

he 10th chapter of RD Sharma Class 10 is Circles. This chapter consists of two exercises of problems dealing with properties of a tangent to a circle, tangent from a point on a circle, length of tangents, cyclic quadrilateral and other types of tangents to intersecting and concentric circles. To know the right way of interpreting and solving those problems the [RD Sharma Solutions for Class 10](#) will definitely help you out for that need. Moreover, the students can also learn the easy tricks and shortcuts of solving problems in this chapter.

## Access the RD Sharma Solutions For Class 10 Chapter 10 – Circles

### RD Sharma Class 10 Chapter 10 Exercise 10.1 Page No: 10.5

#### 1. Fill in the blanks:

- (i) The common point of tangent and the circle is called \_\_\_\_\_.
- (ii) A circle may have \_\_\_\_\_ parallel tangent.
- (iii) A tangent to a circle intersects it in \_\_\_\_\_ point.
- (iv) A line intersecting a circle in two points is called a \_\_\_\_\_
- (v) The angle between tangent at a point P on circle and radius through the point is \_\_\_\_\_

#### Solution:

- (i) The common point of tangent and the circle is called point of contact.
- (ii) A circle may have two parallel tangent.
- (iii) A tangent to a circle intersects it in one point.
- (iv) A line intersecting a circle in two points is called a secant.
- (v) The angle between tangent at a point P on circle and radius through the point is  $90^\circ$ .

#### 2. How many tangents can a circle have?

#### Solution:

A tangent is defined as a line intersecting the circle in one point. Since, there are infinite number of points on the circle, a circle can have many (infinite) tangents.

### RD Sharma Class 10 Chapter 10 Exercise 10.2 Page No: 10.33

1. If PT is a tangent at T to a circle whose centre is O and  $OP = 17$  cm,  $OT = 8$  cm. Find the length of the tangent segment PT.

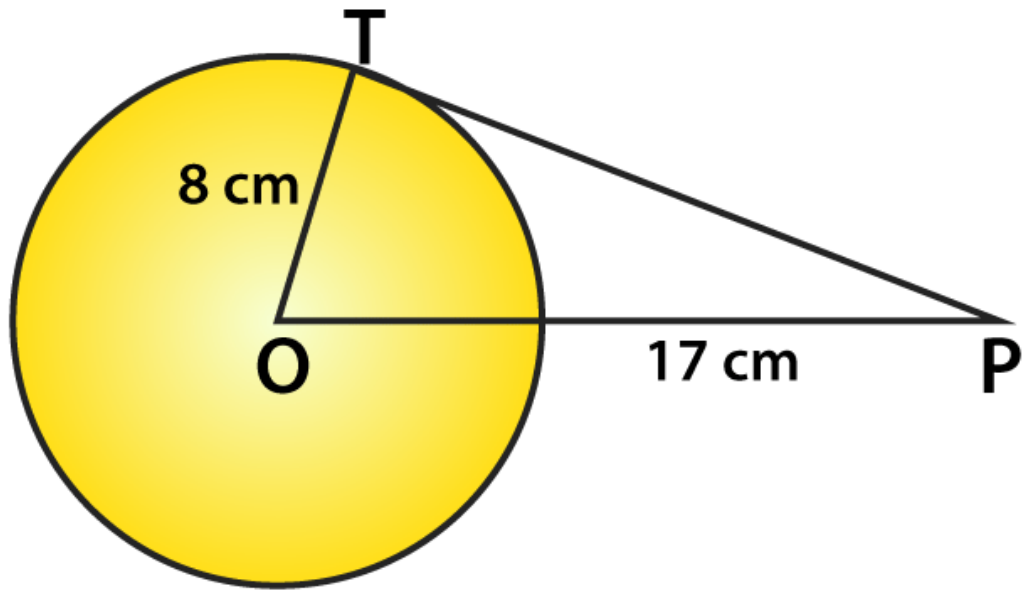
#### Solution:

Given,

$OT = \text{radius} = 8$  cm

$OP = 17$  cm

To find:  $PT = \text{length of tangent} = ?$



Clearly, T is point of contact. And, we know that at point of contact tangent and radius are perpendicular.

$\therefore$  OTP is right angled triangle  $\angle OTP = 90^\circ$ , from Pythagoras theorem  $OT^2 + PT^2 = OP^2$

$$8^2 + PT^2 = 17^2$$

$$8^2 + PT^2 = 17^2$$

$$PT = \sqrt{17^2 - 8^2}$$

$$= \sqrt{289 - 64}$$

$$= \sqrt{225}$$

$\therefore$  PT = length of tangent = 15 cm.

**2. Find the length of a tangent drawn to a circle with radius 5cm, from a point 13 cm from the center of the circle.**

**Solution:**

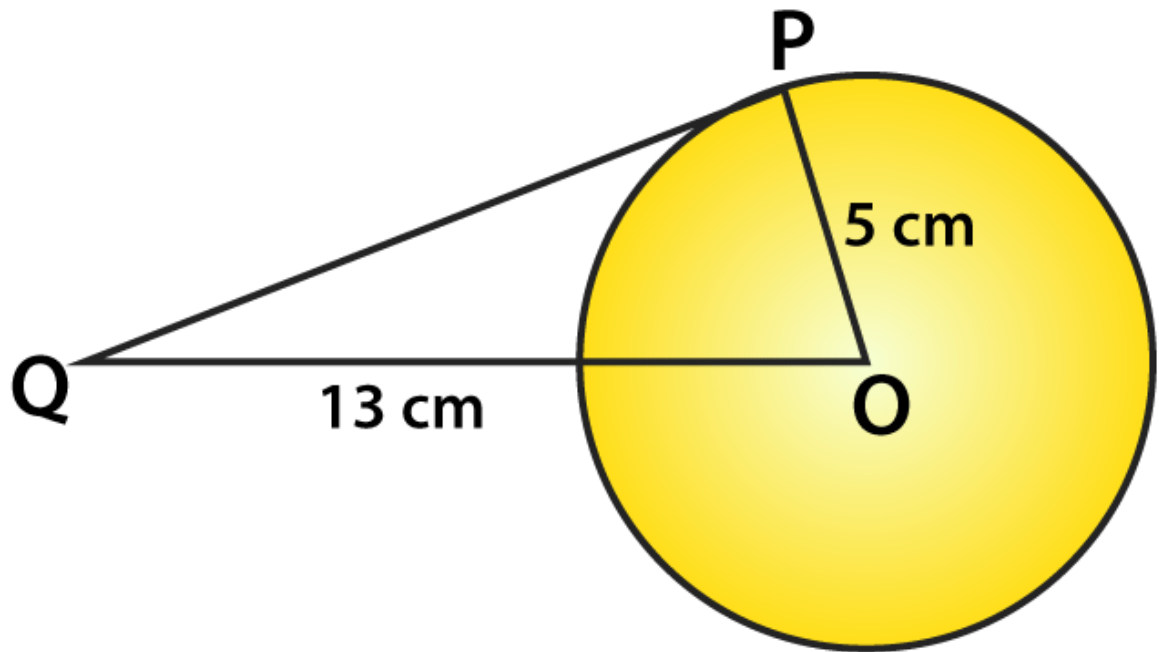
Consider a circle with centre O.

OP = radius = 5 cm. (given)

A tangent is drawn at point P, such that line through O intersects it at Q.

And, OQ = 13cm (given).

To find: Length of tangent PQ = ?



We know that tangent and radius are perpendicular to each other.

$\triangle OPQ$  is right angled triangle with  $\angle OPQ = 90^\circ$

By Pythagoras theorem we have,

$$OQ^2 = OP^2 + PQ^2$$

$$\Rightarrow 13^2 = 5^2 + PQ^2$$

$$\Rightarrow PQ^2 = 169 - 25 = 144$$

$$\Rightarrow PQ = \sqrt{144}$$

$$= 12 \text{ cm}$$

Therefore, the length of tangent = 12 cm

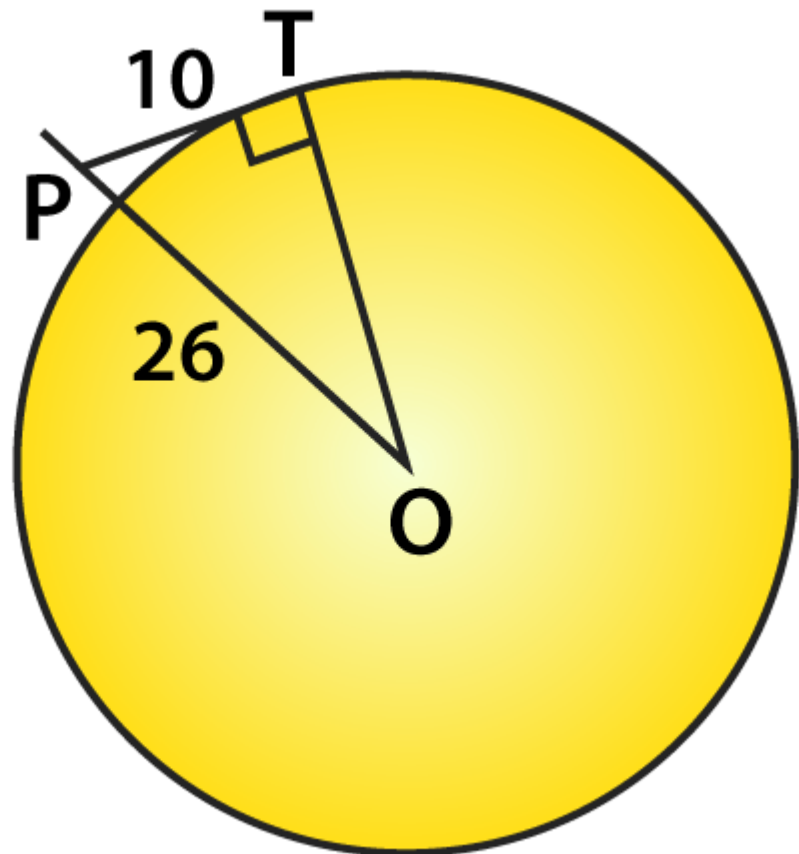
**3. A point P is 26 cm away from O of circle and the length PT of the tangent drawn from P to the circle is 10 cm. Find the radius of the circle.**

**Solution:**

Given,  $OP = 26 \text{ cm}$

$PT = \text{length of tangent} = 10 \text{ cm}$

To find: radius =  $OT = ?$



We know that,

At point of contact, radius and tangent are perpendicular  $\angle OTP = 90^\circ$

So,  $\triangle OTP$  is right angled triangle.

