Building your Deep Neural Network: Step by Step

Welcome to your week 4 assignment (part 1 of 2)! Previously you trained a 2-layer Neural Network with a single hidden layer. This week, you will build a deep neural network with as many layers as you want!

- In this notebook, you'll implement all the functions required to build a deep neural network.
- For the next assignment, you'll use these functions to build a deep neural network for image classification.

By the end of this assignment, you'll be able to:

- Use non-linear units like ReLU to improve your model
- Build a deeper neural network (with more than 1 hidden layer)
- Implement an easy-to-use neural network class

Notation:

- Superscript \$[I]\$ denotes a quantity associated with the \$I^{th}\$ layer.
 - Example: \$a^{[L]}\$ is the \$L^{th}\$ layer activation. \$W^{[L]}\$ and \$b^{[L]}\$ are the \$L^{th}\$ layer parameters.
- Superscript \$(i)\$ denotes a quantity associated with the \$i^{th}\$ example.
 - Example: $x^{(i)}$ is the i^{th} training example.
- Lowerscript \$i\$ denotes the \$i^{th}\$ entry of a vector.
 - Example: \$a^{[I]} i\$ denotes the \$i^{th}\$ entry of the \$I^{th}\$ layer's activations).

Let's get started!

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1 - Packages

First, import all the packages you'll need during this assignment.

- <u>numpy (www.numpy.org)</u> is the main package for scientific computing with Python.
- matplotlib (http://matplotlib.org) is a library to plot graphs in Python.
- dnn_utils provides some necessary functions for this notebook.
- testCases provides some test cases to assess the correctness of your functions
- np.random.seed(1) is used to keep all the random function calls consistent. It helps grade your work. Please don't change the seed!

In [1]:

```
import numpy as np
import h5py
import matplotlib.pyplot as plt
from testCases import *
from dnn_utils import sigmoid, sigmoid_backward, relu, relu_backward
from public_tests import *

%matplotlib inline
plt.rcParams['figure.figsize'] = (5.0, 4.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

%load_ext autoreload
%autoreload 2

np.random.seed(1)
```

2 - Outline

To build your neural network, you'll be implementing several "helper functions." These helper functions will be used in the next assignment to build a two-layer neural network and an L-layer neural network.

Each small helper function will have detailed instructions to walk you through the necessary steps. Here's an outline of the steps in this assignment:

- Initialize the parameters for a two-layer network and for an \$L\$-layer neural network
- Implement the forward propagation module (shown in purple in the figure below)
 - Complete the LINEAR part of a layer's forward propagation step (resulting in \$Z^{[I]}\$).
 - The ACTIVATION function is provided for you (relu/sigmoid)
 - Combine the previous two steps into a new [LINEAR->ACTIVATION] forward function.
 - Stack the [LINEAR->RELU] forward function L-1 time (for layers 1 through L-1) and add a [LINEAR->SIGMOID] at the end (for the final layer \$L\$). This gives you a new L model forward function.
- · Compute the loss
- Implement the backward propagation module (denoted in red in the figure below)
 - Complete the LINEAR part of a layer's backward propagation step
 - The gradient of the ACTIVATE function is provided for you(relu_backward/sigmoid_backward)
 - Combine the previous two steps into a new [LINEAR->ACTIVATION] backward function
 - Stack [LINEAR->RELU] backward L-1 times and add [LINEAR->SIGMOID] backward in a new L_model_backward function
- · Finally, update the parameters

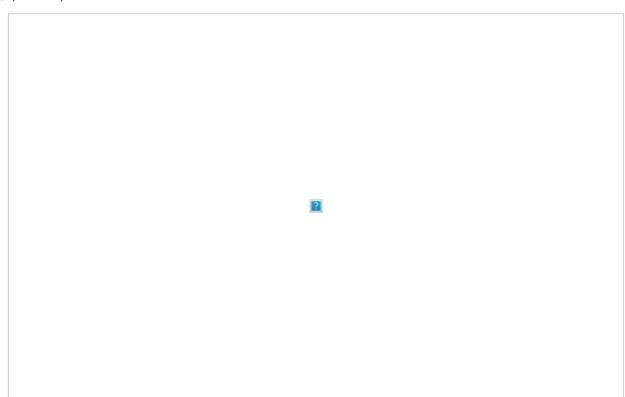


Figure 1

Note

For every forward function, there is a corresponding backward function. This is why at every step of your forward module you will be storing some values in a cache. These cached values are useful for computing gradients.

In the backpropagation module, you can then use the cache to calculate the gradients. Don't worry, this assignment will show you exactly how to carry out each of these steps!

3 - Initialization

You will write two helper functions to initialize the parameters for your model. The first function will be used to initialize parameters for a two layer model. The second one generalizes this initialization process to \$L\$ layers.

3.1 - 2-layer Neural Network

Exercise 1 - initialize_parameters

Create and initialize the parameters of the 2-layer neural network.

