

## 获得的答案

Given that

$$A_{TM}' = \{ \langle M, w \rangle \mid M \text{ is an oracle TM (turing machine) and } M^{A_{TM}'} \text{ accepts } w \}$$

We have to show that  $A_{TM}'$  is undecidable relative to  $A_{TM}$ .

Take a contradiction of  $A_{TM}'$  is decidable relative to  $A_{TM}$ .

Hence there exists an oracle TM  $T$  with oracle access to  $A_{TM}$  which decides  $A_{TM}'$ .

Now we construct another oracle TM  $N$  as follows:

$N =$  "on input

1. Run  $T^{A_{TM}}$  on input  $\langle \rangle$

2. If  $T$  accepts, *reject*.

3. Else if  $T$  rejects, *accept*".

• So  $N^{A_{TM}}$  accepts if and only if  $M$  rejects.

• When the input of  $N$  is  $\langle N \rangle$ , we have  $N^{A_{TM}}$  accepts  $\langle N \rangle$  if and only if  $N$  rejects  $\langle N \rangle$ .

This is a contradiction to our hypothesis, that  $A_{TM}'$  is decidable relative to  $A_{TM}$  is wrong. Hence,  $A_{TM}'$  is un-decidable relative to  $A_{TM}$ .