18

Paging: Introduction

It is sometimes said that the operating system takes one of two approaches when solving most any space-management problem. The first approach is to chop things up into *variable-sized* pieces, as we saw with **segmentation** in virtual memory. Unfortunately, this solution has inherent difficulties. In particular, when dividing a space into different-size chunks, the space itself can become **fragmented**, and thus allocation becomes more challenging over time.

Thus, it may be worth considering the second approach: to chop up space into *fixed-sized* pieces. In virtual memory, we call this idea **paging**, and it goes back to an early and important system, the Atlas [KE+62, L78]. Instead of splitting up a process's address space into some number of variable-sized logical segments (e.g., code, heap, stack), we divide it into fixed-sized units, each of which we call a **page**. Correspondingly, we view physical memory as an array of fixed-sized slots called **page frames**; each of these frames can contain a single virtual-memory page. Our challenge:

> THE CRUX:
> HOW TO VIRTUALIZE MEMORY WITH PAGES
> How can we virtualize memory with pages, so as to avoid the problems of segmentation? What are the basic techniques? How do we make those techniques work well, with minimal space and time overheads?

18.1 A Simple Example And Overview

To help make this approach more clear, let's illustrate it with a simple example. Figure 18.1 (page 2) presents an example of a tiny address space, only 64 bytes total in size, with four 16-byte pages (virtual pages 0, 1, 2, and 3). Real address spaces are much bigger, of course, commonly 32 bits and thus 4-GB of address space, or even 64 bits[1]; in the book, we'll often use tiny examples to make them easier to digest.

[1] A 64-bit address space is hard to imagine, it is so amazingly large. An analogy might help: if you think of a 32-bit address space as the size of a tennis court, a 64-bit address space is about the size of Europe(!).

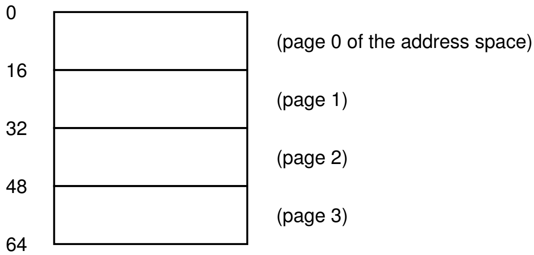


Figure 18.1: **A Simple 64-byte Address Space**

Physical memory, as shown in Figure 18.2, also consists of a number of fixed-sized slots, in this case eight page frames (making for a 128-byte physical memory, also ridiculously small). As you can see in the diagram, the pages of the virtual address space have been placed at different locations throughout physical memory; the diagram also shows the OS using some of physical memory for itself.

Paging, as we will see, has a number of advantages over our previous approaches. Probably the most important improvement will be *flexibility*: with a fully-developed paging approach, the system will be able to support the abstraction of an address space effectively, regardless of how a process uses the address space; we won't, for example, make assumptions about the direction the heap and stack grow and how they are used.

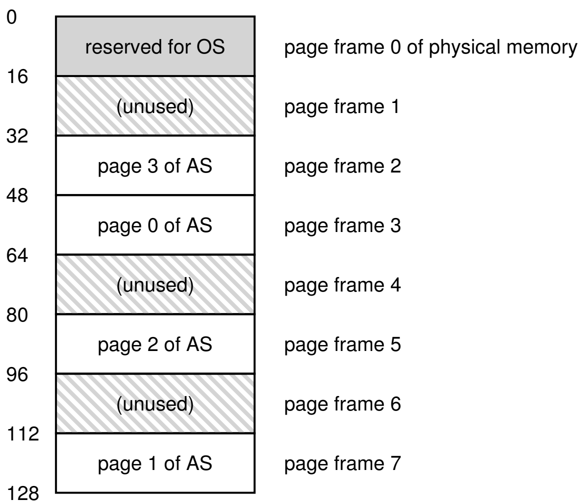


Figure 18.2: **A 64-Byte Address Space In A 128-Byte Physical Memory**

Another advantage is the *simplicity* of free-space management that paging affords. For example, when the OS wishes to place our tiny 64-byte address space into our eight-page physical memory, it simply finds four free pages; perhaps the OS keeps a **free list** of all free pages for this, and just grabs the first four free pages off of this list. In the example, the OS has placed virtual page 0 of the address space (AS) in physical frame 3, virtual page 1 of the AS in physical frame 7, page 2 in frame 5, and page 3 in frame 2. Page frames 1, 4, and 6 are currently free.

To record where each virtual page of the address space is placed in physical memory, the operating system usually keeps a *per-process* data structure known as a **page table**. The major role of the page table is to store **address translations** for each of the virtual pages of the address space, thus letting us know where in physical memory each page resides. For our simple example (Figure 18.2, page 2), the page table would thus have the following four entries: (Virtual Page 0 → Physical Frame 3), (VP 1 → PF 7), (VP 2 → PF 5), and (VP 3 → PF 2).

It is important to remember that this page table is a *per-process* data structure (most page table structures we discuss are per-process structures; an exception we'll touch on is the **inverted page table**). If another process were to run in our example above, the OS would have to manage a different page table for it, as its virtual pages obviously map to *different* physical pages (modulo any sharing going on).

Now, we know enough to perform an address-translation example. Let's imagine the process with that tiny address space (64 bytes) is performing a memory access:

```
movl <virtual address>, %eax
```

Specifically, let's pay attention to the explicit load of the data from address <virtual address> into the register eax (and thus ignore the instruction fetch that must have happened prior).

To **translate** this virtual address that the process generated, we have to first split it into two components: the **virtual page number (VPN)**, and the **offset** within the page. For this example, because the virtual address space of the process is 64 bytes, we need 6 bits total for our virtual address ($2^6 = 64$). Thus, our virtual address can be conceptualized as follows:

Va5	Va4	Va3	Va2	Va1	Va0

In this diagram, Va5 is the highest-order bit of the virtual address, and Va0 the lowest-order bit. Because we know the page size (16 bytes), we can further divide the virtual address as follows:

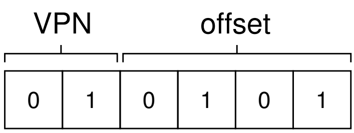
VPN		offset			
Va5	Va4	Va3	Va2	Va1	Va0

The page size is 16 bytes in a 64-byte address space; thus we need to be able to select 4 pages, and the top 2 bits of the address do just that. Thus, we have a 2-bit virtual page number (VPN). The remaining bits tell us which byte of the page we are interested in, 4 bits in this case; we call this the offset.

When a process generates a virtual address, the OS and hardware must combine to translate it into a meaningful physical address. For example, let us assume the load above was to virtual address 21:

```
movl 21, %eax
```

Turning "21" into binary form, we get "010101", and thus we can examine this virtual address and see how it breaks down into a virtual page number (VPN) and offset:



Thus, the virtual address "21" is on the 5th ("0101"th) byte of virtual page "01" (or 1). With our virtual page number, we can now index our page table and find which physical frame virtual page 1 resides within. In the page table above the **physical frame number (PFN)** (also sometimes called the **physical page number** or **PPN**) is 7 (binary 111). Thus, we can translate this virtual address by replacing the VPN with the PFN and then issue the load to physical memory (Figure 18.3).

