (active)
- From scan to CAD blueprints

Disadvantages

- ...
-
-
-
- 2,5D!
Surface vs 3D (interface air-matter vs volumetric 3D scanner, i.e. PET)
- Single viewpoint
Neither panoramic, nor surround view
- Accuracy?
vs MPix cams!

3D Data

Double nature of 3D data



- **Geometric information**

Pure data, measures.

Numerical representation of objects

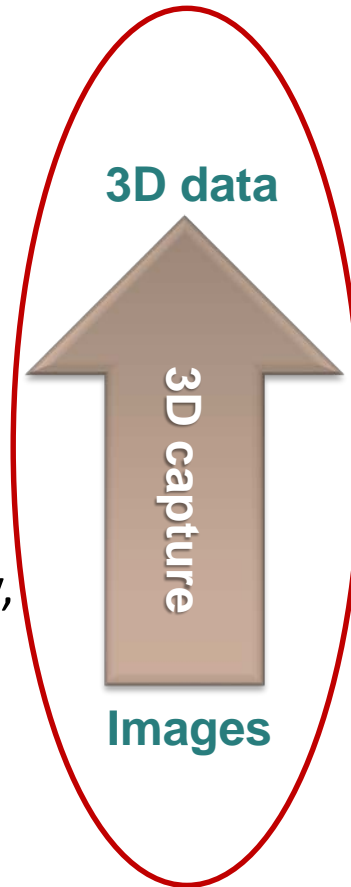
→ calculation, simulation, measurements

... + **reflectivity**

- **Photometric information (images)**

Can be displayed, presented and perceived visually,
by exploiting our perception capabilities

→ exploration, analysis and understanding
(same than looking at the physical world)



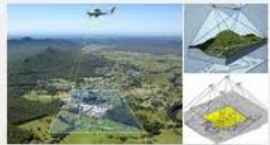
Photogrammetry

Photogrammetry refers to the practice of deriving 3D measurements from photographs.

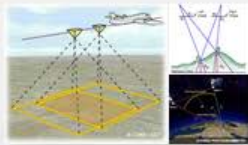
- Advances in digital cameras, processors, and computation, yield **extremely dense and accurate 3D surface data** from a limited number of photos with standard digital photography
- Structure from Motion (SfM) and sub-pixel image matching yield **3D-dimensional structure by analyzing projected 2D motion fields** created by a sequential change of position of the camera sensor relative to the object. Photographic sequences are captured to maximize information available from the change in viewpoint
- Resulting **data sets are software platform-independent** and can be reused

*Disadvantage: **computation time...***

Photogrammetry examples



Aerial



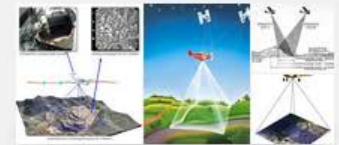
Stereoscopic



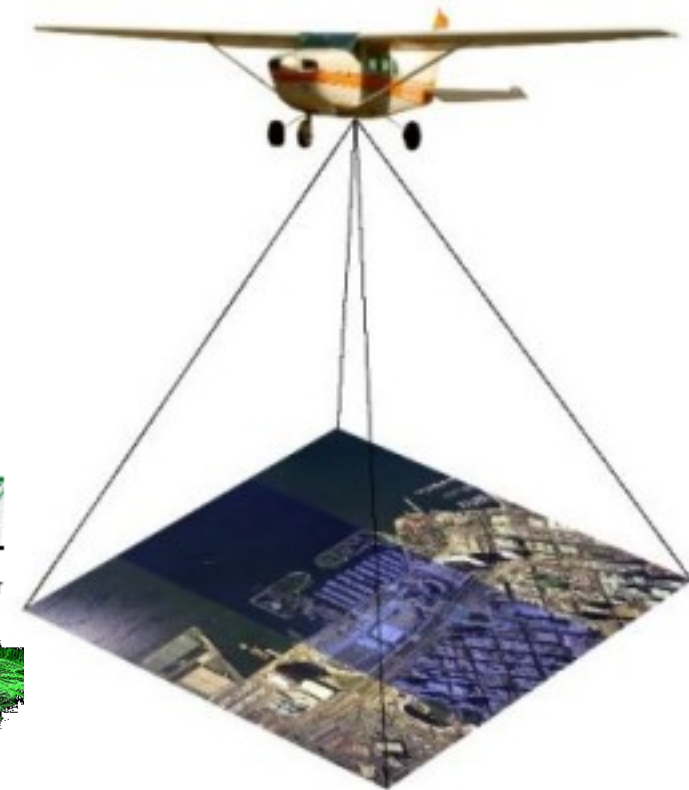
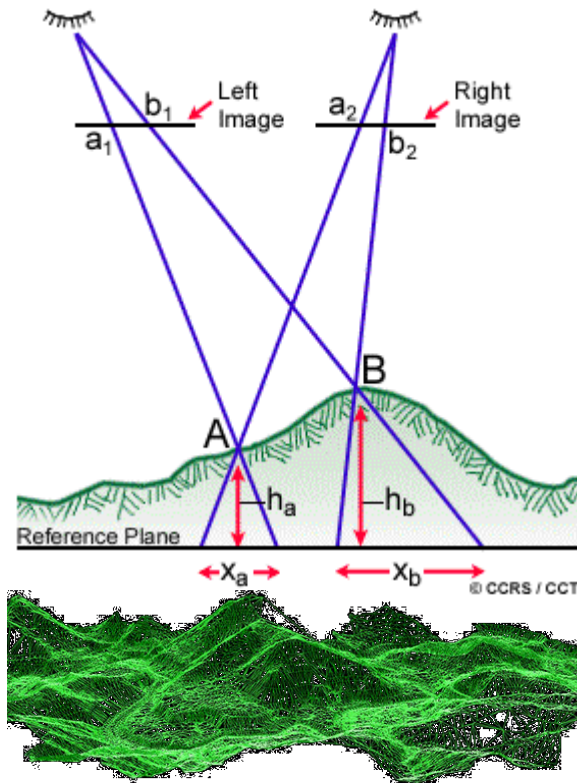
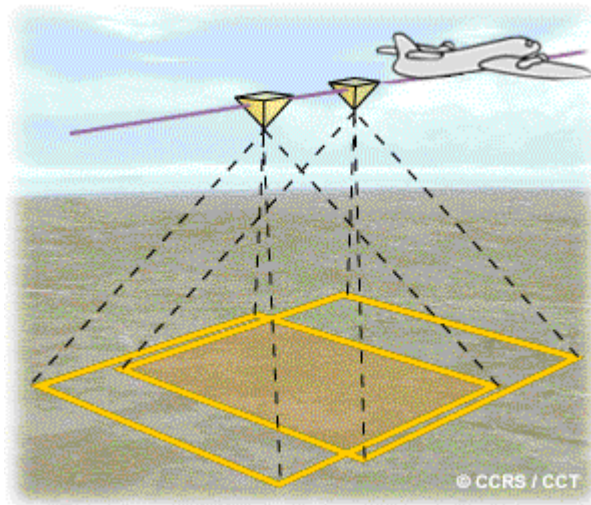
Architecture



Close Range

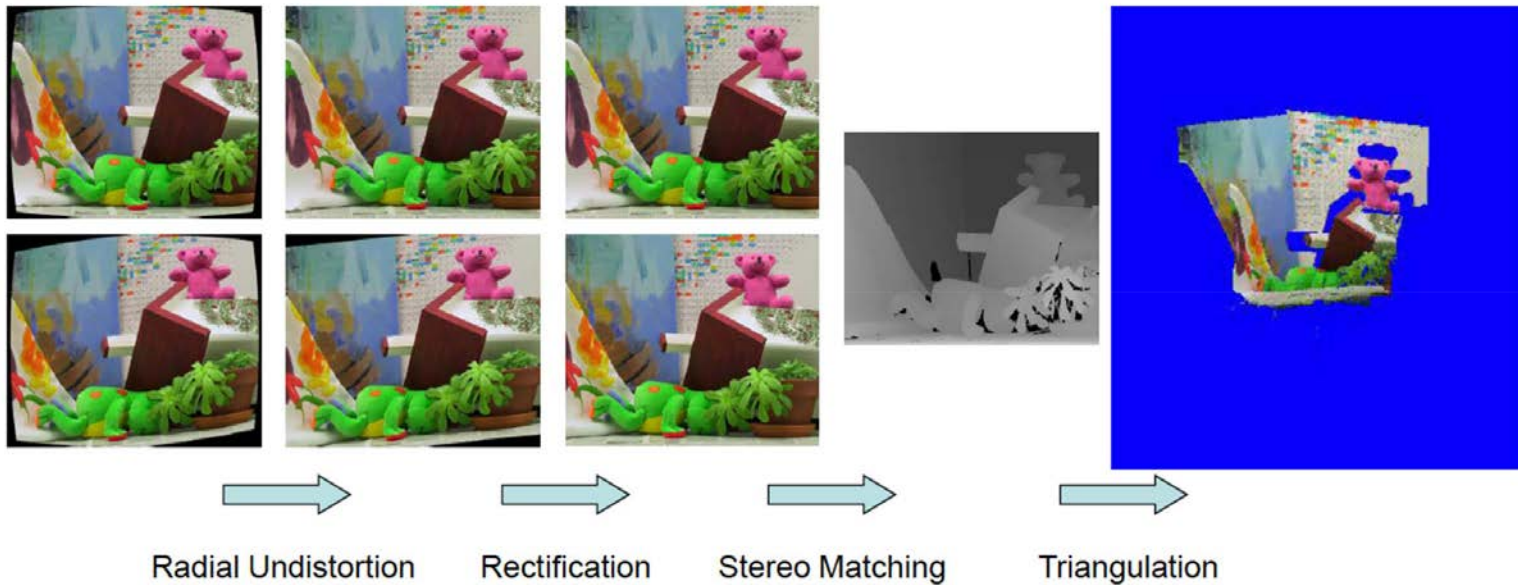


Surveying



3D/range/sensor vs Multiple View

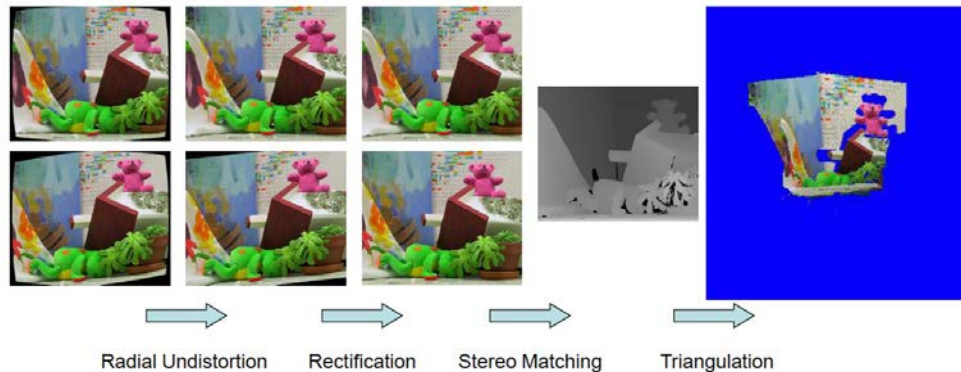
Depth Measurement Using Multiple Camera Views



From N. Navab et al, *TUM* 2011

3D/range/scan sensors vs Multiple View

Depth Measurement Using Multiple Camera Views



Disadvantages:

- At least two calibrated cameras required
- Multiple computationally expensive steps
- Dependence on scene illumination
- Dependence on surface texturing

From N. Navab et al, *TUM* 2011

3D data

Depth, cloud, mesh...

