

获得的答案

Assumption: is a 3CNF formula.

ϕ is a clause that contains two literals with unequal truth values of an \neq - assignment to the variable.

CNF is Conjunctive Normal Form. It has the following rules:

- A literal is Boolean variable or negated Boolean variable in the form.
- Boolean formula is in CNF called a CNF formula.
- If all clauses have three literals, then it is called 3cnf formula.
- Clause contains several literals connected with \vee s and \wedge s.
- Each clause has at least one satisfied literal and one unsatisfied literal in \neq - assignment to ϕ .
- The negation of an \neq - assignment conserve this property.
- Hence, negation of any \neq - to ϕ is also an \neq - assignment.

b)

To show: The formula ϕ is mapped to ϕ' then ϕ is satisfiable if ϕ' has an \neq - assignment.

Assumption: \neq SAT is the collection of 3cnf formulas that have an \neq - assignment.

- Obtain a polynomial time reduction from 3SAT to \neq - SAT by replacing each close c_i of the form $(y_1 \vee y_2 \vee y_3)$ with the two clause $(y_1 \vee y_2 \vee z_i)$ and $(\bar{z}_i \vee y_3 \vee b)$

Where

- z_i is a new variable for each clause c_i
- b is a single additional new variable.

It is known that $SAT = \{(\phi) \mid \phi \text{ is a boolean formula}\}$

- Let ϕ and ϕ' are 3 CNF formulas of input and reduction on input ϕ and ϕ' as output.
- We must prove $\phi \in 3-SAT \Leftrightarrow \phi' \in \neq SAT$ therefore the reduction is correct.

Suppose that $\phi \in 3-SAT$

- ϕ is satisfiable.
- 1 is true and 0 is false. We get an \neq - assignment to ϕ' by extending a satisfying assignment to ϕ in such a way that we assign 1 to $\phi' \in k \neq SAT$.
- Else if both literals y_1 and y_2 are clauses c_i are unsatisfied, else we assign 0 to z_i .
- Finally, we assign 0 to b.
- Extended assignment satisfies ϕ' and it is an \neq - assignment to ϕ' .

Therefore, $\boxed{\phi' \in \neq SAT}$

Suppose that $\phi' \in k \neq SAT$

- \neq has an \neq - assignment

Satisfying assignment to ϕ as follows:

- From part(a) we obtain \neq - assignment assigns 0 to b, otherwise simply negate the assignment.
- This \neq - assignment cannot assign 0 to all y_1, y_2 and y_3 as doing so would force one of the two clauses, $(y_1 \vee y_2 \vee z_i)$ and $(\bar{z}_i \vee y_3 \vee b)$, to have all 0's

- Hence restricting this assignment to the variables of ϕ yields a satisfying assignment to ϕ .

Therefore, 3SAT is polynomial time reducible to \neq SAT

(c)

NP-COMPLETE: A language B is NP-complete if it satisfies two conditions

- B is in NP
- Every A in NP is polynomial time reducible to B.

$\neq SAT \in NP$, as it is easy to verify whether an assignment is an \neq – assignment.

Part(b) also proved $3SAT \leq_p \neq SAT$, $\neq SAT$ is NP-complete.