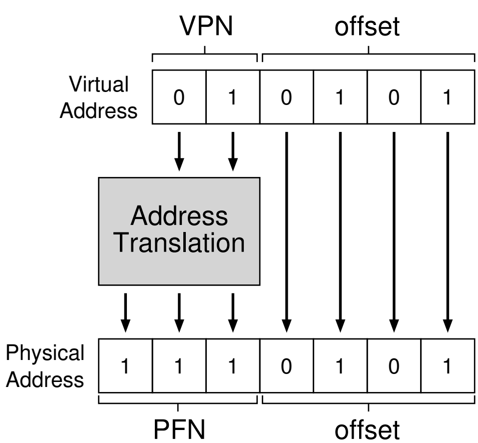


Figure 18.3: **The Address Translation Process**

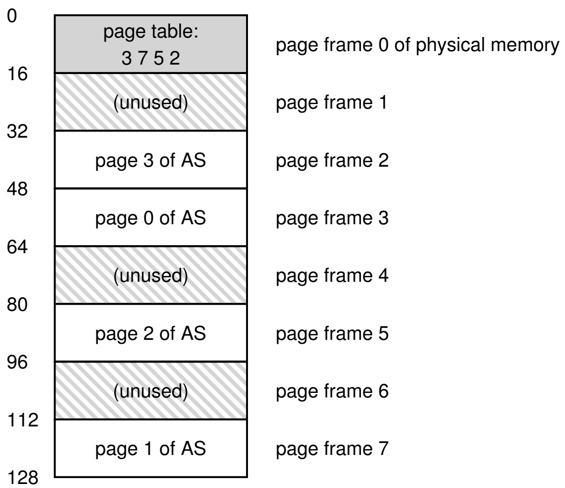


Figure 18.4: **Example: Page Table in Kernel Physical Memory**

Note the offset stays the same (i.e., it is not translated), because the offset just tells us which byte *within* the page we want. Our final physical address is 1110101 (117 in decimal), and is exactly where we want our load to fetch data from (Figure 18.2, page 2).

With this basic overview in mind, we can now ask (and hopefully, answer) a few basic questions you may have about paging. For example, where are these page tables stored? What are the typical contents of the page table, and how big are the tables? Does paging make the system (too) slow? These and other beguiling questions are answered, at least in part, in the text below. Read on!

18.2 Where Are Page Tables Stored?

Page tables can get terribly large, much bigger than the small segment table or base/bounds pair we have discussed previously. For example, imagine a typical 32-bit address space, with 4KB pages. This virtual address splits into a 20-bit VPN and 12-bit offset (recall that 10 bits would be needed for a 1KB page size, and just add two more to get to 4KB).

A 20-bit VPN implies that there are 2^{20} translations that the OS would have to manage for each process (that's roughly a million); assuming we need 4 bytes per **page table entry (PTE)** to hold the physical translation plus any other useful stuff, we get an immense 4MB of memory needed for each page table! That is pretty large. Now imagine there are 100 processes running: this means the OS would need 400MB of memory just for all those address translations! Even in the modern era, where

ASIDE: DATA STRUCTURE — THE PAGE TABLE

One of the most important data structures in the memory management subsystem of a modern OS is the **page table**. In general, a page table stores **virtual-to-physical address translations**, thus letting the system know where each page of an address space actually resides in physical memory. Because each address space requires such translations, in general there is one page table per process in the system. The exact structure of the page table is either determined by the hardware (older systems) or can be more flexibly managed by the OS (modern systems).

machines have gigabytes of memory, it seems a little crazy to use a large chunk of it just for translations, no? And we won't even think about how big such a page table would be for a 64-bit address space; that would be too gruesome and perhaps scare you off entirely.

Because page tables are so big, we don't keep any special on-chip hardware in the MMU to store the page table of the currently-running process. Instead, we store the page table for each process in *memory* somewhere. Let's assume for now that the page tables live in physical memory that the OS manages; later we'll see that much of OS memory itself can be virtualized, and thus page tables can be stored in OS virtual memory (and even swapped to disk), but that is too confusing right now, so we'll ignore it. In Figure 18.4 (page 5) is a picture of a page table in OS memory; see the tiny set of translations in there?

18.3 What's Actually In The Page Table?

Let's talk a little about page table organization. The page table is just a data structure that is used to map virtual addresses (or really, virtual page numbers) to physical addresses (physical frame numbers). Thus, any data structure could work. The simplest form is called a **linear page table**, which is just an array. The OS *indexes* the array by the virtual page number (VPN), and looks up the page-table entry (PTE) at that index in order to find the desired physical frame number (PFN). For now, we will assume this simple linear structure; in later chapters, we will make use of more advanced data structures to help solve some problems with paging.

As for the contents of each PTE, we have a number of different bits in there worth understanding at some level. A **valid bit** is common to indicate whether the particular translation is valid; for example, when a program starts running, it will have code and heap at one end of its address space, and the stack at the other. All the unused space in-between will be marked **invalid**, and if the process tries to access such memory, it will generate a trap to the OS which will likely terminate the process. Thus, the valid bit is crucial for supporting a sparse address space; by simply marking all the unused pages in the address space invalid, we remove the need to allocate physical frames for those pages and thus save a great deal of memory.

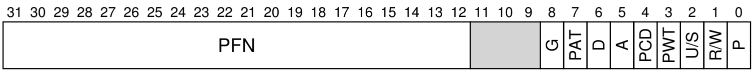


Figure 18.5: **An x86 Page Table Entry (PTE)**

We also might have **protection bits**, indicating whether the page could be read from, written to, or executed from. Again, accessing a page in a way not allowed by these bits will generate a trap to the OS.

There are a couple of other bits that are important but we won't talk about much for now. A **present bit** indicates whether this page is in physical memory or on disk (i.e., it has been **swapped out**). We will understand this machinery further when we study how to **swap** parts of the address space to disk to support address spaces that are larger than physical memory; swapping allows the OS to free up physical memory by moving rarely-used pages to disk. A **dirty bit** is also common, indicating whether the page has been modified since it was brought into memory.

A **reference bit** (a.k.a. **accessed bit**) is sometimes used to track whether a page has been accessed, and is useful in determining which pages are popular and thus should be kept in memory; such knowledge is critical during **page replacement**, a topic we will study in great detail in subsequent chapters.

Figure 18.5 shows an example page table entry from the x86 architecture [I09]. It contains a present bit (P); a read/write bit (R/W) which determines if writes are allowed to this page; a user/supervisor bit (U/S) which determines if user-mode processes can access the page; a few bits (PWT, PCD, PAT, and G) that determine how hardware caching works for these pages; an accessed bit (A) and a dirty bit (D); and finally, the page frame number (PFN) itself.

Read the Intel Architecture Manuals [I09] for more details on x86 paging support. Be forewarned, however; reading manuals such as these, while quite informative (and certainly necessary for those who write code to use such page tables in the OS), can be challenging at first. A little patience, and a lot of desire, is required.

ASIDE: WHY NO VALID BIT?

You may notice that in the Intel example, there are no separate valid and present bits, but rather just a present bit (P). If that bit is set (P=1), it means the page is both present and valid. If not (P=0), it means that the page may not be present in memory (but is valid), or may not be valid. An access to a page with P=0 will trigger a trap to the OS; the OS must then use additional structures it keeps to determine whether the page is valid (and thus perhaps should be swapped back in) or not (and thus the program is attempting to access memory illegally). This sort of judiciousness is common in hardware, which often just provide the minimal set of features upon which the OS can build a full service.

18.4 Paging: Also Too Slow

With page tables in memory, we already know that they might be too big. As it turns out, they can slow things down too. For example, take our simple instruction:

```
movl 21, %eax
```

Again, let's just examine the explicit reference to address 21 and not worry about the instruction fetch. In this example, we'll assume the hardware performs the translation for us. To fetch the desired data, the system must first **translate** the virtual address (21) into the correct physical address (117). Thus, before fetching the data from address 117, the system must first fetch the proper page table entry from the process's page table, perform the translation, and then load the data from physical memory.

