

NCERT Solutions for Class 10 Maths Chapter 1

- Real Numbers

Chapter 1 - Real Numbers Exercise Ex. 1.1

Solution 1

(i) 135 and 225

Step 1: Since $225 > 135$, apply Euclid's division lemma, to $a = 225$ and $b = 135$ to find q and r such

that $225 = 135q + r$, $0 \leq r$

On dividing 225 by 135 we get quotient as 1 and remainder as 90

i.e $225 = 135 \times 1 + 90$

Step 2: Remainder r which is $90 \neq 0$, we apply Euclid's division lemma to $b = 135$ and $r = 90$ to find whole numbers q and r such that

$135 = 90 \times q + r$, $0 \leq r < 90$

On dividing 135 by 90 we get quotient as 1 and remainder as 45

i.e $135 = 90 \times 1 + 45$

Step 3: Again remainder $r = 45 \neq 0$ so we apply Euclid's division lemma to $b = 90$ and $r = 45$ to find q and r such that

$90 = 90 \times q + r$, $0 \leq r < 45$

On dividing 90 by 45 we get quotient as 2 and remainder as 0

i.e $90 = 2 \times 45 + 0$

Step 4: Since the remainder is zero, the divisor at this stage will be HCF of (135, 225).

Since the divisor at this stage is 45, therefore, the HCF of 135 and 225 is 45.

(ii) 196 and 38220

Step 1: Since $38220 > 196$, apply Euclid's division lemma to $a = 38220$ and $b = 196$ to find whole numbers q and r such that

$38220 = 196q + r$, $0 \leq r < 196$

On dividing 38220 we get quotient as 195 and remainder r as 0

i.e $38220 = 196 \times 195 + 0$

Since the remainder is zero, divisor at this stage will be HCF

Since divisor at this stage is 196, therefore, HCF of 196 and 38220 is 196.

NOTE: $\text{HCF}(a, b) = a$ if a is a factor of b . Here, 196 is a factor of 38220 so HCF is 196.

(iii) 867 and 255

Step 1: Since $867 > 255$, apply Euclid's division lemma, to $a = 867$ and $b = 255$ to find q and r such

that $867 = 255q + r$, $0 \leq r < 255$

On dividing 867 by 255 we get quotient as 3 and remainder as 102

i.e $867 = 255 \times 3 + 102$

Step 2: Since remainder $102 \neq 0$, we apply the division lemma to $a = 255$ and $b = 102$ to find whole numbers q and r such that

$$255 = 102q + r \text{ where } 0 \leq r < 102$$

On dividing 255 by 102 we get quotient as 2 and remainder as 51

$$\text{i.e } 255 = 102 \times 2 + 51$$

Step 3: Again remainder 51 is non zero, so we apply the division lemma to $a=102$ and $b= 51$ to find whole numbers q and r such that

$$102 = 51 q + r \text{ where } 0 \leq r < 51$$

On dividing 102 by 51 quotient is 2 and remainder is 0

$$\text{i.e } 102 = 51 \times 2 + 0$$

Since the remainder is zero, the divisor at this stage is the HCF

Since the divisor at this stage is 51, therefore, HCF of 867 and 255 is 51.

Concept Insight: To crack such problem remember to apply the Euclid's division Lemma which states that "Given positive integers a and b , there exists unique integers q and r satisfying $a = bq + r$, where

$$0 \leq r < b$$

" in the correct order.

Here, $a > b$.

Euclid's algorithm works since Dividing 'a' by 'b', replacing 'b' by 'r' and 'a' by 'b' and repeating the process of division till remainder 0 is reached, gives a number which divides a and b exactly.

$$\text{i.e } \text{HCF}(a,b) = \text{HCF}(b,r)$$

Note that do not find the HCF using prime factorisation in this question when the method is specified and do not skip steps.

Solution 2

Let a be any odd positive integer we need to prove that a is of the form $6q + 1$, or $6q + 3$, or $6q + 5$, where q is some integer.

Since a is an integer consider $b = 6$ another integer applying Euclid's division lemma we get

$$a = 6q + r \text{ for some integer } q \geq 0, \text{ and } r = 0, 1, 2, 3, 4, 5 \text{ since}$$

$$0 \leq r < 6.$$

Therefore, $a = 6q$ or $6q + 1$ or $6q + 2$ or $6q + 3$ or $6q + 4$ or $6q + 5$

However since a is odd so a cannot take the values $6q$, $6q+2$ and $6q+4$ (since all these are divisible by 2)

Also, $6q + 1 = 2 \times 3q + 1 = 2k_1 + 1$, where k_1 is a positive integer

$6q + 3 = (6q + 2) + 1 = 2(3q + 1) + 1 = 2k_2 + 1$, where k_2 is an integer

$6q + 5 = (6q + 4) + 1 = 2(3q + 2) + 1 = 2k_3 + 1$, where k_3 is an integer

Clearly, $6q + 1$, $6q + 3$, $6q + 5$ are of the form $2k + 1$, where k is an integer.

