

The alphabet  $\Sigma$  is given by  $\{0, 1\}$

(a)

The context free grammar that generates the language

$\{\omega \mid \omega \text{ contains at least three 1s}\}$  is given by

$$S \rightarrow P1P1P1P$$

$$P \rightarrow 0P \mid 1P \mid \varepsilon$$

(b)

The context free grammar that generates the language  $\{\omega \mid \omega \text{ starts and ends with the same symbol}\}$  is given by

$$S \rightarrow 0P0 \mid 1P1 \mid 0 \mid 1$$

$$P \rightarrow 0P \mid 1P \mid \varepsilon$$

(c)

The context free grammar that generates the language

$\{\omega \mid \text{the length of } \omega \text{ is odd}\}$  is given by

$$S \rightarrow 0 \mid 1 \mid 00S \mid 01S \mid 10S \mid 11S$$

(or)

$$S \rightarrow 0 \mid 1 \mid 0S0 \mid 0S1 \mid 1S0 \mid 1S1$$

(d)

The context free grammar that generates the language  $\{\omega \mid \text{the length of } \omega \text{ is odd and its middle symbol is a 0}\}$  is given by

$$S \rightarrow 0 \mid 0S0 \mid 0S1 \mid 1S0 \mid 1S1$$

(e)

The context free grammar that generates the language  $\{\omega \mid \omega = \omega^R, \text{ that is, } \omega \text{ is a palindrome}\}$  is given by

$$S \rightarrow 0 \mid 1 \mid 0S0 \mid 1S1 \mid \varepsilon$$

(f)

The context free grammar that generates the language

$\{ \}$  is given by

$$S \rightarrow S$$