3D data representation

- Depth map
 - **2.5D** (concept: $\text{RGBD} = \text{2D} + \text{depth}$)
- Point cloud
 - **organized**: keeps relationships in sensor neighborhood
 - **unorganized**: one can *just* compute nearest neighbors in 3D
- Mesh
 - nice scanned/reconstructed surfaces: watertight / convex...

Point cloud data

■ Organized point-cloud

Resemble an organized image (or matrix-like) structure, with data split into rows and columns (data from stereo, depth or TOF sensors)

→ **projectable** point cloud: has a correlation according to a pinhole camera model between the (u,v) index of a point in the organized point cloud and the actual 3D values.

This correlation can be expressed as: $u = f \cdot x / z$ and $v = f \cdot y / z$

→ knowing the relationship between adjacent points (e.g. pixels), nearest neighbor operations are much more efficient, thus speeding up the computation and lowering the costs of certain algorithms in PCL

■ Unorganized point-cloud

Non-regular sampling of 3D space

Neighborhood operations require KD tree search!

<http://pointclouds.org/documentation>

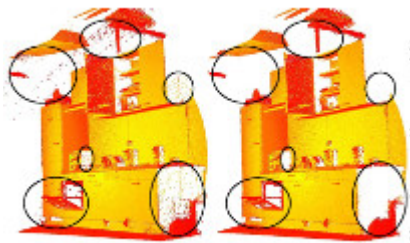
[Rusu 2009, Rusu 2011]

Point Clouds

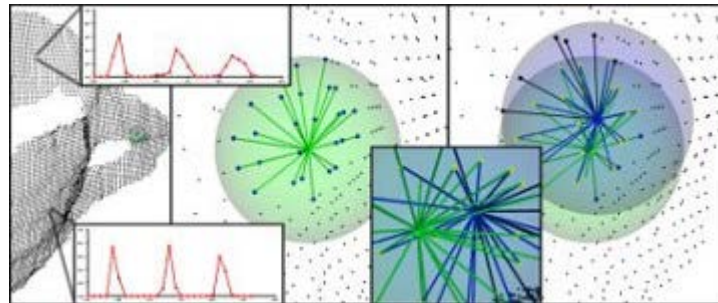
- New trend to process raw data produced by scanners

– Point Cloud → PCL library

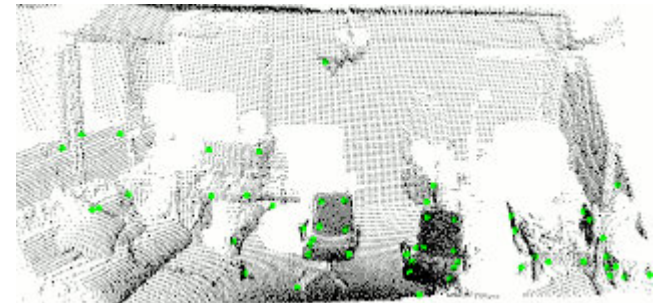
pointclouds.org



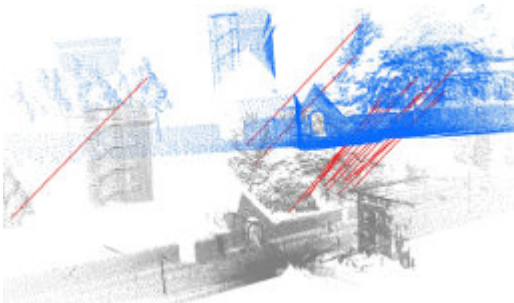
Filters



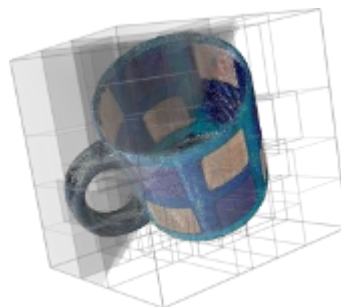
Features



Key points



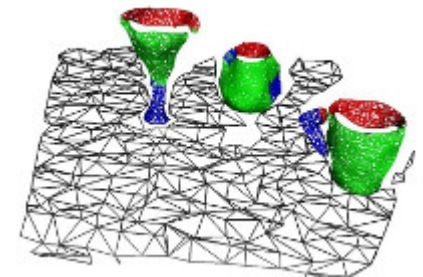
Segmentation



RANSAC



Octree

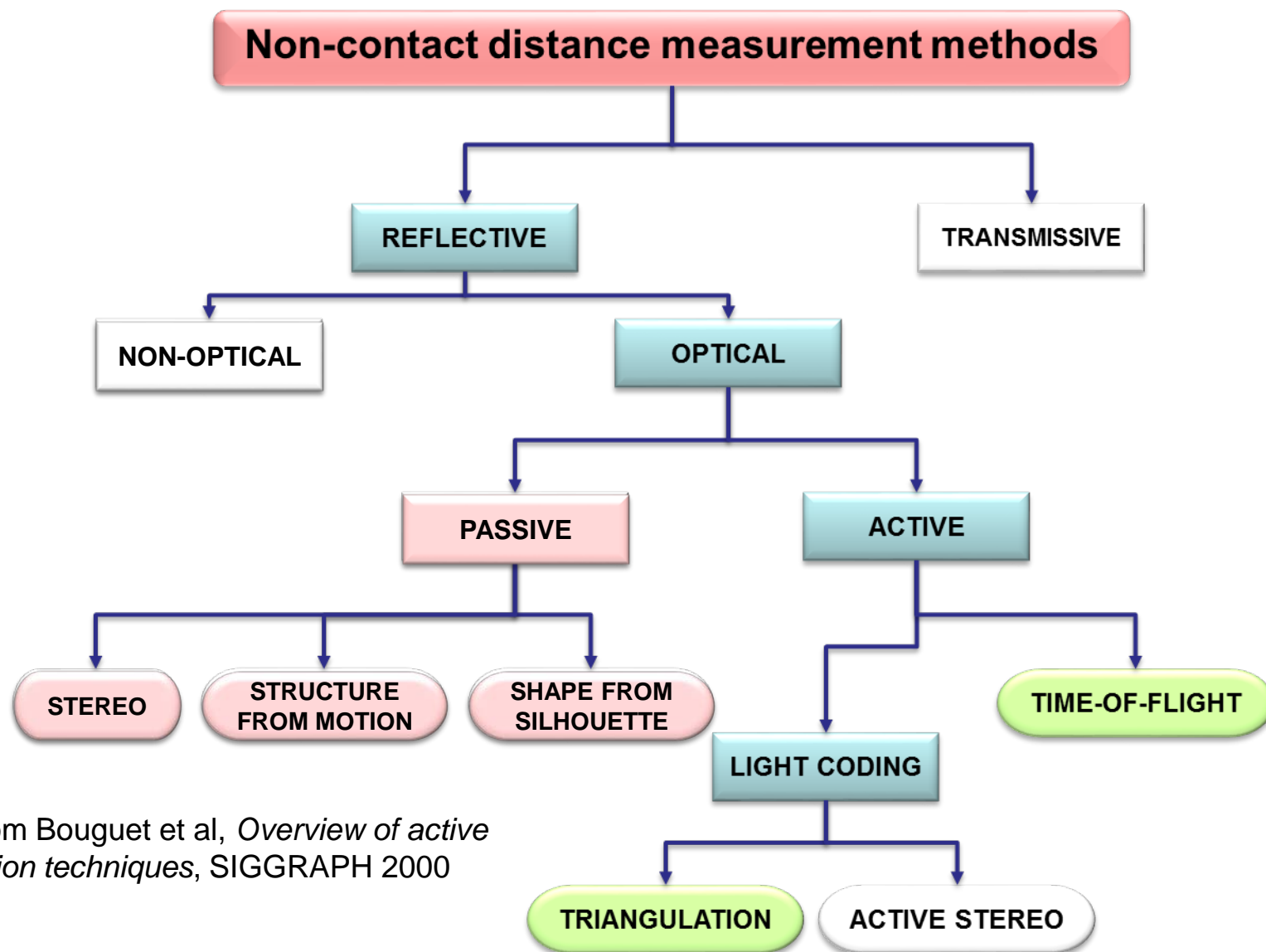


Visualization

3D sensors

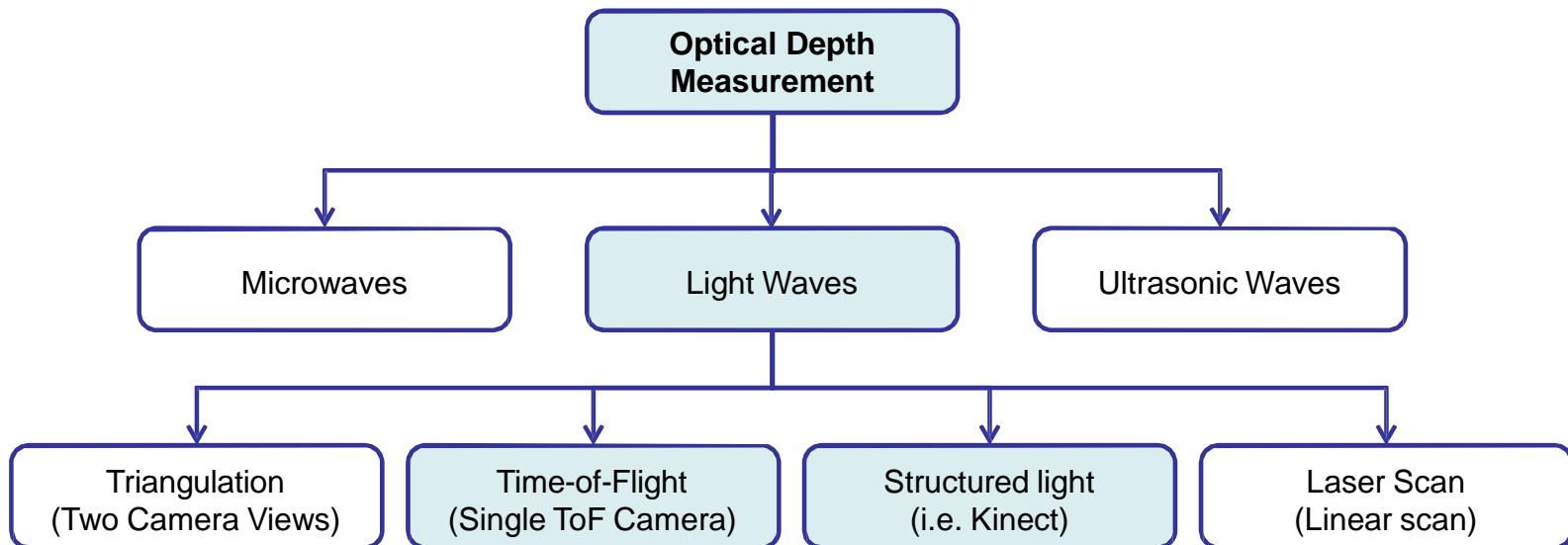
Depth, range, scan...

