a)

The **Resolution** is defined as "it is proof procedure which uses **refutation**". In other words, "it can be defined as a formula which is used to proof that a formula is unsatisfiable by deriving \bot from the formula". Resolution shows both of the behavior, that is, complete and sound.

- The Resolution is said to be sound if satisfiable formula can never be declared unsatisfiable by it.
- The Resolution is said to be complete if all the unsatisfiable formulas are declared to be unsatisfiable.

Now, consider the lemma which said that" if an application of resolution rule produces a clause H (which is given as $H = H_1 \setminus \{L\} \cup C_2 \setminus \{\neg L\}$) under a valuation Q, then from the conjunction of the hypothesis of the rule, $H_1 \wedge H_2$, is false under Q".

- The above lemma can be proved by assuming H is false under Q, but H₁ ∧ H₂ gives
 true value under Q. It is already given that H₁ shows a disjunction behavior, then one
 of its literals must be possess true under Q.
- All the literals other that L, then it is also exist in H and therefore H show true behavior, that shows a contradiction. Now, if L is taken as a literal then -L will be false under O.
- It is already known that under Q, H₂ is true, then it must consists a literals other than

 —L that shows true behavior under Q. But this show that it is also exists in H and
 therefore H shows a true nature under Q, that is a contradiction.

Thus, it can be said that $H_1 \wedge H_2$ must be false under Q. Now by using the concept of induction, it can be said that a satisfiable formulas can never be declared as unsatisfiable. Therefore, it can be said that Resolution is sound.

The **complete** property of **Resolution** can be proved by using the concept of induction. The induction will be applied on the excess number of literals.

 The excess number of literals in a clause is explained to be the number of literals, except in the clause. That is,

$$excess(H) = \{0if | H | < 2and | H | -1if | H | \ge 2$$

 The number of excess literals in a clause set is just the sum of excess literals in every clause, that is,

$$excess(H) = \sum_{i=1}^{n} excess(H_i)$$

Thus, an induction concept will be applied on the above. Therefore, it can be said that Resolution is complete.

b)

Consider the decidability of 2SAT. It is known that 2SAT is polynomial time decidable. To proof this problem, efficiently a path searches in graphs can be used. A depth search or breadth search algorithm can be used in path search of graphs.

- If there exists an edge between (a,b)then there must be exists a clause similar to (¬a,b) and also there exists a path between (¬b,¬a).
- Now, consider a 2-CNF formula β. This formula is unsatisfiable if and only if
 there exists a variable q in such a way that: "In graph, there exists a path from q to
 -q and also a path from -q to q".
- Now consider there exists a path q..¬q and ¬q..q fro a given variable q, but there exists also an assignment δ fro which δ(q) = T and similarly, δ(q) = F.

Hence, from the above explanation, it can be said that $2SAT \in P$.