

An integer can be factorized in multinomial time if  $P = NP$  has given.

- Consider the language

$$L = \{ \langle n, x, y \rangle \mid n \text{ has a factor } p \text{ in the range } x \leq p \leq y \}.$$

- Assume  $P = NP$  and the above language can be decided by a polynomial algorithm.
- Each time the search space is divided into half by using repeated applications of the algorithm.
- The repetition is done by asking "Is a factor exists in the range  $\left(x, \frac{x+y}{2}\right)$ ?". If the factor is not in this region then it can be said that there is a factor in other range.
- The number of times the algorithm applied here is sufficient to  $\log n$ . In other words it can also be said that, it will take  $O(k)$ , if  $k$  is the number of bits exists in  $n$ . So, one factor can be isolated by using the algorithm which consist polynomial number of applications.

Since it has maximum  $O(k)$  factors, therefore it can be said that, every factors can be found in polynomial time.