“Non-contact” – distance measurement methods



From Bouguet et al, *Overview of active vision techniques*, SIGGRAPH 2000

Optical Depth Measurement Techniques



From N. Navab et al, *TUM* 2011

Depth or Range sensing Methods

Reflective optical methods:

■ Passive range sensing

3D distance measurement by the way of **radiation already present in the scene**. Not necessarily in the visible spectrum

- E.g. stereo, multi-camera (triangulation, SfS...)

Off-the-shelf light field cams have demonstrated improved depth estimation using multiview stereo configs [Bishop 2012]

■ Active range sensing

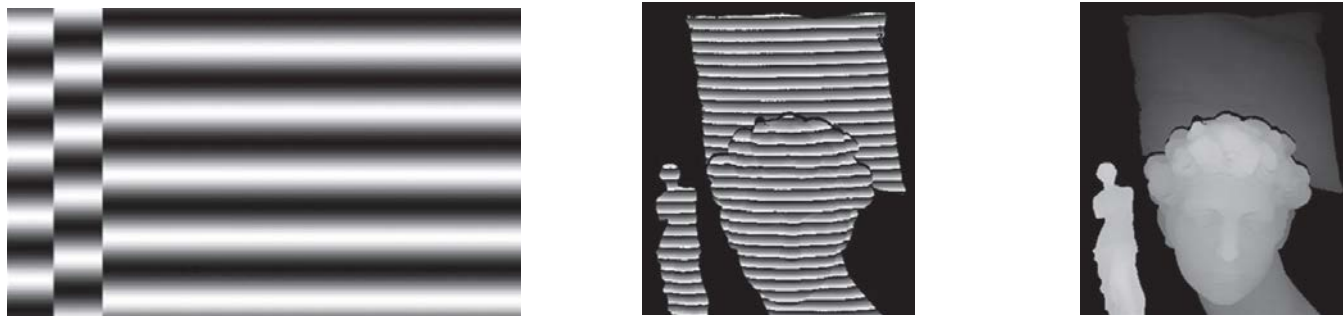
3D distance measurement obtained by projecting in the scene **some form of radiation**

- ToF (IR/laser) → high frame rate, low res, noise [Foix 2011]
- Lidar (UV/visible/IR) → sequential (low frame rate)
- Structured Light (IR/visible) → artifacts, noise, indoor [Salvi 2010]

Computational Depth Sensing

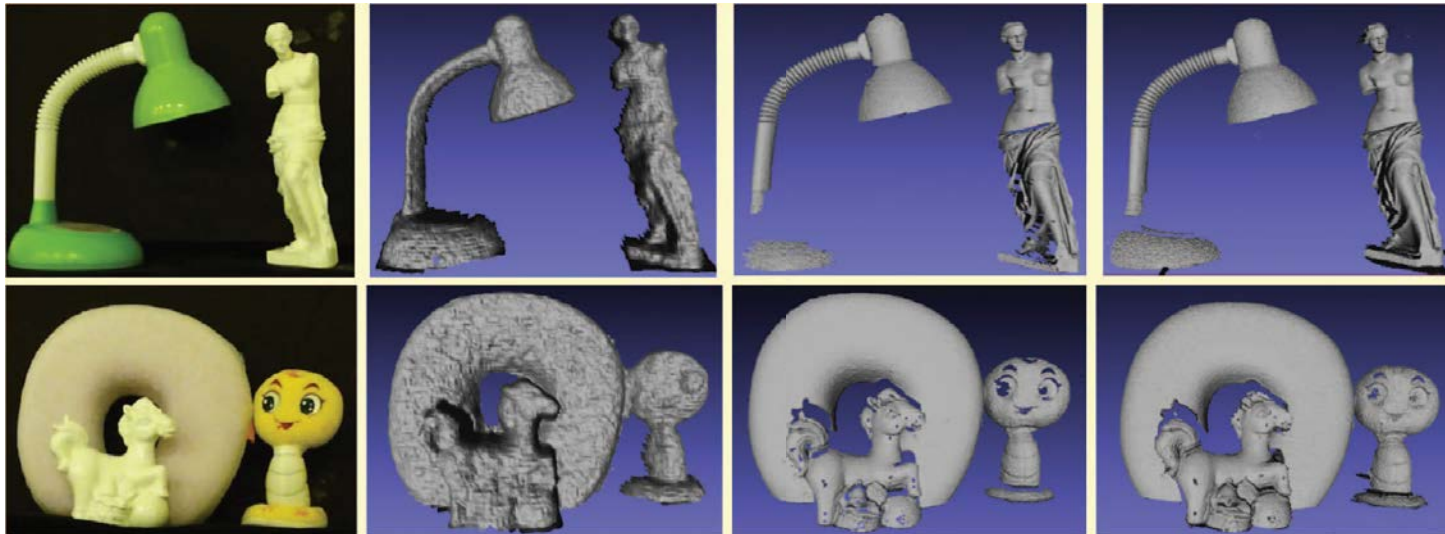
- Depth cameras do not sense depth information directly, rather, through either the space deformation or the time delay of light signals
- Computation needed!

Computational Depth Sensing: image sensors with onboard advanced signal processing algorithms (Redesign [Xiong 2017])



Example of phase shifting (Xiong et al, 2017)

3D reconstruction results



3D reconstruction results for texture-less surfaces:

(a) color image

(b) ToF results

(c) three-frequency phase shifting (nine patterns)

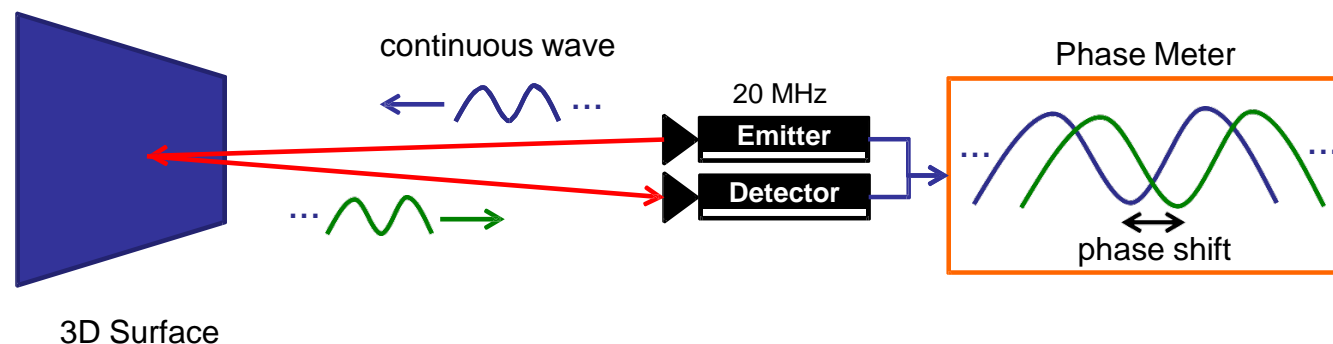
(d) ToF and phase-shifting **fusion** (three patterns)

(Xiong et al, 2017)

Principles of ToF sensors

Continuous Wave Modulation

- Continuous light waves instead of short light pulses
- Modulation in terms of frequency of sinusoidal waves
- Detected wave after reflection has shifted phase
- Phase shift proportional to distance from reflecting surface



Principles of ToF sensors

Continuous Wave Modulation



Advantages:

- Variety of light sources available as no short/strong pulses required
- Applicable to different modulation techniques (other than frequency)
- Simultaneous range and amplitude images



Disadvantages:

- In practice, integration over time required to reduce noise
- Frame rates limited by integration time
- Motion blur caused by long integration time

TOF Imaging



Swissranger™ SR4000
Mesa Imaging



Kinect for Xbox One by
Microsoft

Matricial Time-Of-Flight Cameras

- Active sensors
- Acquire 3D geometry at video rate (up to 50fps)
- E.g. MESA Imaging
PMD Technologies
Optrima SoftKinetic
CANESTA (*acquired by Microsoft in 2010*)

...



D-IMager
Panasonic



pmd[vision] CamCube
PMD Technologies



FOTONIC-B70
Fotonic



3D MLI Sensor
IEE S.A.

