获得的答案

Consider a language **D** (as discussed in **Church-Turing thesis**), which is defined as:

 $D = \{\langle p \rangle | p \text{ is a polynomial in several variable having an integral root} \}$

Here, the given language D can be shown as NP - hard. This can be obtained by using the fact of NP - completeness property of the language D.

Now, consider the way to proof the NP – completeness property of the given language. The language D can be shown as NP – complete by using a reduction from 3SAT.

- An expression L in 3SAT can be converted into L by using the following facts:
- $\sim a = (1-a)$ (Where the sign (\sim) is defined as a **NOT logic** operator)

a and b = (ab)

 $a \operatorname{or} b = (a+b-ab)$

• Now, for simplicity, a function f(a,b,c) could be defined for each of the eight possibilities for all the clauses in 3SAT. Here, eight possibilities will be taken because each variable a,b and c will acquire a value 1/0.

An algorithm can be used which replace every clause with one of the replacements and also used for putting the symbol multiplication between them. In other word, the description of above algorithm can be given as:

$$f(a \text{ or } b \text{ or } \sim c) = [(a+b-ab)+(1-c)-(a+b-ab)(1-c)]$$

The running time of the above given algorithm is linear.

- The result L'shows a polynomial behavior that consist an integral root if and only if L is in SAT*. Therefore, the language D can be said as NP-complete.
- It is already known to be **un-decidable**, thus it will **not exist in** NP. Therefore from the above explanation, it can be said that **the language** D is NP-hard.