

The equivalence between the queue automaton Q and the Turing machine M is required to be shown.

It means it is required to be shown that the language that can be recognized by the automaton, it can also be recognized by the Turing machine and vice versa.

This can be done by showing simulation which means that simulate the automaton Q to behave exactly like the Turing machine M and vice versa.

The Automaton can be simulated by the Turing machine as follows:

Consider the entire tape as a queue. One by one each symbol is altered and the movement of the tape takes place to the right. If more than one numbers are to be pushed in the queue, then it is done by shifting contents to the right. If the end of the tape is reached, the leftmost symbol of the tape is approached.

The Turing machine can be simulated by the automaton as follows:

The alphabet of the Turing machine M is expanded by inserting an extra symbol. A left end marker $\#$ is inserted to the queue. The symbols are pushed to left and read (popped) from the right.