

## 获得的答案

Given language is

"The set of strings over the alphabet  $\{a, b\}$  with more  $a$ 's than  $b$ 's"

The context – free grammar generating the given language is

$$\begin{aligned} S &\rightarrow Aa \mid BS \mid SBA \\ A &\rightarrow Aa \mid \epsilon \\ B &\rightarrow \epsilon \mid BB \mid bBa \mid aBb \end{aligned}$$

In the above grammar  $S$  will generate all strings with as many  $a$ 's as  $b$ 's.  $R$  Forces an extra  $a$  which gives the required strings of the language.

Given language is

"The compliment of the language  $\{a^n b^n : n \geq 0\}$ "

Let  $L$  be the language that is a compliment of given language.  $L$  can be obtained as  $L = \{a^n b^m : n \neq m\} \cup \{(a \cup b)^* ba(a \cup b)^*\}$

Let us consider

$$\begin{aligned} L_1 &= \{a^n b^m : n \neq m\} \\ L_2 &= \{(a \cup b)^* ba(a \cup b)^*\} \end{aligned}$$

The context – free grammar generating the language  $L_1$  is

$$\begin{aligned} S_1 &\rightarrow aS_1b \mid T \mid U \\ T &\rightarrow aT \mid a \\ U &\rightarrow Ub \mid a \end{aligned}$$

The context – free grammar generating the language  $L_2$  is

$$\begin{aligned} S_2 &\rightarrow RbaR \\ R &\rightarrow RR \mid a \mid b \mid \epsilon \end{aligned}$$

Therefore, the required context – free grammar generating the language  $L$  is given by

$$\begin{aligned} L &= L_1 \cup L_2 \\ S &\rightarrow S_1 \mid S_2 \\ S_1 &\rightarrow aS_1b \mid T \mid U \\ S_2 &\rightarrow RbaR \\ T &\rightarrow aT \mid a \\ U &\rightarrow Ub \mid a \\ R &\rightarrow RR \mid a \mid b \mid \epsilon \end{aligned}$$

Given language is

$$\{w \# x : w^R \text{ is a substring of } x \text{ for } w, x \in \{0, 1\}^*\}$$

The context – free grammar generating the given language is

$$\begin{aligned} R &\rightarrow SX \\ S &\rightarrow 0S0 \mid 1S1 \mid \#X \\ X &\rightarrow XX \mid 1 \mid 0 \mid \epsilon \end{aligned}$$

The nonterminal  $S$  ends only with  $\#X$ ,  $S$  must generate a string whose beginning and end are mirror images. Since  $X$  generates  $(0 \cup 1)^*$ , the symbol  $S$  generates all strings of the form  $w \# (0 \cup 1)^* w^R$ . The above grammar generates all the substrings of  $x$  for  $w, x \in \{0, 1\}^*$ .

Given language is

$$\{x_1 \# x_2 \# \dots \# x_k \mid k \geq 1, \text{ each } x_i \in \{a, b\}^*, \text{ and for some } i \text{ and } j, x_i = x_j^R\}$$

浙ICP备16034203号-2

The context – free grammar generating the given language is

$$R \rightarrow S | J \# S \# J | J \# S | S \# J$$

$$S \rightarrow aSa | bSb | \# | \# J \#$$

$$J \rightarrow aJ | bJ | \# J | \varepsilon$$

The strings in the language contain matching pair of strings with at least one # between them. Before, after and between the matching pairs there can be any number of strings of ***a*'s and *b*'s** separated by #. Because the strings can be of any length, the stretch of the strings of ***a*'s, *b*'s and #s** can be of any length. The symbol ***S*** generates a matching pair, with strings of ***a*'s, *b*'s and #s** optionally inserted in the middle. The symbol ***J*** generates strings of ***a*'s, *b*'s and #s**. The string generated by ***J*** may start or end with ***a* or *b***, so rules for ***M* and *S*** must ensure that the symbol ***J*** is always separated properly from the two matching strings.