To do so, the hardware must know where the page table is for the currently-running process. Let's assume for now that a single **page-table base register** contains the physical address of the starting location of the page table. To find the location of the desired PTE, the hardware will thus perform the following functions:

```
VPN     = (VirtualAddress & VPN_MASK) >> SHIFT
PTEAddr = PageTableBaseRegister + (VPN * sizeof(PTE))
```

In our example, `VPN_MASK` would be set to 0x30 (hex 30, or binary 110000) which picks out the VPN bits from the full virtual address; `SHIFT` is set to 4 (the number of bits in the offset), such that we move the VPN bits down to form the correct integer virtual page number. For example, with virtual address 21 (010101), and masking turns this value into 010000; the shift turns it into 01, or virtual page 1, as desired. We then use this value as an index into the array of PTEs pointed to by the page table base register.

Once this physical address is known, the hardware can fetch the PTE from memory, extract the PFN, and concatenate it with the offset from the virtual address to form the desired physical address. Specifically, you can think of the PFN being left-shifted by `SHIFT`, and then bitwise OR'd with the offset to form the final address as follows:

```
offset   = VirtualAddress & OFFSET_MASK
PhysAddr = (PFN << SHIFT) | offset
```

Finally, the hardware can fetch the desired data from memory and put it into register `eax`. The program has now succeeded at loading a value from memory!

To summarize, we now describe the initial protocol for what happens on each memory reference. Figure 18.6 (page 9) shows the approach. For every memory reference (whether an instruction fetch or an explicit load or store), paging requires us to perform one extra memory reference in order to first fetch the translation from the page table. That is a lot of

```
// Extract the VPN from the virtual address
VPN = (VirtualAddress & VPN_MASK) >> SHIFT

// Form the address of the page-table entry (PTE)
PTEAddr = PTBR + (VPN * sizeof(PTE))

// Fetch the PTE
PTE = AccessMemory(PTEAddr)

// Check if process can access the page
if (PTE.Valid == False)
    RaiseException(SEGMENTATION_FAULT)
else if (CanAccess(PTE.ProtectBits) == False)
    RaiseException(PROTECTION_FAULT)
else
    // Access is OK: form physical address and fetch it
    offset   = VirtualAddress & OFFSET_MASK
    PhysAddr = (PTE.PFN << PFN_SHIFT) | offset
    Register = AccessMemory(PhysAddr)
```

Figure 18.6: **Accessing Memory With Paging**

work! Extra memory references are costly, and in this case will likely slow down the process by a factor of two or more.

And now you can hopefully see that there are *two* real problems that we must solve. Without careful design of both hardware and software, page tables will cause the system to run too slowly, as well as take up too much memory. While seemingly a great solution for our memory virtualization needs, these two crucial problems must first be overcome.

18.5 A Memory Trace

Before closing, we now trace through a simple memory access example to demonstrate all of the resulting memory accesses that occur when using paging. The code snippet (in C, in a file called `array.c`) that we are interested in is as follows:

```
int array[1000];
...
for (i = 0; i < 1000; i++)
    array[i] = 0;
```

We compile `array.c` and run it with the following commands:

```
prompt> gcc -o array array.c -Wall -O
prompt> ./array
```

Of course, to truly understand what memory accesses this code snippet (which simply initializes an array) will make, we'll have to know (or assume) a few more things. First, we'll have to **disassemble** the resulting binary (using `objdump` on Linux, or `otool` on a Mac) to see what assembly instructions are used to initialize the array in a loop. Here is the resulting assembly code:

```
1024 movl $0x0,(%edi,%eax,4)
1028 incl %eax
1032 cmpl $0x03e8,%eax
1036 jne  0x1024
```

The code, if you know a little **x86**, is actually quite easy to understand[2]. The first instruction moves the value zero (shown as `$0x0`) into the virtual memory address of the location of the array; this address is computed by taking the contents of `%edi` and adding `%eax` multiplied by four to it. Thus, `%edi` holds the base address of the array, whereas `%eax` holds the array index (`i`); we multiply by four because the array is an array of integers, each of size four bytes.

The second instruction increments the array index held in `%eax`, and the third instruction compares the contents of that register to the hex value `0x03e8`, or decimal 1000. If the comparison shows that two values are not yet equal (which is what the `jne` instruction tests), the fourth instruction jumps back to the top of the loop.

To understand which memory accesses this instruction sequence makes (at both the virtual and physical levels), we'll have to assume something about where in virtual memory the code snippet and array are found, as well as the contents and location of the page table.

For this example, we assume a virtual address space of size 64KB (unrealistically small). We also assume a page size of 1KB.

All we need to know now are the contents of the page table, and its location in physical memory. Let's assume we have a linear (array-based) page table and that it is located at physical address 1KB (1024).

As for its contents, there are just a few virtual pages we need to worry about having mapped for this example. First, there is the virtual page the code lives on. Because the page size is 1KB, virtual address 1024 resides on the second page of the virtual address space (VPN=1, as VPN=0 is the first page). Let's assume this virtual page maps to physical frame 4 (VPN 1 $\rightarrow$ PFN 4).

Next, there is the array itself. Its size is 4000 bytes (1000 integers), and we assume that it resides at virtual addresses 40000 through 44000 (not including the last byte). The virtual pages for this decimal range are VPN=39 ... VPN=42. Thus, we need mappings for these pages. Let's assume these virtual-to-physical mappings for the example: (VPN 39 $\rightarrow$ PFN 7), (VPN 40 $\rightarrow$ PFN 8), (VPN 41 $\rightarrow$ PFN 9), (VPN 42 $\rightarrow$ PFN 10).

[2]We are cheating a little bit here, assuming each instruction is four bytes in size for simplicity; in actuality, x86 instructions are variable-sized.

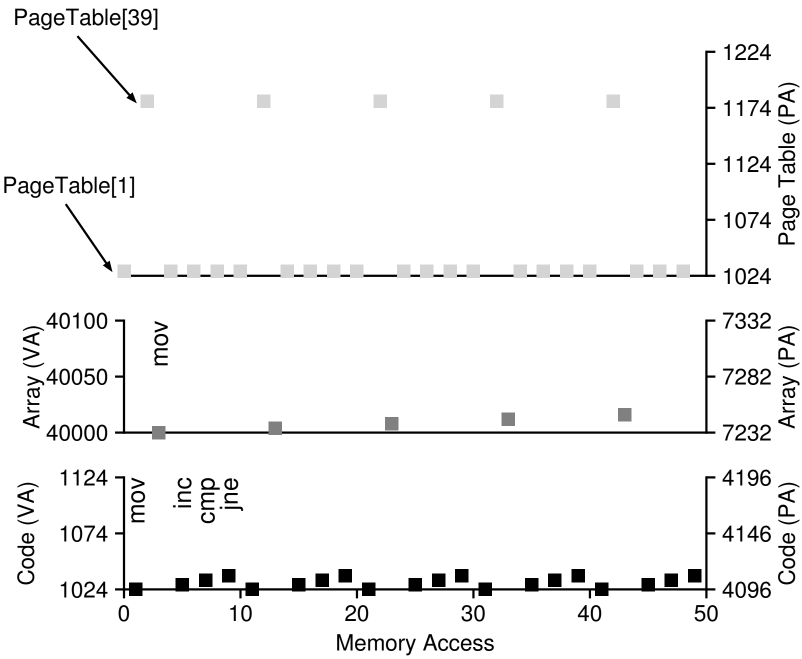


Figure 18.7: **A Virtual (And Physical) Memory Trace**

We are now ready to trace the memory references of the program. When it runs, each instruction fetch will generate two memory references: one to the page table to find the physical frame that the instruction resides within, and one to the instruction itself to fetch it to the CPU for processing. In addition, there is one explicit memory reference in the form of the `mov` instruction; this adds another page table access first (to translate the array virtual address to the correct physical one) and then the array access itself.

The entire process, for the first five loop iterations, is depicted in Figure 18.7 (page 11). The bottom most graph shows the instruction memory references on the y-axis in black (with virtual addresses on the left, and the actual physical addresses on the right); the middle graph shows array accesses in dark gray (again with virtual on left and physical on right); finally, the topmost graph shows page table memory accesses in light gray (just physical, as the page table in this example resides in physical memory). The x-axis, for the entire trace, shows memory accesses across the first five iterations of the loop; there are 10 memory accesses per loop, which includes four instruction fetches, one explicit update of memory, and five page table accesses to translate those four fetches and one explicit update.

