Given the context – free grammar $\emph{\textbf{G}}$ is

$$R \rightarrow XRX \mid S$$

$$S \rightarrow aTb \mid bTa$$

$$T \to XTX \mid X \mid \varepsilon$$

$$X \to a \,|\, b$$

a. The variables of G are R, S, T and X

Variables are the non-terminal symbols that appear in the rules of the grammar.

b. The terminals of G are a,b.

Terminals are the terminal symbols that appear in the rules of the grammar.

c. The start variable of G is R.

$$R \rightarrow XRX \mid S$$

Start variable is a variable usually occurs on the left – hand side of the topmost rule.

d. Case1: Consider the rule $R \rightarrow S$

Substitute S with rule $S \rightarrow aTb$

$R \rightarrow aTb$

Substitute T with rule $T \rightarrow \varepsilon$.

$$R \rightarrow a \in b$$

$$R \rightarrow ab$$

Case2: Consider the rule $R \rightarrow S$

Substitute S with rule $S \rightarrow bTa$

$R \rightarrow bTa$

Substitute T with rule $T \rightarrow \varepsilon$.

$R \to b \in a$

$$R \rightarrow ba$$

Case3: Consider the rule $R \rightarrow S$

Substitute S with rule $S \rightarrow aTb$

$$R \rightarrow aTb$$

Substitute T with rule $T \rightarrow X$.

$R \rightarrow aXb$

Substitute X with rule $X \rightarrow a$.

$R \rightarrow aab$

Therefore, the 3 strings in L(G) are ab, ba and aab.

e. The three strings not in L(G) are aba, b and ε . Since these strings cannot be derived from the given grammar G.

f. False

 $T \Rightarrow aba$, the string cannot be derived using G.

g. True

 $T \stackrel{\bullet}{\Rightarrow} aba'$ the string can be derived using G.

h. False

浙ICP备16034203号-2

 $T \Rightarrow T$, the string cannot be derived using G.

i. True

 $T \stackrel{*}{\Rightarrow} T$, the string can be derived using G.

j. True

 $XXX \Rightarrow aba'$ the string can be derived using G.

k. False

 $X \stackrel{*}{\Rightarrow} aba'$ the string cannot be derived using G.

I. True

 $T \stackrel{*}{\Rightarrow} XX'$, the string can be derived using G.

m. True

 $T \stackrel{*}{\Rightarrow} XXX$, the string can be derived using G.

n. False

 $s\overset{*}{\Rightarrow} arepsilon'$ the string cannot be derived using G.

o. L(G) consists of all strings that are not palindromes and are formed over terminal symbols a and b.