Therefore, $6q + 1$, $6q + 3$, $6q + 5$ are odd numbers.

Therefore, any odd integer can be expressed is of the form

$6q + 1$, or $6q + 3$, or $6q + 5$ where q is some integer

Concept Insight: In order to solve such problems Euclid's division lemma is applied to two integers a and b the integer b must be taken in accordance with what is to be proved, for example here the integer b was taken 6 because a must be of the form $6q + 1$, $6q + 3$, $6q + 5$.

Basic definition of even and odd numbers and the fact that addition and , multiplication of integers is always an integer are applicable here.

Solution 3

Maximum number of columns in which the Army contingent and the band can march will be given by HCF (616, 32)

We can use Euclid's algorithm to find the HCF.

Step 1: since $616 > 32$ so applying Euclid's division lemma to $a = 616$ and $b = 32$ we get integers q and r as 32 and 19
i.e $616 = 32 \times 19 + 8$

Step 2: since remainder $r \neq 0$ so again applying Euclid's lemma to 32 and 8 we get integers 4 and 0 as the quotient and remainder
i.e $32 = 8 \times 4 + 0$

Step 3: Since remainder is zero so divisor at this stage will be the HCF

The HCF (616, 32) is 8.

Therefore, they can march in 8 columns each.

Concept Insight: In order to solve the word problems first step is to interpret the problem and identify what is to be determined. The key word "Maximum" means we need to find the HCF. Do not forget to write the unit in the answer.

Solution 4

Let a be any positive integer we need to prove that a^2 is of the form $3m$ or $3m + 1$ for some integer m .

Let $b = 3$ be the other integer so applying Euclid's division lemma to a and $b = 3$

We get $a = 3q + r$ for some integer $q \geq 0$ and $r = 0, 1, 2$

Therefore, $a = 3q$ or $3q + 1$ or $3q + 2$

Now Consider a^2

$$a^2 = (3q)^2 \text{ or } (3q+1)^2 \text{ or } (3q+2)^2$$

$$a^2 = (9q^2) \text{ or } 9q^2 + 6q + 1 \text{ or } 9q^2 + 12q + 4$$

$$= 3 \times (3q^2) \text{ or } 3(3q^2 + 2q) + 1 \text{ or } 3(3q^2 + 4q + 1) + 1$$

$$= 3k_1 \text{ or } 3k_2 + 1 \text{ or } 3k_3 + 1$$

Where $k_1 = 3q^2$, $k_2 = 3q^2 + 2q$ and $k_3 = 3q^2 + 4q + 1$ since $q, 2, 3, 1$ etc are all integers so is their sum and product.

So k_1, k_2, k_3 are all integers.

Hence, it can be said that the square of any positive integer is either of the form $3m$ or $3m + 1$ for any integer m .

Concept Insight: In order to solve such problems Euclid's division lemma is applied to two integers a and b the integer b must be taken in accordance with what is to be proved, for example here the integer b was taken 3 because a must be of the form $3m$ or $3m + 1$. Do not forget to take a^2 . Note that variable is just a notation and not the absolute value.

Solution 5

Let a be any positive integer and $b = 3$

$$a = 3q + r, \text{ where } q \geq 0 \text{ and } 0 \leq r < 3$$

$$\therefore a = 3q \text{ or } 3q + 1 \text{ or } 3q + 2$$

Therefore, every number can be represented as these three forms. There are three cases.

Case 1: When $a = 3q$,

$$a^3 = (3q)^3 = 27q^3 = 9(3q^3) = 9m,$$

Where m is an integer such that $m = 3q^3$

Case 2: When $a = 3q + 1$,

$$a^3 = (3q + 1)^3$$

$$a^3 = 27q^3 + 27q^2 + 9q + 1$$

$$a^3 = 9(3q^3 + 3q^2 + q) + 1$$

$$a^3 = 9m + 1$$

Where m is an integer such that $m = (3q^3 + 3q^2 + q)$

Case 3: When $a = 3q + 2$,

$$a^3 = (3q + 2)^3$$

$$a^3 = 27q^3 + 54q^2 + 36q + 8$$

$$a^3 = 9(3q^3 + 6q^2 + 4q) + 8$$

$$a^3 = 9m + 8$$

Where m is an integer such that $m = (3q^3 + 6q^2 + 4q)$

Therefore, the cube of any positive integer is of the form $9m$, $9m + 1$, or $9m + 8$.

