获得的答案

Pumping Lemma:

If A is regular language, there is a number \mathbf{p} (the pumping length) where S is any string in A of length at least P, then S may be divided into three pieces, S = xyz, satisfying the following conditions.

- 1. For each $i \ge 0$, $xy^i z \in A$
- 2. |y| > 0, and
- 3. $|xy| \le p$

(a)

Consider the language, $A_1 = \{0^n 1^n 2^n \mid n \ge 0\}$.

Assume $A_{\mathbf{l}}$ is a regular language.

Let p be the pumping length given by the pumping lemma consider a string $S = 0^p 1^p 2^p \in A_1$

|S| > Pso, by pumping lemma, take $S = 0^p 1^p 2^p = xyz$ such that $|xy| \le p, |y| > 0$ consider the following 2 possibilities:

Let 001122 be the string that belongs to A_1 . $S = 0^p 1^p 2^p = 001122$. The pumping length of the string is 2. To satisfy the conditions of the pumping lemma, x = 0, y = 0, z = 1122.

$$S = 001122$$

$$= \frac{0}{x} \frac{0}{v} \frac{1122}{z}$$

Pump the middle part such that xy^iz $(i \ge 0)$. For i=2, the y becomes 00. The string after pumping is 0001122.

$$S = (0) (0)^{i} (1122)$$

$$= \frac{0}{x} \frac{00}{y} \frac{1122}{z}$$
 [when $i = 2$]

The string $0001122 \notin A_1$ because the string that is accepted by the language should have equal number of 0's, 1's and 2's. It is a contradiction. So, the pumping lemma is violated.

Therefore, A_{l} is not a regular language.

(b)

Consider the language, $A_2 = \{www \mid w \in \{a, b\}^*\}$.

Assume A_2 is a regular language.

Let p be the pumping length given by the pumping lemma.

Consider a string $S = a^p b a^p b a^p b \in A_2$.

By pumping lemma, this string can be divided into three pieces xyz such that $|xy| \le p, |y| > 0$ and $xy^tz \in A_2 \forall i \ge 0$

So
$$S = a^p b a^p b a^p b = xyz$$
.

Let aabaabaab be the string that belongs to A_2 . The pumping length of the string is 2. To satisfy the conditions of the pumping lemma, x = a, y = a, z = baabaab.

$$S = aabaabaab$$

$$=\frac{a}{r}\frac{a}{v}\frac{baabaab}{r}$$

Pump the middle part such that xy^iz $(i \ge 0)$. For i=2, the y becomes aa. The string after pumping is aaabaabaab.

https://www.512218.cn

The string $aaabaabaab \notin A_2$ It is a contradiction. So, the pumping lemma is violated.

Therefore, A_2 is not a regular language.

(c)

Consider the language, $A_3 = \left\{a^{2^n} \mid n \ge 0\right\}$ (Here, a^{2^n} means a string of 2^n a's).

Assume that A_3 is regular language.

Let p be the pumping length given by pumping lemma consider a string $S = a^{2^p} \in A_3$. And |S| > p

By pumping lemma, this string can be divided into three pieces xyz such that $|xy| \le p, |y| > 0$ and $xy^iz \in A_2 \forall i \ge 0$

Let aaaa be the string that belongs to A_3 . The pumping length of the string is 2. To satisfy the conditions of the pumping lemma, x = a, y = a, z = aa.

$$S = aaaa$$

$$= \frac{a}{x} \frac{a}{y} \frac{aa}{z}$$

Pump the middle part such that xy^iz $(i \ge 0)$. For i=2, the y becomes aa. The string after pumping is aaaaa.

$$S = (a) (a)^{i} (aa)$$
$$= \frac{a}{x} \frac{aa}{v} \frac{aa}{z} [when i = 2]$$

The string $aaaaa \notin A_3$. It is a contradiction. So, the pumping lemma is violated.

Therefore, A_3 is not a regular language.

2/2

https://www.512218.cn