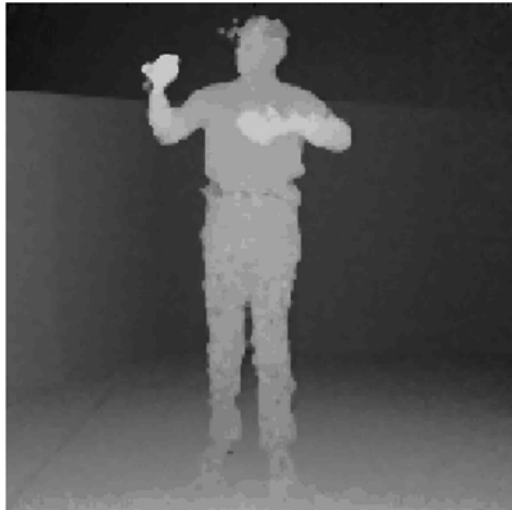


pmd[vision] CamBoard
PMD Technologies

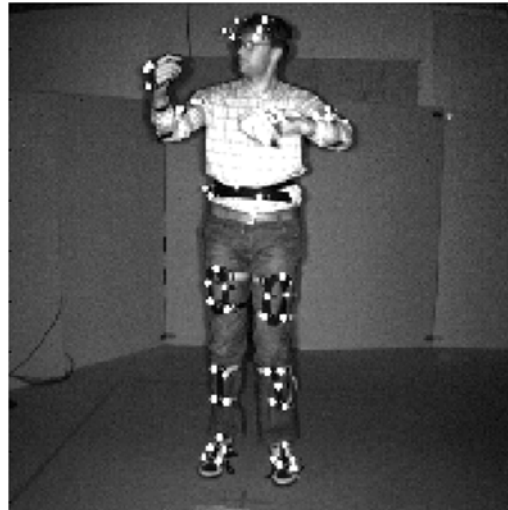
Principles of ToF Imaging

Continuous Wave Modulation

- Simultaneous availability of (co-registered) range and amplitude images



Depth Image



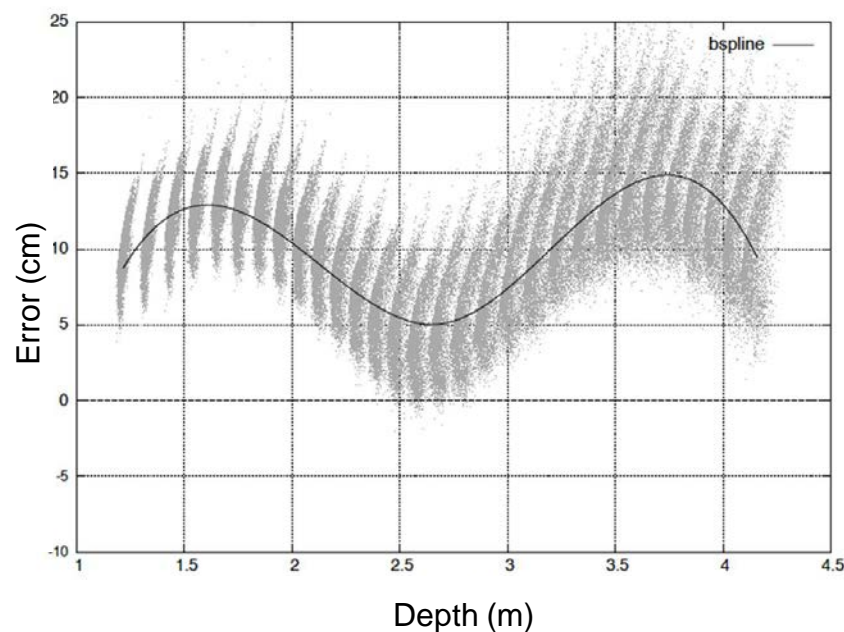
Amplitude Image

Computer Vision with ToF Cameras

Measurement Errors and Noise

Systematic distance error

- Perfect sinusoidal signals hard to achieve in practice
- Depth reconstructed from imperfect signals is erroneous
- Solution 1: camera-specific calibration to know distance error
- Solution 2: alternative demodulation techniques not assuming perfect sinusoidal signals

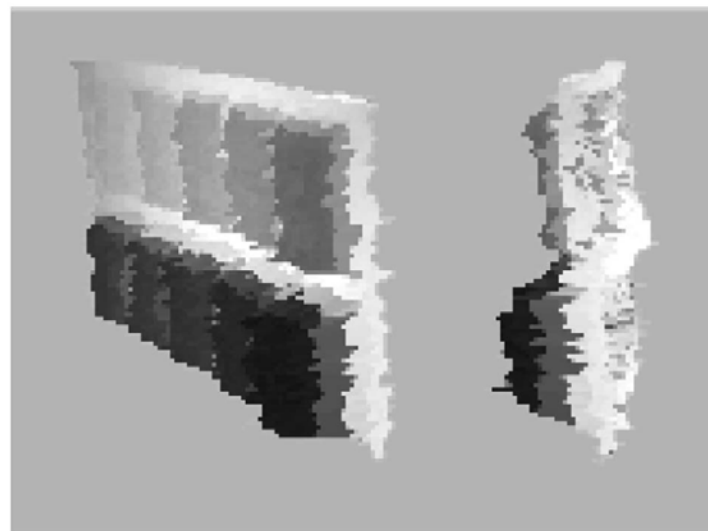


Computer Vision with ToF Cameras

Measurement Errors and Noise

Intensity-related distance error

- Computed distance depending on amount of incident light
- Inconsistencies at surfaces with low infrared-light reflectivity
- Correction by means of corresponding amplitude image



Depth images of planar object
with patches of different reflectivity

Computer Vision with ToF Cameras

Measurement Errors and Noise

Depth inhomogeneity

- Current ToF cameras have low pixel resolution
- Individual pixels get different depth measurements
- Inhomogeneous
- „Flying pixels“, especially at object boundaries
- Correction: discard pixels along rays parallel to viewing direction

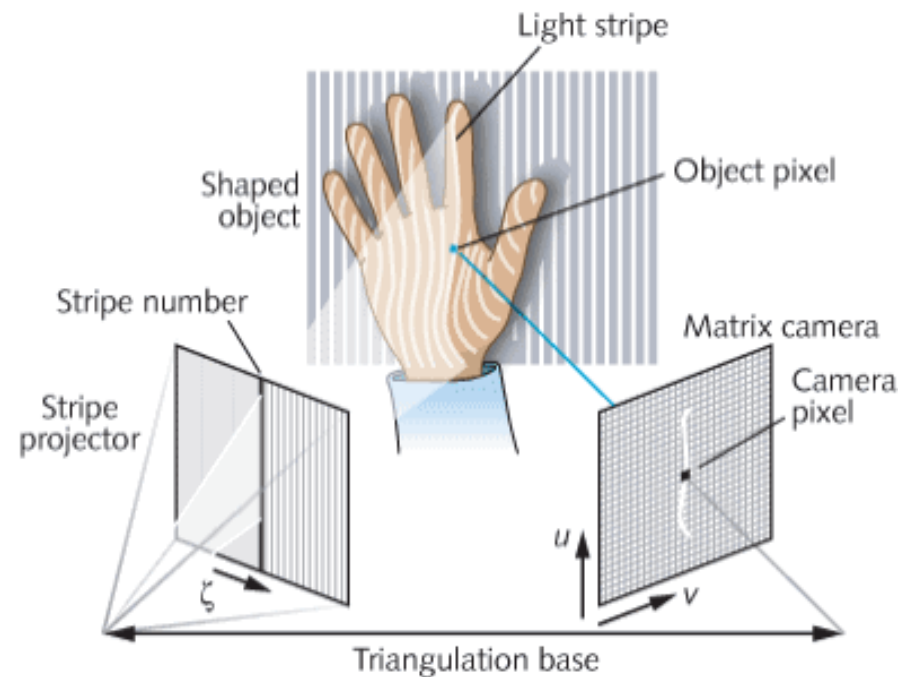


Red circles: „flying pixels“

Structured Light methods

Structured light methods

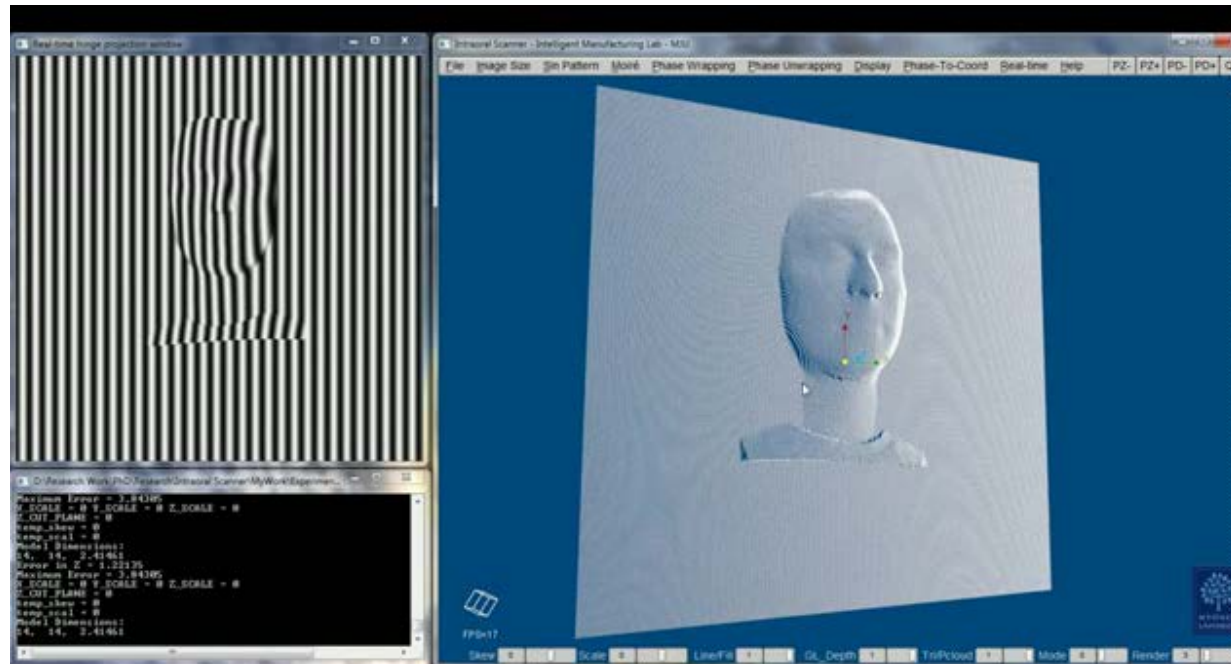
- Calculate the shape by how the strip is distorted.



<http://www.laserfocusworld.com/articles/2011/01/lasers-bring-gesture-recognition-to-the-home.html>

Real time Virtual 3D Scanner - Structured Light Technology

- Demo



http://www.youtube.com/watch?v=a6pgzNUjh_s

What is Kinect?