Then by Pythagoras theorem, we have

$$OP^2 = OT^2 + PT^2$$

$$26^2 = OT^2 + 10^2$$

$$OT^2 = 676 - 100$$

$$OT = \sqrt{576}$$

$$OT = 24 \text{ cm}$$

Thus,  $OT = \text{length of tangent} = 24 \text{ cm}$

**4. If from any point on the common chord of two intersecting circles, tangents be drawn to the circles, prove that they are equal.**

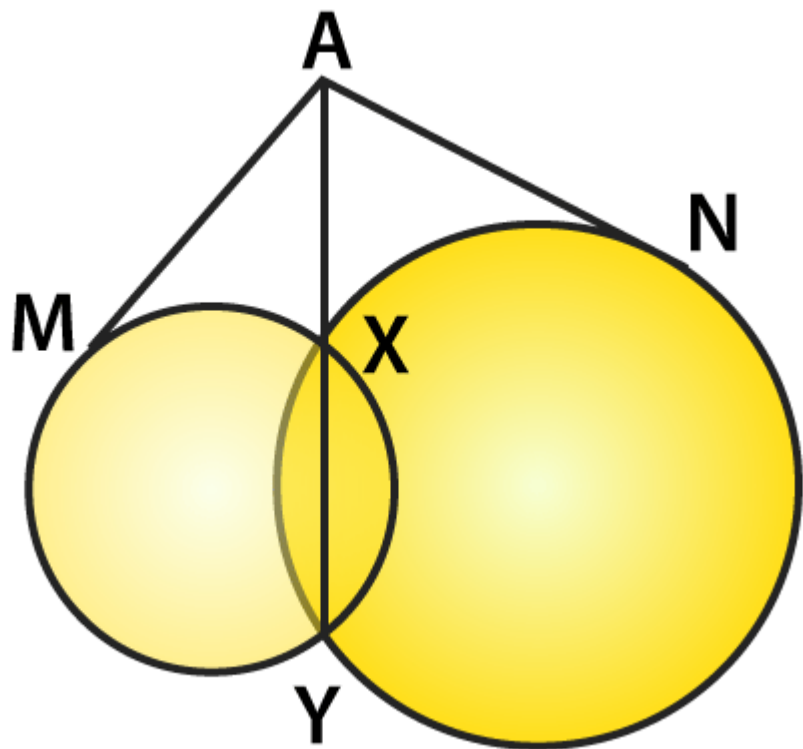
**Solution:**

Let the two circles intersect at points X and Y.

So, XY is the common chord.

Suppose 'A' is a point on the common chord and AM and AN be the tangents drawn A to the circle

Then it's required to prove that  $AM = AN$ .



In order to prove the above relation, following property has to be used.

“Let PT be a tangent to the circle from an external point P and a secant to the circle through P intersecting the circle at points A and B, then  $PT^2 = PA \times PB$ ”

Now AM is the tangent and AXY is a secant

$$\therefore AM^2 = AX \times AY \dots (i)$$

Similarly, AN is a tangent and AXY is a secant

$$\therefore AN^2 = AX \times AY \dots (ii)$$

From (i) & (ii), we have  $AM^2 = AN^2$

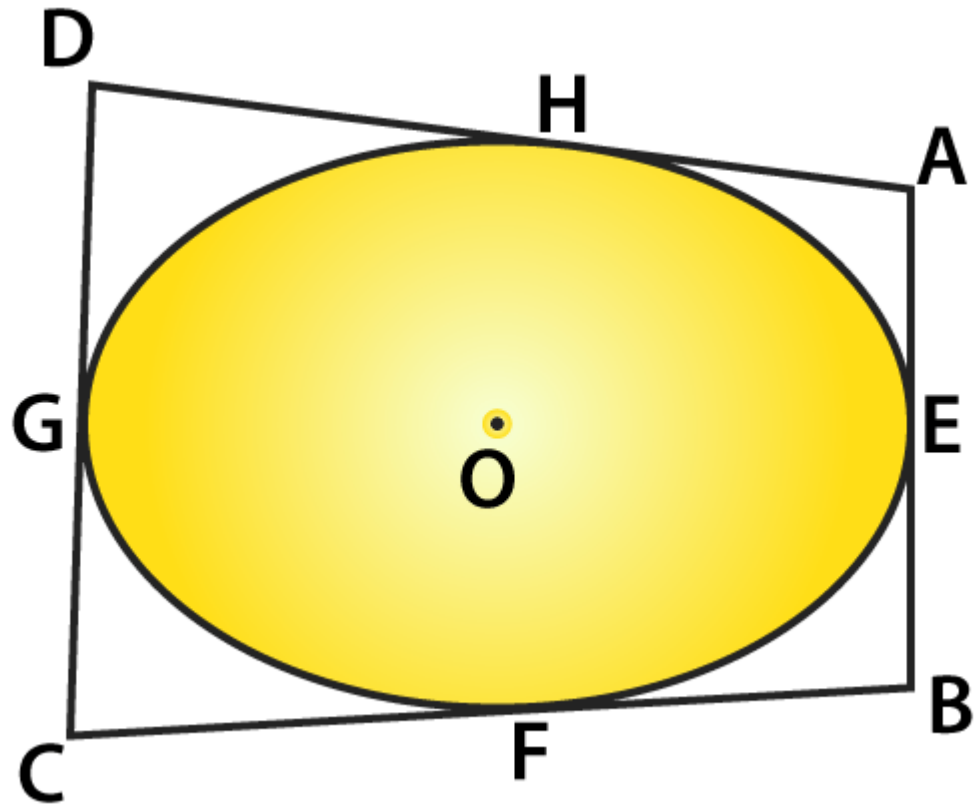
$$\therefore AM = AN$$

Therefore, tangents drawn from any point on the common chord of two intersecting circles are equal.

- Hence Proved

**5. If the quadrilateral sides touch the circle, prove that sum of pair of opposite sides is equal to the sum of other pair.**

**Solution:**



Consider a quadrilateral ABCD touching circle with centre O at points E, F, G and H as shown in figure.

We know that,

The tangents drawn from same external points to the circle are equal in length.

Consider tangents:

1. From point A [AH & AE]

$AH = AE \dots (i)$

2. From point B [EB & BF]

$BF = EB \dots (ii)$

3. From point C [CF & GC]

$FC = CG \dots (iii)$

4. From point D [DG & DH]

$DH = DG \dots (iv)$

Adding (i), (ii), (iii), & (iv)

$(AH + BF + FC + DH) = [(AC + CB) + (CG + DG)]$

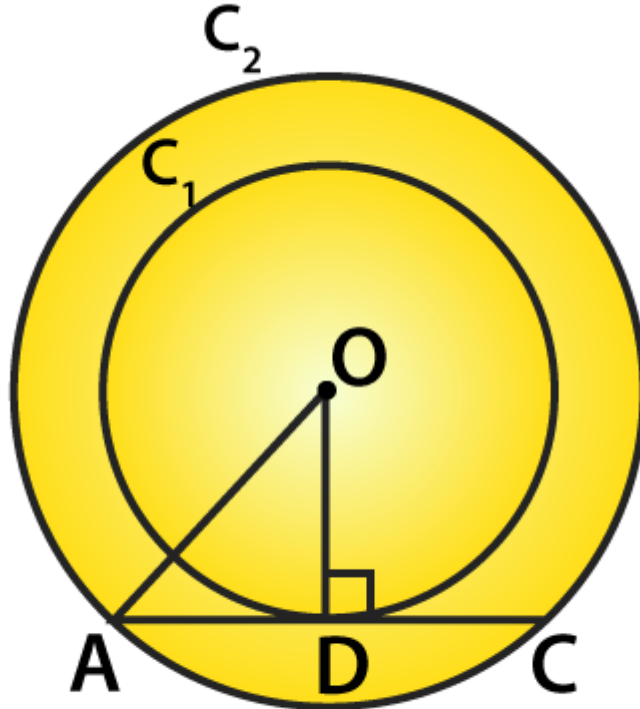
$\Rightarrow (AH + DH) + (BF + FC) = (AE + EB) + (CG + DG)$

$\Rightarrow AD + BC = AB + DC$  [from fig.]

Therefore, the sum of one pair of opposite sides is equal to other.

- Hence Proved

6. Out of the two concentric circles, the radius of the outer circle is 5 cm and the chord AC of length 8 cm is a tangent to the inner circle. Find the radius of the inner circle.  
Solution:



Let  $C_1$  and  $C_2$  be the two circles having same center O.

And, AC is a chord which touches the  $C_1$  at point D

let's join OD.

So,  $OD \perp AC$

$AD = DC = 4$  cm [perpendicular line OD bisects the chord]

Thus, in right angled  $\triangle AOD$ ,

$OA^2 = AD^2 + DO^2$  [By Pythagoras theorem]

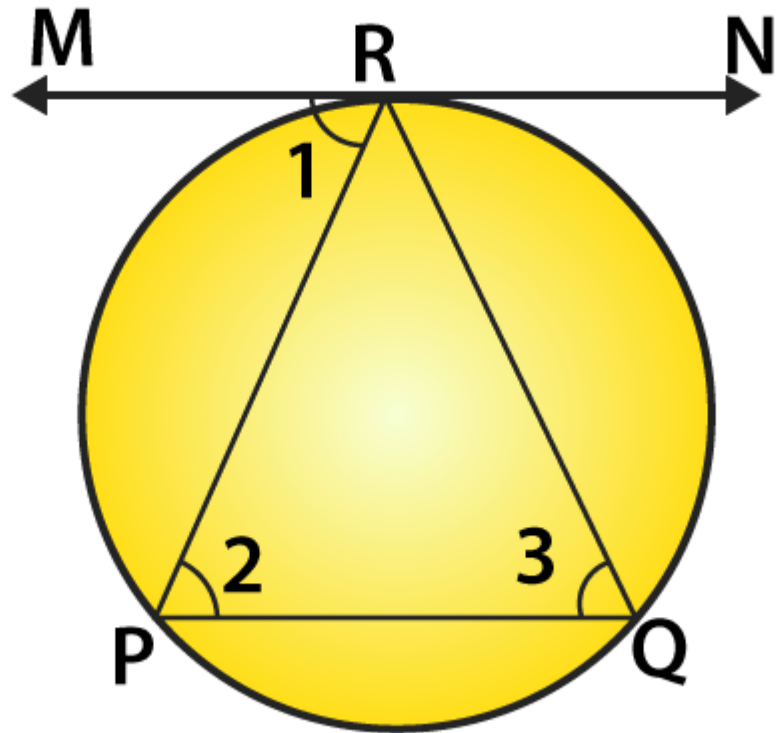
$$DO^2 = 5^2 - 4^2 = 25 - 16 = 9$$

$$DO = 3 \text{ cm}$$

Therefore, the radius of the inner circle  $OD = 3$  cm.