Concept Insight: In this problem Euclid's division lemma can be applied to integers a and b = 9 as well but using 9 will give us 9 values of r and hence as many cases so solution will be lengthy. Since every number which is divisible by 9 is also divisible by 3 so 3 is used.

Do not forget to take a^3 and all the different values of a i.e

$$\therefore a = 3q \text{ or } 3q + 1 \text{ or } 3q + 2$$

Chapter 1 - Real Numbers Exercise Ex. 1.2

Solution 1

$$(i) \quad 140 = 2 \times 2 \times 5 \times 7 = 2^2 \times 5 \times 7$$

$$(ii) \quad 156 = 2 \times 2 \times 3 \times 13 = 2^2 \times 3 \times 13$$

$$(iii) \quad 3825 = 3 \times 3 \times 5 \times 5 \times 17 = 3^2 \times 5^2 \times 17$$

$$(iv) \quad 5005 = 5 \times 7 \times 11 \times 13$$

$$(v) \quad 7429 = 17 \times 19 \times 23$$

Concept Insight: Since the given number needs to be expressed as the product of prime factors so in order to solve this problem knowing prime numbers is required. Do not forget to put the exponent in case a prime number is repeating.

Solution 2

$$(i) \quad 26 \text{ and } 91$$

$$26 = 2 \times 13$$

$$91 = 7 \times 13$$

$$\text{HCF} = 13$$

$$\text{LCM} = 2 \times 7 \times 13 = 182$$

$$\text{Product of the two numbers} = 26 \times 91 = 2366$$

$$\text{HCF} \times \text{LCM} = 13 \times 182 = 2366$$

Hence, product of two numbers = HCF \times LCM

(ii) 510 and 92
 $510 = 2 \times 3 \times 5 \times 17$
 $92 = 2 \times 2 \times 23$
 $HCF = 2$
 $LCM = 2 \times 2 \times 3 \times 5 \times 17 \times 23 = 23460$
 Product of the two numbers = $510 \times 92 = 46920$
 $HCF \times LCM = 2 \times 23460$
 $= 46920$
 Hence, product of two numbers = $HCF \times LCM$

(iii) 336 and 54
 $336 = 2 \times 2 \times 2 \times 2 \times 3 \times 7$
 $336 = 2^4 \times 3 \times 7$
 $54 = 2 \times 3 \times 3 \times 3$
 $54 = 2 \times 3^3$
 $HCF = 2 \times 3 = 6$
 $LCM = 2^4 \times 3^3 \times 7 = 3024$
 Product of the two numbers = $336 \times 54 = 18144$
 $HCF \times LCM = 6 \times 3024 = 18144$
 Hence, product of two numbers = $HCF \times LCM$

Concept Insight: HCF is the product of common prime factors raised to least power, while LCM is product of prime factors raised to highest power. HCF is always a factor of the LCM.

Do not skip verification product of two numbers = $HCF \times LCM$ as it can help in cross checking the answer.

Solution 3

(i) 12, 15 and 21
 $12 = 2^2 \times 3$
 $15 = 3 \times 5$
 $21 = 3 \times 7$
 $HCF = 3$
 $LCM = 2^2 \times 3 \times 5 \times 7 = 420$

(ii) 17, 23 and 29
 $17 = 1 \times 17$
 $23 = 1 \times 23$
 $29 = 1 \times 29$
 $HCF = 1$
 $LCM = 17 \times 23 \times 29 = 11339$

(iii) 8, 9 and 25
 $8 = 2 \times 2 \times 2$
 $9 = 3 \times 3$
 $25 = 5 \times 5$
 $HCF = 1$
 $LCM = 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5 = 1800$

Concept Insight: HCF is the product of common prime factors of all three numbers raised to least power, while LCM is product of prime factors of all here raised to highest power. Use the fact that HCF is always a factor of the LCM to verify the answer. Note HCF of (a,b,c) can also be calculated by taking two numbers at a time i.e HCF (a,b) and then HCF (b,c) .