See if you can make sense of the patterns that show up in this visualization. In particular, what will change as the loop continues to run beyond these first five iterations? Which new memory locations will be accessed? Can you figure it out?

This has just been the simplest of examples (only a few lines of C code), and yet you might already be able to sense the complexity of understanding the actual memory behavior of real applications. Don't worry: it definitely gets worse, because the mechanisms we are about to introduce only complicate this already complex machinery. Sorry[3]!

18.6 Summary

We have introduced the concept of **paging** as a solution to our challenge of virtualizing memory. Paging has many advantages over previous approaches (such as segmentation). First, it does not lead to external fragmentation, as paging (by design) divides memory into fixed-sized units. Second, it is quite flexible, enabling the sparse use of virtual address spaces.

However, implementing paging support without care will lead to a slower machine (with many extra memory accesses to access the page table) as well as memory waste (with memory filled with page tables instead of useful application data). We'll thus have to think a little harder to come up with a paging system that not only works, but works well. The next two chapters, fortunately, will show us how to do so.

[3]We're not really sorry. But, we are sorry about not being sorry, if that makes sense.

References

[KE+62] "One-level Storage System" by T. Kilburn, D.B.G. Edwards, M.J. Lanigan, F.H. Sumner. IRE Trans. EC-11, 2, 1962. Reprinted in Bell and Newell, "Computer Structures: Readings and Examples". McGraw-Hill, New York, 1971. *The Atlas pioneered the idea of dividing memory into fixed-sized pages and in many senses was an early form of the memory-management ideas we see in modern computer systems.*

[I09] "Intel 64 and IA-32 Architectures Software Developer's Manuals" Intel, 2009. Available: http://www.intel.com/products/processor/manuals. *In particular, pay attention to "Volume 3A: System Programming Guide Part 1" and "Volume 3B: System Programming Guide Part 2".*

[L78] "The Manchester Mark I and Atlas: A Historical Perspective" by S. H. Lavington. Communications of the ACM, Volume 21:1, January 1978. *This paper is a great retrospective of some of the history of the development of some important computer systems. As we sometimes forget in the US, many of these new ideas came from overseas.*

Homework (Simulation)

In this homework, you will use a simple program, which is known as `paging-linear-translate.py`, to see if you understand how simple virtual-to-physical address translation works with linear page tables. See the README for details.

Questions

1. Before doing any translations, let's use the simulator to study how linear page tables change size given different parameters. Compute the size of linear page tables as different parameters change. Some suggested inputs are below; by using the `-v flag`, you can see how many page-table entries are filled. First, to understand how linear page table size changes as the address space grows, run with these flags:

   ```
   -P 1k -a 1m -p 512m -v -n 0
   -P 1k -a 2m -p 512m -v -n 0
   -P 1k -a 4m -p 512m -v -n 0
   ```

   Then, to understand how linear page table size changes as page size grows:

   ```
   -P 1k -a 1m -p 512m -v -n 0
   -P 2k -a 1m -p 512m -v -n 0
   -P 4k -a 1m -p 512m -v -n 0
   ```

   Before running any of these, try to think about the expected trends. How should page-table size change as the address space grows? As the page size grows? Why not use big pages in general?

2. Now let's do some translations. Start with some small examples, and change the number of pages that are allocated to the address space with the `-u flag`. For example:

   ```
   -P 1k -a 16k -p 32k -v -u 0
   -P 1k -a 16k -p 32k -v -u 25
   -P 1k -a 16k -p 32k -v -u 50
   -P 1k -a 16k -p 32k -v -u 75
   -P 1k -a 16k -p 32k -v -u 100
   ```

   What happens as you increase the percentage of pages that are allocated in each address space?

3. Now let's try some different random seeds, and some different (and sometimes quite crazy) address-space parameters, for variety:

```
-P 8  -a 32   -p 1024 -v -s 1
-P 8k -a 32k  -p 1m   -v -s 2
-P 1m -a 256m -p 512m -v -s 3
```

Which of these parameter combinations are unrealistic? Why?

4. Use the program to try out some other problems. Can you find the limits of where the program doesn't work anymore? For example, what happens if the address-space size is *bigger* than physical memory?

19

Paging: Faster Translations (TLBs)

Using paging as the core mechanism to support virtual memory can lead to high performance overheads. By chopping the address space into small, fixed-sized units (i.e., pages), paging requires a large amount of mapping information. Because that mapping information is generally stored in physical memory, paging logically requires an extra memory lookup for each virtual address generated by the program. Going to memory for translation information before every instruction fetch or explicit load or store is prohibitively slow. And thus our problem:

> THE CRUX:
> HOW TO SPEED UP ADDRESS TRANSLATION
>
> How can we speed up address translation, and generally avoid the extra memory reference that paging seems to require? What hardware support is required? What OS involvement is needed?

When we want to make things fast, the OS usually needs some help. And help often comes from the OS's old friend: the hardware. To speed address translation, we are going to add what is called (for historical reasons [CP78]) a **translation-lookaside buffer**, or **TLB** [CG68, C95]. A TLB is part of the chip's **memory-management unit** (**MMU**), and is simply a hardware **cache** of popular virtual-to-physical address translations; thus, a better name would be an **address-translation cache**. Upon each virtual memory reference, the hardware first checks the TLB to see if the desired translation is held therein; if so, the translation is performed (quickly) *without* having to consult the page table (which has all translations). Because of their tremendous performance impact, TLBs in a real sense make virtual memory possible [C95].

```
1  VPN = (VirtualAddress & VPN_MASK) >> SHIFT
2  (Success, TlbEntry) = TLB_Lookup(VPN)
3  if (Success == True)   // TLB Hit
4      if (CanAccess(TlbEntry.ProtectBits) == True)
5          Offset   = VirtualAddress & OFFSET_MASK
6          PhysAddr = (TlbEntry.PFN << SHIFT) | Offset
7          Register = AccessMemory(PhysAddr)
8      else
9          RaiseException(PROTECTION_FAULT)
10 else                  // TLB Miss
11     PTEAddr = PTBR + (VPN * sizeof(PTE))
12     PTE = AccessMemory(PTEAddr)
13     if (PTE.Valid == False)
14         RaiseException(SEGMENTATION_FAULT)
15     else if (CanAccess(PTE.ProtectBits) == False)
16         RaiseException(PROTECTION_FAULT)
17     else
18         TLB_Insert(VPN, PTE.PFN, PTE.ProtectBits)
19         RetryInstruction()
```

Figure 19.1: **TLB Control Flow Algorithm**

19.1 TLB Basic Algorithm

Figure 19.1 shows a rough sketch of how hardware might handle a virtual address translation, assuming a simple **linear page table** (i.e., the page table is an array) and a **hardware-managed TLB** (i.e., the hardware handles much of the responsibility of page table accesses; we'll explain more about this below).

The algorithm the hardware follows works like this: first, extract the virtual page number (VPN) from the virtual address (Line 1 in Figure 19.1), and check if the TLB holds the translation for this VPN (Line 2). If it does, we have a **TLB hit**, which means the TLB holds the translation. Success! We can now extract the page frame number (PFN) from the relevant TLB entry, concatenate that onto the offset from the original virtual address, and form the desired physical address (PA), and access memory (Lines 5–7), assuming protection checks do not fail (Line 4).