7. A chord PQ of a circle is parallel to the tangent drawn at a point R of the circle. Prove that R bisects the arc PRQ.

Solution:



Given: Chord PQ is parallel tangent at R.

To prove: R bisects the arc PRQ.

Proof:

Since  $PQ \parallel$  tangent at R.

$\angle 1 = \angle 2$  [alternate interior angles]

$\angle 1 = \angle 3$

[angle between tangent and chord is equal to angle made by chord in alternate segment]

So,  $\angle 2 = \angle 3$

$\Rightarrow PR = QR$  [sides opposite to equal angles are equal]

Hence, clearly R bisects PQ.



**8. Prove that a diameter AB of a circle bisects all those chords which are parallel to the tangent at the point A.**

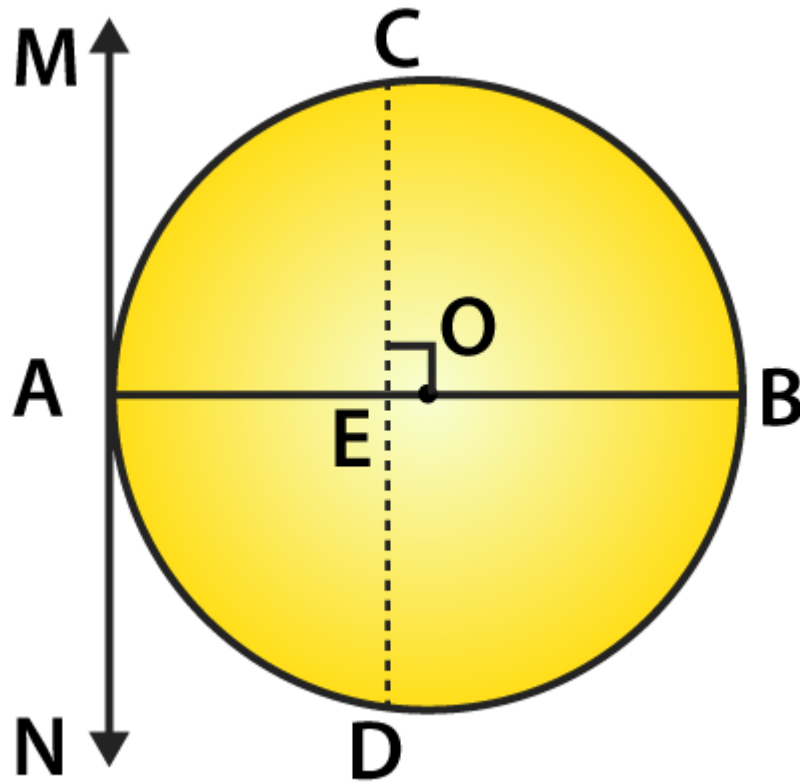
**Solution:**

Given,

AB is a diameter of the circle.

A tangent is drawn from point A.

Construction: Draw a chord CD parallel to the tangent MAN.



So now, CD is a chord of the circle and OA is a radius of the circle.

$$\angle MAO = 90^\circ$$

[Tangent at any point of a circle is perpendicular to the radius through the point of contact]

$$\angle CEO = \angle MAO \text{ [corresponding angles]}$$

$$\angle CEO = 90^\circ$$

Therefore, OE bisects CD.

[perpendicular from center of circle to chord bisects the chord]

Similarly, the diameter AB bisects all the chords which are parallel to the tangent at the point A.

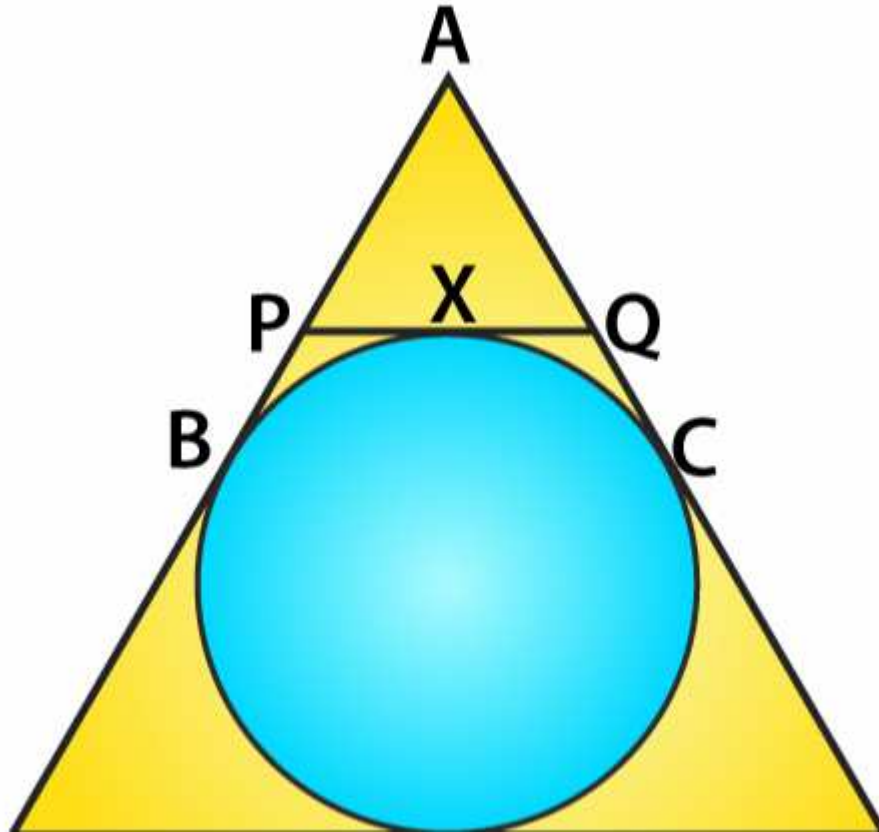
**9. If AB, AC, PQ are the tangents in the figure, and AB = 5 cm, find the perimeter of  $\triangle APQ$ .**

**Solution:**

Given,

AB, AC, PQ are tangents

And, AB = 5 cm



Perimeter of  $\triangle APQ$ ,

$$\text{Perimeter} = AP + AQ + PQ$$

$$= AP + AQ + (PX + QX)$$

We know that,

The two tangents drawn from external point to the circle are equal in length from point A,

$$\text{So, } AB = AC = 5 \text{ cm}$$

From point P,  $PX = PB$  [Tangents from an external point to the circle are equal.]

From point Q,  $QX = QC$  [Tangents from an external point to the circle are equal.]

Thus,

$$\text{Perimeter (P)} = AP + AQ + (PB + QC)$$

$$= (AP + PB) + (AQ + QC)$$

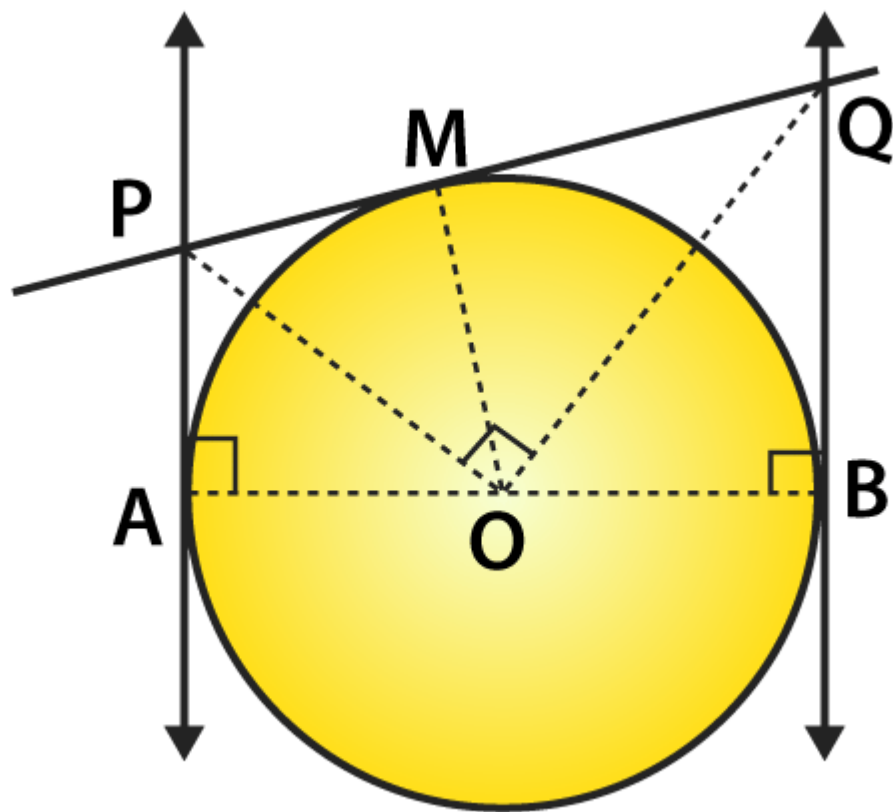
$$= AB + AC = 5 + 5$$

$$= 10 \text{ cm.}$$

**10. Prove that the intercept of a tangent between two parallel tangents to a circle subtends a right angle at centre.**

**Solution:**

Consider a circle with centre 'O' and has two parallel tangents through A & B at ends of diameter.



Let tangent through M intersect the parallel tangents at P and Q

Then, required to prove:  $\angle POQ = 90^\circ$ .