Solution 4

$$\text{HCF}(306, 657) = 9$$

We know that, $\text{LCM} \times \text{HCF} = \text{Product of two numbers}$

$$\therefore \text{LCM} \times \text{HCF} = 306 \times 657$$

$$\text{LCM} = \frac{306 \times 657}{\text{HCF}} = \frac{306 \times 657}{9}$$

$$\text{LCM} = 22338$$

Concept Insight: This problem must be solved using product of two numbers = HCF x LCM rather than prime factorisation

Solution 5

If any number ends with the digit 0, it should be divisible by 10 or in other words its prime factorisation must include primes 2 and 5 both

$$\text{Prime factorisation of } 6_n = (2 \times 3)_n$$

By Fundamental Theorem of Arithmetic Prime factorisation of a number is unique. So 5 is not a prime factor of 6_n .

Hence, for any value of n, 6_n will not be divisible by 5.

Therefore, 6_n cannot end with the digit 0 for any natural number n.

Concept Insight: In order solve such problems the concept used is if a number is to end with zero then it must be divisible by 10 and the prime factorisation of a number is unique.

Solution 6

Numbers are of two types - prime and composite. Prime numbers has only two factors namely 1 and the number itself whereas composite numbers have factors other than 1 and itself.

It can be observed that

$$\begin{aligned} 7 \times 11 \times 13 + 13 &= 13 \times (7 \times 11 + 1) = 13 \times (77 + 1) \\ &= 13 \times 78 \\ &= 13 \times 13 \times 6 \end{aligned}$$

The given expression has 6 and 13 as its factors. Therefore, it is a composite number.

$$\begin{aligned} 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 + 5 &= 5 \times (7 \times 6 \times 4 \times 3 \times 2 \times 1 + 1) \\ &= 5 \times (1008 + 1) \\ &= 5 \times 1009 \end{aligned}$$

1009 cannot be factorised further. Therefore, the given expression has 5 and 1009 as its factors. Hence, it is a composite number.

Concept Insight: Definition of prime numbers and composite numbers is used. Do not miss the reasoning.

Solution 7

It can be observed that Ravi and Sonia does not take same amount of time Ravi takes lesser time than Sonia for completing 1 round of the circular path.

As they are going in the same direction, they will meet again at the same time when Ravi will have completed 1 round of that circular path with respect to Sonia.

i.e When Sonia completes one round then ravi completes 1.5 rounds. So they will meet first time at the time which is a common multiple of the time taken by them to complete 1 round

i.e LCM of 18 minutes and 12 minutes.

Now

$$18 = 2 \times 3 \times 3 = 2 \times 3^2$$

$$\text{And, } 12 = 2 \times 2 \times 3 = 2^2 \times 3$$

LCM of 12 and 18 = product of factors raised to highest exponent =
 $2^2 \times 3^2 = 36$

Therefore, Ravi and Sonia will meet together at the starting point after 36 minutes.

Concept Insight: In order to solve the word problems first step is to interpret the problem and identify what is to be determined. The problem asks for simultaneous reoccurrence of events so we need to find LCM. The key word for simultaneous reoccurrence of events is LCM. Do not forget to write the final answer.

Chapter 1 - Real Numbers Exercise Ex. 1.3

Solution 1

Let us assume, on the contrary that $\sqrt{5}$ is a rational number.

Therefore, we can find two integers a, b (b \neq 0) such that $\sqrt{5} = \frac{a}{b}$
Where a and b are co-prime integers.

$$\sqrt{5} = \frac{a}{b}$$

$$\Rightarrow a = \sqrt{5}b$$

$$\Rightarrow a^2 = 5b^2$$

Therefore, a^2 is divisible by 5 then a is also divisible by 5.

So $a = 5k$, for some integer k.

$$\text{Now, } a^2 = (5k)^2 = 5(5k^2) = 5b^2$$

$$\Rightarrow b^2 = 5k^2$$

This means that b^2 is divisible by 5 and hence, b is divisible by 5.

This implies that a and b have 5 as a common factor.

And this is a contradiction to the fact that a and b are co-prime.

So our assumption that $\sqrt{5}$ is rational is wrong.

Hence, $\sqrt{5}$ cannot be a rational number. Therefore, $\sqrt{5}$ is irrational.

Concept Insight: There are various ways of proving in mathematics proof by contradiction is one of them. In this approach we assume something which is contrary to what needs to be proved and arrive at a fact which contradicts something which is true in general. Key result used here is "If P is a prime number and it divides a^2 then it divides a as well".

Solution 2

Let us assume, on the contrary that $3 + 2\sqrt{5}$ is rational.