- RGB, Depth Sensor, and Multi-mic Array
- Works with structured light (dots rather than strips) to determine distance for each pixel

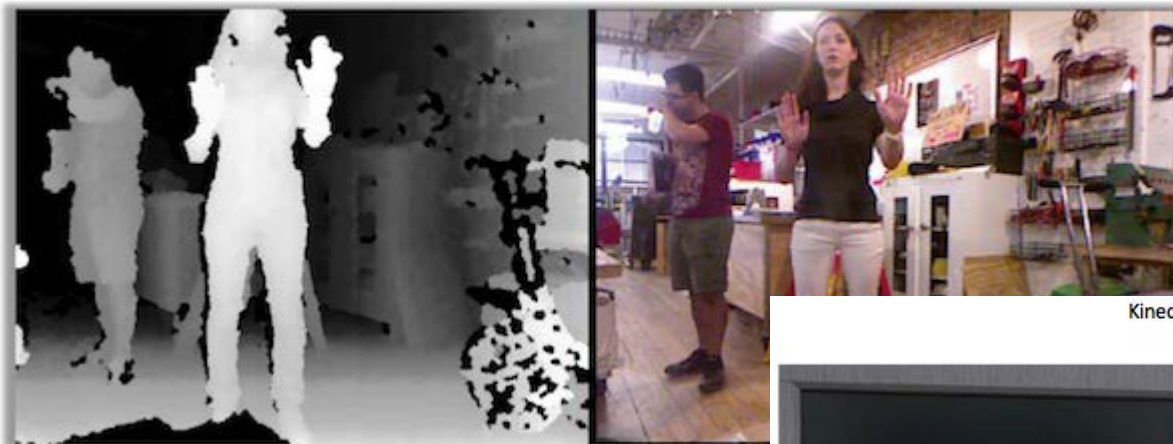


History

- Original technology developed in 2005
- Announced in 2009 as codenamed Natal after the city and because of its relation to being “of or related to birth”
- Released Kinect for Windows Beta on June 16, 2011
- On February 1st, released commercial version
- Kinect for Xbox ONE (v2, 2013)
 - Time-of-flight sensor replacing the old technology from PrimeSense with CANESTA technology

Kinect

Kinect For Windows 1



Kinect For Windows 2



Image via <http://blogs.msdn.com>

Commercial Depth Sensors: Specifications



	<u>Kinect</u>	<u>Kinect-2</u>	<u>Xtion Pro Live</u>	<u>Structure</u>
Color	640x480 (2x!) @30fps	1920x1080 @30fps	1280x1024 @30fps	(iPad cam)
Depth	320x240 16bit	512x424	640x480 (320x240@60)	640x480 (320x240@60)
Range (m)	(0.4)0.8-3,5	0.5-4,5	0.8-3,5	0.4-3,5
FoV (VxH)	43° x 57°	60° x 70°	58° x 45°	58° x 45°
Tilt motor Accelerom.	±27° (V) 2G(1°)/4G/8G	—	—	—
Audio	16bit PCM @16kHz 4 mics	16bit PCM @16kHz 4 mics	2 mics	(iPad mic)
USB	2.0	3.0	2.0	2.0 (hack)
Tracker	20 joints (2x)	26 joints (6x)	—	—

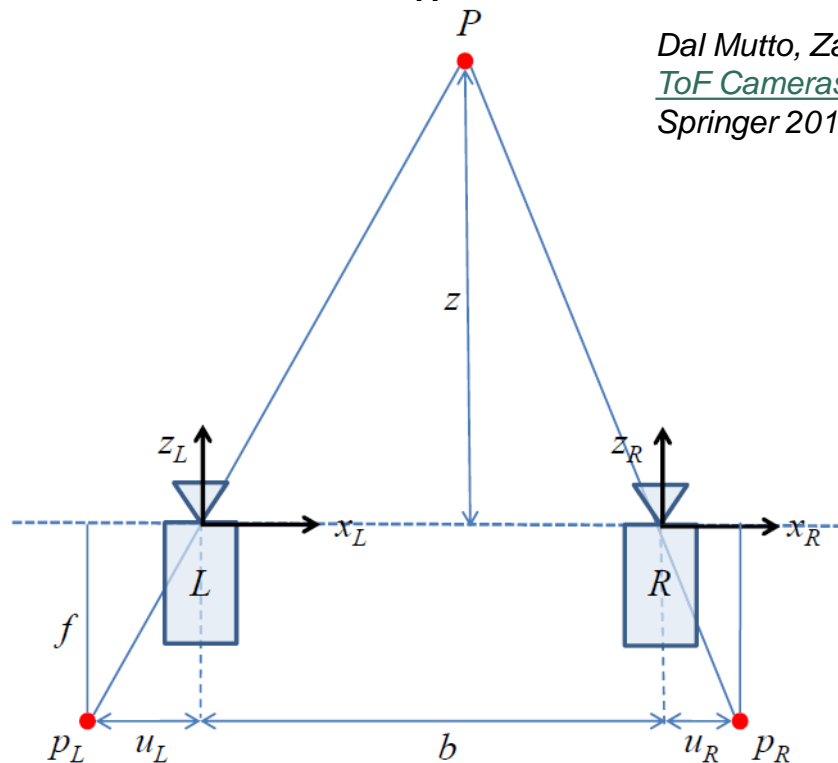
Others: e.g. [faceshift](#)

Kinect: depth imaging principles

- **Active** triangulation
- **Matricial** arrangement
- Structured light coding
 - Correspondence solving: **codewords**
- Artifacts
- Light coding strategies
 - Kinect pattern
- Practical issues
 - Calibration, artifacts
 - Comparison to other 3D scanning methods
- Demo

Active Triangulation

Stereo Triangulation

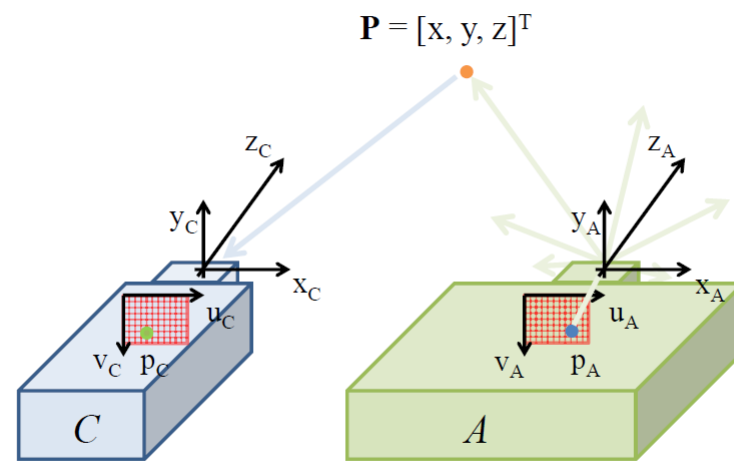


Conjugate pixels: p_L, p_R
 Disparity: $d = u_L - u_R$
 Depth: $z = bf/d$

(calibrated and rectified)

Dal Mutto, Zanuttigh, Cortelazzo
ToF Cameras and MS Kinect
 Springer 2012

Active Triangulation



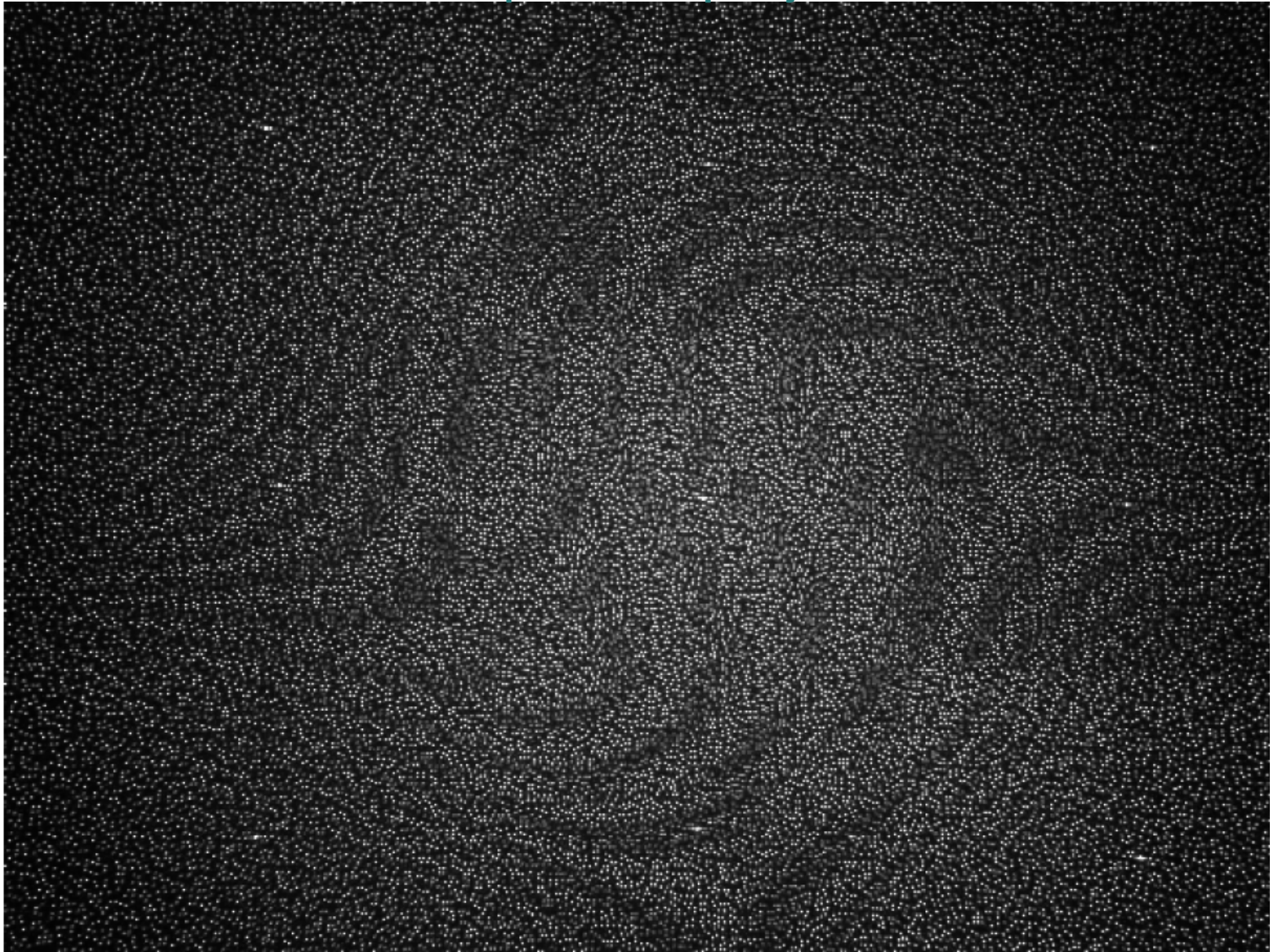
Same geometry:

camera (R) replaced by projector (A)
 p_A pattern pixel, p_C camera pixel
 p_A, p_C are conjugate \rightarrow disparity d

