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Assignment 2

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Download the python code, latex file and the pdf doc from

https://github.com/Rishab9991/EE5609/tree/master/ Assignments/Assignment2

1) **Solution:**

$$A = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \tag{1}$$

$$\implies A^T = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \tag{2}$$

$$\begin{pmatrix} a1\\a2 \end{pmatrix} = \begin{pmatrix} a1 & -a2\\a2 & a1 \end{pmatrix} \begin{pmatrix} 1\\0 \end{pmatrix}$$
 (3)

$$i.e \ A = \begin{pmatrix} \cos \alpha \\ -\sin \alpha \end{pmatrix} \tag{4}$$

$$A^T = \begin{pmatrix} \cos \alpha \\ \sin \alpha \end{pmatrix} \tag{5}$$

$$\implies A^T A = \begin{pmatrix} \cos \alpha \\ \sin \alpha \end{pmatrix} \begin{pmatrix} \cos \alpha \\ -\sin \alpha \end{pmatrix} \tag{6}$$

$$\implies A^T A = I \tag{7}$$

2) Solution:

$$A = \begin{pmatrix} \sin \alpha & \cos \alpha \\ -\cos \alpha & \sin \alpha \end{pmatrix} \tag{8}$$

$$\implies A^T = \begin{pmatrix} \sin \alpha & -\cos \alpha \\ \cos \alpha & \sin \alpha \end{pmatrix} \tag{9}$$

Using (3),

$$i.e \ A = \begin{pmatrix} \sin \alpha \\ -\cos \alpha \end{pmatrix} \tag{10}$$

$$A^T = \begin{pmatrix} \sin \alpha \\ \cos \alpha \end{pmatrix} \tag{11}$$

$$\implies A^T A = \begin{pmatrix} \sin \alpha \\ \cos \alpha \end{pmatrix} \begin{pmatrix} \sin \alpha \\ -\cos \alpha \end{pmatrix} \tag{12}$$

$$\implies A^T A = I$$
 (13)

Hence Proved for both (1) and (2).