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Consider the context free grammar (CFG) G is as follows:

$$S \rightarrow aSb \mid bY \mid Ya$$

$$Y \rightarrow bY \mid aY \mid \varepsilon$$

Language $L(G)$ for the G is as follows:

Consider the productions in the grammar

$$S \rightarrow aSb$$

$$S \rightarrow bY$$

$$S \rightarrow Ya$$

$$Y \rightarrow bY$$

$$Y \rightarrow aY$$

$$Y \rightarrow \varepsilon$$

Case 1:

Consider production $S \rightarrow Ya$ to derive the language.

Substitute Y with production $Y \rightarrow \varepsilon$ then

$$S \rightarrow \varepsilon a$$

$$S \rightarrow a$$

Case 2:

Consider production $S \rightarrow bY$ to derive the language.

Substitute Y with production $Y \rightarrow \varepsilon$ then

$$S \rightarrow \varepsilon b$$

$$S \rightarrow b$$

Case 3:

Consider production $S \rightarrow aSb$ to derive the language

Substitute S with production $S \rightarrow bY$ then

$$S \rightarrow abYb$$

Substitute Y with production $Y \rightarrow bY$ then

$$S \rightarrow abbYb$$

Substitute Y with production $Y \rightarrow \varepsilon$ then

$$S \rightarrow abb \varepsilon b$$

$$S \rightarrow abbb$$

Case 4:

Consider production $S \rightarrow bY$ to derive the language.

Substitute Y with production $Y \rightarrow bY$ then

$$S \rightarrow bbY$$

Substitute Y with production $Y \rightarrow \varepsilon$ then

$$S \rightarrow bb \varepsilon$$

$$S \rightarrow bb$$

Therefore from the Case 1, Case 2, Case 3 and Case 4 the language obtained is as follows:

$$L(G) = \{a, b, abbb, bb...\}$$

Using the grammar G , many more strings can be generated.

Description of the $L(G)$ is as follows:

The grammar G generates a language $L(G)$ consists of the strings which are described as follows:

- Strings with consecutive number of a 's with a length ranging from 1 to infinity.
- Strings with consecutive number of b 's with a length ranging from 1 to infinity.
- String with start symbol a followed by number of b 's.
- Strings with start symbol b followed by number of a 's.
- Strings with a as start symbol and b as end symbol.
- Strings with b as start symbol and a as end symbol.
- Strings that contains the same start and end symbols. For example, aba , bab etc.

From the above description as $L(G)$ is generating all the possible combination of a 's and b 's except $a^i b^i$ where $i \geq 0$. The $L(G)$ does not produce strings like ϵ , ab , $aabb$, $aaabbb$. . .

The complements of $L(G)$ i.e. $\overline{L(G)} = \{\epsilon, ab, aabb, aaabbb \dots\}$

The grammar for $\overline{L(G)}$ is $a^i b^i$ where $i \geq 0$.

Therefore, the CFG G' for $\overline{L(G)}$ is as follows:

$$S \rightarrow aSb | \epsilon$$