

a) Stationary: $\left(\frac{\partial L}{\partial Q_1}, \frac{\partial L}{\partial Q_2} \right) = 0$

$$\therefore \frac{\partial L}{\partial Q_1} = 1 + 2\lambda Q_1, \quad \frac{\partial L}{\partial Q_2} = 2 + 8\lambda Q_2$$

$$\therefore [1 + 2\lambda Q_1, 2 + 8\lambda Q_2] = 0$$

b) Complementary slackness:

$$\lambda (Q_1^2 + 4Q_2^2 - 4) = 0$$

c) Primal feasibility:

$$Q_1^2 + 4Q_2^2 - 4 \leq 0$$

d) Dual feasibility:

$$\lambda \geq 0$$

Ans.