From fig. it is clear that ABQP is a quadrilateral

$\angle A + \angle B = 90^\circ + 90^\circ = 180^\circ$  [At point of contact tangent & radius are perpendicular]

$\angle A + \angle B + \angle P + \angle Q = 360^\circ$  [Angle sum property of a quadrilateral]

So,

$\angle P + \angle Q = 360^\circ - 180^\circ = 180^\circ \dots (i)$

At P & Q

$$\angle APO = \angle OPQ = \frac{1}{2} \angle P \dots (ii)$$

$$\angle BQO = \angle PQO = \frac{1}{2} \angle Q \dots (iii)$$

Using (ii) and (iii) in (i)  $\Rightarrow$

$$2\angle OPQ + 2\angle PQO = 180^\circ$$

$$\angle OPQ + \angle PQO = 90^\circ \dots (iv)$$

In  $\triangle OPQ$ ,

$$\angle OPQ + \angle PQO + \angle POQ = 180^\circ [\text{Angle sum property}]$$

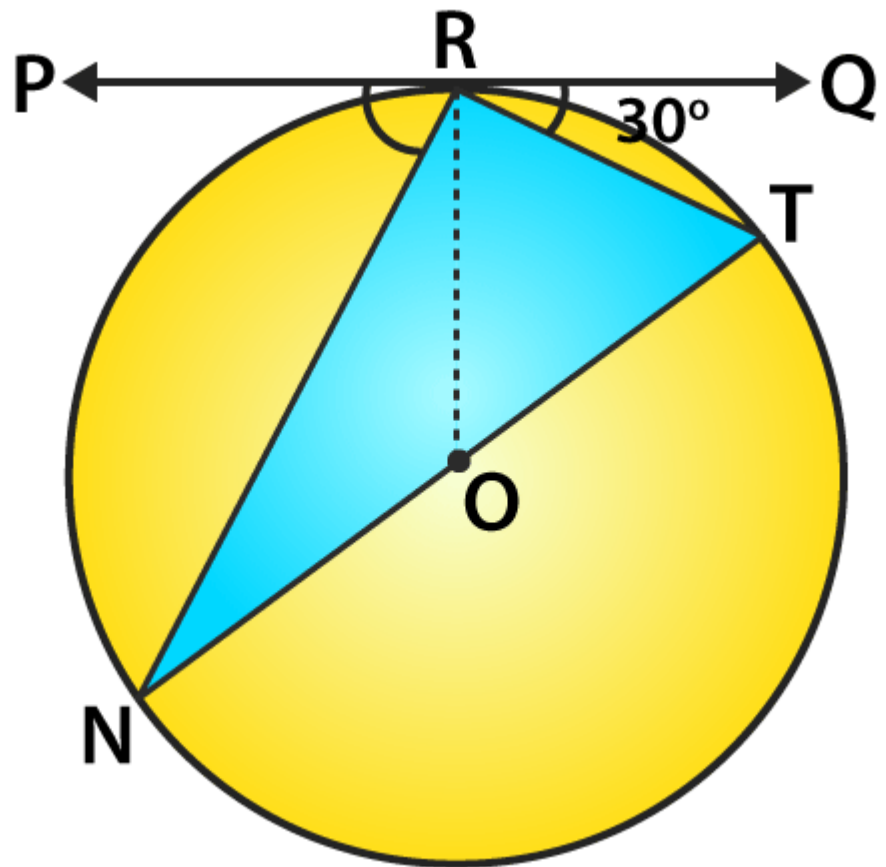
$$90^\circ + \angle POQ = 180^\circ \quad [\text{from (iv)}]$$

$$\angle POQ = 180^\circ - 90^\circ = 90^\circ$$

Hence,  $\angle POQ = 90^\circ$

**11. In Fig below, PQ is tangent at point R of the circle with center O. If  $\angle TRQ = 30^\circ$ , find  $\angle PRS$ .**

**Solution:**



Given,

$$\angle TRQ = 30^\circ.$$

At point R,  $OR \perp RQ$ .

$$\text{So, } \angle ORQ = 90^\circ$$

$$\Rightarrow \angle TRQ + \angle ORT = 90^\circ$$

$$\Rightarrow \angle ORT = 90^\circ - 30^\circ = 60^\circ$$

It's seen that, ST is diameter,

So,  $\angle SRT = 90^\circ$  [  $\because$  Angle in semicircle =  $90^\circ$  ]

Then,

$$\angle ORT + \angle SRO = 90^\circ$$

$$\angle SRO + \angle PRS = 90^\circ$$

$$\therefore \angle PRS = 90^\circ - 30^\circ = 60^\circ$$

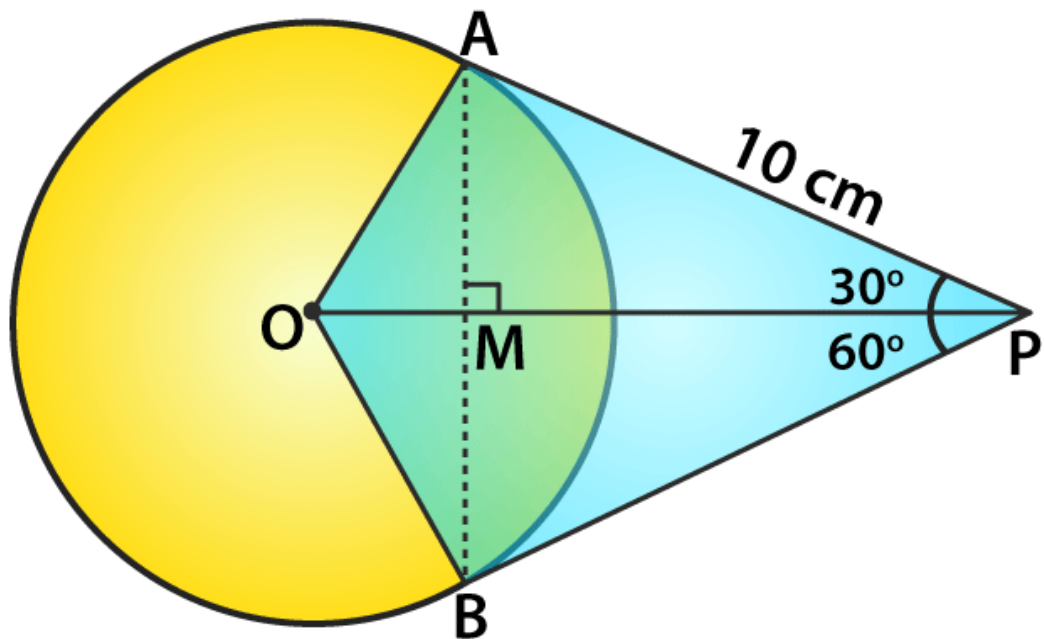
**12. If PA and PB are tangents from an outside point P. such that PA = 10 cm and  $\angle APB = 60^\circ$ . Find the length of chord AB.**

**Solution:**

Given,

$$AP = 10 \text{ cm and } \angle APB = 60^\circ$$

Represented in the figure



We know that,

A line drawn from centre to point from where external tangents are drawn divides or bisects the angle made by tangents at that point

So,  $\angle APO = \angle OPB = \frac{1}{2} \times 60^\circ = 30^\circ$

And, the chord AB will be bisected perpendicularly

$\therefore AB = 2AM$

In  $\triangle AMP$ ,

$$\sin 30^\circ = \frac{\text{opp. side}}{\text{hypotenuse}} = \frac{AM}{AP}$$

$$AM = AP \sin 30^\circ$$

$$AP/2 = 10/2 = 5\text{cm [As } AB = 2AM]$$

$$\text{So, } AP = 2 AM = 10 \text{ cm}$$

$$\text{And, } AB = 2 AM = 10\text{cm}$$

Alternate method:

In  $\triangle AMP$ ,  $\angle AMP = 90^\circ$ ,  $\angle APM = 30^\circ$

$$\angle AMP + \angle APM + \angle MAP = 180^\circ$$

$$90^\circ + 30^\circ + \angle MAP = 180^\circ$$

$$\angle MAP = 60^\circ$$

$$\text{In } \triangle PAB, \angle MAP = \angle BAP = 60^\circ, \angle APB = 60^\circ$$

$$\text{We also get, } \angle PBA = 60^\circ$$

$\therefore \triangle PAB$  is equilateral triangle

$$AB = AP = 10 \text{ cm}$$

**13. In a right triangle ABC in which  $\angle B = 90^\circ$ , a circle is drawn with AB as diameter intersecting the**

**hypotenuse AC at P. Prove that the tangent to the circle at P bisects BC.**

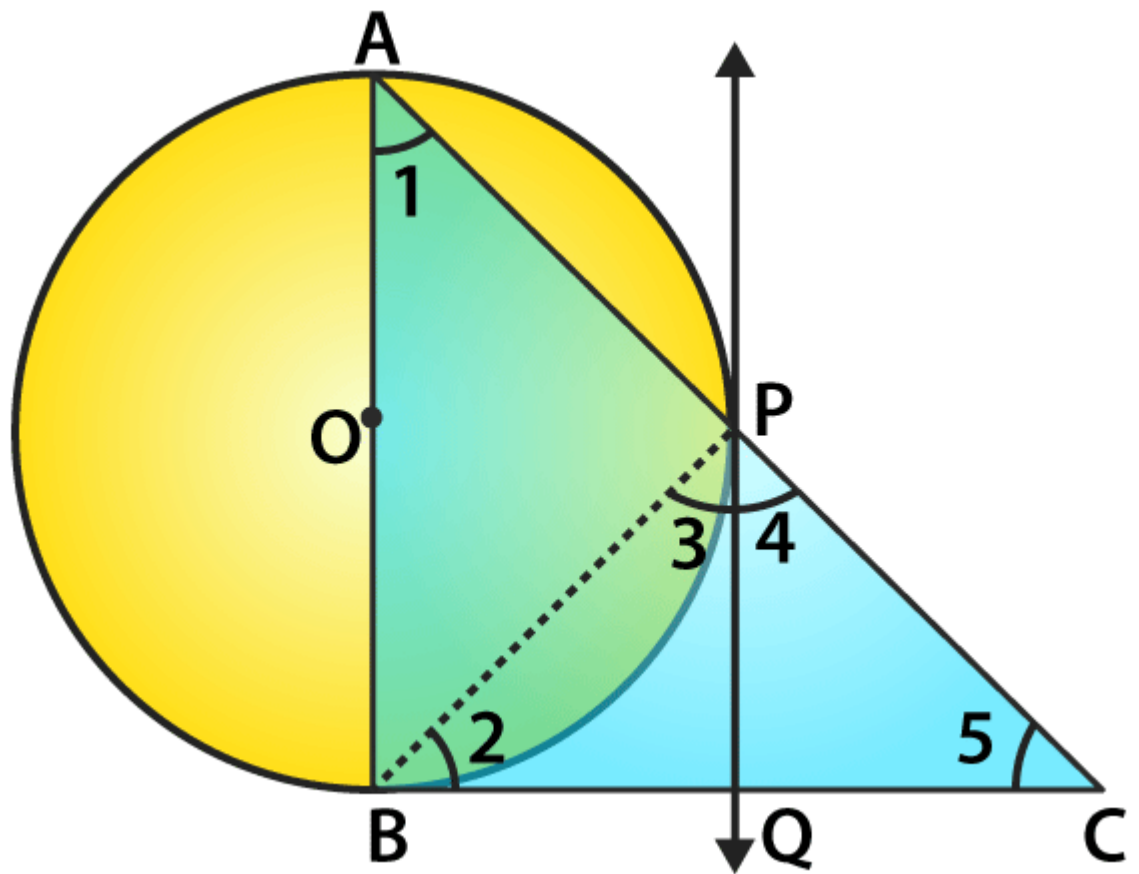
**Solution:**

Let O be the center of the given circle. Suppose, the tangent at P meets BC at Q.