Therefore, we can find two integers a, b (b \neq 0) such that

$$3 + 2\sqrt{5} = \frac{a}{b}$$

$$2\sqrt{5} = \frac{a}{b} - 3$$

$$\sqrt{5} = \frac{1}{2} \left(\frac{a}{b} - 3 \right)$$

Since a and b are integers, $\frac{1}{2} \left(\frac{a}{b} - 3 \right)$ will also be rational and therefore, $\sqrt{5}$ is rational.

This contradicts the fact that $\sqrt{5}$ is irrational. Hence, our assumption that $3 + 2\sqrt{5}$ is rational is false. Therefore, $3 + 2\sqrt{5}$ is irrational.

Concept Insight: This problem is solved using proof by contradiction. The key concept used is if p is prime number then \sqrt{p} is irrational. Do not prove this question by assuming sum of rational and irrational is irrational.

Solution 3

(i) $\frac{1}{\sqrt{2}}$

Let us assume that $\frac{1}{\sqrt{2}}$ is rational.

Therefore, we can find two integers a, b ($b \neq 0$) such that

$$\frac{1}{\sqrt{2}} = \frac{a}{b}$$

$$\sqrt{2} = \frac{b}{a}$$

$\frac{b}{a}$ is rational as a and b are integers.

Therefore, $\sqrt{2}$ is rational which contradicts to the fact that $\sqrt{2}$ is irrational.

Hence, our assumption is false and $\frac{1}{\sqrt{2}}$ is irrational.

(ii) $7\sqrt{5}$

Let us assume that $7\sqrt{5}$ is rational.

Therefore, we can find two integers a, b ($b \neq 0$) such that

$$7\sqrt{5} = \frac{a}{b} \text{ for some integers } a \text{ and } b$$

$$\therefore \sqrt{5} = \frac{a}{7b}$$

$\frac{a}{7b}$ is rational as a and b are integers.

Therefore, $\sqrt{5}$ should be rational.

This contradicts the fact that $\sqrt{5}$ is irrational. Therefore, our assumption that $7\sqrt{5}$ is rational is false. Hence, $7\sqrt{5}$ is irrational.

(iii) $6 + \sqrt{2}$

Let $6 + \sqrt{2}$ be rational.

Therefore, we can find two integers a, b ($b \neq 0$) such that

$$6 + \sqrt{2} = \frac{a}{b}$$

$$\sqrt{2} = \frac{a}{b} - 6$$

Since a and b are integers, $\frac{a}{b} - 6$ is also rational and hence, $\sqrt{2}$ should be rational. This contradicts the fact that $\sqrt{2}$ is irrational. Therefore, our assumption is false and hence, $6 + \sqrt{2}$ is irrational.

Concept Insight: This problem is solved using proof by contradiction. The key concept used is if p is prime number then \sqrt{p} is irrational. Do not prove this question by assuming sum or product of rational and irrational is irrational.

Chapter 1 - Real Numbers Exercise Ex. 1.4

Solution 1

(i) $\frac{13}{3125}$

$$3125 = 5^5$$

The denominator is of the form 5^m .

Hence, the decimal expansion of $\frac{13}{3125}$ is terminating.

(ii) $\frac{17}{8}$

$$8 = 2^3$$

The denominator is of the form 2^m .

Hence, the decimal expansion of $\frac{17}{8}$ is terminating.

(iii) $\frac{64}{455}$

$$455 = 5 \times 7 \times 13$$

Since the denominator is not in the form $2^m \times 5^n$, and it also contains 7 and 13 as its factors, its decimal expansion will be non-terminating repeating.

(iv) $\frac{15}{1600}$

$$1600 = 2^6 \times 5^2$$

The denominator is of the form $2_m \times 5_n$.

Hence, the decimal expansion of $\frac{15}{1600}$ is terminating.

$$(v) \quad \frac{29}{343}$$

$$343 = 7^3$$

Since the denominator is not in the form $2_m \times 5_n$, and it has 7 as its factor,

the decimal expansion of $\frac{29}{343}$ is non-terminating repeating.

$$(vi) \quad \frac{23}{2^3 \times 5^2}$$

The denominator is of the form $2_m \times 5_n$.

Hence, the decimal expansion of $\frac{23}{2^3 \times 5^2}$ is terminating.

$$(vii) \quad \frac{129}{2^2 \times 5^7 \times 7^5}$$

Since the denominator is not of the form $2^m \times 5^n$, and it also has 7 as its

factor, the decimal expansion of $\frac{129}{2^2 \times 5^7 \times 7^5}$ is non-terminating repeating.

$$(viii) \quad \frac{6}{15} = \frac{2 \times 3}{3 \times 5} = \frac{2}{5}$$

The denominator is of the form 5_n .

