

## $\Rightarrow$ 0/1 Knapsack Problem

$n$  = number of objects

$W$  = Capacity of knapsack

Table =  $v(1 \dots n, 0 \dots W)$  [ $v[i][j]$ ]

- ① Make  $v[i][0] = 0$  for  $0 \leq i \leq n$
- ② if  $j < w_i$  then take  $v[i][j] = v[i-1][j]$
- ③ if  $j \geq w_i$  then take  $v[i][j] = \max(v[i-1][j], v[i-1][j - w_i] + v_i)$

### Example

Item	weight	value
1	1	1
2	2	6
3	5	18
4	6	22
5	7	28

		$\rightarrow$	0	1	2	3	4	5	6	7	8	9	10	11
	$\downarrow i$	0	0	0	0	0	0	0	0	0	0	0	0	0
$w_1=1$	$v_1=1$	1	0	1	1	1	1	1	1	1	1	1	1	1
$w_2=2$	$v_2=6$	2	0	1	6	7	7	7	7	7	7	7	7	7
$w_3=5$	$v_3=18$	3	0	1	6	7	7	18	19	24	25	25	25	25
$w_4=6$	$v_4=22$	4	0	1	6	7	7	18	22	24	28	29	29	40
$w_5=7$	$v_5=28$	5	0	1	6	7	7	18	22	28	29	34	35	40

$\rightarrow v[i][j]$

$$\begin{aligned}
 \rightarrow v[i][j] &= \max(v[i-1][j], v[i-1][j-w_i] + v_i) \\
 &= \max(v[0][1], v[0][0] + v_1) \\
 &= \max(0, 1+0) \\
 &= 1
 \end{aligned}$$

$$\begin{aligned}
 \rightarrow v[3][1] &= v[i] + v[i-1][j] \\
 &= v[2][1] \\
 &= 1
 \end{aligned}$$