

**TRUE (or) FALSE**

**Small – o Notation:**

Let  $f$  and  $g$  be functions  $f, g : N \rightarrow R^+$  say that  $f(n) = O(g(n))$  if for any real number

$c > 0$ , a number  $n_0$  exists, where  $f(n) < c \cdot g(n)$  for all  $n \geq n_0$ .

(a)

**False.**

The statement  $n = o(2n)$  is invalid, because the functions  $n$  and  $2n$  grows equality

That is  $f(n) = c \cdot g(n)$ . But according to definition  $f(n) < c \cdot g(n)$

Therefore  $n = o(2n)$  is false

(b)

**True.**

The statement  $2n = o(n^2)$  is valid, because the functions  $n^2 = n \cdot n$  which will grow faster than  $n$ . That is  $f(n) < g(n)$ .

Therefore from the definition of small – o notation,  $2n = o(n^2)$  is true.

(c)

**True.**

The statement  $2^n = o(3^n)$  is valid, because the function  $2^n$  runs slower than

the function  $3^n$ .

Then,  $2^n < 3^n$ .

That is  $f(n) < c \cdot g(n)$

Hence from the definition of small – o notation,  $2^n = o(3^n)$  is true.

(d)

**True.**

The statement  $1 = o(n)$  is valid, because the function  $n$  grows faster than a number 1.

Therefore  $f(n) < c \cdot g(n)$

By the definition of small – o notation,  $1 = o(n)$  is true.

(e)

**False.**

The statement  $n = o(\log n)$  is not valid, because the functions  $\log n$  grows slower than the function  $n$ , which is a contradiction.

Hence  $n = o(\log n)$  is false.

(f)

**False.**

The statement  $1 = o(1/n)$  is not valid, because the function  $1/n$  grows slower than 1.

Therefore  $f(n) > g(n)$ .

Which is a contradiction

Hence  $1 = o(1/n)$  is false .