Experimental loss in purity vs. Logical rotation angle β cluster state with $\phi = \frac{\pi}{4}$ NNN-XX rotation

