

Optimization Techniques and Application

Marketing Management

 **GROUP 27**

| | |
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Objective 1 :-

In the given project we have to decrease the transportation expenditure to its minimum value for marketing management.

Problem Statement:-

In this problem ,we have to produce products at supply locations and transport them to destinations where they are demanded at minimum cost.The origins are two plants at Jaipur and Kota which supplies or capacities of 400kg and 600kg while the destination are three distributions centre i.e. Mumbai,Pune and Bangalore with demand of 300,400 and 250kg respectively. The cost of transporting 1kg of the product from Jaipur to distribution centers are Rs.7,Rs.8 and Rs.9 respectively and from Kota are Rs.10,Rs.11 and Rs.12 respectively. The cost of product per kg in Jaipur and Kota are Rs.26 and Rs.30 respectively.

Optimize the transportation cost that the marketing manager has to pay to the transportation company.

| <i>To→</i> <i>From↓</i> | <i>Mumbai</i> | <i>Pune</i> | <i>Banglore</i> | <i>Supply</i> |
|----------------------------|---------------|-------------|-----------------|---------------|
| <i>Jaipur</i> | 7 | 8 | 9 | 400 kg |
| <i>Kota</i> | 10 | 11 | 12 | 600 kg |
| <i>Demand</i> | 300 kg | 400 kg | 250 kg | |

FORMULATION :-

For the formulation of the above problem, we need to define some notations that are given below:-

| Notation | Definitions |
|----------|--|
| X1 | Product transported from Jaipur to Mumbai |
| y1 | Product transported from Jaipur to Pune |
| z1 | Product transported from Jaipur to Bangalore |
| x2 | Product transported from Kota to Mumbai |
| y2 | Product transported from Kota to Pune |
| z2 | Product transported from Kota to Bangalore |

Objective Function :-

The objective is to minimize **the total transportation cost** that is to be paid to the transportation .

Minimize

$$Z = 7x_1 + 8y_1 + 9z_1 + 10x_2 + 11y_2 + 12z_2$$

Subject to Constraints :

$$x_1 + y_1 + z_1 \leq 400k$$

$$x_2 + y_2 + z_2 \leq 600k$$

$$x_1 + x_2 = 300k$$

$$y_1 + y_2 = 400k$$

$$z_1 + z_2 = 250k$$

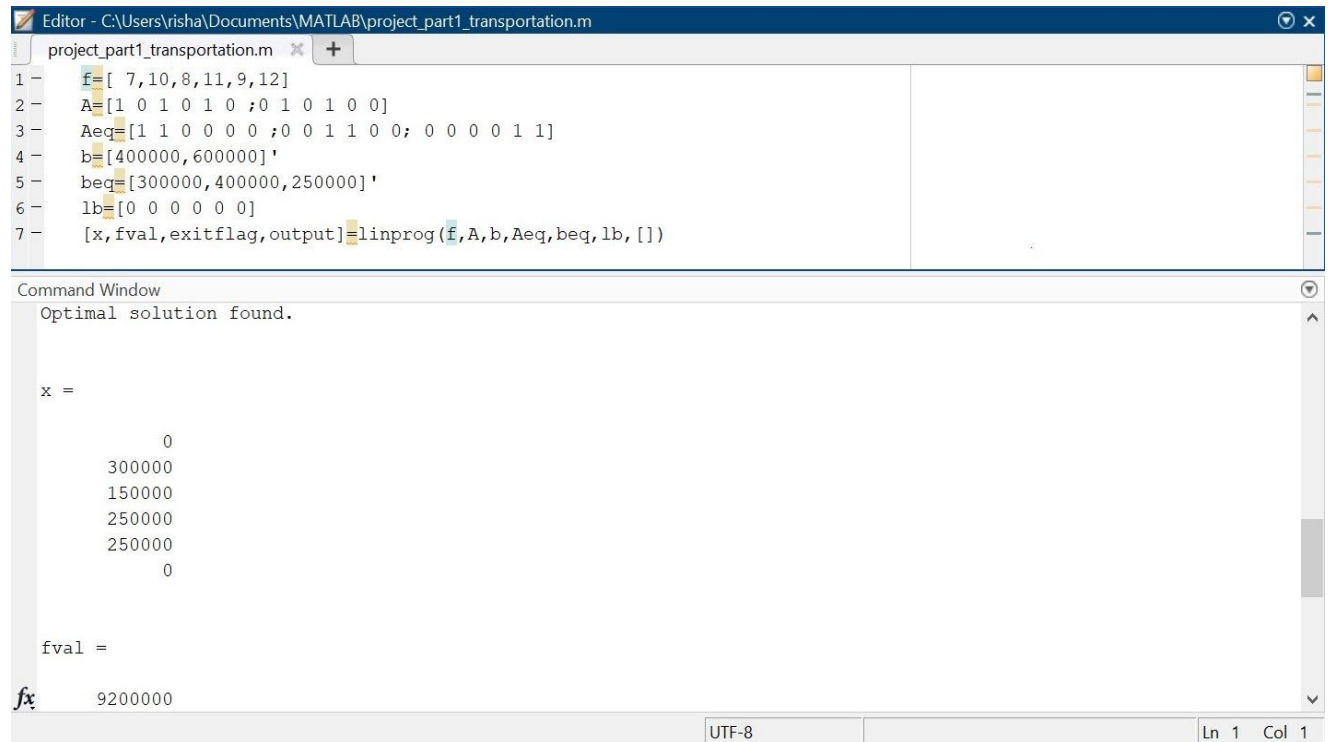
$$x_1, y_1, z_1, x_2, y_2, z_2 \geq 0$$

METHOD USED-DUAL SIMPLEX METHOD

Reason:

As the given problem is linear so we can use either simplex or dual simplex method .Dual simplex method is better because the possibility of infeasible solution gets removed by its use.

Matlab and Results:-



The image shows a MATLAB environment with an Editor window and a Command Window. The Editor window displays a script named `project_part1_transportation.m` with the following code:

```
1 f=[ 7,10,8,11,9,12]
2 A=[1 0 1 0 1 0 ;0 1 0 1 0 0]
3 Aeq=[1 1 0 0 0 0 ;0 0 1 1 0 0; 0 0 0 0 1 1]
4 b=[400000,600000]'
5 beq=[300000,400000,250000]'
6 lb=[0 0 0 0 0 0]
7 [x,fval,exitflag,output]=linprog(f,A,b,Aeq,beq,lb,[])
```

The Command Window displays the results of the `linprog` function:

```
Optimal solution found.

x =

    0
 300000
 150000
 250000
 250000
    0

fval =

fx 9200000
```

The status bar at the bottom indicates the file encoding is UTF-8 and the cursor is at Line 1, Column 1.

Objective 2 :-

In the following problem we have to create a model which allows the marketing manager to analyze its audience coverage and its advertisement from the accessible media, given the advertising budget as the constraints.

Problem Statement:-

The duty of manager is to suggest allotment of budget between different platforms like TELEVISION , NEWSPAPERS ,HOARDINGS, GOOGLE ADS and Facebook. These allotments are done supposing that our office has done investigation in setting up web analytics service and is calculating conversions through path length reports while performing Multi Channel Funnel Analysis. It has been learnt that a Rs.1 spent on each channel has customer reach as:

Channel(#customers reached)

TV(3),Newspapers(0.4),Hoardings(1.9),Google Ads(1.1),Facebook(2).

| Ways of Advertisement | ROI(in Percent) |
|-----------------------|-----------------|
| TV | 9 |
| Newspapers | 11 |
| Hoardings | 13 |
| Google Ads | 15 |
| Facebook | 17 |

FORMULATION :-

For the formulation of the above problem, we need to define some notations that are given below:-

| Notation | Definitions |
|----------|----------------------------|
| X1 | Budget for TV |
| X2 | Budget for Newspapers |
| X3 | Budget for Hoardings |
| X4 | Budget for Google Ads |
| X5 | Budget for facebook market |

Objective Function:-

Maximize customer outreach

$$Z = (0.09x_1 + 0.11x_2 + 0.13x_3 + 0.15x_4 + 0.17x_5)$$

Subject to Constraints:

1) Total budget should not exceed Rs.10 Million

$$x_1 + x_2 + x_3 + x_4 + x_5 \leq 10000k$$

2) TV advertising costs at least Rs.1000k

$$x_1 \geq 1000k$$

3) Budget of printing of newspapers is not greater than 50000k

$$x_2 \leq 500k \quad \text{changed to } x_2 < 50000k$$

4) Minimum cost of printing of newspaper is at least Rs.400k

$$x_2 \geq 400k$$

5) Budget for Hoardings and google Ads is at least 60% of budget

$$x_3 + x_4 \geq 0.6(x_1 + x_2 + x_3 + x_4 + x_5)$$

$$0.6x_1 + 0.6x_2 - 0.4x_3 - 0.4x_4 + 0.6x_5 \leq 0$$

6) Budget for google ads is not to be more than 3.5 times of budget of hoardings

$$x_4 > 3.5x_3$$

7) Budget for google ads more than 400k

$$-x_4 < 400k$$

8) Budget for google ads not more than 800k
 $x_4 < 8000k$

9) Facebook advertising costs at least Rs.200k
 $x_5 > 200k$

10) Budget for Hoardings should be greater than 15000
 $x_3 > 15000$,

11) Reaching more than 3 million customers
 $3x_1 + 0.4x_2 + 1.9x_3 + 1.1x_4 + 2x_5 > 3000k$