Then join BP.

Required to prove:  $BQ = QC$





Proof :

$\angle ABC = 90^\circ$  [tangent at any point of circle is perpendicular to radius through the point of contact]

In  $\triangle ABC$ ,  $\angle 1 + \angle 5 = 90^\circ$  [angle sum property,  $\angle ABC = 90^\circ$ ]

And,  $\angle 3 = \angle 1$

[angle between tangent and the chord equals angle made by the chord in alternate segment]  
So,

$\angle 3 + \angle 5 = 90^\circ \dots\dots(i)$

Also,  $\angle APB = 90^\circ$  [angle in semi-circle]

$$\angle 3 + \angle 4 = 90^\circ \dots\dots(ii) \quad [\angle APB + \angle BPC = 180^\circ, \text{linear pair}]$$

From (i) and (ii), we get

$$\angle 3 + \angle 5 = \angle 3 + \angle 4$$

$$\angle 5 = \angle 4$$

$$\Rightarrow PQ = QC \text{ [sides opposite to equal angles are equal]}$$

$$\text{Also, } QP = QB$$

[tangents drawn from an internal point to a circle are equal]

$$\Rightarrow QB = QC$$

– Hence proved.

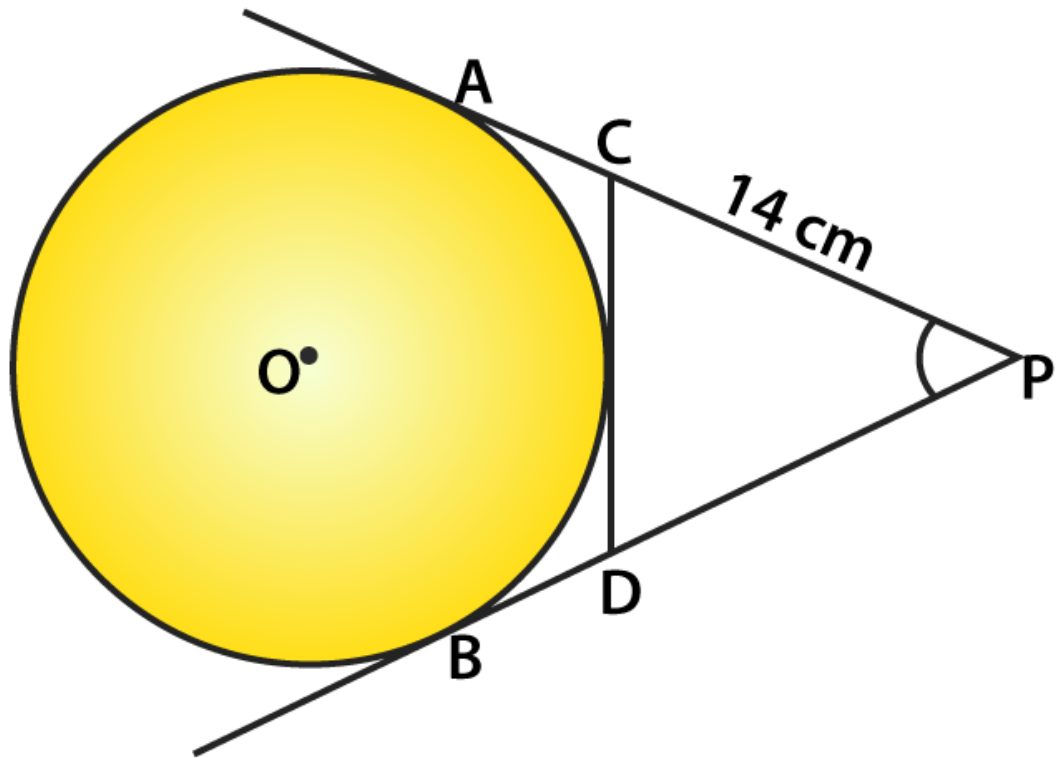
**14. From an external point P, tangents PA and PB are drawn to a circle with centre O. If CD is the tangent to the circle at a point E and PA = 14 cm, find the perimeter of  $\triangle PCD$ .**

**Solution:**

Given,

PA and PB are the tangents drawn from a point P outside the circle with centre O.

CD is another tangents to the circle at point E which intersects PA and PB at C and D respectively.



$$PA = 14 \text{ cm}$$

PA and PB are the tangents to the circle from P

$$\text{So, } PA = PB = 14 \text{ cm}$$

Now, CA and CE are the tangents from C to the circle.

$$CA = CE \dots(i)$$

Similarly, DB and DE are the tangents from D to the circle.

$$DB = DE \dots(ii)$$

Now, perimeter of  $\triangle PCD$

$$= PC + PD + CD$$

$$= PC + PD + CE + DE$$

$$= PC + CE + PD + DE$$

$$= PC + CA + PD + DB \text{ \{From (i) and (ii)\}}$$

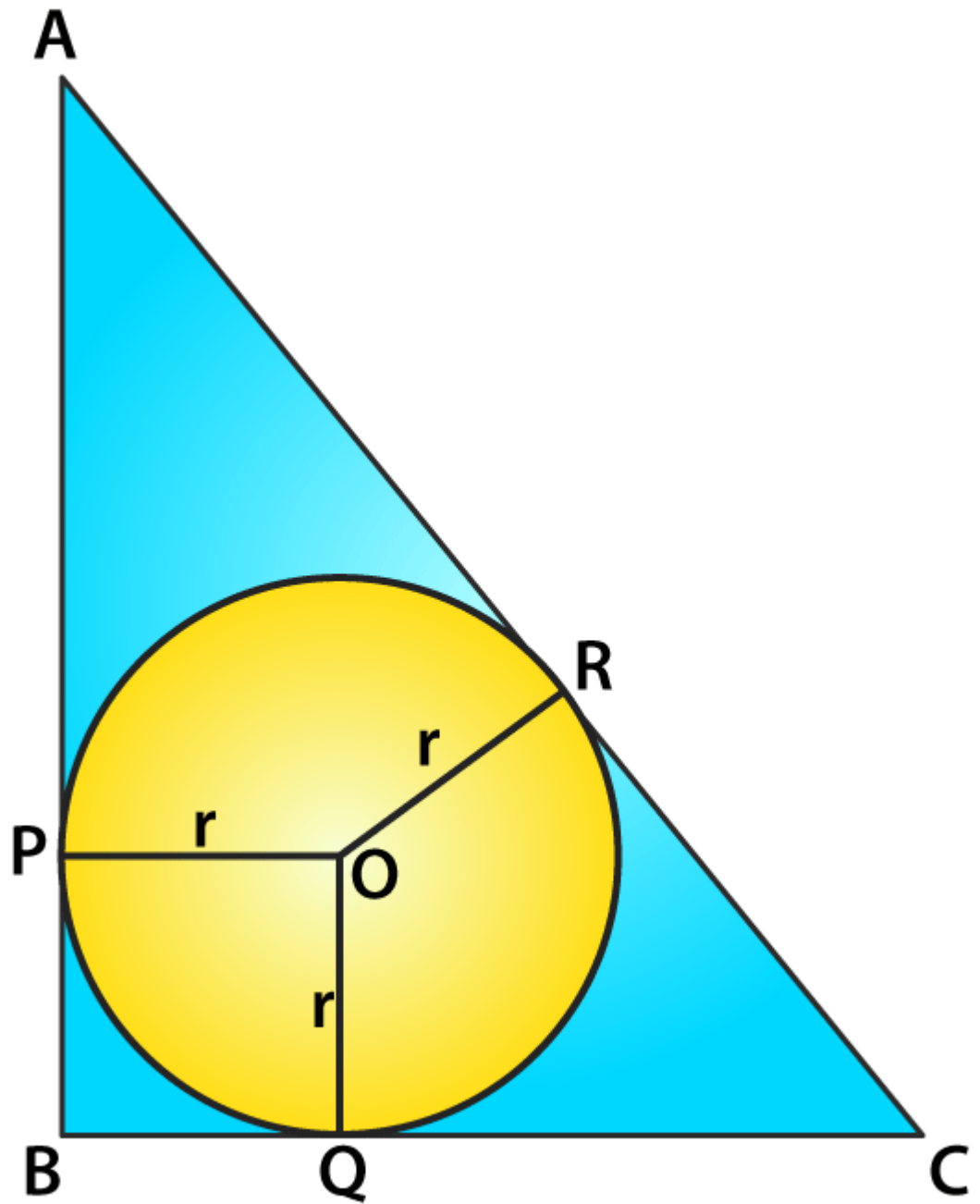
$$= PA + PB$$

$$= 14 + 14$$

$$= 28 \text{ cm}$$

**15. In the figure, ABC is a right triangle right-angled at B such that BC = 6 cm and AB = 8 cm. Find the radius of its incircle.**

**Solution:**



Given,

In right  $\triangle ABC$ ,  $\angle B = 90^\circ$

And,  $BC = 6$  cm,  $AB = 8$  cm

Let  $r$  be the radius of incircle whose centre is  $O$  and touches the sides  $AB$ ,  $BC$  and  $CA$  at  $P$ ,  $Q$  and  $R$  respectively.