Instructions:

- The model's structure is: LINEAR -> RELU -> LINEAR -> SIGMOID.
- Use this random initialization for the weight matrices: np.random.randn(shape)*0.01 with the correct shape
- Use zero initialization for the biases: np.zeros(shape)

In [2]:

```
# GRADED FUNCTION: initialize_parameters
def initialize_parameters(n_x, n_h, n_y):
   Araument:
   n x -- size of the input layer
   n h -- size of the hidden layer
   n_y -- size of the output layer
   Returns:
   parameters -- python dictionary containing your parameters:
                    W1 -- weight matrix of shape (n h, n x)
                    b1 -- bias vector of shape (n_h, 1)
                    W2 -- weight matrix of shape (n_y, n_h)
                    b2 -- bias vector of shape (n_y, 1)
   np.random.seed(1)
   #(≈ 4 lines of code)
   \# W1 = ...
   # b1 = ...
   # W2 = ...
   # b2 = ..
   # YOUR CODE STARTS HERE
   W1 = np.random.randn(n h, n x) * 0.01;
   b1 = np.zeros((n_h, 1));
   W2 = np.random.randn(n_y, n_h) * 0.01;
   b2 = np.zeros((n_y, 1));
   # YOUR CODE ENDS HERE
   parameters = {"W1": W1,
                  "b1": b1,
                  "W2": W2.
                  "b2": b2}
    return parameters
```

In [3]:

All tests passed.

```
parameters = initialize_parameters(3,2,1)

print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))

initialize_parameters_test(initialize_parameters)

W1 = [[ 0.01624345 -0.00611756 -0.00528172]
[-0.01072969   0.00865408 -0.02301539]]
b1 = [[0.]
[0.]]
W2 = [[ 0.01744812 -0.00761207]]
b2 = [[ 0.1]
```

Expected output

```
W1 = [[ 0.01624345 -0.00611756 -0.00528172]

[-0.01072969  0.00865408 -0.02301539]]

b1 = [[0.]

[0.]]

W2 = [[ 0.01744812 -0.00761207]]

b2 = [[0.]]
```

3.2 - L-layer Neural Network

The initialization for a deeper L-layer neural network is more complicated because there are many more weight matrices and bias vectors. When completing the initialize_parameters_deep function, you should make sure that your dimensions match between each layer. Recall that $n^{[l]}$ is the number of units in layer \$1\$. For example, if the size of your input \$X\$ is \$(12288, 209)\$ (with \$m=209\$ examples) then:

Shape of Activation	Activation	Shape of b	Shape of W	
\$(n^{[1]},209)\$	$Z^{[1]} = W^{[1]} X + b^{[1]} $	\$(n^{[1]},1)\$	\$(n^{[1]},12288)\$	Layer 1
\$(n^{[2]}, 209)\$	\$Z^{[2]} = W^{[2]} A^{[1]} + b^{[2]}\$	\$(n^{[2]},1)\$	\$(n^{[2]}, n^{[1]})\$	Layer 2
\vdots\	\$\vdots\$	\$\vdots\$	\$\vdots\$	\$\vdots\$
\$(n^{[L-1]}, 209)\$	$Z^{[L-1]} = W^{[L-1]} A^{[L-2]} + b^{[L-1]}$	\$(n^{[L-1]}, 1)\$	\$(n^{[L-1]}, n^{[L-2]})\$	Layer L-1
\$(n^{[L]}, 209)\$	\$Z^{[L]} = W^{[L]} A^{[L-1]} + b^{[L]}\$	\$(n^{[L]}, 1)\$	\$(n^{[L]}, n^{[L-1]})\$	Layer L

Remember that when you compute \$W X + b\$ in python, it carries out broadcasting. For example, if: \$\$ W = \begin{bmatrix} w_{00} & w_{01} & w_{10} & w_{11} & w_{12} \ w_{20} & w_{21} & w_{22} \hd{bmatrix};;; X = \hd{bmatrix} x_{00} & x_{01} & x_{11} & x_{12} & x_{22} \hd{bmatrix} x_{11} & x_{12} & x_{22} \hd{bmatrix} x_{22} \hd{bmatrix} b 0 \ b 1 \ b 2 \hd{bmatrix} x_{22}\$\$

Then \$WX + b\$ will be:

```
 \$WX + b = \begin{array}{l} \$WX
```

Exercise 2 - initialize_parameters_deep

Implement initialization for an L-layer Neural Network.

Instructions:

- The model's structure is [LINEAR -> RELU] \$ \times\$ (L-1) -> LINEAR -> SIGMOID. I.e., it has \$L-1\$ layers using a ReLU activation function followed by an output layer with a sigmoid activation function.
- Use random initialization for the weight matrices. Use np. random. randn(shape) * 0.01.
- Use zeros initialization for the biases. Use np.zeros(shape).
- You'll store \$n^{[I]}\$, the number of units in different layers, in a variable layer_dims. For example, the layer_dims for last week's Planar Data classification model would have been [2,4,1]: There were two inputs, one hidden layer with 4 hidden units, and an output layer with 1 output unit. This means W1's shape was (4,2), b1 was (4,1), W2 was (1,4) and b2 was (1,1). Now you will generalize this to \$L\$ layers!
- Here is the implementation for \$L=1\$ (one layer neural network). It should inspire you to implement the general case (L-layer neural network).

```
if L == 1:
    parameters["W" + str(L)] = np.random.randn(layer_dims[1], layer_dims[0]) * 0.01
    parameters["b" + str(L)] = np.zeros((layer_dims[1], 1))
```

```
In [4]:
# GRADED FUNCTION: initialize_parameters_deep
def initialize_parameters_deep(layer_dims):
   Arguments:
    layer_dims -- python array (list) containing the dimensions of each layer in our network
   Returns:
   parameters -- python dictionary containing your parameters "W1", "b1", ..., "WL", "bL":
                   Wl -- weight matrix of shape (layer_dims[l], layer_dims[l-1])
                   bl -- bias vector of shape (layer_dims[l], 1)
   np.random.seed(3)
   parameters = \{\}
   L = len(layer_dims) # number of layers in the network
   for l in range(1, L):
       #(≈ 2 lines of code)
       # parameters['W' + str(l)] = ...
        \# parameters['b' + str(l)] = ...
        # YOUR CODE STARTS HERE
       parameters["W" + str(l)] = np.random.randn(layer_dims[l], layer_dims[l - 1]) * 0.01;
       parameters["b" + str(l)] = np.zeros((layer_dims[l], 1));
       # YOUR CODE ENDS HERE
       assert(parameters['W' + str(l)].shape == (layer dims[l], layer dims[l - 1]))
       assert(parameters['b' + str(l)].shape == (layer dims[l], 1))
    return parameters
In [5]:
parameters = initialize_parameters_deep([5,4,3])
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))
initialize_parameters_deep_test(initialize_parameters_deep)
W1 = [ [ 0.01788628   0.0043651 ]
                               0.00096497 -0.01863493 -0.00277388]
b1 = [[0.]]
 [0.]
 [0.]
 [0.]]
W2 = [[-0.01185047 -0.0020565]]
                              0.01486148 0.00236716]
 [-0.01023785 \ -0.00712993 \ \ 0.00625245 \ -0.00160513]
 [-0.00768836 -0.00230031 0.00745056 0.01976111]]
b2 = [[0.]]
 [0.]
 [0.]]
```