If the CPU does not find the translation in the TLB (a **TLB miss**), we have some more work to do. In this example, the hardware accesses the page table to find the translation (Lines 11–12), and, assuming that the virtual memory reference generated by the process is valid and accessible (Lines 13, 15), updates the TLB with the translation (Line 18). These set of actions are costly, primarily because of the extra memory reference needed to access the page table (Line 12). Finally, once the TLB is updated, the hardware retries the instruction; this time, the translation is found in the TLB, and the memory reference is processed quickly.

The TLB, like all caches, is built on the premise that in the common case, translations are found in the cache (i.e., are hits). If so, little overhead is added, as the TLB is found near the processing core and is designed to be quite fast. When a miss occurs, the high cost of paging is incurred; the page table must be accessed to find the translation, and an extra memory reference (or more, with more complex page tables) results. If this happens often, the program will likely run noticeably more slowly; memory accesses, relative to most CPU instructions, are quite costly, and TLB misses lead to more memory accesses. Thus, it is our hope to avoid TLB misses as much as we can.

19.2 Example: Accessing An Array

To make clear the operation of a TLB, let's examine a simple virtual address trace and see how a TLB can improve its performance. In this example, let's assume we have an array of 10 4-byte integers in memory, starting at virtual address 100. Assume further that we have a small 8-bit virtual address space, with 16-byte pages; thus, a virtual address breaks down into a 4-bit VPN (there are 16 virtual pages) and a 4-bit offset (there are 16 bytes on each of those pages).

Figure 19.2 (page 4) shows the array laid out on the 16 16-byte pages of the system. As you can see, the array's first entry (`a[0]`) begins on (VPN=06, offset=04); only three 4-byte integers fit onto that page. The array continues onto the next page (VPN=07), where the next four entries (`a[3]` ... `a[6]`) are found. Finally, the last three entries of the 10-entry array (`a[7]` ... `a[9]`) are located on the next page of the address space (VPN=08).

Now let's consider a simple loop that accesses each array element, something that would look like this in C:

```
int sum = 0;
for (i = 0; i < 10; i++) {
    sum += a[i];
}
```

For the sake of simplicity, we will pretend that the only memory accesses the loop generates are to the array (ignoring the variables `i` and `sum`, as well as the instructions themselves). When the first array element (`a[0]`) is accessed, the CPU will see a load to virtual address 100. The hardware extracts the VPN from this (VPN=06), and uses that to check the TLB for a valid translation. Assuming this is the first time the program accesses the array, the result will be a TLB miss.

The next access is to `a[1]`, and there is some good news here: a TLB hit! Because the second element of the array is packed next to the first, it lives on the same page; because we've already accessed this page when accessing the first element of the array, the translation is already loaded

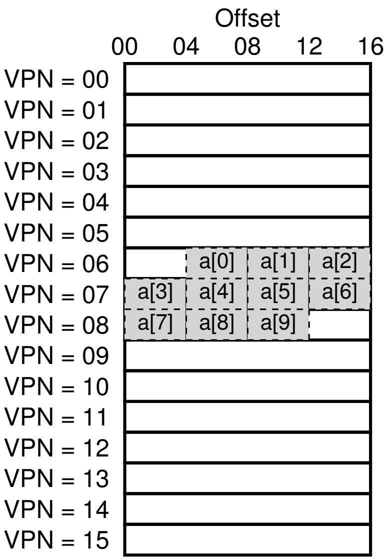


Figure 19.2: **Example: An Array In A Tiny Address Space**

into the TLB. And hence the reason for our success. Access to `a[2]` encounters similar success (another hit), because it too lives on the same page as `a[0]` and `a[1]`.

Unfortunately, when the program accesses `a[3]`, we encounter another TLB miss. However, once again, the next entries (`a[4]` ... `a[6]`) will hit in the TLB, as they all reside on the same page in memory.

Finally, access to `a[7]` causes one last TLB miss. The hardware once again consults the page table to figure out the location of this virtual page in physical memory, and updates the TLB accordingly. The final two accesses (`a[8]` and `a[9]`) receive the benefits of this TLB update; when the hardware looks in the TLB for their translations, two more hits result.

Let us summarize TLB activity during our ten accesses to the array: **miss**, hit, hit, **miss**, hit, hit, hit, **miss**, hit, hit. Thus, our TLB **hit rate**, which is the number of hits divided by the total number of accesses, is 70%. Although this is not too high (indeed, we desire hit rates that approach 100%), it is non-zero, which may be a surprise. Even though this is the first time the program accesses the array, the TLB improves performance due to **spatial locality**. The elements of the array are packed tightly into pages (i.e., they are close to one another in **space**), and thus only the first access to an element on a page yields a TLB miss.

Also note the role that page size plays in this example. If the page size

TIP: USE CACHING WHEN POSSIBLE

Caching is one of the most fundamental performance techniques in computer systems, one that is used again and again to make the "common-case fast" [HP06]. The idea behind hardware caches is to take advantage of **locality** in instruction and data references. There are usually two types of locality: **temporal locality** and **spatial locality**. With temporal locality, the idea is that an instruction or data item that has been recently accessed will likely be re-accessed soon in the future. Think of loop variables or instructions in a loop; they are accessed repeatedly over time. With spatial locality, the idea is that if a program accesses memory at address x, it will likely soon access memory near x. Imagine here streaming through an array of some kind, accessing one element and then the next. Of course, these properties depend on the exact nature of the program, and thus are not hard-and-fast laws but more like rules of thumb.

Hardware caches, whether for instructions, data, or address translations (as in our TLB) take advantage of locality by keeping copies of memory in small, fast on-chip memory. Instead of having to go to a (slow) memory to satisfy a request, the processor can first check if a nearby copy exists in a cache; if it does, the processor can access it quickly (i.e., in a few CPU cycles) and avoid spending the costly time it takes to access memory (many nanoseconds).

You might be wondering: if caches (like the TLB) are so great, why don't we just make bigger caches and keep all of our data in them? Unfortunately, this is where we run into more fundamental laws like those of physics. If you want a fast cache, it has to be small, as issues like the speed-of-light and other physical constraints become relevant. Any large cache by definition is slow, and thus defeats the purpose. Thus, we are stuck with small, fast caches; the question that remains is how to best use them to improve performance.

had simply been twice as big (32 bytes, not 16), the array access would suffer even fewer misses. As typical page sizes are more like 4KB, these types of dense, array-based accesses achieve excellent TLB performance, encountering only a single miss per page of accesses.

One last point about TLB performance: if the program, soon after this loop completes, accesses the array again, we'd likely see an even better result, assuming that we have a big enough TLB to cache the needed translations: hit, hit, hit, hit, hit, hit, hit, hit, hit, hit. In this case, the TLB hit rate would be high because of **temporal locality**, i.e., the quick re-referencing of memory items in **time**. Like any cache, TLBs rely upon both spatial and temporal locality for success, which are program properties. If the program of interest exhibits such locality (and many programs do), the TLB hit rate will likely be high.

```
1  VPN = (VirtualAddress & VPN_MASK) >> SHIFT
2  (Success, TlbEntry) = TLB_Lookup(VPN)
3  if (Success == True)    // TLB Hit
4      if (CanAccess(TlbEntry.ProtectBits) == True)
5          Offset   = VirtualAddress & OFFSET_MASK
6          PhysAddr = (TlbEntry.PFN << SHIFT) | Offset
7          Register = AccessMemory(PhysAddr)
8      else
9          RaiseException(PROTECTION_FAULT)
10 else                      // TLB Miss
11     RaiseException(TLB_MISS)
```

Figure 19.3: **TLB Control Flow Algorithm (OS Handled)**

19.3 Who Handles The TLB Miss?

One question that we must answer: who handles a TLB miss? Two answers are possible: the hardware, or the software (OS). In the olden days, the hardware had complex instruction sets (sometimes called **CISC**, for complex-instruction set computers) and the people who built the hardware didn't much trust those sneaky OS people. Thus, the hardware would handle the TLB miss entirely. To do this, the hardware has to know exactly *where* the page tables are located in memory (via a **page-table base register**, used in Line 11 in Figure 19.1), as well as their *exact format*; on a miss, the hardware would "walk" the page table, find the correct page-table entry and extract the desired translation, update the TLB with the translation, and retry the instruction. An example of an "older" architecture that has **hardware-managed TLBs** is the Intel x86 architecture, which uses a fixed **multi-level page table** (see the next chapter for details); the current page table is pointed to by the CR3 register [I09].

