获得的答案

## **Decidability**

Consider a decider M which is used to check whether language of CFG is finite or infinite. Use another decider that is Turing machine W which shows that is  $C_{CFG}$  decidable.

- 1. W = "on input(G, k)" where G is CFG and k is string
- 2. Check L(G) is infinite using decider M.
- If L(G) is infinite and  $k = \infty$ , it is accepted
- If L(G) is infinite and  $k \neq \infty$ , it is rejected
- If L(G) is finite and  $k = \infty$ , it is rejected
- If L(G) is finite and  $k \neq \infty$ , continue
- 3. Calculate the pumping length *l* for grammar *G*.
- 4. Set count = 0
- 5. Use for loop i = 0 to l
- Use for loop to get all strings S whose length equal to i
- If S can be generated by G then make an increment in count.
- 6. Check value of *count* is equal to *k* then it is accept, otherwise reject.

## **Explanation:**

- The Step 2 checks whether L(G) is infinite or not. After step 2 there is grammar whose language which has finite set. In order to prove  $C_{CFG}$  is decidable there is only need to prove that the size of language is k.
- To do so use loop to find the all the possible string can be generated by grammar G. The grammar is finite therefore the length of string cannot be more than pumping length *l*.
- Make an increment in variable count if the string can be generated by grammar G.
- In the last step check value of *count* is equal to *k*.
- Now, it has finite number of steps therefore it can easily check.

Thus W is decider, therefore  $C_{\mathit{CFG}}$  is also decidable language.