Depth of scene point P: $z = bf/d$

(calibrated and rectified)

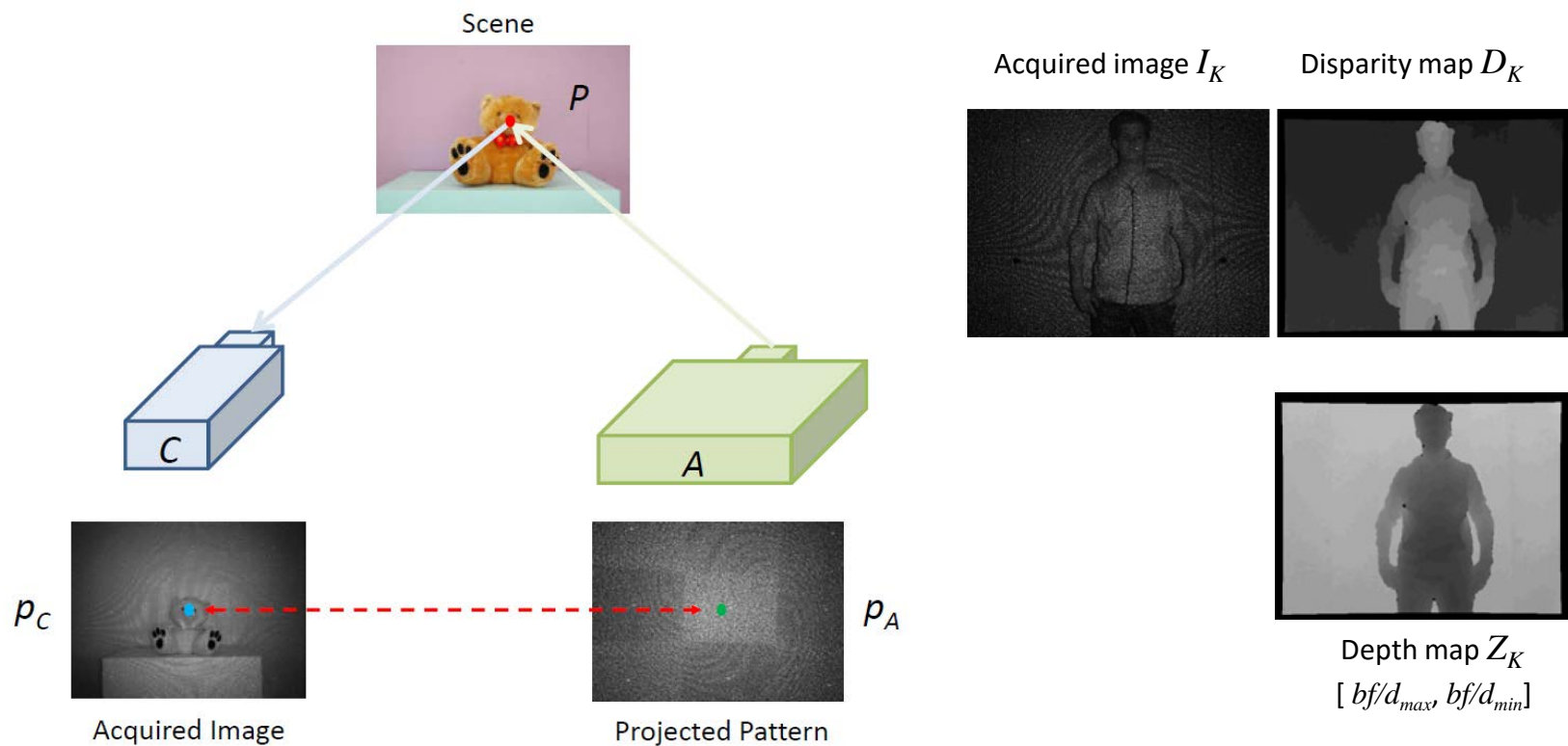
Kinect pattern projected



(from Dal Mutto, et al 2012)

Matricial Active Triangulation

IR Projector and camera (invisible)



(from Dal Mutto, et al 2012)

Structured light coding



- Solves the correspondence problem
 - Each pixel of the pattern is associated to a *codeword* (specific local configuration of the projected pattern)
 - The pattern is projected (A), reflected in scene and captured (R)
 - A *correspondence estimation* algorithm analyzes the received codewords in the acquired image (I_K) in order to compute the conjugate of each projected pattern
 - Pattern design adopts *codewords effectively decodable* in presence of non-idealities of the projection/acquisition process

Decodable codewords

The projection/acquisition process introduces an horizontal shift d (disparity) proportional to the inverse of the depth z of scene point P for each pixel p_A which is associated to a codeword (window centered at p_A).

Codewords should be:

- Different enough: low cardinality!
- Row-separable

In calibrated & rectified setups conjugate points lie in horizontal lines

- The more the local pattern distribution of a single pixel differs from the local pattern distribution of other pixels of the same row, the more **robust** will be the coding
- Local distribution of the pattern for pixel p_A given by the illumination values of the pixels in a window around p_A
- For windows n_W pixels, there are $n_p^{n_W}$ possible pattern configurations
 $n_p = 2^8$ for an 8-bit grayscale projector

Codeword artifacts

Artifacts in the projection acquisition process:

- **Perspective** distortion, due to varying depths in scene
- **Color** (gray level) distortion, due to reflectivity properties of objects
- **External illumination**, due to other light sources in the scene (IR noise)
- **Occlusions**, not all pixels projected will be seen by the camera
- Projector and camera **non-idealities** (non-linear characteristics)
- Projector and camera **noise** (Gaussian, additive)

Light coding strategies

- Direct coding
 - unique pattern value at every pixel $\rightarrow n_p$ codewords
 - A: able to deal with occlusions and perspective distortion
 - D: sensitive to color/gray distortion, noise and camera non-idealities
- Time multiplexing
 - sequence of T values projected/measured T times $\rightarrow n_p^T$ codewords
 - A: similar direct coding, but more robust against noise
 - D: need some integration time: not suited to dynamic scenes
- Spatial multiplexing \rightarrow **Kinect sensor (PrimeSense)**
 - spatial distribution in n_W pixels window around $p_A \rightarrow n_p^{n_W}$ codewords
 - A: can handle color/gray distortion, reflectivity, illumination, noise
 - B: worse with occlusion and perspective distortion
 - \rightarrow smaller n_W , more robust to perspective, but less to noise, color/gray distortion

Lidar

Surveying method/Measurement technique:

Pulser laser light illuminates an object, the reflected pulses are recovered and measured with a solid-state sensor

Time elapsed provides an automated measurement of distance to target (concept also referred to as ladar or ToF imaging)

Popular applications:

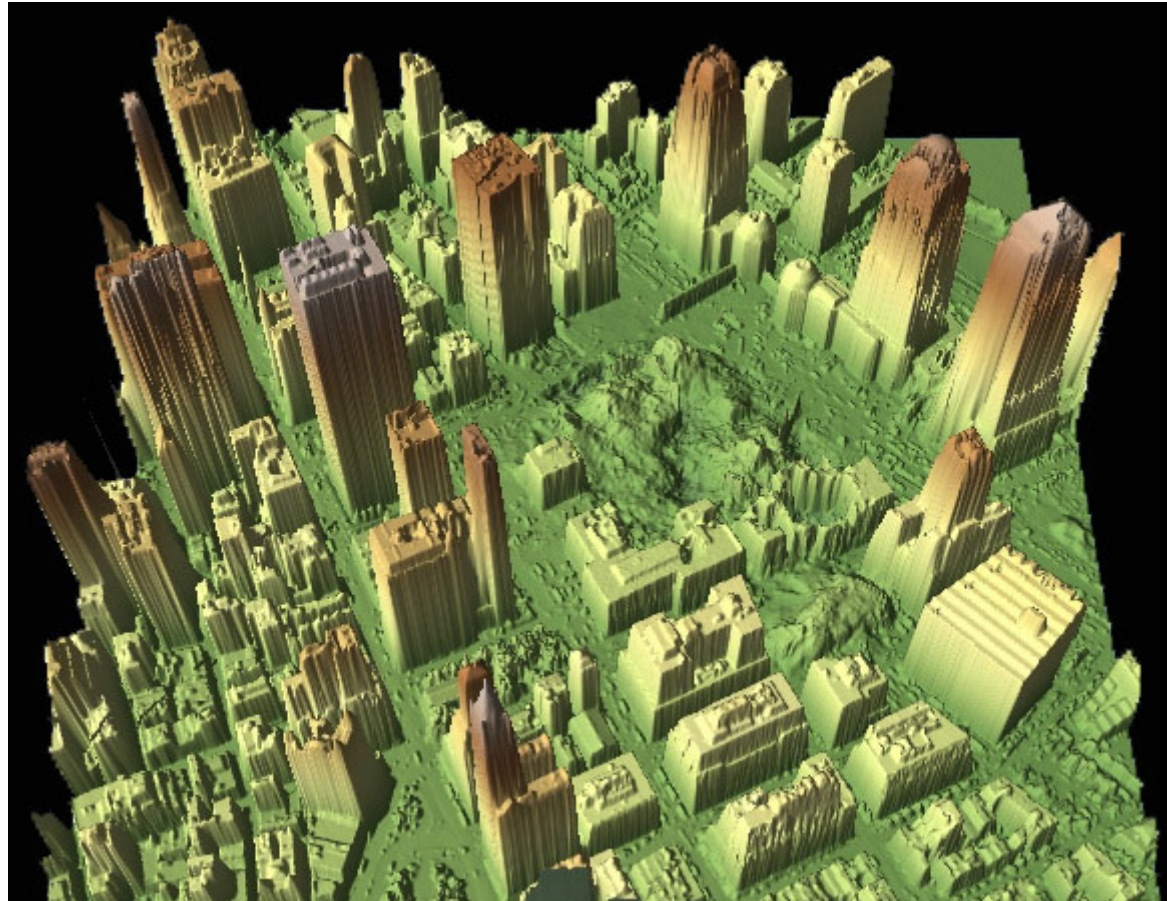
Earth resources exploration, landing aids, object recognition, self-guided vehicles and safety and security applications in transport

The Marching Bear Mound Group in High Definition LIDAR



LIDAR light detection and ranging scanner

<http://www.youtube.com/watch?v=MuwQTc8KK44>



Leica
lidar

<http://hodcivil.edublogs.org/2011/11/06/lidar-%E2%80%93-light-detection-and-ranging/>

http://commons.wikimedia.org/wiki/File:Lidar_P1270901.jpg

FARO scanners



HOW THE LASER SCANNER WORKS

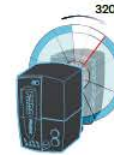
Data capture

USES A LASER BEAM for measuring large areas. The beam is reflected back to the Scanner by the objects in its path. The data is captured and transmitted via WLAN for calculating precise 3D renderings of the area.