More modern architectures (e.g., MIPS R10k [H93] or Sun's SPARC v9 [WG00], both **RISC** or reduced-instruction set computers) have what is known as a **software-managed TLB**. On a TLB miss, the hardware simply raises an exception (line 11 in Figure 19.3), which pauses the current instruction stream, raises the privilege level to kernel mode, and jumps to a **trap handler**. As you might guess, this trap handler is code within the OS that is written with the express purpose of handling TLB misses. When run, the code will lookup the translation in the page table, use special "privileged" instructions to update the TLB, and return from the trap; at this point, the hardware retries the instruction (resulting in a TLB hit).

Let's discuss a couple of important details. First, the return-from-trap instruction needs to be a little different than the return-from-trap we saw before when servicing a system call. In the latter case, the return-from-trap should resume execution at the instruction *after* the trap into the OS, just as a return from a procedure call returns to the instruction immediately following the call into the procedure. In the former case, when returning from a TLB miss-handling trap, the hardware must resume execution at the instruction that *caused* the trap; this retry thus lets the in-

How are they different?

ASIDE: RISC VS. CISC

In the 1980's, a great battle took place in the computer architecture community. On one side was the **CISC** camp, which stood for **Complex Instruction Set Computing**; on the other side was **RISC**, for **Reduced Instruction Set Computing** [PS81]. The RISC side was spear-headed by David Patterson at Berkeley and John Hennessy at Stanford (who are also co-authors of some famous books [HP06]), although later John Cocke was recognized with a Turing award for his earliest work on RISC [CM00].

CISC instruction sets tend to have a lot of instructions in them, and each instruction is relatively powerful. For example, you might see a string copy, which takes two pointers and a length and copies bytes from source to destination. The idea behind CISC was that instructions should be high-level primitives, to make the assembly language itself easier to use, and to make code more compact.

RISC instruction sets are exactly the opposite. A key observation behind RISC is that instruction sets are really compiler targets, and all compilers really want are a few simple primitives that they can use to generate high-performance code. Thus, RISC proponents argued, let's rip out as much from the hardware as possible (especially the microcode), and make what's left simple, uniform, and fast.

In the early days, RISC chips made a huge impact, as they were noticeably faster [BC91]; many papers were written; a few companies were formed (e.g., MIPS and Sun). However, as time progressed, CISC manufacturers such as Intel incorporated many RISC techniques into the core of their processors, for example by adding early pipeline stages that transformed complex instructions into micro-instructions which could then be processed in a RISC-like manner. These innovations, plus a growing number of transistors on each chip, allowed CISC to remain competitive. The end result is that the debate died down, and today both types of processors can be made to run fast.

struction run again, this time resulting in a TLB hit. Thus, depending on how a trap or exception was caused, the hardware must save a different PC when trapping into the OS, in order to resume properly when the time to do so arrives.

Second, when running the TLB miss-handling code, the OS needs to be extra careful not to cause an infinite chain of TLB misses to occur. Many solutions exist; for example, you could keep TLB miss handlers in physical memory (where they are **unmapped** and not subject to address translation), or reserve some entries in the TLB for permanently-valid translations and use some of those permanent translation slots for the handler code itself; these **wired** translations always hit in the TLB.

Isse kya hoga?

The primary advantage of the software-managed approach is *flexibility*: the OS can use any data structure it wants to implement the page

main diff
not clear?

ASIDE: TLB VALID BIT $\neq$ PAGE TABLE VALID BIT

A common mistake is to confuse the valid bits found in a TLB with those found in a page table. In a page table, when a page-table entry (PTE) is marked invalid, it means that the page has not been allocated by the process, and should not be accessed by a correctly-working program. The usual response when an invalid page is accessed is to trap to the OS, which will respond by killing the process.

A TLB valid bit, in contrast, simply refers to whether a TLB entry has a valid translation within it. When a system boots, for example, a common initial state for each TLB entry is to be set to invalid, because no address translations are yet cached there. Once virtual memory is enabled, and once programs start running and accessing their virtual address spaces, the TLB is slowly populated, and thus valid entries soon fill the TLB.

The TLB valid bit is quite useful when performing a context switch too, as we'll discuss further below. By setting all TLB entries to invalid, the system can ensure that the about-to-be-run process does not accidentally use a virtual-to-physical translation from a previous process.

table, without necessitating hardware change. Another advantage is *simplicity*, as seen in the TLB control flow (line 11 in Figure 19.3, in contrast to lines 11–19 in Figure 19.1). The hardware doesn't do much on a miss: just raise an exception and let the OS TLB miss handler do the rest.

19.4 TLB Contents: What's In There?

Let's look at the contents of the hardware TLB in more detail. A typical TLB might have 32, 64, or 128 entries and be what is called **fully associative**. Basically, this just means that any given translation can be anywhere in the TLB, and that the hardware will search the entire TLB in parallel to find the desired translation. A TLB entry might look like this:

VPN | PFN | other bits

Note that both the VPN and PFN are present in each entry, as a translation could end up in any of these locations (in hardware terms, the TLB is known as a **fully-associative** cache). The hardware searches the entries in parallel to see if there is a match.

More interesting are the "other bits". For example, the TLB commonly has a **valid** bit, which says whether the entry has a valid translation or not. Also common are **protection** bits, which determine how a page can be accessed (as in the page table). For example, code pages might be marked *read and execute*, whereas heap pages might be marked *read and write*. There may also be a few other fields, including an **address-space identifier**, a **dirty bit**, and so forth; see below for more information.

19.5 TLB Issue: Context Switches

With TLBs, some new issues arise when switching between processes (and hence address spaces). Specifically, the TLB contains virtual-to-physical translations that are only valid for the currently running process; these translations are not meaningful for other processes. As a result, when switching from one process to another, the hardware or OS (or both) must be careful to ensure that the about-to-be-run process does not accidentally use translations from some previously run process.

To understand this situation better, let's look at an example. When one process (P1) is running, it assumes the TLB might be caching translations that are valid for it, i.e., that come from P1's page table. Assume, for this example, that the 10th virtual page of P1 is mapped to physical frame 100.

In this example, assume another process (P2) exists, and the OS soon might decide to perform a context switch and run it. Assume here that the 10th virtual page of P2 is mapped to physical frame 170. If entries for both processes were in the TLB, the contents of the TLB would be:

VPN	PFN	valid	prot
10	100	1	rwx
—	—	0	—
10	170	1	rwx
—	—	0	—

In the TLB above, we clearly have a problem: VPN 10 translates to either PFN 100 (P1) or PFN 170 (P2), but the hardware can't distinguish which entry is meant for which process. Thus, we need to do some more work in order for the TLB to correctly and efficiently support virtualization across multiple processes. And thus, a crux:

> THE CRUX:
> HOW TO MANAGE TLB CONTENTS ON A CONTEXT SWITCH
> When context-switching between processes, the translations in the TLB for the last process are not meaningful to the about-to-be-run process. What should the hardware or OS do in order to solve this problem?

There are a number of possible solutions to this problem. One approach is to simply **flush** the TLB on context switches, thus emptying it before running the next process. On a software-based system, this can be accomplished with an explicit (and privileged) hardware instruction; with a hardware-managed TLB, the flush could be enacted when the page-table base register is changed (note the OS must change the PTBR on a context switch anyhow). In either case, the flush operation simply sets all valid bits to 0, essentially clearing the contents of the TLB.

