

Cook – Levin theorem:

*SAT* is *NP–Complete*. This theorem restates that  $SAT \in P$  iff  $P = NP$ .

- In the proof of the Cook-Levin theorem, a window size to be a  $2 \times 3$  rectangle of cells.
- If we had used  $2 \times 2$  windows that we can only use  $2 \times 2$  sub windows of the ones, obtained by deleting the leftmost or the rightmost column.
- Legal window  $2 \times 3$  is as follows.

$a$	$q_1$	$b$
$q_2$	$a$	$c$

- In the window of figure (head move left), the right two columns allow the head to move left.
- The left two columns allow the head to move left into a state  $q_2$ , but this state is no longer restricted by what symbol was scanned by the head.
- So if there is some state  $q_2$  into which it is possible to move while moving left, this window allows switching into this state on any left move.
- This will allow typically many tableaux (and so many satisfying assignments) that do not correspond to computations of our nondeterministic Turing machine.