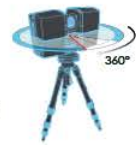
Vertical Rotation

DISTRIBUTES THE LASER BEAM, enabling the Scanner to capture an angular range of 320°. Illustration below shows the 40° blind spot at the base of the device.



Horizontal Rotation

THIS LASER SCANNER REVOLVES the full 360° around its horizontal axis when operating. The distance to the objects defining an area is calculated, as well as their relative vertical and horizontal angles in producing a 3D rendering.



Laser Scanner

KEY FEATURES



Optical Measurement

THE INTELLIGENT LASER SYSTEM facilitates remote measurements of large areas with an extraordinary accuracy of up to 2mm.



Resolution

THE LASER CAPTURES up to 976,000 measurement points per second, and renders a 3D image with an extremely high resolution of up to 711 million pixels per scan.



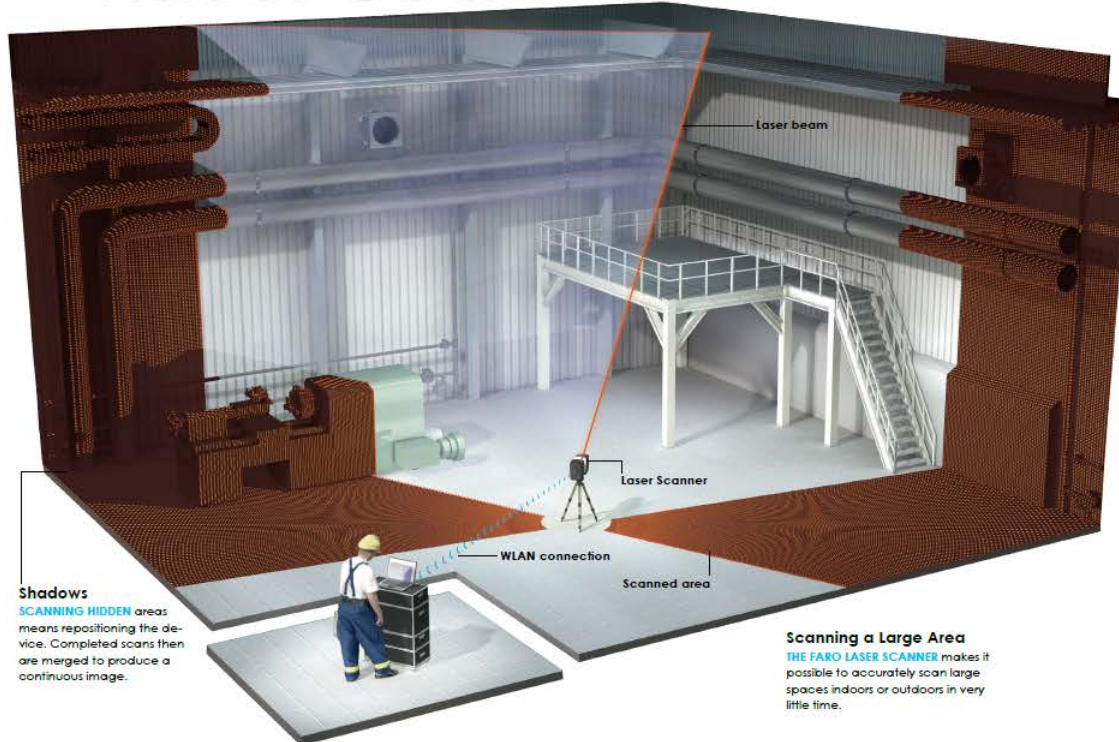
Measuring Volume

SPHERICAL MEASUREMENT VOLUMES with a radius of up to 120 metres can be made indoors or outdoors. Anything from 60cm away can be measured.



Portability

WEIGHING ONLY 14.5 KILOS the laser scanner is easy to transport. The battery provides power for more than 6 hours of continuous operation.



Shadows

SCANNING HIDDEN areas means repositioning the device. Completed scans then are merged to produce a continuous image.

SCANS LARGE OBJECTS TOO

A statue rendered as a "point cloud"



A POINT CLOUD is a data file representing the surface of a scanned object or space. It is created as a 3D image through a set of vertices measured by the Laser Scanner.

Scanning a Large Area

THE FARO LASER SCANNER makes it possible to accurately scan large spaces indoors or outdoors in very little time.

Facts and figures

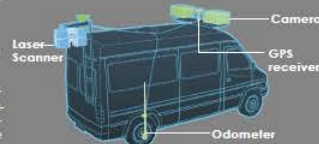
RANGE	0.6m - 20m (Photon 20) 0.6m - 120m (Photon 120)
MEASUREMENT SPEED	976 000 points/second
WEIGHT	14.5kg (31.7lb)
VERTICAL VIEW	320° vertical
HORIZONTAL VIEW	360° horizontal
SCAN TIME	at 20 million points approx. 30 seconds
AMBIENT TEMPERATURE	5° - 40°C

SCANNER CONTROL via ethernet cable or WLAN using PC or iPad Touch within a local network or Internet.

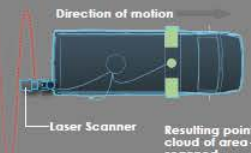
APPLICATIONS Mining, geology, heritage, architecture, petrochemistry, aerospace, automobile manufacturing, ship building and forensics

How to scan a road

ACCURATE SCANNING of roads, alleys, railways and tunnels are useful for creating construction plans. The laser scanner can be mounted on a vehicle to produce 3D images of site locations in full colour. A combination of four devices is required. The Scanner is first mounted on a vehicle. Digital cameras produce a stream of images of the environment every three meters as the vehicle moves along.



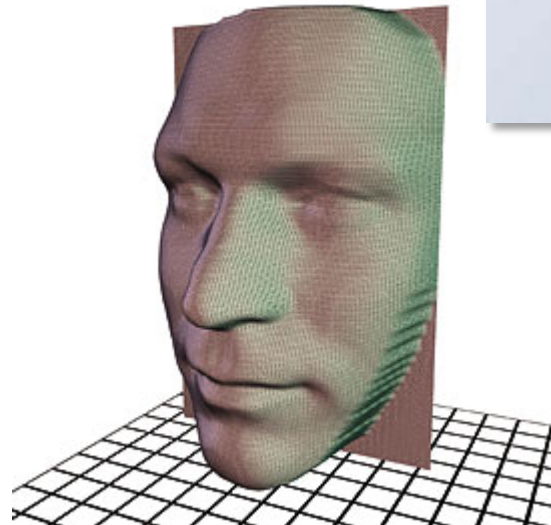
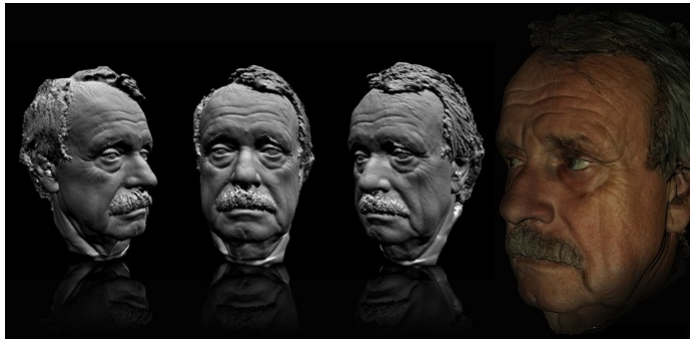
An odometer records the distance the vehicle travels as its coordinates moving through space are tracked and captured simultaneously via a GPS receiver. This data is then collated and stored by an on-board computer, and processed later by the Laser Scanner software.



Applications of 3D scanners

- Industrial design “CAD/CAM”.
- Orthotics and Prosthetics
- Entertainment industry: production of movies and video games
- Reverse engineering
- Inspection and documentation of cultural artifacts

E.g. Metrology (QC): nub3d.com, [FARO](http://FARO.com)
Face scanners



Comparison chart

Technology	Outdoor	Detection range [m]	Accuracy [cm]	FOV	Angular resolution	Obst Det. Terr Mapp.
HD-LIDAR	✓	120	4	27°V 360°H	0.4°V 0.09°H	Not included
Multi-Plane LIDAR	✓	120	10	3°V 85°H	0.8°V 0.125°H	OD, external unit
Kinect	✗	4-5	Up to 0.2	43°V 57°H	0.09°V 0.09°H	Not included
3DV	✓	Up to 40	Variable	32-50°V 40-65°H	0.06°V 0.06°H	OD+TM, plugins

3DV VisLab.it ([video](#))

Motto and fundamental questions

Motto:

Computer Vision = “Teaching computers to see”



Antonio Torralba (MIT)

Talk@CVC 20th Anniversary, Barcelona July 9th, 2015

*Exciting time for CV: new architectures, DBs, productivization, future
Fundamental problems: **reconstruct 3D world**, recognize...*

Questions around this:

*Q1: Is “**projective vision**” a natural way to capture the 3D world?*

*Q2: Do we need **photometry** to get **geometry**?*

*Q3: Does **3D vision** mean the same than **3D geometry**?*

*Q4: Does 2D/3D matter for “**Teaching computers to see**”?*

References (3D sensors)

[Bhandari 2016] A. Bhandari, R. Raskar, **Signal processing for TOF imaging sensors: An introduction to inverse problems in computational 3-D imaging**, IEEE SPM 33(5), 2012

[Bishop 2012] E. Bishop, P. Favaro: **The Light Field Camera: Extended Depth of Field, Aliasing, and Superresolution**. IEEE PAMI 34(5), 2012

[Mutto 2012] C. Dal Mutto, P. Zanuttigh, and G.M. Cortelazzo, **Time-of-flight Cameras and Microsoft Kinect**, *Springerbriefs*, Springer, 2012

[Foix 2011] S. Foix et al, **Lock-in Time-of-Flight (ToF) Cameras: A Survey**, IEEE Sensors 11(9), 2011

[Salvi 2010] J. Salvi et al, **A state of the art in structured light patterns for surface profilometry**, Pattern Recognition 43(8), 2010

[Smisek 2011] J. Smisek, et al, **3D with Kinect**, *ICCV Workshops* 2011

[Xiong 2017] Z. Xiong, et al, **Computational Depth Sensing : Toward high-performance commodity depth cameras**, IEEE SPM 34(3), 2017