Since,  $AP$  and  $AR$  are the tangents to the circle  $AP = AR$

Similarly,  $CR = CQ$  and  $BQ = BP$

OP and OQ are radii of the circle

$OP \perp AB$  and  $OQ \perp BC$  and  $\angle B = 90^\circ$  (given)

Hence, BPOQ is a square

Thus,  $BP = BQ = r$  (sides of a square are equal)

So,

$$AR = AP = AB - BP = 8 - r$$

$$\text{and } CR = CQ = BC - BQ = 6 - r$$

But  $AC^2 = AR^2 + CR^2$  (By Pythagoras Theorem)

$$= (8 - r)^2 + (6 - r)^2 = 64 + 36 = 100 = (10)^2$$

$$\text{So, } AC = 10 \text{ cm}$$

$$\Rightarrow AR + CR = 10$$

$$\Rightarrow 8 - r + 6 - r = 10$$

$$\Rightarrow 14 - 2r = 10$$

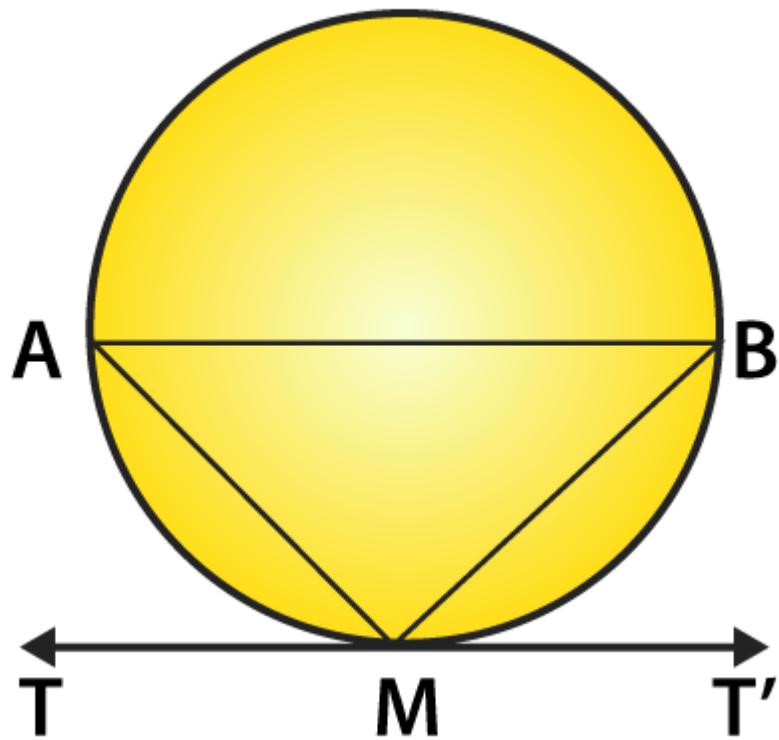
$$\Rightarrow 2r = 14 - 10 = 4$$

$$\Rightarrow r = 2$$

Therefore, the radius of the incircle = 2 cm

**16. Prove that the tangent drawn at the mid-point of an arc of a circle is parallel to the chord joining the end points of the arc.**

**Solution:**



Let mid-point of an arc AMB be M and TMT' be the tangent to the circle.

Now, join AB, AM and MB.

Since, arc AM = arc MB

$\Rightarrow$  Chord AM = Chord MB

In  $\triangle AMB$ , AM = MB

$\Rightarrow \angle MAB = \angle MBA \dots\dots(i)$

[equal sides corresponding to the equal angle]

Since, TMT' is a tangent line.

$\angle AMT = \angle MBA$

[angle in alternate segment are equal]

Thus,  $\angle AMT = \angle MAB$  [from Eq. (i)]

But  $\angle AMT$  and  $\angle MAB$  are alternate angles, which is possible only when  $AB \parallel TMT'$

Hence, the tangent drawn at the mid-point of an arc of a circle is parallel to the chord joining the end points of the arc.

– Hence proved

**17. From a point P, two tangents PA and PB are drawn to a circle with centre O. If OP = diameter of the circle, show that  $\triangle APB$  is equilateral.**

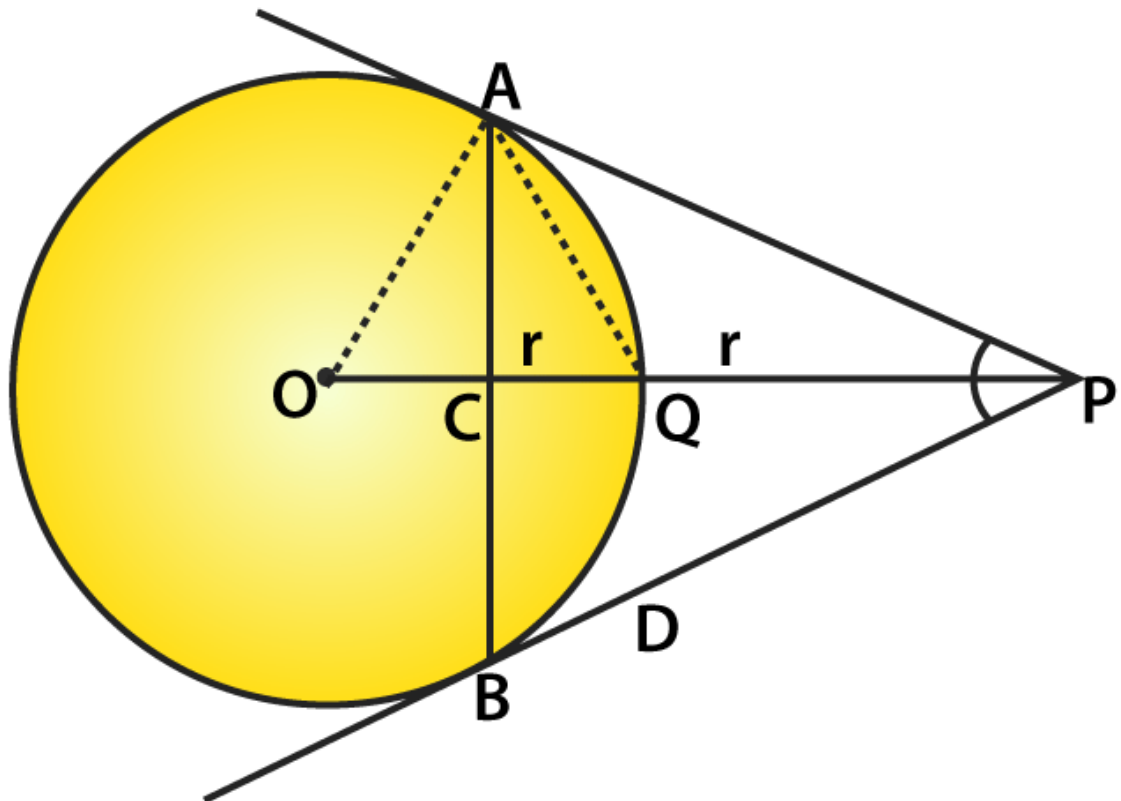
**Solution:**

Given: From a point P outside the circle with centre O, PA and PB are the tangents to the circle such that OP is diameter.

And, AB is joined.

Required to prove:  $\triangle APB$  is an equilateral triangle

Construction: Join OP, AQ, OA



Proof:

We know that,  $OP = 2r$

$$\Rightarrow OQ + QP = 2r$$

$$\Rightarrow OQ = QP = r$$

Now in right  $\triangle OAP$ ,

OP is its hypotenuse and Q is its mid-point

Then,  $OA = AQ = OQ$

(mid-point of hypotenuse of a right triangle is equidistant from its vertices)

Thus,  $\triangle OAQ$  is an equilateral triangle. So,  $\angle AOQ = 60^\circ$

Now in right  $\triangle OAP$ ,

$$\angle APO = 90^\circ - 60^\circ = 30^\circ$$

$$\Rightarrow \angle APB = 2 \angle APO = 2 \times 30^\circ = 60^\circ$$

But  $PA = PB$  (Tangents from P to the circle)

$$\Rightarrow \angle PAB = \angle PBA = 60^\circ$$

Hence  $\triangle APB$  is an equilateral triangle.

**18. Two tangent segments PA and PB are drawn to a circle with centre O such that  $\angle APB = 120^\circ$ . Prove**

**that  $OP = 2 AP$ .**

**Solution:**

Given: From a point P. Outside the circle with centre O, PA and PB are tangents drawn and  $\angle APB = 120^\circ$

And, OP is joined.

Required to prove:  $OP = 2 AP$

Construction: Take mid-point M of OP and join AM, join also OA and OB.





So,

$$OP = 2 MP = 2 AP$$

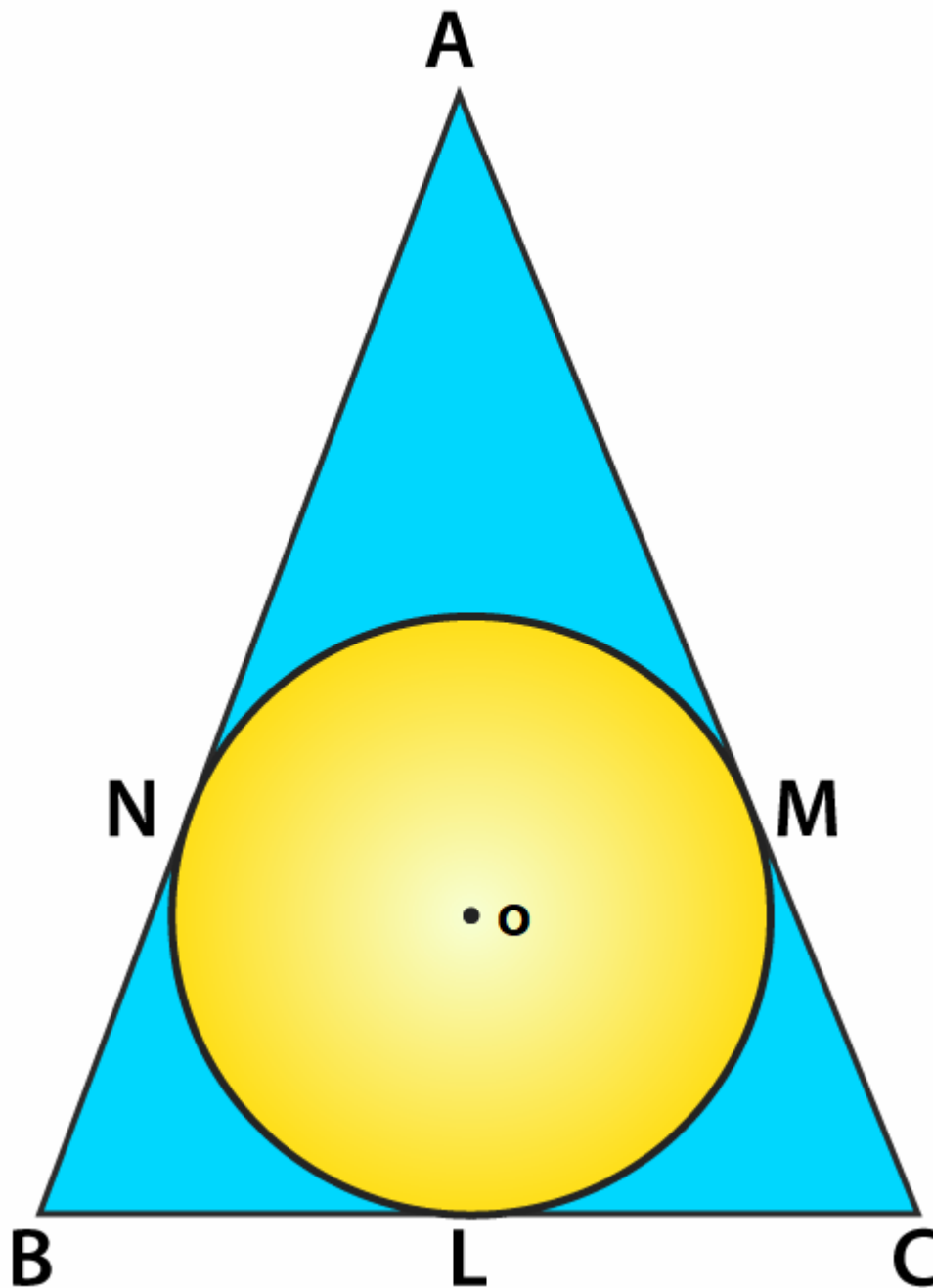
– Hence proved.

