## **Constraints:**

A is any language and  $A_{\frac{1}{3}\frac{1}{3}} = \{x \mid \text{ for some } y, |x| = |y| = |z| \text{ and } xyz \in A\}$  is the set of all strings in A with their middle thirds removed.

- Let  $A = \{a * \#b *\}$  is regular language
- We know that  $\{a*b*\}$  is a regular language.
- Also we know that "Regular languages are closed under intersection"

• Now 
$$A_{\frac{1}{2},\frac{1}{2}} \cap \{a * b *\} = \{a^n b^n \mid n \ge 0\}$$

• Clearly  $\left\{a^nb^n\,|\,n\!\ge\!0\right\}$  is not regular, because if p is the pumping length and

$$S = xyz = aabb$$
 is  $p = 2$  Here  $x = a$   $y = a$   $z = bb$ , obtain  $xy^2z = aaabb$ 

<u>Pumping lemma</u>: If A is a regular language, then there is a pumping length p where, if s is any string in A of length at least P, then s may be divided into three pieces, s = xyz, satisfying following conditions

- (i) For each  $i \ge 0$ ,  $xy^i z \in A$
- (ii) |y| > 0 and
- (iii)  $|xy| \le p$

So according to pumping lemma  $xy^2z=a^3b^2\not\in \left\{a*b*\right\}$ 

Hence  $\{0*1*\}$  is not regular.

As regular languages are closed under intersection and  $\{0^*1^*\}$  is not regular,  $\frac{A_{1-\frac{1}{3}}}{3}$  is not regular. If A is regular, then  $\frac{A_{1-\frac{1}{3}}}{3}$  is not necessarily regular is proved.