Expected output

All tests passed.

```
W1 = [[ 0.01788628  0.0043651  0.00096497 -0.01863493 -0.00277388]
  [-0.00354759 -0.00082741 -0.00627001 -0.00043818 -0.00477218]
  [-0.01313865  0.00884622  0.00881318  0.01709573  0.00050034]
  [-0.00404677 -0.0054536 -0.01546477  0.00982367 -0.01101068]]
b1 = [[0.]
  [0.]
  [0.]
  [0.]
  [0.]]
W2 = [[-0.01185047 -0.0020565  0.01486148  0.00236716]
  [-0.01023785 -0.00712993  0.00625245 -0.00160513]
  [-0.00768836 -0.00230031  0.00745056  0.01976111]]
b2 = [[0.]
  [0.]
  [0.]
```

4 - Forward Propagation Module

4.1 - Linear Forward

Now that you have initialized your parameters, you can do the forward propagation module. Start by implementing some basic functions that you can use again later when implementing the model. Now, you'll complete three functions in this order:

- LINEAR
- LINEAR -> ACTIVATION where ACTIVATION will be either ReLU or Sigmoid.
- [LINEAR -> RELU] \$\times\$ (L-1) -> LINEAR -> SIGMOID (whole model)

The linear forward module (vectorized over all the examples) computes the following equations:

 $\Z^{[i]} = W^{[i]}A^{[i-1]} +b^{[i]}\times\{4\}$

where $A^{[0]} = X$.

Exercise 3 - linear_forward

Build the linear part of forward propagation.

Reminder: The mathematical representation of this unit is $Z^{[l]} = W^{[l]}A^{[l-1]} + b^{[l]}$. You may also find np.dot() useful. If your dimensions don't match, printing W.shape may help.

In [6]:

```
# GRADED FUNCTION: linear forward
def linear forward(A, W, b):
   Implement the linear part of a layer's forward propagation.
   Arguments:
   A -- activations from previous layer (or input data): (size of previous layer, number of examples)
   W -- weights matrix: numpy array of shape (size of current layer, size of previous layer)
   b -- bias vector, numpy array of shape (size of the current layer, 1)
   Z -- the input of the activation function, also called pre-activation parameter
   cache -- a python tuple containing "A", "W" and "b"; stored for computing the backward pass efficiently
   #(≈ 1 line of code)
   \#Z = \dots
   # YOUR CODE STARTS HERE
   Z = np.dot(W, A) + b;
   # YOUR CODE ENDS HERE
   cache = (A, W, b)
   return Z, cache
```

In [7]:

```
t_A, t_W, t_b = linear_forward_test_case()
t_Z, t_linear_cache = linear_forward(t_A, t_W, t_b)
print("Z = " + str(t_Z))
linear_forward_test(linear_forward)
```

```
Z = [[ 3.26295337 -1.23429987]]
All tests passed.
```

Expected output

```
Z = [[ 3.26295337 - 1.23429987]]
```

4.2 - Linear-Activation Forward

In this notebook, you will use two activation functions:

• **Sigmoid**: \$\sigma(Z) = \sigma(W A + b) = \frac{1}{ 1 + e^{-(W A + b)}}}\$. You've been provided with the sigmoid function which returns **two** items: the activation value " a " and a " cache " that contains " Z " (it's what we will feed in to the corresponding backward function). To use it you could just call:

```
A, activation cache = sigmoid(Z)
```

• **ReLU**: The mathematical formula for ReLu is \$A = RELU(Z) = max(0, Z)\$. You've been provided with the relu function. This function returns **two** items: the activation value " A " and a " cache " that contains " Z " (it's what you'll feed in to the corresponding backward function). To use it you could just call:

```
A, activation cache = relu(Z)
```

For added convenience, you're going to group two functions (Linear and Activation) into one function (LINEAR->ACTIVATION). Hence, you'll implement a function that does the LINEAR forward step, followed by an ACTIVATION forward step.

Exercise 4 - linear_activation_forward

Implement the forward propagation of the LINEAR->ACTIVATION layer. Mathematical relation is: $A^{[[]]} = g(Z^{[]]}) = g(W^{[]]}A^{[]-1]} + b^{[]]}$ where the activation "g" can be sigmoid() or relu(). Use linear forward() and the correct activation function.