**19. If  $\triangle ABC$  is isosceles with  $AB = AC$  and  $C(0, r)$  is the incircle of the  $\triangle ABC$  touching  $BC$  at  $L$ . Prove that  $L$  bisects  $BC$ .**

**Solution:**

Given: In  $\triangle ABC$ ,  $AB = AC$  and a circle with centre  $O$  and radius  $r$  touches the side  $BC$  of  $\triangle ABC$  at  $L$ .

Required to prove :  $L$  is mid-point of  $BC$ .



Proof :

$AM$  and  $AN$  are the tangents to the circle from  $A$ .

So,  $AM = AN$

But  $AB = AC$  (given)

$AB - AN = AC - AM$

$\Rightarrow BN = CM$

Now  $BL$  and  $BN$  are the tangents from  $B$

So,  $BL = BN$

Similarly,  $CL$  and  $CM$  are tangents

$CL = CM$

But  $BN = CM$  (proved above)

So,  $BL = CL$

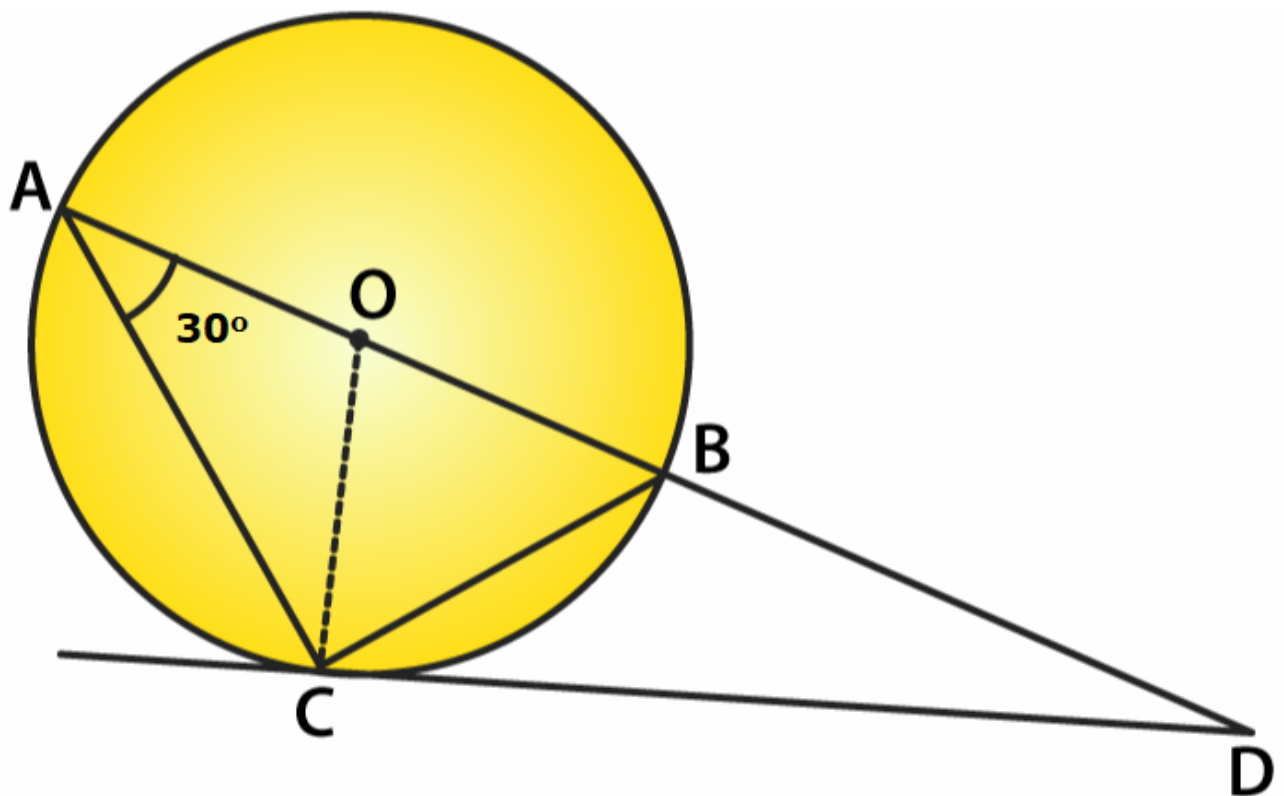
Therefore,  $L$  is mid-point of  $BC$ .

**20.  $AB$  is a diameter and  $AC$  is a chord of a circle with centre  $O$  such that  $\angle BAC = 30^\circ$ . The tangent at  $C$**

**intersects  $AB$  at a point  $D$ . Prove that  $BC = BD$ . [NCERT Exemplar] Solution:**

Required to prove:  $BC = BD$

Join  $BC$  and  $OC$ .



Given,  $\angle BAC = 30^\circ$

$$\Rightarrow \angle BCD = 30^\circ$$

[angle between tangent and chord is equal to angle made by chord in the alternate segment]

$$\angle ACD = \angle ACO + \angle OCD$$

$$\angle ACD = 30^\circ + 90^\circ = 120^\circ$$

[ $OC \perp CD$  and  $OA = OC = \text{radius} \Rightarrow \angle OAC = \angle OCA = 30^\circ$ ]

In  $\triangle ACD$ ,

$$\angle CAD + \angle ACD + \angle ADC = 180^\circ [\text{Angle sum property of a triangle}]$$

$$\Rightarrow 30^\circ + 120^\circ + \angle ADC = 180^\circ$$

$$\Rightarrow \angle ADC = 180^\circ - (30^\circ + 120^\circ) = 30^\circ$$

Now, in  $\triangle BCD$ ,

$$\angle BCD = \angle BDC = 30^\circ$$

$$\Rightarrow BC = BD [\text{As sides opposite to equal angles are equal}]$$

- Hence Proved

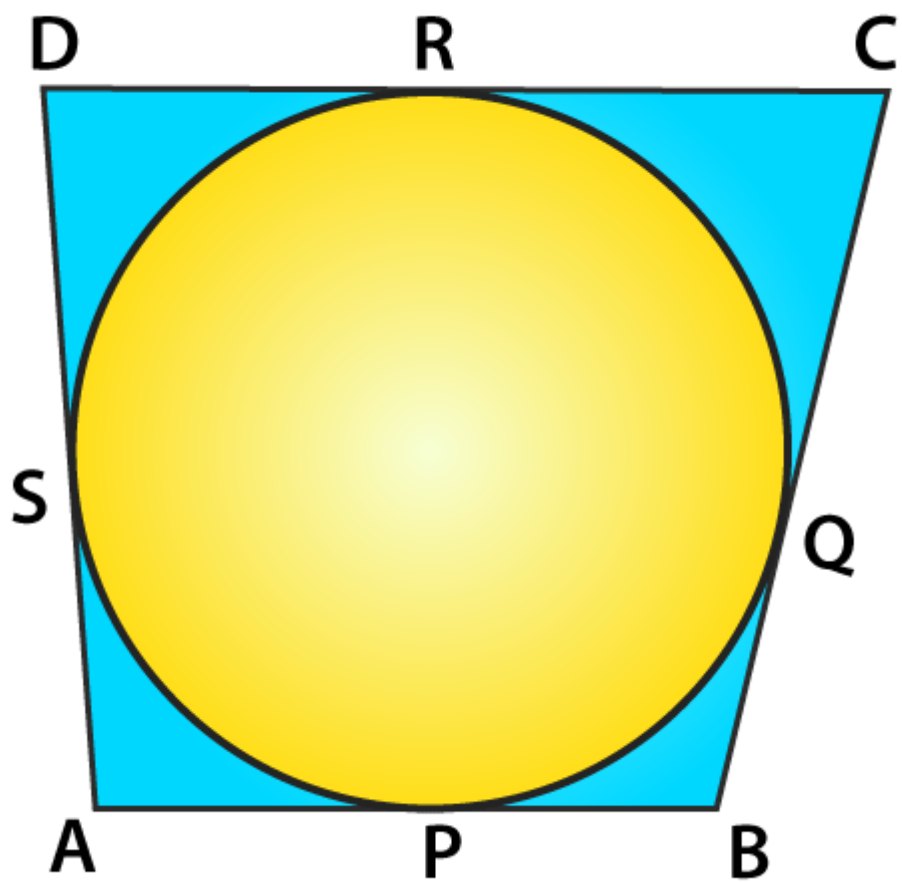
**21. In the figure, a circle touches all the four sides of a quadrilateral ABCD with  $AB = 6$  cm,  $BC = 7$  cm, and  $CD = 4$  cm. Find AD.**

**Solution:**

Given,

A circle touches the sides AB, BC, CD and DA of a quadrilateral ABCD at P, Q, R and S respectively.

