

Consider the Turing-recognizable language A which contains the descriptions of all the Turing machines, therefore there must exist an enumerator E to enumerate it.

Consider $\langle M_i \rangle$ is the i^{th} output of E . Assume $s_1, s_2, s_3, \dots, s_i$ are the all possible strings of $\{0, 1\}^*$. It means $s_1, s_2, s_3, \dots, s_i$ are made up of combinations of 0's and 1's.

Consider a decidable language D is defined as follows:

For a string S_i ,

- If $\langle M_i \rangle$ accepts then S_i does not belongs to the language D .
- If $\langle M_i \rangle$ rejects then S_i belongs to the language D .

Here, the language D is a decidable language and its decider is not present in the list. Therefore, it is proved that there is a decidable language D whose decider is not present in A .