In [8]:

```
# GRADED FUNCTION: linear activation forward
def linear activation forward(A prev, W, b, activation):
   Implement the forward propagation for the LINEAR->ACTIVATION layer
   Arguments:
   A_prev -- activations from previous layer (or input data): (size of previous layer, number of examples)
   W -- weights matrix: numpy array of shape (size of current layer, size of previous layer)
   b -- bias vector, numpy array of shape (size of the current layer, 1)
   activation -- the activation to be used in this layer, stored as a text string: "sigmoid" or "relu"
   A -- the output of the activation function, also called the post-activation value
   cache -- a python tuple containing "linear cache" and "activation cache";
             stored for computing the backward pass efficiently
   if activation == "sigmoid":
       \#(\approx 2 \text{ lines of code})
       # Z, linear_cache = ...
       # A, activation cache =
       # YOUR CODE STARTS HERE
       Z, linear_cache = linear_forward(A_prev, W, b)
       A, activation cache = sigmoid(Z)
        # YOUR CODE ENDS HERE
   elif activation == "relu":
       #(≈ 2 lines of code)
       \# Z, linear\_cache = ...
       # A, activation cache = ...
       # YOUR CODE STARTS HERE
       Z, linear cache = linear forward(A prev, W, b)
       A, activation cache = relu(Z)
        # YOUR CODE ENDS HERE
   cache = (linear_cache, activation_cache)
    return A, cache
```

In [9]:

```
t_A_prev, t_W, t_b = linear_activation_forward_test_case()

t_A, t_linear_activation_cache = linear_activation_forward(t_A_prev, t_W, t_b, activation = "sigmoid")
print("With sigmoid: A = " + str(t_A))

t_A, t_linear_activation_cache = linear_activation_forward(t_A_prev, t_W, t_b, activation = "relu")
print("With ReLU: A = " + str(t_A))

linear_activation_forward_test(linear_activation_forward)
```

```
With sigmoid: A = [[0.96890023 \ 0.11013289]] With ReLU: A = [[3.43896131 \ 0. ]] All tests passed.
```

Expected output

```
With sigmoid: A = [[0.96890023 \ 0.11013289]] With ReLU: A = [[3.43896131 \ 0.]]
```

Note: In deep learning, the "[LINEAR->ACTIVATION]" computation is counted as a single layer in the neural network, not two layers.

4.3 - L-Layer Model

For even *more* convenience when implementing the \$L\$-layer Neural Net, you will need a function that replicates the previous one (linear activation forward with RELU) \$L-1\$ times, then follows that with one linear activation forward with SIGMOID.

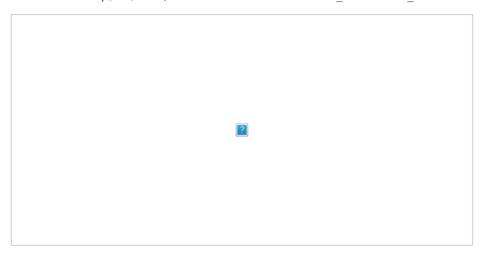


Figure 2: *[LINEAR -> RELU] \$\times\$ (L-1) -> LINEAR -> SIGMOID* model

Exercise 5 - L_model_forward

Implement the forward propagation of the above model.

Instructions: In the code below, the variable AL will denote $A^{[L]} = \sum_{C \in \mathbb{Z}^{[L]}} A^{[L-1]} + b^{[L]}$. (This is sometimes also called Yhat , i.e., this is \hat{S}).

Hints:

- Use the functions you've previously written
- Use a for loop to replicate [LINEAR->RELU] (L-1) times
- Don't forget to keep track of the caches in the "caches" list. To add a new value c to a list, you can use list.append(c).

```
In [10]:
```

```
# GRADED FUNCTION: L_model_forward
def L_model_forward(X, parameters):
    Implement forward propagation for the [LINEAR->RELU]*(L-1)->LINEAR->SIGMOID computation
    Arguments:
    X -- data, numpy array of shape (input size, number of examples)
    parameters -- output of initialize parameters deep()
    Returns:
    AL -- activation value from the output (last) layer
    caches -- list of caches containing:
                every cache of linear activation forward() (there are L of them, indexed from 0 to L-1)
    caches = []
    A = X
                                               # number of layers in the neural network
    L = len(parameters) // 2
    \# Implement [LINEAR -> RELU]*(L-1). Add "cache" to the "caches" list.
    # The for loop starts at 1 because layer 0 is the input
    for l in range(1, L):
        A prev = A
        \#(\approx 2 \text{ lines of code})
        \# A, cache = ...
        # caches ...
        # YOUR CODE STARTS HERE
        A, linear activation cache = linear activation forward(A prev, parameters["W" + str(l)], parameters["b" +
str(l)], "relu");
        caches.append(linear_activation_cache);
        # YOUR CODE ENDS HERE
    # Implement LINEAR -> SIGMOID. Add "cache" to the "caches" list.
    \#(\approx 2 \text{ lines of code})
    # AL, cache = ...
    # caches ..
    # YOUR CODE STARTS HERE
   AL, linear_activation_cache = linear_activation_forward(A, parameters["W" + str(L)], parameters["b" + str(L)]
   caches.append(linear_activation_cache);
    # YOUR CODE ENDS HERE
    return AL, caches
```

In [11]:

```
t_X, t_parameters = L_model_forward_test_case_2hidden()
t_AL, t_caches = L_model_forward(t_X, t_parameters)
print("AL = " + str(t_AL))
L_model_forward_test(L_model_forward)
```

```
AL = [[0.03921668 \ 0.70498921 \ 0.19734387 \ 0.04728177]] All tests passed.
```

Expected output

```
AL = [[0.03921668 \ 0.70498921 \ 0.19734387 \ 0.04728177]]
```

Awesome! You've implemented a full forward propagation that takes the input X and outputs a row vector \$A^{[L]}\$ containing your predictions. It also records all intermediate values in "caches". Using \$A^{[L]}\$, you can compute the cost of your predictions.

