

a.

The pumping length could not be 3 as 000 being in the language it cannot be pumped. Consider the string length be 4 or more and divide in  $xyz$  as  $x$  being 000,  $y$  being the first 1 and  $z$  being everything after then it satisfies every condition of pumping lemma.

**Hence the minimum pumping length is 4.**

b.

String  $\epsilon$  is in the language but it could not be pumped so the pumping length could not be 0. According to pumping lemma's three condition arises which are as follows:

- If user divide the string in  $xyz$  as  $x$  is  $\epsilon$
- $y$  is first symbol (0|1)
- $z$  being the everything after then it holds.

**Hence the minimum pumping length is 1.**

c.

The string 001 is in the language but if it is generated by 001 then it cannot be pumped. If string  $s$  is larger than 3 and in the language, then it is generated by  $0^*1^*$ . Dividing the string according to Pumping Lemma's condition into a string  $xyz$  where  $x$  is  $\epsilon$ ,  $y$  be the first symbol and  $z$  be the remaining, user can pump the string.

**Hence the minimum pumping length is 4.**

d.

The string 11 is in the language but it cannot be pumped so the length is not 2. Let  $s$  be the string in the language of length at least 3. If  $s$  is generated by  $0^*1^*0^*1^*$  it can be divided in  $xyz$  as  $x$  is  $\epsilon$ ,  $y$  is the first string and  $z$  is everything else so it can be pumped.

Again if  $s$  is generated by  $10^*1$  then also user can write it as  $xyz$  where  $x$  is 1,  $y$  is 0, and  $z$  is the remainder so it could be pumped.

**Hence the minimum pumping length is 3.**

e.

Let  $s$  be a string in the language.

Now  $s$  could be  $\epsilon$  but it cannot be pumped so the length is not 0. Next  $s$  could be 01 which if divide in  $xyz$  as  $x$  is empty string  $\epsilon$ ,  $y$  is 01, and  $z$  is everything after then it satisfies the three conditions of pumping lemma.

Pumping length is not 1 because since there is no string of length 1 in the language.

**Hence the minimum pumping length is 2.**

f.

Let  $s$  be a string in the language then  $s$  is  $\epsilon$  and according to pumping lemma it cannot be pumped. As per the pumping lemma, pumping length should greater then equal to 1.

**Hence the minimum pumping length is 0.**

g.

The minimum pumping length of the language could not be 2 as 00 being in the language it could not be pumped. Let  $s$  be the string of length at least 3 in the language so minimally  $s$  could be 100 or 010 or 001.

Now dividing  $s$  in  $xyz$  in all the three cases user get, for 100  $x$  is  $\epsilon$ ,  $y$  is 1, and  $z$  is the remainder, for 010  $x$  is 0,  $y$  is 1, and  $z$  is the remainder and for 001  $x$  is 00,  $y$  is 1, and  $z$  is the remainder. All satisfies Pumping Lemma's three conditions.

**Hence the minimum pumping length is 3.**

h.

The minimum length string in the given language is 100 but it cannot be pumped. Next minimum length string is 10100. If divide it according to the pumping lemma in  $xyz$  then  $x$  be 10,  $y$  be 10, and  $z$  be the rest of the string then  $y$  can be pumped.

[浙ICP备16034203号-2](#)

**Hence the minimum pumping length is 4.**

i.

If  $s$  be a string in the language then  $s$  is **1011**. If set  $p = 4$ , then claim  $s$  is pumpable (which it is not, as it is the only string in the language). This should be 5.

**Hence then the minimum pumping length is 5.**

j.

Say  $s$  be a string in the language  $\Sigma^*$ . According to pumping lemma if divide  $s$  in  $xyz$  then  $x$  be the empty string,  $y$  is **( $\epsilon$ |0|1)** and  $z$  is empty string. Now  $\epsilon$  could not be pumped.

**Hence the minimum pumping length is 1.**