获得的答案

Consider the difference hierarchy $D_i P$, which is **defined** recursively as

- $D_1P = NP$ and
- $D_i P = \{ A \mid A = B \cap \overline{C} \text{ for } B \text{ in } NP \text{ and } C \text{ in } D_{i-1}P \}$

Now consider the statement which is given below:

$$Z = \{ \langle G_1, k_1, G_2, k_2 \rangle | G_1 \text{ has a } k_1 - \text{clique and } G_2 \text{ doesn't have a } k_2 - \text{clique} \}$$

Here, it is already known that Z will be in DPand every language in DPis polynomial time reducible to Z.

Now, consider the NP-completeness behavior of MAX-CLIQUE. To prove the given statement, first a 3-SAT problem will be reduced to MAX-CLIQUE.

• Particularly, a m clause and n variables, a 3-CNF formula F will be generated. First for every clause d of F, every assignment assigned to a variable c will be created as a node.

$$F = \left(x_1 \vee x_2 \vee \overline{x_4}\right) \wedge \left(\overline{x_3} \vee x_4\right) \wedge \left(\overline{x_2} \vee \overline{x_3}\right) \wedge \dots$$

Which show that there exist no edges between any two nodes of the same clauses.

- So it can be said that, the maximum clique size, that it shows, is k. It is well known that if a graph consist k-clique, then this graph will definitely acquire one node per clause d.
- · Also, reduction which is taken will be in polynomial time. So, the produced graph shows the quadratic size of the graph.
- In other word it can be said that, it will take F(O(k)) nodes which consists $O(k^2)$ edges. Therefore, it can be said that, MAX CLIQUE is NP-complete.

Therefore, from the above discussion and from the definition of DP, every language in DP is polynomial time reducible to Z and DP is also in NP. Also, MAX - CLIOUE is DP complete. Hence it can be said that, MAX - CLIOUE is DP complete.