5 - Cost Function

Now you can implement forward and backward propagation! You need to compute the cost, in order to check whether your model is actually learning.

Exercise 6 - compute_cost

In [12]:

```
# GRADED FUNCTION: compute_cost
def compute_cost(AL, Y):
    Implement the cost function defined by equation (7).
   Arguments:
   AL -- probability vector corresponding to your label predictions, shape (1, number of examples)
   Y -- true "label" vector (for example: containing 0 if non-cat, 1 if cat), shape (1, number of examples)
   Returns:
   cost -- cross-entropy cost
   m = Y.shape[1]
   # Compute loss from aL and y.
   # (≈ 1 lines of code)
   \# cost = ...
   # YOUR CODE STARTS HERE
   cost = -1 / m * (np.dot(Y, np.log(AL).T) + np.dot(1 - Y, np.log(1 - AL).T));
   # YOUR CODE ENDS HERE
                            # To make sure your cost's shape is what we expect (e.g. this turns [[17]] into
    cost = np.squeeze(cost)
17).
    return cost
```

In [13]:

```
t_Y, t_AL = compute_cost_test_case()
t_cost = compute_cost(t_AL, t_Y)
print("Cost: " + str(t_cost))
compute_cost_test(compute_cost)
```

Cost: 0.2797765635793422 All tests passed.

Expected Output:

cost 0.2797765635793422

6 - Backward Propagation Module

Just as you did for the forward propagation, you'll implement helper functions for backpropagation. Remember that backpropagation is used to calculate the gradient of the loss function with respect to the parameters.

Reminder:



Figure 3: Forward and Backward propagation for LINEAR->RELU->LINEAR->SIGMOID

The purple blocks represent the forward propagation, and the red blocks represent the backward propagation.

Now, similarly to forward propagation, you're going to build the backward propagation in three steps:

- LINEAR backward
- 2. LINEAR -> ACTIVATION backward where ACTIVATION computes the derivative of either the ReLU or sigmoid activation
- 3. [LINEAR -> RELU] \$\times\$ (L-1) -> LINEAR -> SIGMOID backward (whole model)

For the next exercise, you will need to remember that:

- b is a matrix(np.ndarray) with 1 column and n rows, i.e: b = [[1.0], [2.0]] (remember that b is a constant)
- · np.sum performs a sum over the elements of a ndarray
- axis=1 or axis=0 specify if the sum is carried out by rows or by columns respectively
- keepdims specifies if the original dimensions of the matrix must be kept.
- · Look at the following example to clarify:

In [14]:

```
A = np.array([[1, 2], [3, 4]])

print('axis=1 and keepdims=True')
print(np.sum(A, axis=1, keepdims=True))
print('axis=1 and keepdims=False')
print(np.sum(A, axis=1, keepdims=False))
print('axis=0 and keepdims=True')
print(np.sum(A, axis=0, keepdims=True))
print('axis=0 and keepdims=False')
print(np.sum(A, axis=0, keepdims=False))
```

```
axis=1 and keepdims=True
[[3]
  [7]]
axis=1 and keepdims=False
[3 7]
axis=0 and keepdims=True
[[4 6]]
axis=0 and keepdims=False
[4 6]
```

6.1 - Linear Backward

For layer $|x| \in W^{[l]} A^{[l-1]} + b^{[l]}$ (followed by an activation).

Suppose you have already calculated the derivative \$dZ^{[i]} = \frac{\partial \mathcal{L} }{\partial Z^{[i]}}\$. You want to get \$(dW^{[i]}, db^{[i]}, dA^{[i-1]})\$.

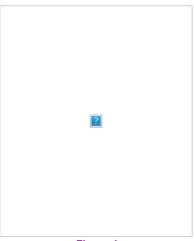


Figure 4

The three outputs $(dW^{[i]}, dA^{[i]})$ are computed using the input $dZ^{[i]}$.

Here are the formulas you need: \$\$ $dW^{[[]]} = \frac{J}{m} dZ^{[[]]} A^{[[-1] T} dZ^{[[]]} = \frac{J}{m} dZ^{[]} =$

\$A^{[I-1] T}\$ is the transpose of \$A^{[I-1]}\$.

Exercise 7 - linear_backward

Use the 3 formulas above to implement linear backward().