Hence the decimal expansion of $\frac{6}{15}$ is terminating.

$$(ix) 50 = 2 \times 5 \times 5$$

The denominator is of the form $2^m \times 5^n$.

Hence, the decimal expansion of $\frac{35}{50}$ is terminating.

$$(x) \quad \frac{77}{210} = \frac{11 \times 7}{30 \times 7} = \frac{11}{30}$$

$$30 = 2 \times 3 \times 5$$

Since the denominator is not of the form $2^m \times 5^n$, and it also has 3 as its factors,

the decimal expansion of $\frac{77}{210}$ is non-terminating repeating.

Concept Insight: The concept used in this problem is that

The decimal expansion of rational number $\frac{p}{q}$ where p and q are coprime numbers,

terminates if and only if the prime factorisation of q is of the form $2^n 5^m$, where n and m are non negative integers. Do not forget that 0 is also a non negative integer so n or m can take value 0. Generally mistake is committed in identifying terminating decimals when either of the two prime numbers 2 or 5 is appearing in the prime factorisation.

Solution 2

$$(i) \quad \frac{13}{3125} = 0.00416$$

$$\begin{array}{r}
 0.00416 \\
 3125 \overline{)13.00000} \\
 \underline{-0} \\
 130 \\
 \underline{-0} \\
 1300 \\
 \underline{-0} \\
 13000 \\
 \underline{-12500} \\
 5000 \\
 \underline{-3125} \\
 18750 \\
 \underline{-18750} \\
 \times
 \end{array}$$

$$(ii) \quad \frac{17}{8} = 2.125$$

$$\begin{array}{r}
 2.125 \\
 8 \overline{)17} \\
 \underline{-16} \\
 10 \\
 \underline{-8} \\
 20 \\
 \underline{-16} \\
 40 \\
 \underline{-40} \\
 \times
 \end{array}$$

$$(iv) \quad \frac{15}{1600} = 0.009375$$

$$\begin{array}{r}
 0.009375 \\
 1600 \overline{)15.000000} \\
 \underline{-0} \\
 150 \\
 \underline{-0} \\
 1500 \\
 \underline{-0} \\
 15000 \\
 \underline{-14400} \\
 6000 \\
 \underline{-4800} \\
 12000 \\
 \underline{-11200} \\
 8000 \\
 \underline{-8000} \\
 \times
 \end{array}$$

$$(vi) \quad \frac{23}{2^3 \times 5^2} = \frac{23}{200} = 0.115$$

$$\begin{array}{r} 0.115 \\ 200 \overline{) 23.000} \\ \underline{- 0} \\ 230 \\ \underline{- 200} \\ 300 \\ \underline{- 200} \\ 1000 \\ \underline{- 1000} \\ \times \end{array}$$

$$(viii) \quad \frac{6}{15} = \frac{2 \times 3}{3 \times 5} = \frac{2}{5} = 0.4$$

$$\begin{array}{r} 0.4 \\ 5 \overline{) 2.0} \\ \underline{- 0} \\ 20 \\ \underline{- 20} \\ \times \end{array}$$

$$(ix) \quad \frac{35}{50} = 0.7$$

$$\begin{array}{r} 0.7 \\ 50 \overline{) 35.0} \\ \underline{- 0} \\ 350 \\ \underline{- 350} \\ \times \end{array}$$

Concept Insight: This is based on performing the long division and expressing the rational number in the decimal form learnt in lower classes.

Solution 3

(i) 43.123456789

Since this number has a terminating decimal expansion, it is a rational number of the form $\frac{p}{q}$ and q is of the form $2^m \times 5^n$,

i.e., the prime factors of q will be either 2 or 5 or both.

(ii) 0.120120012000120000...

The decimal expansion is neither terminating nor recurring. Therefore, the given number is an irrational number.

(iii) $\overline{43.123456789}$

Since the decimal expansion is non-terminating recurring, the given number is a rational number of

the form $\frac{p}{q}$ and q is not of the form $2_m \times 5_n$ i.e., the prime factors of q will also have a

factor other than 2 or 5.

Concept Insight: The concept used in this problem is that,

If the decimal expansion of rational number $\frac{p}{q}$, [where p and q are coprime numbers] terminates, then prime factorization of q is of the form $2^n 5^m$, where n and m are non negative integers.

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