By flushing the TLB on each context switch, we now have a working solution, as a process will never accidentally encounter the wrong translations in the TLB. However, there is a cost: each time a process runs, it must incur TLB misses as it touches its data and code pages. If the OS switches between processes frequently, this cost may be high.

To reduce this overhead, some systems add hardware support to enable sharing of the TLB across context switches. In particular, some hardware systems provide an **address space identifier** (**ASID**) field in the TLB. You can think of the ASID as a **process identifier** (**PID**), but usually it has fewer bits (e.g., 8 bits for the ASID versus 32 bits for a PID).

If we take our example TLB from above and add ASIDs, it is clear processes can readily share the TLB: only the ASID field is needed to differentiate otherwise identical translations. Here is a depiction of a TLB with the added ASID field:

VPN	PFN	valid	prot	ASID
10	100	1	rwx	1
—	—	0	—	—
10	170	1	rwx	2
—	—	0	—	—

Thus, with address-space identifiers, the TLB can hold translations from different processes at the same time without any confusion. Of course, the hardware also needs to know which process is currently running in order to perform translations, and thus the OS must, on a context switch, set some privileged register to the ASID of the current process.

As an aside, you may also have thought of another case where two entries of the TLB are remarkably similar. In this example, there are two entries for two different processes with two different VPNs that point to the *same* physical page:

VPN	PFN	valid	prot	ASID
10	101	1	r-x	1
—	—	0	—	—
50	101	1	r-x	2
—	—	0	—	—

This situation might arise, for example, when two processes *share* a page (a code page, for example). In the example above, Process 1 is sharing physical page 101 with Process 2; P1 maps this page into the 10th page of its address space, whereas P2 maps it to the 50th page of its address space. Sharing of code pages (in binaries, or shared libraries) is useful as it reduces the number of physical pages in use, thus reducing memory overheads.

19.6 Issue: Replacement Policy

As with any cache, and thus also with the TLB, one more issue that we must consider is **cache replacement**. Specifically, when we are installing a new entry in the TLB, we have to **replace** an old one, and thus the question: which one to replace?

> THE CRUX: HOW TO DESIGN TLB REPLACEMENT POLICY
>
> Which TLB entry should be replaced when we add a new TLB entry? The goal, of course, being to minimize the **miss rate** (or increase **hit rate**) and thus improve performance.

We will study such policies in some detail when we tackle the problem of swapping pages to disk; here we'll just highlight a few typical policies. One common approach is to evict the **least-recently-used** or **LRU** entry. LRU tries to take advantage of locality in the memory-reference stream, assuming it is likely that an entry that has not recently been used is a good candidate for eviction. Another typical approach is to use a **random** policy, which evicts a TLB mapping at random. Such a policy is useful due to its simplicity and ability to avoid corner-case behaviors; for example, a "reasonable" policy such as LRU behaves quite unreasonably when a program loops over $n + 1$ pages with a TLB of size n; in this case, LRU misses upon every access, whereas random does much better.

19.7 A Real TLB Entry

Finally, let's briefly look at a real TLB. This example is from the MIPS R4000 [H93], a modern system that uses software-managed TLBs; a slightly simplified MIPS TLB entry can be seen in Figure 19.4.

The MIPS R4000 supports a 32-bit address space with 4KB pages. Thus, we would expect a 20-bit VPN and 12-bit offset in our typical virtual address. However, as you can see in the TLB, there are only 19 bits for the VPN; as it turns out, user addresses will only come from half the address space (the rest reserved for the kernel) and hence only 19 bits of VPN are needed. The VPN translates to up to a 24-bit physical frame number (PFN), and hence can support systems with up to 64GB of (physical) main memory (2^{24} 4KB pages).

There are a few other interesting bits in the MIPS TLB. We see a *global* bit (G), which is used for pages that are globally-shared among processes. Thus, if the global bit is set, the ASID is ignored. We also see the 8-bit *ASID*, which the OS can use to distinguish between address spaces (as

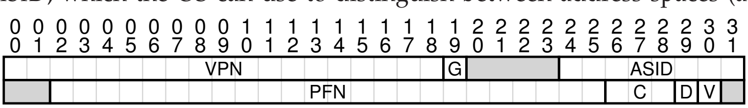


Figure 19.4: **A MIPS TLB Entry**

TIP: RAM ISN'T ALWAYS RAM (CULLER'S LAW)

The term **random-access memory**, or **RAM**, implies that you can access any part of RAM just as quickly as another. While it is generally good to think of RAM in this way, because of hardware/OS features such as the TLB, accessing a particular page of memory may be costly, particularly if that page isn't currently mapped by your TLB. Thus, it is always good to remember the implementation tip: **RAM isn't always RAM**. Sometimes randomly accessing your address space, particularly if the number of pages accessed exceeds the TLB coverage, can lead to severe performance penalties. Because one of our advisors, David Culler, used to always point to the TLB as the source of many performance problems, we name this law in his honor: **Culler's Law**.

described above). One question for you: what should the OS do if there are more than 256 (2^8) processes running at a time? Finally, we see 3 *Coherence* (C) bits, which determine how a page is cached by the hardware (a bit beyond the scope of these notes); a *dirty* bit which is marked when the page has been written to (we'll see the use of this later); a *valid* bit which tells the hardware if there is a valid translation present in the entry. There is also a *page mask* field (not shown), which supports multiple page sizes; we'll see later why having larger pages might be useful. Finally, some of the 64 bits are unused (shaded gray in the diagram).

MIPS TLBs usually have 32 or 64 of these entries, most of which are used by user processes as they run. However, a few are reserved for the OS. A *wired* register can be set by the OS to tell the hardware how many slots of the TLB to reserve for the OS; the OS uses these reserved mappings for code and data that it wants to access during critical times, where a TLB miss would be problematic (e.g., in the TLB miss handler).

Because the MIPS TLB is software managed, there needs to be instructions to update the TLB. The MIPS provides four such instructions: `TLBP`, which probes the TLB to see if a particular translation is in there; `TLBR`, which reads the contents of a TLB entry into registers; `TLBWI`, which replaces a specific TLB entry; and `TLBWR`, which replaces a random TLB entry. The OS uses these instructions to manage the TLB's contents. It is of course critical that these instructions are **privileged**; imagine what a user process could do if it could modify the contents of the TLB (hint: just about anything, including take over the machine, run its own malicious "OS", or even make the Sun disappear).

19.8 Summary

We have seen how hardware can help us make address translation faster. By providing a small, dedicated on-chip TLB as an address-translation cache, most memory references will hopefully be handled *without* having to access the page table in main memory. Thus, in the common case, the performance of the program will be almost as if memory isn't being virtualized at all, an excellent achievement for an operating system, and certainly essential to the use of paging in modern systems.

However, TLBs do not make the world rosy for every program that exists. In particular, if the number of pages a program accesses in a short period of time exceeds the number of pages that fit into the TLB, the program will generate a large number of TLB misses, and thus run quite a bit more slowly. We refer to this phenomenon as exceeding the **TLB coverage**, and it can be quite a problem for certain programs. One solution, as we'll discuss in the next chapter, is to include support for larger page sizes; by mapping key data structures into regions of the program's address space that are mapped by larger pages, the effective coverage of the TLB can be increased. Support for large pages is often exploited by programs such as a **database management system** (a **DBMS**), which have certain data structures that are both large and randomly-accessed.

One other TLB issue worth mentioning: TLB access can easily become a bottleneck in the CPU pipeline, in particular with what is called a **physically-indexed cache**. With such a cache, address translation has to take place *before* the cache is accessed, which can slow things down quite a bit. Because of this potential problem, people have looked into all sorts of clever ways to access caches with *virtual* addresses, thus avoiding the expensive step of translation in the case of a cache hit. Such a **virtually-indexed cache** solves some performance problems, but introduces new issues into hardware design as well. See Wiggins's fine survey for more details [W03].