Hint:

• In numpy you can get the transpose of an ndarray A using A.T or A.transpose()

```
In [15]:
# GRADED FUNCTION: linear_backward
def linear_backward(dZ, cache):
   Implement the linear portion of backward propagation for a single layer (layer l)
   Arguments:
   dZ -- Gradient of the cost with respect to the linear output (of current layer l)
   cache -- tuple of values (A prev, W, b) coming from the forward propagation in the current layer
   Returns:
   dA prev -- Gradient of the cost with respect to the activation (of the previous layer l-1), same shape as A p
rev
   dW -- Gradient of the cost with respect to W (current layer l), same shape as W
   db -- Gradient of the cost with respect to b (current layer l), same shape as b
   A prev, W, b = cache
   m = A prev.shape[1]
   ### START CODE HERE ### (≈ 3 lines of code)
   \# db = ... sum by the rows of dZ with keepdims=True
   # dA_prev = ...
   # YOUR CODE STARTS HERE
   dW = 1 / m * np.dot(dZ, A\_prev.T);
   db = 1 / m * np.sum(dZ, axis = 1, keepdims = True);
   dA prev = np.dot(W.T, dZ);
   # YOUR CODE ENDS HERE
   return dA_prev, dW, db
In [16]:
t dZ, t linear cache = linear backward test case()
t dA prev, t dW, t db = linear backward(t dZ, t linear cache)
print("dA prev: " + str(t dA prev))
print("dW: " + str(t dW))
print("db: " + str(t db))
linear_backward_test(linear_backward)
dA prev: [[-1.15171336  0.06718465 -0.3204696
                                             2.09812712]
[ 0.60345879 -3.72508701 5.81700741 -3.84326836]
 [-0.4319552 -1.30987417 1.72354705 0.05070578]
dW: [[ 0.07313866 -0.0976715 -0.87585828 0.73763362 0.00785716]
 [ 0.97913304 -0.24376494 -0.08839671  0.55151192 -0.10290907]]
db: [[-0.14713786]
 [-0.11313155]
 [-0.13209101]]
All tests passed.
```

Expected Output:

db: [[-0.14713786] [-0.11313155] [-0.13209101]]

dA prev: [[-1.15171336 0.06718465 -0.3204696 2.09812712]

dw: [[0.07313866 -0.0976715 -0.87585828 0.73763362 0.00785716] [0.85508818 0.37530413 -0.59912655 0.71278189 -0.58931808] [0.97913304 -0.24376494 -0.08839671 0.55151192 -0.10290907]]

[0.60345879 -3.72508701 5.81700741 -3.84326836] [-0.4319552 -1.30987417 1.72354705 0.05070578] [-0.38981415 0.60811244 -1.25938424 1.47191593] [-2.52214926 2.67882552 -0.67947465 1.48119548]]

6.2 - Linear-Activation Backward

Next, you will create a function that merges the two helper functions: **linear_backward** and the backward step for the activation **linear_activation_backward**.

To help you implement linear activation backward, two backward functions have been provided:

• sigmoid backward: Implements the backward propagation for SIGMOID unit. You can call it as follows:

```
dZ = sigmoid_backward(dA, activation_cache)
```

• relu backward: Implements the backward propagation for RELU unit. You can call it as follows:

```
dZ = relu_backward(dA, activation_cache)
```

Exercise 8 - linear activation backward

Implement the backpropagation for the LINEAR->ACTIVATION layer.

In [17]:

```
# GRADED FUNCTION: linear activation backward
def linear activation backward(dA, cache, activation):
   Implement the backward propagation for the LINEAR->ACTIVATION layer.
   Arguments:
   dA -- post-activation gradient for current layer l
   cache -- tuple of values (linear_cache, activation_cache) we store for computing backward propagation efficie
ntly
   activation -- the activation to be used in this layer, stored as a text string: "sigmoid" or "relu"
    dA prev -- Gradient of the cost with respect to the activation (of the previous layer l-1), same shape as A p
rev
   dW -- Gradient of the cost with respect to W (current layer l), same shape as W
   db -- Gradient of the cost with respect to b (current layer l), same shape as b
    linear cache, activation cache = cache
   if activation == "relu":
        #(≈ 2 lines of code)
        \# dZ =
               . . .
        # dA prev, dW, db =
        # YOUR CODE STARTS HERE
        dZ = relu_backward(dA, activation_cache);
        dA prev, dW, db = linear backward(dZ, linear cache);
        # YOUR CODE ENDS HERE
   elif activation == "sigmoid":
        #(≈ 2 lines of code)
        \# dZ = \dots
        # dA_prev, dW, db = ...
        # YOUR CODE STARTS HERE
        dZ = sigmoid_backward(dA, activation_cache);
        dA prev, dW, db = linear backward(dZ, linear cache);
        # YOUR CODE ENDS HERE
   return dA_prev, dW, db
```

```
In [18]:
t_dAL, t_linear_activation_cache = linear_activation_backward_test_case()
t_dA_prev, t_dW, t_db = linear_activation_backward(t_dAL, t_linear_activation_cache, activation = "sigmoid")
print("With sigmoid: dA_prev = " + str(t_dA_prev))
print("With sigmoid: dW = " + str(t_dW))
print("With sigmoid: db = " + str(t_db))
t_dA\_prev, \ t_dW, \ t_db = linear_activation\_backward(t_dAL, \ t_linear_activation\_cache, \ activation = "relu")
print("With relu: dA prev = " + str(t dA prev))
print("With relu: dW = " + str(t dW))
print("With relu: db = " + str(t_db))
linear_activation_backward_test(linear_activation_backward)
With sigmoid: dA prev = [[ 0.11017994 \ 0.01105339]
 [ 0.09466817  0.00949723]
 [-0.05743092 -0.00576154]]
With sigmoid: dW = [[ 0.10266786 \ 0.09778551 \ -0.01968084]]
With sigmoid: db = [[-0.05729622]]
With relu: dA_prev = [[ 0.44090989 0.
 [ 0.37883606 0.
 [-0.2298228
              0.
With relu: dW = [[ 0.44513824  0.37371418 -0.10478989]]
With relu: db = [[-0.20837892]]
All tests passed.
Expected output:
```

```
With sigmoid: dA_prev = [[ 0.11017994  0.01105339]
  [ 0.09466817  0.00949723]
  [-0.05743092  -0.00576154]]
With sigmoid: dW = [[ 0.10266786  0.09778551  -0.01968084]]
With sigmoid: db = [[ -0.05729622]]
With relu: dA_prev = [[ 0.44090989  0.  ]
  [ 0.37883606  0.  ]
  [-0.2298228  0.  ]]
With relu: dW = [[ 0.44513824  0.37371418  -0.10478989]]
With relu: db = [[ -0.20837892]]
```

6.3 - L-Model Backward

Now you will implement the backward function for the whole network!

