

Multiplying Large Integers Problems

- The positional numeral system is not convenient for performing multiplication of large integers.

The generalize formula is :-

$$c = a * b$$

$$C = C_2 10^n + C_1 10^{n/2} + C_0$$

where n is the no. of digits in the integer

$$C_2 = a_1 * b_1$$

$$C_0 = a_0 * b_0$$

$$C_1 = (a_1 + a_0) * (b_1 + b_0) - (C_2 + C_0)$$

The two digit no. are

$$a = a_1 a_0$$

$$b = b_1 b_0$$

Example

Input no. 12 and 20

$$\therefore a = 12$$

$$b = 20$$

$$\text{where } a_1 = 1, a_0 = 2$$

$$b_1 = 2, b_0 = 0$$

Now, find C_1, C_2, C_0

$$\begin{aligned}\rightarrow c_2 &= a_1 * b_1 \\ &= 1 * 2 \\ &= 2\end{aligned}$$

$$\boxed{c_2 = 2}$$

$$\begin{aligned}\rightarrow c_0 &= a_0 * b_0 \\ &= 2 * 0 \\ &= 0\end{aligned}$$

$$\boxed{c_0 = 0}$$

$$\begin{aligned}\rightarrow c_1 &= (a_1 + a_0) * (b_1 + b_0) - (c_2 + c_0) \\ &= (1 + 2) * (2 + 0) - (2 + 0) \\ &= 3 * 2 - 2 \\ &= 4\end{aligned}$$

$$\boxed{c_1 = 4}$$

$$\begin{aligned}\rightarrow a * b &= c_2 10^2 + c_1 10^1 + c_0 \\ &= 2 \times 10^2 + 4 \times 10^1 + 0 \\ &= 200 + 40 + 0\end{aligned}$$

$$\boxed{a * b = 240}$$