String order parameter vs. Distance d between endpoints, cluster state with  $\phi = \frac{\pi}{4}$  NNN XX-rotation

