

Here, $\text{PRIMES}(P) = \{m \mid m \text{ is a prime number in binary}\} \in \text{NP}$ can be proved by the following approach.

Now, consider two situations:

1. Consider a situation where $p > 1$: (Because all prime numbers are greater than 1).
2. The multiplicative group $Z_p^* = \{x \mid x \text{ is relatively prime to } p \text{ and } 1 \leq x \leq p\}$.

Here, a situation is considered where x is a relative prime number the value of x lies between 0 and 1.

- Both conditions are cyclic as the both situations can be combined and can lie between 1 and p .
- **Order of these conditions is $p-1$ if p is prime as the range lies between 1 and p then the order between $p-1$. This fact is alone sufficient to prove the statement $\text{PRIMES}(P) = \{m \mid m \text{ is a prime number in binary}\} \in \text{NP}$ and second considered situation are quite enough itself to justify the statement.**
- It can be proved by **the fact of belonging of prime numbers to co-NP and consider prime numbers belong to co-RP .**
- **Thus, required statement will be true as well, because belongingness of NP can be proved only if belongs to co-NP and co-RP as well.**

This it is quite obvious that, $\text{PRIMES}(P) = \{m \mid m \text{ is a prime number in binary}\} \in \text{NP}$.