

Given Grammar G_4 is

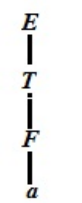
$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T \times F \mid F \\ F &\rightarrow (E) \mid a \end{aligned}$$

Derivation: The sequence of substitutions to obtain a string is called a *derivation*.

Parse Tree: The pictorial representation of derivation of a string is a *parse tree*.

a)

The parse tree to generate string a is as follows:

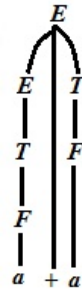


The derivation for the string a is as follows:

$$\begin{aligned} E &\Rightarrow T \\ T &\Rightarrow F \\ F &\Rightarrow a \end{aligned}$$

b)

The parse tree to generate string $a + a$ is as follows:

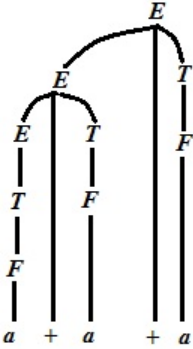


The derivation for the string $a + a$ is as follows:

$$\begin{aligned} E &\Rightarrow E + T \\ E &\Rightarrow T + T \\ E &\Rightarrow F + T \\ E &\Rightarrow a + T \\ E &\Rightarrow a + F \\ E &\Rightarrow a + a \end{aligned}$$

c)

The parse tree to generate string $a + a + a$ is as follows:



The derivation for the string $a + a + a$ is as follows:

$E \Rightarrow E + T$
 $E \Rightarrow E + T + T$
 $E \Rightarrow T + T + T$
 $E \Rightarrow F + T + T$
 $E \Rightarrow a + T + T$
 $E \Rightarrow a + F + T$
 $E \Rightarrow a + a + T$
 $E \Rightarrow a + a + F$
 $E \Rightarrow a + a + a$

d)

The parse tree to generate string $((a))$ is as follows:

E
|
 T
|
 F
|
 (E)
|
 (T)
|
 (F)
|
 $((E))$
|
 $((T))$
|
 $((F))$
|
 $((a))$

The derivation for the string $((a))$ is as follows:

$E \Rightarrow T$
 $E \Rightarrow F$
 $E \Rightarrow (E)$
 $E \Rightarrow (T)$
 $E \Rightarrow (F)$
 $E \Rightarrow ((E))$
 $E \Rightarrow ((T))$
 $E \Rightarrow ((F))$
 $E \Rightarrow ((a))$