Recall that when you implemented the L_model_forward function, at each iteration, you stored a cache which contains (X,W,b, and z). In the back propagation module, you'll use those variables to compute the gradients. Therefore, in the L_model_backward function, you'll iterate through all the hidden layers backward, starting from layer \$L\$. On each step, you will use the cached values for layer \$I\$ to backpropagate through layer \$I\$. Figure 5 below shows the backward pass.



Figure 5: Backward pass

Initializing backpropagation:

To backpropagate through this network, you know that the output is: $A^{[L]} = \sum_{Z^{[L]}}$. Your code thus needs to compute dAL $A^{[L]}$ are this formula (derived using calculus which, again, you don't need in-depth knowledge of!):

```
dAL = -(np.divide(Y, AL) - np.divide(1 - Y, 1 - AL)) # derivative of cost with respect to AL
```

You can then use this post-activation gradient dAL to keep going backward. As seen in Figure 5, you can now feed in dAL into the LINEAR->SIGMOID backward function you implemented (which will use the cached values stored by the L_model_forward function).

After that, you will have to use a for loop to iterate through all the other layers using the LINEAR->RELU backward function. You should store each dA, dW, and db in the grads dictionary. To do so, use this formula: \$grads["dW" + str(l)] = $\frac{dW^{[l]}}{ag\{15\}}$ \$

For example, for $l=3\$ this would store $dW^{[l]}\$ in grads["dW3"].

Exercise 9 - L model backward

Implement backpropagation for the [LINEAR->RELU] \$\times\$ (L-1) -> LINEAR -> SIGMOID model.

```
# GRADED FUNCTION: L_model_backward
def L_model_backward(AL, Y, caches):
    Implement the backward propagation for the [LINEAR->RELU] * (L-1) -> LINEAR -> SIGMOID group
    Arguments:
    AL -- probability vector, output of the forward propagation (L_model_forward())
    Y -- true "label" vector (containing 0 if non-cat, 1 if cat)
    caches -- list of caches containing:
                every cache of linear_activation_forward() with "relu" (it's caches[l], for l in range(L-1) i.e l
= 0...L-2)
                the cache of linear_activation_forward() with "sigmoid" (it's caches[L-1])
    Returns:
    grads -- A dictionary with the gradients
             grads["dA" + str(l)] = ...
             qrads["dW" + str(l)] = ...
             grads["db" + str(l)] = ...
    grads = \{\}
   L = len(caches) # the number of layers
    m = AL.shape[1]
    Y = Y.reshape(AL.shape) # after this line, Y is the same shape as AL
    # Initializing the backpropagation
    #(1 line of code)
    \# dAL = ...
    # YOUR CODE STARTS HERE
    dAL = -(np.divide(Y, AL) - np.divide(1 - Y, 1 - AL))
    # YOUR CODE ENDS HERE
    # Lth layer (SIGMOID -> LINEAR) gradients. Inputs: "dAL, current cache". Outputs: "grads["dAL-1"], grads["dWL
"], grads["dbL"]
    #(approx. 5 lines)
    # current cache =
    # dA prev temp, dW temp, db temp = ...
    \# grads["dA" + str(L-1)] = \dots
    \# grads["dW" + str(L)] = ...
    \# grads["db" + str(L)] = \dots
    # YOUR CODE STARTS HERE
    dA\_prev, \ dW, \ db = linear\_activation\_backward(dAL, \ caches[L \ - \ 1], \ "sigmoid");
    grads["dA" + str(L-1)], grads["dW" + str(L)], grads["db" + str(L)] = dA prev, dW, db;
    # YOUR CODE ENDS HERE
    # Loop from l=L-2 to l=0
    for l in reversed(range(L-1)):
        # lth layer: (RELU -> LINEAR) gradients.
        \# Inputs: "grads["dA" + str(l + 1)], current_cache". Outputs: "grads["dA" + str(l)] , grads["dW" + str(l)]
+ 1)] , grads["db" + str(l + 1)]
        #(approx. 5 lines)
        # current cache = ..
        # dA prev temp, dW temp, db temp = ...
        # grads["dA" + str(l)] = ...
# grads["dW" + str(l + 1)] = ...
        # qrads["db" + str(l + 1)] = ...
        # YOUR CODE STARTS HERE
        dA = dA prev;
        dA_prev, dW, db = linear_activation_backward(dA, caches[l], "relu");
        grads["dA" + str(l)] = dA\_prev;
        grads["dW" + str(l + 1)] = dW;
        grads["db" + str(l + 1)] = db;
        # YOUR CODE ENDS HERE
    return grads
```

```
In [43]:
```

```
t_AL, t_Y_assess, t_caches = L_model_backward_test_case()
grads = L_model_backward(t_AL, t_Y_assess, t_caches)

print("dA0 = " + str(grads['dA0']))
print("dA1 = " + str(grads['dA1']))
print("dW1 = " + str(grads['dW1']))
print("dW2 = " + str(grads['dW2']))
print("db1 = " + str(grads['db1']))
print("db2 = " + str(grads['db2']))

L_model_backward_test(L_model_backward)
```

```
dA0 = [[0.
                       0.52257901]
[ 0.
               -0.3269206 1
 [ 0.
               -0.32070404]
 ΓΘ.
              -0.7407918711
dA1 = [[ 0.12913162 - 0.44014127]
[-0.14175655 0.48317296]
[ 0.01663708 -0.05670698]]
dW1 = [[0.41010002 \ 0.07807203 \ 0.13798444 \ 0.10502167]
 [0.
             0.
                          0.
                                      0.
 [0.05283652 0.01005865 0.01777766 0.0135308 ]]
dW2 = [[-0.39202432 -0.13325855 -0.04601089]]
db1 = [[-0.22007063]]
 [ 0.
 [-0.0283534911
db2 = [[0.15187861]]
All tests passed.
```