$$x_1, x_2, x_3, x_4, x_5 \geq 0$$

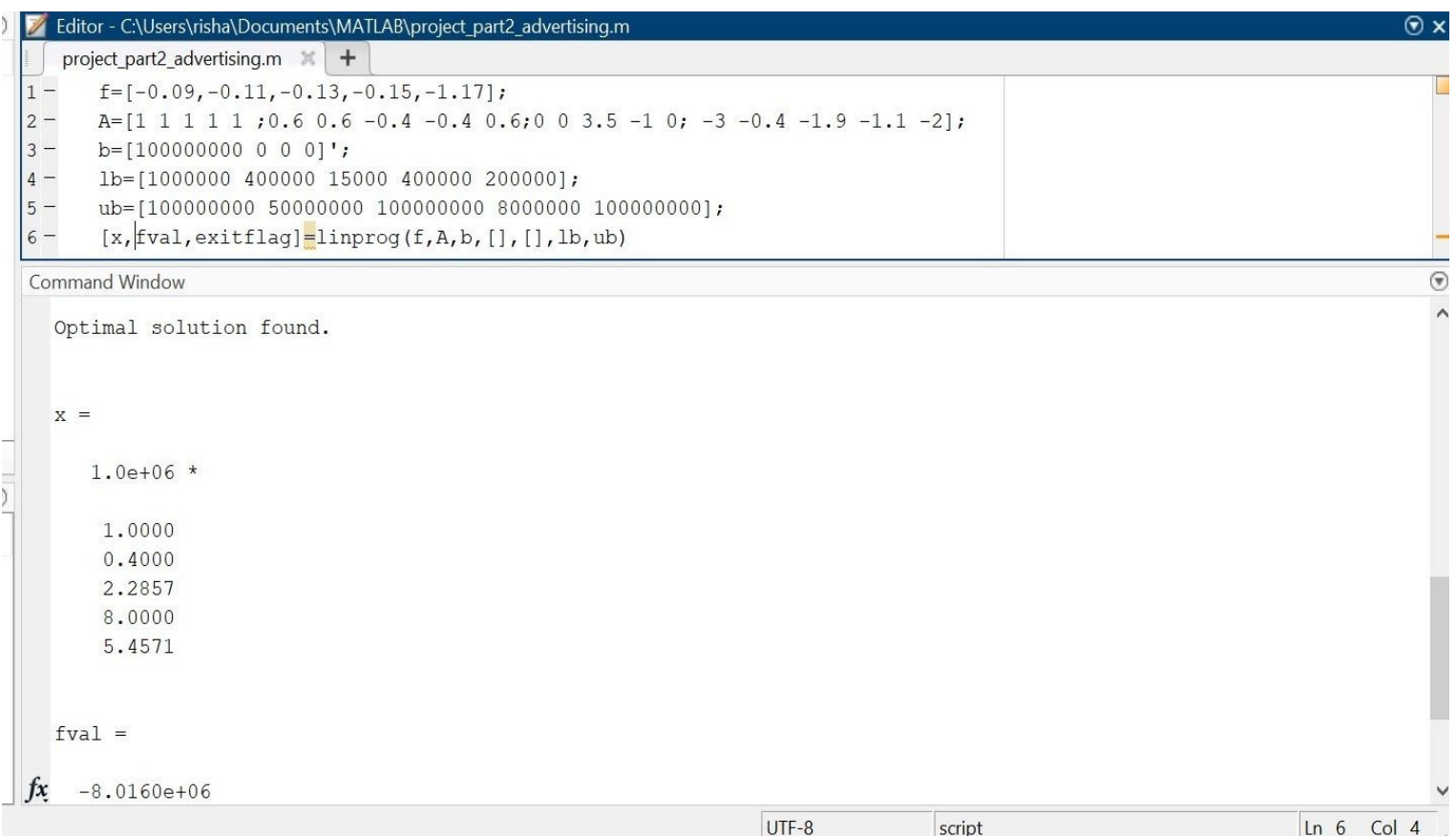
Method Used-Dual simplex method

Reason:

As the given problem is linear so we can use either simplex or dual simplex method. Dual simplex method is better because the possibility of infeasible solution gets removed by its use.

As minimization is default in linear programming. So maximization is done by taking $-z$. So we will find $-z$.

Matlab and Results:-



The screenshot displays the MATLAB environment. The Editor window shows a script named 'project_part2_advertising.m' with the following code:

```
1- f=[-0.09,-0.11,-0.13,-0.15,-1.17];  
2- A=[1 1 1 1 1 ;0.6 0.6 -0.4 -0.4 0.6;0 0 3.5 -1 0; -3 -0.4 -1.9 -1.1 -2];  
3- b=[100000000 0 0 0]';  
4- lb=[1000000 400000 15000 400000 200000];  
5- ub=[100000000 50000000 100000000 8000000 100000000];  
6- [x,fval,exitflag]=linprog(f,A,b,[],[],lb,ub)
```

The Command Window shows the output of the script:

```
Optimal solution found.  
  
x =  
  
1.0e+06 *  
  
1.0000  
0.4000  
2.2857  
8.0000  
5.4571  
  
fval =  
  
fx -8.0160e+06
```

The status bar at the bottom indicates the file encoding is UTF-8, the file type is script, and the cursor is at line 6, column 4.

References:

- Lecture notes and Guidance by Dr. Jayaprakash Kar
- Book referred Engineering Optimization, Theory and Practice 4th Edition by Singiresu S. Rao, JOHN WILEY & SONS, INC

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