

A binary search tree is built in such a way that the right child must be greater than the parent and the left child must be less than the parent. Therefore, sort a set of numbers by building a binary search tree and print using tree walk (or tree traversing).

The algorithm to sort and print set of numbers using binary search tree is as follows:

TREE-SORT (A)

1. **for** $i = 1$ **to** n

2. TREE-INSERT($T, A[i]$) //let T be an empty binary search tree

3. INORDER-TREE-WALK($T.root$)

TREE-INSERT (T, z)

1. $y = \text{NIL}$

2. $x = T.root$

3. **while** $x \neq \text{NIL}$

4. $y = x$

5. **if** $z.key < x.key$

6. $x = x.left$

7. **else** $x = x.right$

8. $z.p = y$

9. **if** $y = \text{NIL}$

10. $T.root = z$ // tree T was empty

11. **elseif** $z.key < y.key$

12. $y.left = z$

13. **else** $y.right = z$

INORDER-TREE-WALK (x)

1. **if** $x \neq \text{NIL}$

2. INORDER-TREE-WALK ($x.left$)

3. print $x.key$

4. INORDER-TREE-WALK ($x.right$)

Worst case running time analysis for TREE-SORT:

If the linear chain of numbers (numbers in ascending or descending order) is to be inserted, TREE-INSERT takes worst case running time.

That is, in the worst case, TREE-INSERT checks the nodes proportional to height of the tree and inserts a node in $\Theta(n)$ time.

If array A contains 'n' numbers in ascending order or descending order in each iteration of for loop, TREE-INSERT executes in time proportional to height of the tree.

Thus, the for loop executes overall in $(1(1^{\text{st}} \text{ iteration}) + 2(2^{\text{nd}} \text{ iteration}) + \dots + n(n^{\text{th}} \text{ iteration}))$

$$1 + 2 + \dots + n = \frac{n(n+1)}{2} = \frac{n^2 + n}{2} = \Theta(n^2)$$

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Hence, the worst case running time for TREE-SORT is $\Theta(n^2)$.

Best case running time for TREE-SORT:

If the set of nonlinear numbers (numbers neither in ascending nor in descending order) is to be inserted, TREE-INSERT takes best case running time.

That is TREE-INSERT inserts a node in $\Theta(\log n)$ time.

If array A contains 'n' nonlinear numbers, the for loop executes n times and each time TREE-INSERT executes in $\log n$ time. Overall, the for loop executes $n \times \log n$ times.

Hence, the best case running time for TREE-SORT is $\Theta(n \log n)$.