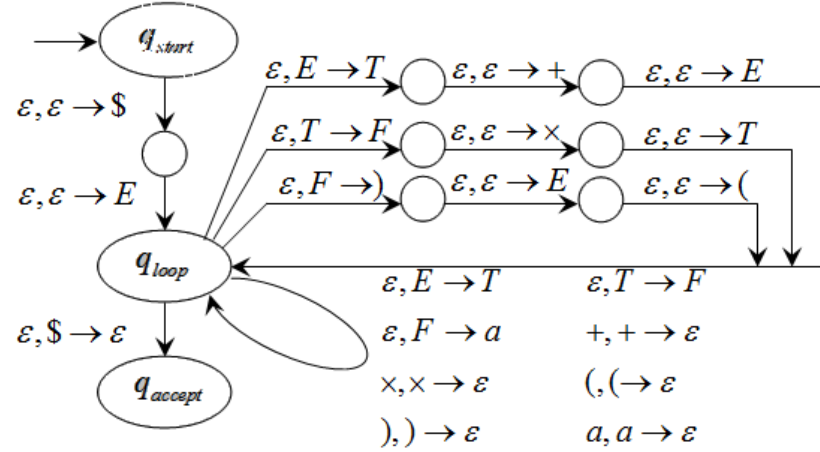


Given CFG (Context-free grammar)  $G_4$  is

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T \times F \mid F \\ F &\rightarrow (E) \mid a \end{aligned}$$

Equivalent PDA for the CFG  $G_4$  is as follows:



#### Explanation:

1. A shorthand notation is used for pushing multiple symbols onto the stack.
2. Initially, at the start variable on the stack a marker symbol '\$' is inserted. The start state is  $q_{start}$ . The transition function is  $\delta(q_{start}, \epsilon, \epsilon) = \{(q_{loop}, S\$)\}$
3. If the stack top is a non-terminal variable E. Select one of the rules of E and substitutes its value on the right hand side of the rule. Repeat this process until the end of the string.

The transition function is  $\delta(q_{loop}, \epsilon, E) = \{(q_{loop}, w) \mid E \rightarrow w \text{ is a rule in CFG}\}$

#### Example:

- Consider the rule  $E \rightarrow E + T$ .
  - Another rule for E is  $E \rightarrow T$ . Substitute the value of E in the above rule.
  - Then, the equation becomes  $E \rightarrow T + T$ .
4. If the stack top is a terminal variable such as (,),a,+ and x the next symbol is read from the input rule. Repeat step-3 if again a non-terminal variable is encountered.

The transition function is  $\delta(q_{loop}, a, a) = \{(q_{loop}, \epsilon)\}$ .

5. If the stack top is a '\$' symbol, the accept state is entered because, the input is read completely.

The transition function is  $\delta(q_{loop}, \epsilon, \$) = \{(q_{accept}, \epsilon)\}$ .