

A Deterministic Finite State automaton can be simulated on the Turing Machine with stay put instead of left. The modifications can be done if transitions are added from state in F to q_{accept} and from the states outside F to q_{reject} when a blank symbol is read.

Assume there is a Turing Machine M , such that $M = (Q, \Sigma, \Gamma, \delta, q_0, q_{accept}, q_{reject})$ with stay put instead of left. Create a DFA such that the DFA $(Q', \Sigma', \delta', q_0', F)$ recognizes the same language.

The machine M cannot move left and cannot write anything that it can written on the tape while moving to the right. Thus, the access is one-way.

For every DFA, there exists a Turing Machine that accepts the same language because a DFA is a Turing Machine with read only tape and tape head with moves to right.

The transition function δ' for the NFA is as follows:

First, set $\delta'(q_{start}, P) = \{q_{OP}\}$ where q_{OP} is the start state of TM variant.

Next, set $\delta'(q_{accept}, i) = \{q_{accept}\}$ For any i

If $\delta(p, a) = (q_{accept}, b, w)$ where $w = R$ or S , set $\delta'(q_{pa}, \epsilon) = \{q_{accept}\}$

R is RIGHT S is stay put.

If $\delta(p, a) = (q_{reject}, b, w)$ where $w = R$ or S , we set $\delta'(q_{pa}, \epsilon) = \{q_{reject}\}$

- For each $a \in \Sigma$, set $\delta'(q_{start}, a) = \{q_0, a\}$, where q_0 is start state of S .

- For each $p, q \in Q$ where $p \notin \{q_{accept}, q_{reject}\}$, for each $a \in \Gamma$, if S has transition of form $\delta(p, a) = (q_{accept}, b, w)$ or $\delta(p, a) = (q_{reject}, b, w)$, w becomes R for each $c \in \Sigma$, set $\delta'(\langle p, a \rangle, c) = \{\langle q, c \rangle\}$.

- For each $p, q \in Q$ where $p \notin \{q_{accept}, q_{reject}\}$, for each $a \in \Sigma$, if S has transition of form $\delta(p, a) = (q_{accept}, b, w)$ or $\delta(p, a) = (q_{reject}, b, w)$, w becomes S then set $\delta'(\langle p, a \rangle, \epsilon) = \{\langle q, b \rangle\}$

Thus, an NFA is constructed which is defined as follows:

$(Q' = Q, \Sigma' = \Sigma, \delta', q_{op} = q_{start}, F)$ From our TM variant S .

The language recognized by NFA is regular languages.