References

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[CM00] "The evolution of RISC technology at IBM" by John Cocke, V. Markstein. IBM Journal of Research and Development, 44:1/2. *A summary of the ideas and work behind the IBM 801, which many consider the first true RISC microprocessor.*

[C95] "The Core of the Black Canyon Computer Corporation" by John Couleur. IEEE Annals of History of Computing, 17:4, 1995. *In this fascinating historical note, Couleur talks about how he invented the TLB in 1964 while working for GE, and the fortuitous collaboration that thus ensued with the Project MAC folks at MIT.*

[CG68] "Shared-access Data Processing System" by John F. Couleur, Edward L. Glaser. Patent 3412382, November 1968. *The patent that contains the idea for an associative memory to store address translations. The idea, according to Couleur, came in 1964.*

[CP78] "The architecture of the IBM System/370" by R.P. Case, A. Padegs. Communications of the ACM. 21:1, 73-96, January 1978. *Perhaps the first paper to use the term **translation lookaside buffer**. The name arises from the historical name for a cache, which was a **lookaside buffer** as called by those developing the Atlas system at the University of Manchester; a cache of address translations thus became a **translation lookaside buffer**. Even though the term lookaside buffer fell out of favor, TLB seems to have stuck, for whatever reason.*

[H93] "MIPS R4000 Microprocessor User's Manual". by Joe Heinrich. Prentice-Hall, June 1993. Available: http://cag.csail.mit.edu/raw/ . documents/R4400_Uman_book_Ed2.pdf *A manual, one that is surprisingly readable. Or is it?*

[HP06] "Computer Architecture: A Quantitative Approach" by John Hennessy and David Patterson. Morgan-Kaufmann, 2006. *A great book about computer architecture. We have a particular attachment to the classic first edition.*

[I09] "Intel 64 and IA-32 Architectures Software Developer's Manuals" by Intel, 2009. Available: http://www.intel.com/products/processor/manuals. *In particular, pay attention to "Volume 3A: System Programming Guide" Part 1* and "Volume 3B: System Programming Guide Part 2".

[PS81] "RISC-I: A Reduced Instruction Set VLSI Computer" by D.A. Patterson and C.H. Sequin. ISCA '81, Minneapolis, May 1981. *The paper that introduced the term RISC, and started the avalanche of research into simplifying computer chips for performance.*

[SB92] "CPU Performance Evaluation and Execution Time Prediction Using Narrow Spectrum Benchmarking" by Rafael H. Saavedra-Barrera. EECS Department, University of California, Berkeley. Technical Report No. UCB/CSD-92-684, February 1992.. *A great dissertation about how to predict execution time of applications by breaking them down into constituent pieces and knowing the cost of each piece. Probably the most interesting part that comes out of this work is the tool to measure details of the cache hierarchy (described in Chapter 5). Make sure to check out the wonderful diagrams therein.*

[W03] "A Survey on the Interaction Between Caching, Translation and Protection" by Adam Wiggins. University of New South Wales TR UNSW-CSE-TR-0321, August, 2003. *An excellent survey of how TLBs interact with other parts of the CPU pipeline, namely hardware caches.*

[WG00] "The SPARC Architecture Manual: Version 9" by David L. Weaver and Tom Germond. SPARC International, San Jose, California, September 2000. Available: `www.sparc.org/standards/SPARCV9.pdf`. *Another manual. I bet you were hoping for a more fun citation to end this chapter.*

Homework (Measurement)

In this homework, you are to measure the size and cost of accessing a TLB. The idea is based on work by Saavedra-Barrera [SB92], who developed a simple but beautiful method to measure numerous aspects of cache hierarchies, all with a very simple user-level program. Read his work for more details.

The basic idea is to access some number of pages within a large data structure (e.g., an array) and to time those accesses. For example, let's say the TLB size of a machine happens to be 4 (which would be very small, but useful for the purposes of this discussion). If you write a program that touches 4 or fewer pages, each access should be a TLB hit, and thus relatively fast. However, once you touch 5 pages or more, repeatedly in a loop, each access will suddenly jump in cost, to that of a TLB miss.

The basic code to loop through an array once should look like this:

```
int jump = PAGESIZE / sizeof(int);
for (i = 0; i < NUMPAGES * jump; i += jump)
    a[i] += 1;
```

In this loop, one integer per page of the array `a` is updated, up to the number of pages specified by `NUMPAGES`. By timing such a loop repeatedly (say, a few hundred million times in another loop around this one, or however many loops are needed to run for a few seconds), you can time how long each access takes (on average). By looking for jumps in cost as `NUMPAGES` increases, you can roughly determine how big the first-level TLB is, determine whether a second-level TLB exists (and how big it is if it does), and in general get a good sense of how TLB hits and misses can affect performance.

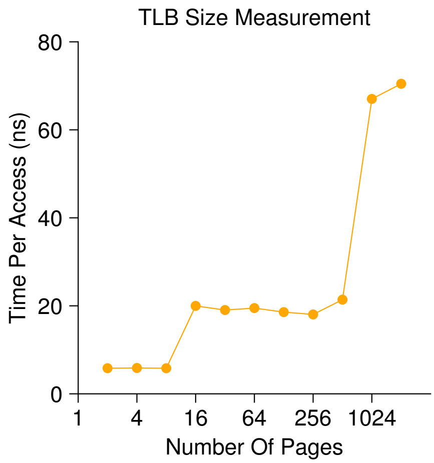

Figure 19.5: **Discovering TLB Sizes and Miss Costs**

Figure 19.5 (page 15) shows the average time per access as the number of pages accessed in the loop is increased. As you can see in the graph, when just a few pages are accessed (8 or fewer), the average access time is roughly 5 nanoseconds. When 16 or more pages are accessed, there is a sudden jump to about 20 nanoseconds per access. A final jump in cost occurs at around 1024 pages, at which point each access takes around 70 nanoseconds. From this data, we can conclude that there is a two-level TLB hierarchy; the first is quite small (probably holding between 8 and 16 entries); the second is larger but slower (holding roughly 512 entries). The overall difference between hits in the first-level TLB and misses is quite large, roughly a factor of fourteen. TLB performance matters!

Questions

1. For timing, you'll need to use a timer (e.g., `gettimeofday()`). How precise is such a timer? How long does an operation have to take in order for you to time it precisely? (this will help determine how many times, in a loop, you'll have to repeat a page access in order to time it successfully)
2. Write the program, called `tlb.c`, that can roughly measure the cost of accessing each page. Inputs to the program should be: the number of pages to touch and the number of trials.
3. Now write a script in your favorite scripting language (bash?) to run this program, while varying the number of pages accessed from 1 up to a few thousand, perhaps incrementing by a factor of two per iteration. Run the script on different machines and gather some data. How many trials are needed to get reliable measurements?
4. Next, graph the results, making a graph that looks similar to the one above. Use a good tool like `ploticus` or even `zplot`. Visualization usually makes the data much easier to digest; why do you think that is?
5. One thing to watch out for is compiler optimization. Compilers do all sorts of clever things, including removing loops which increment values that no other part of the program subsequently uses. How can you ensure the compiler does not remove the main loop above from your TLB size estimator?
6. Another thing to watch out for is the fact that most systems today ship with multiple CPUs, and each CPU, of course, has its own TLB hierarchy. To really get good measurements, you have to run your code on just one CPU, instead of letting the scheduler bounce it from one CPU to the next. How can you do that? (hint: look up "pinning a thread" on Google for some clues) What will happen if you don't do this, and the code moves from one CPU to the other?
7. Another issue that might arise relates to initialization. If you don't initialize the array `a` above before accessing it, the first time you access it will be very expensive, due to initial access costs such as demand zeroing. Will this affect your code and its timing? What can you do to counterbalance these potential costs?