[Zhang 2012] Z. Zhang, **Microsoft Kinect Sensor and Its Effect**, *IEEE Multim* 19(2), 2012

Websites: www.openni.org, openkinect.org, www.primesense.com, kinecthacks.net

References (pointclouds, processing and meshes)

[Izadi et al 2011] S. Izadi et al, KinectFusion: **Real-time 3D Reconstruction and Interaction Using a Moving Depth Camera**, *ACM Symposium on User Interface Software and Technology*, October 2011

[Kazhdan 2006] M. Kazhdan 2006, **Poisson Surface Reconstruction**, research.microsoft.com/en-us/um/people/hoppe/proj/poissonrecon

[Meshlab] Visual Computing Lab CNR (it), **Meshlab**, meshlab.sourceforge.net, [tutorials](#)

[Newcombe et al 2011] **KinectFusion: Real-Time Dense Surface Mapping and Tracking**, *IEEE ISMAR*, October 2011

[PCL] PointClouds.org, **PCL and tutorials**, pointclouds.org/documentation

[OpenMesh] OpenMesh.org, **OpenMesh**, www.openmesh.org

[Rusu 2009] R. B. Rusu, **Semantic 3D Object Maps for Everyday Manipulation in Human Living Environments**, Technische Universität München, **PhD 2009**

[Salvador et al 2011] J. Salvador and J. Casas, **Multi-View Video Representation Based on Fast Monte Carlo Surface Reconstruction**, *IEEE Trans. IP* 22 (9) 2013

Complete courses

- Poisson Surface Reconstruction
research.microsoft.com/en-us/um/people/hoppe/proj/poissonrecon
- Digital Geometry Processing, Technion
webcourse.cs.technion.ac.il/236329/Spring2013
- VCGlib and Meshlab
vcg.isti.cnr.it/vcglib, Visual Computing Lab CNR (it) [course](#)
meshlab.sourceforge.net, [tutorials](#)
- PCL and tutorials
pointclouds.org/documentation
- OpenMesh
www.openmesh.org

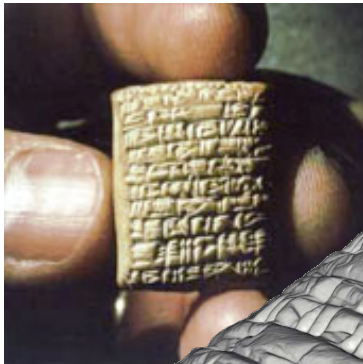
What to do with the results?

MESHING

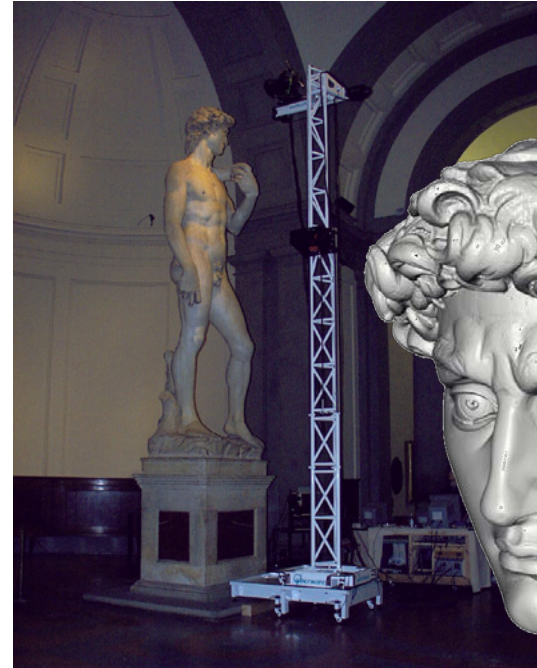
Motivation for meshing

In many domains, scanners are used to obtain virtual representations of 3D shapes

<http://www.jhu.edu/digitalhammurabi/>



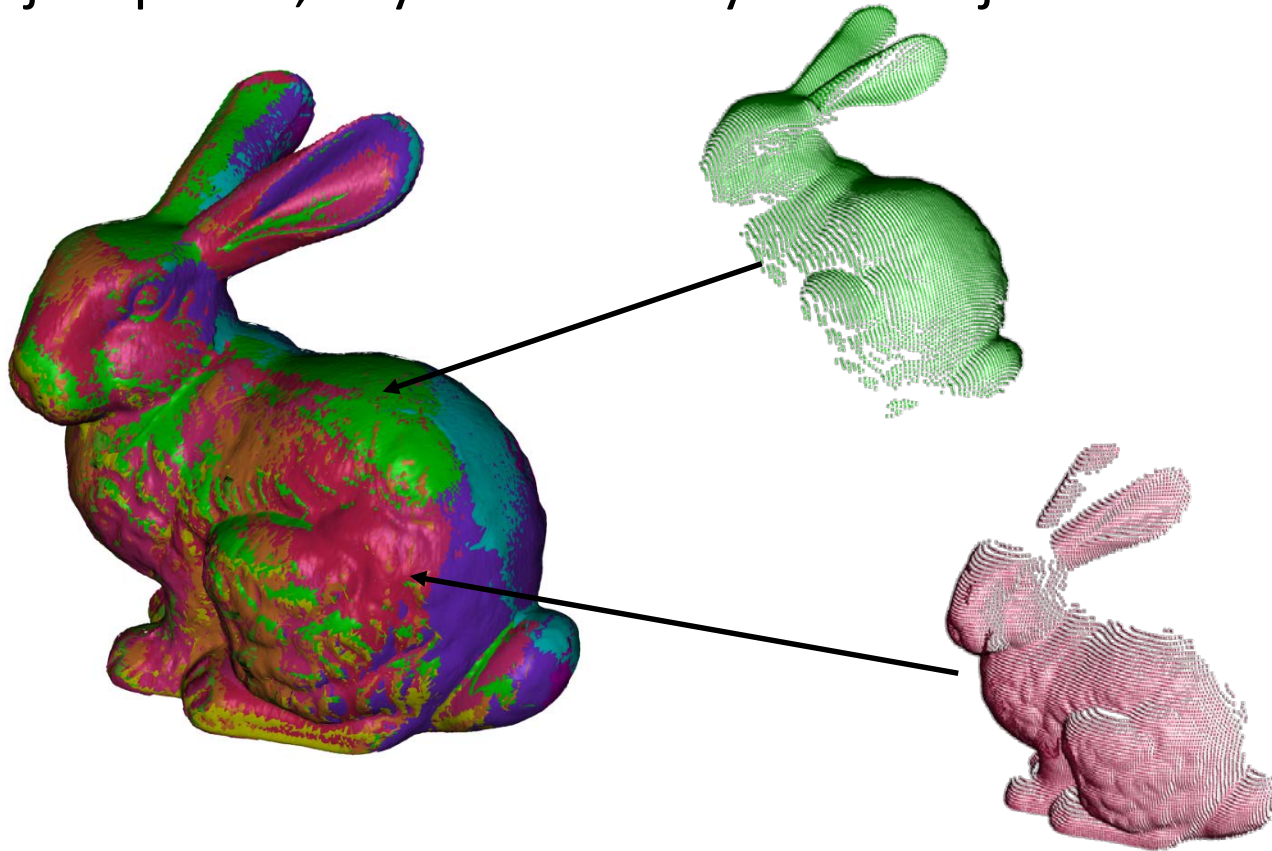
<http://graphics.stanford.edu/projects/mich/>



Scanner results

Scanning often gives only **local connectivity**...

...or even just points, any connectivity at all → just a **PointCloud**!



but yet... There is some motivation for meshing

We want a 3D Mesh for:

- Parameterization
- Computational Analysis
- Rapid Prototyping
- Rendering
- Collision Detection

Meshing

Mesh

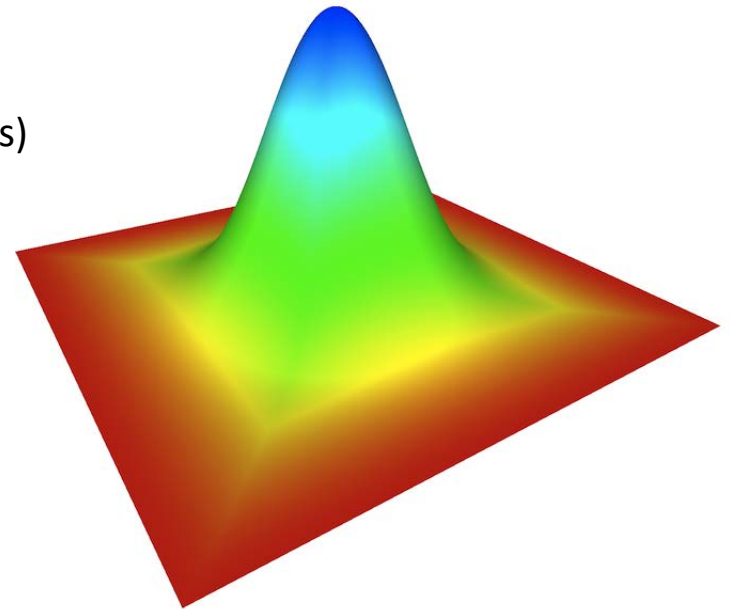
Defines an ordering of the surface points (vertices) for interpolating a continuous surface in intermediate positions

Strategy

Greedy contour propagation under a set of rules for topological correctness

Implementation

Efficient 3D spatial queries of neighbor points via *kd-tree* applied iteratively for processing disconnected sets of points



Surface Reconstruction

M. Kazhdan *Johns Hopkins Univ. Poisson Reconstruction Eurographics 2006*

Generate a mesh from a set of surface samples



Surface Reconstruction

Generate a mesh from a set of surface samples

- Three general approaches:

1. Computational Geometry

Boissonnat, 1984
Amenta *et al.*, 1998

Edelsbrunner, 1984
Dey *et al.*, 2003

2. Surface Fitting

Terzopoulos *et al.*, 1991

Chen *et al.*, 1995

3. Implicit Function Fitting

Hoppe *et al.*, 1992
Whitaker, 1998
Davis *et al.*, 2002
Turk *et al.*, 2004
Kazhdan, 2005

Curless *et al.*, 1996
Carr *et al.*, 2001
Ohtake *et al.*, 2004
Shen *et al.*, 2004

Meshing benchmark

- RMS *Hausdorff* distance between two non-empty subsets X and Y of a metric space (M, d) , with d the Euclidean distance in 3D space:

$$d_H(X, Y) = \sqrt{\frac{1}{N} \sum_{x \in X} \left\| \inf_{y \in Y} d(x, y) \right\|^2}$$

- Computation time
- Memory footprint