Expected output:

```
dA\theta = [[ \theta.
                      0.52257901]
[ 0.
              -0.3269206 1
[ 0.
              -0.320704041
              -0.74079187]]
[ 0.
dA1 = [[ 0.12913162 - 0.44014127]
[-0.14175655 0.48317296]
[ 0.01663708 -0.05670698]]
dW1 = [[0.41010002 \ 0.07807203 \ 0.13798444 \ 0.10502167]
            0.
                        0.
                                    0.
[0.05283652 0.01005865 0.01777766 0.0135308 ]]
dW2 = [[-0.39202432 -0.13325855 -0.04601089]]
db1 = [[-0.22007063]
[ 0.
[-0.02835349]]
db2 = [[0.15187861]]
```

6.4 - Update Parameters

In this section, you'll update the parameters of the model, using gradient descent: $\$ W^{[i]} = W^{[i]} - \alpha \text{} dW^{[i]} \tag{16}\$\$\$\$ b^{[i]} = b^{[i]} - \alpha \text{} db^{[i]} \tag{17}\$\$

where \$\alpha\$ is the learning rate.

After computing the updated parameters, store them in the parameters dictionary.

Exercise 10 - update_parameters

Implement update_parameters() to update your parameters using gradient descent.

Instructions: Update parameters using gradient descent on every $W^{[i]}$ and $b^{[i]}$ for i = 1, 2, ..., L.

```
In [29]:
```

```
# GRADED FUNCTION: update_parameters
def update_parameters(params, grads, learning_rate):
    Update parameters using gradient descent
    Arguments:
    params -- python dictionary containing your parameters
    grads -- python dictionary containing your gradients, output of L model backward
    parameters -- python dictionary containing your updated parameters
                  parameters["W" + str(l)] = ...
                  parameters["b" + str(l)] = ...
    parameters = params.copy()
    L = len(parameters) // 2 # number of layers in the neural network
    # Update rule for each parameter. Use a for loop.
    #(≈ 2 lines of code)
    for i in range(1,L+1):
        # parameters["W" + str(l+1)] = ...
        # parameters["b" + str(l+1)] = ...
        # YOUR CODE STARTS HERE
        parameters["W" + str(i)] = parameters["W" + str(i)] - learning\_rate*grads["dW"+str(i)]
        parameters["b" + str(i)] = parameters["b" + str(i)] - learning rate*grads["db"+str(i)]
        # YOUR CODE ENDS HERE
    return parameters
In [301:
```

```
t_parameters, grads = update_parameters_test_case()
t_parameters = update_parameters(t_parameters, grads, 0.1)

print ("W1 = "+ str(t_parameters["W1"]))
print ("b1 = "+ str(t_parameters["b1"]))
print ("W2 = "+ str(t_parameters["W2"]))
print ("b2 = "+ str(t_parameters["b2"]))

update_parameters_test(update_parameters)
```

```
 \begin{aligned} & \text{W1} = [[-0.59562069 \ -0.09991781 \ -2.14584584 \ \ 1.82662008] \\ & [-1.76569676 \ -0.80627147 \ \ 0.51115557 \ -1.18258802] \\ & [-1.0535704 \ \ -0.86128581 \ \ 0.68284052 \ \ 2.20374577]] \\ & \text{b1} = [[-0.04659241] \\ & [-1.28888275] \\ & [\ 0.53405496]] \\ & \text{W2} = [[-0.55569196 \ \ 0.0354055 \ \ \ 1.32964895]] \\ & \text{b2} = [[-0.84610769]] \\ & \text{All tests passed.} \end{aligned}
```

Expected output:

```
W1 = [[-0.59562069 -0.09991781 -2.14584584   1.82662008]

[-1.76569676 -0.80627147   0.51115557 -1.18258802]

[-1.0535704   -0.86128581   0.68284052   2.20374577]]

b1 = [[-0.04659241]

[-1.28888275]

[ 0.53405496]]

W2 = [[-0.55569196   0.0354055   1.32964895]]

b2 = [[-0.84610769]]
```

Congratulations!

You've just implemented all the functions required for building a deep neural network, including:

- Using non-linear units improve your model
- Building a deeper neural network (with more than 1 hidden layer)
- Implementing an easy-to-use neural network class

This was indeed a long assignment, but the next part of the assignment is easier. ;)

In the next assignment, you'll be putting all these together to build two models:

- A two-layer neural network
- An L-layer neural network

You will in fact use these models to classify cat vs non-cat images! (Meow!) Great work and see you next time.