$AB = 6$  cm,  $BC = 7$  cm,  $CD = 4$  cm



Let  $AD = x$

As AP and AS are the tangents to the circle

$$AP = AS$$

Similarly,

$$BP = BQ$$

$$CQ = CR$$

$$\text{and } OR = DS$$

So, In ABCD

$$AB + CD = AD + BC \text{ (Property of a cyclic quadrilateral)}$$

$$\Rightarrow 6 + 4 = 7 + x$$

$$\Rightarrow 10 = 7 + x$$

$$\Rightarrow x = 10 - 7 = 3$$

Therefore,  $AD = 3$  cm.

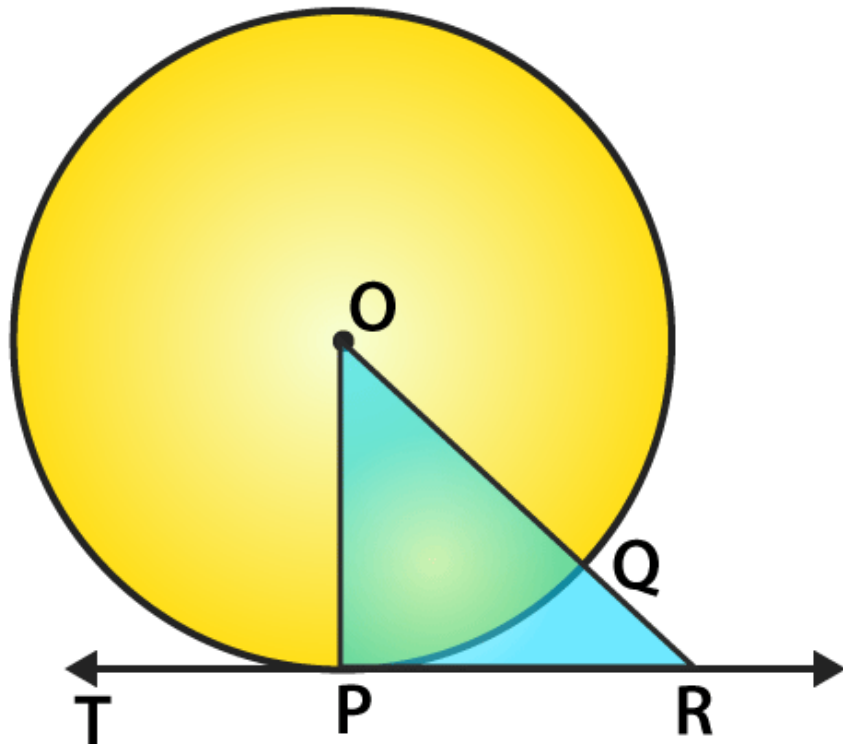
**22. Prove that the perpendicular at the point contact to the tangent to a circle passes through the centre of the circle.**

**Solution:**

Given: TS is a tangent to the circle with centre O at P, and OP is joined.

Required to prove: OP is perpendicular to TS which passes through the centre of the circle

Construction: Draw a line OR which intersect the circle at Q and meets the tangent TS at R



Proof:

$OP = OQ$  (radii of the same circle)

And  $OQ < OR$

$\Rightarrow OP < OR$

similarly, we can prove that OP is less than all lines which can be drawn from O to TS.

OP is the shortest

OP is perpendicular to TS

Therefore, the perpendicular through P will pass through the centre of the circle

– Hence proved.

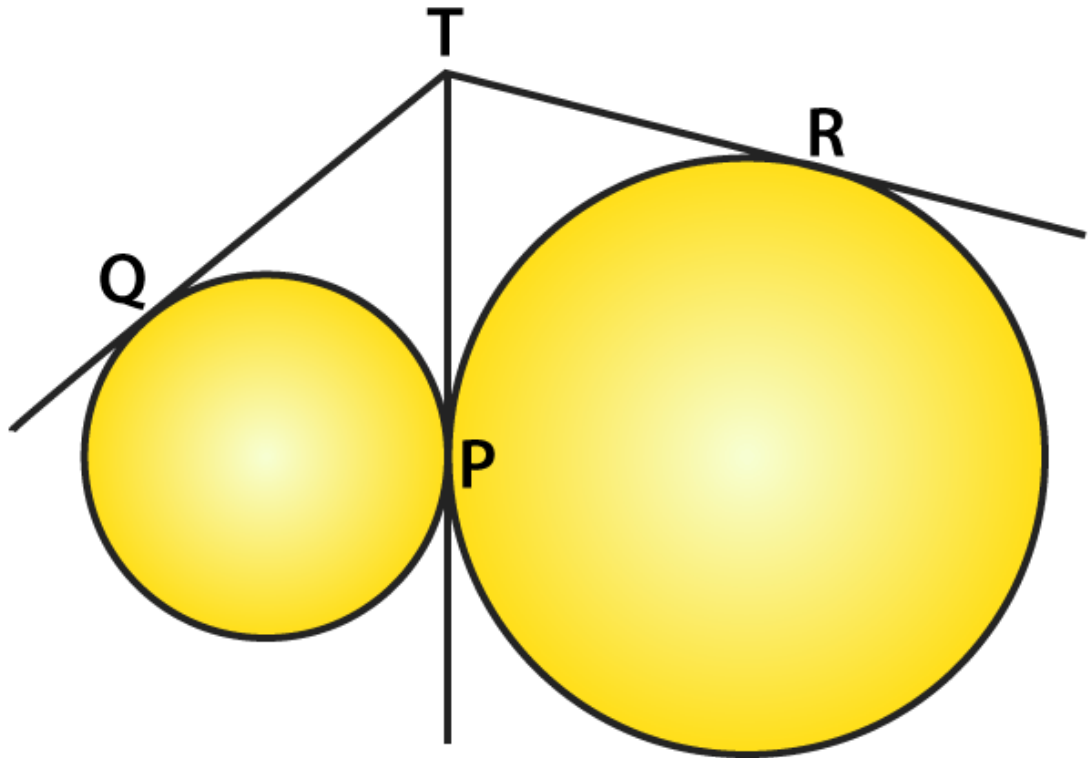
**23. Two circles touch externally at a point P. From a point T on the tangent at P, tangents TQ and TR are drawn to the circles with points of contact Q and R respectively. Prove that  $TQ = TR$ .**

**Solution:**

Given: Two circles with centres O and C touch each other externally at P. PT is its common tangent

From a point T: PT, TR and TQ are the tangents drawn to the circles.

Required to prove:  $TQ = TR$



Proof:

From T, TR and TP are two tangents to the circle with centre O

So,  $TR = TP$  ....(i)

Similarly, from point T

TQ and TP are two tangents to the circle with centre C

$TQ = TP$  ....(ii)

From (i) and (ii)  $\Rightarrow$

$TQ = TR$

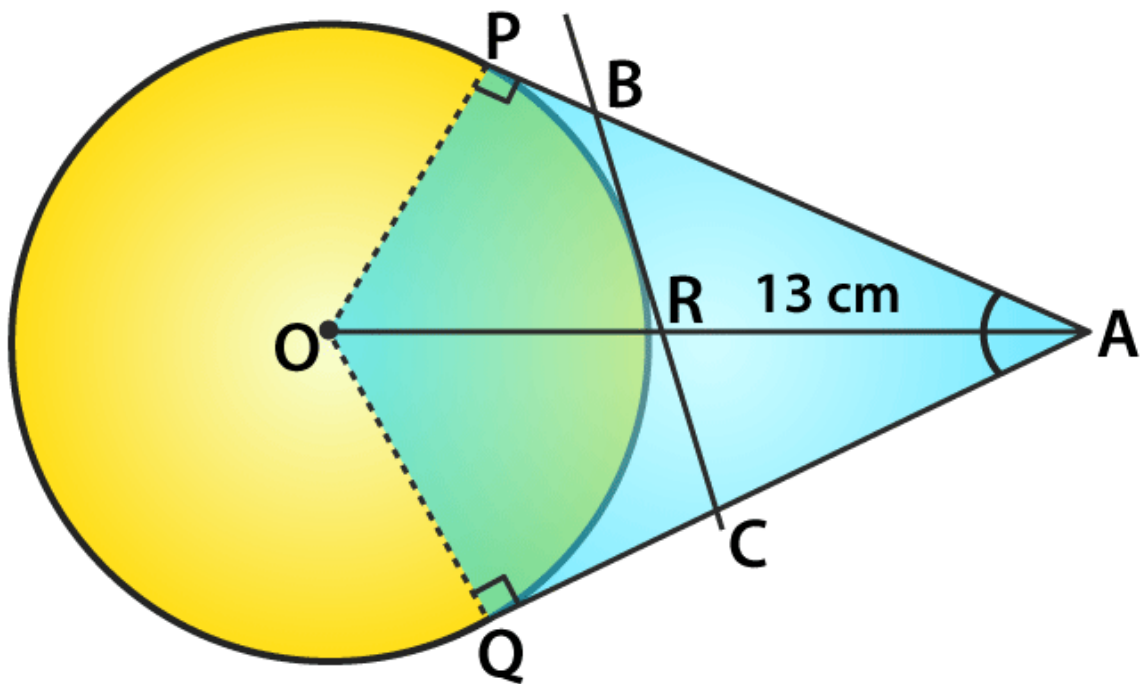
– Hence proved.

**24. A is a point at a distance 13 cm from the centre O of a circle of radius 5 cm. AP and AQ are the tangents to the circle at P and Q. If a tangent BC is drawn at a point R lying on the minor arc PQ to intersect AP at B and AQ at C, find the perimeter of the  $\triangle ABC$ .**

**Solution:**

Given: Two tangents are drawn from an external point A to the circle with centre O. Tangent BC is drawn at a point R and radius of circle = 5 cm.

Required to find : Perimeter of  $\triangle ABC$ .



Proof:

We know that,

$\angle OPA = 90^\circ$  [Tangent at any point of a circle is perpendicular to the radius through the point of contact]

$OA^2 = OP^2 + PA^2$  [by Pythagoras Theorem]

$$(13)^2 = 5^2 + PA^2$$

$$\Rightarrow PA^2 = 144 = 12^2$$

$$\Rightarrow PA = 12 \text{ cm}$$

Now, perimeter of  $\triangle ABC = AB + BC + CA = (AB + BR) + (RC + CA)$

$= AB + BP + CQ + CA$  [BR = BP, RC = CQ tangents from internal point to a circle are equal]

$$= AP + AQ = 2AP = 2 \times (12) = 24 \text{ cm}$$

[AP = AQ tangents from internal point to a circle are equal]

Therefore, the perimeter of  $\triangle ABC = 24 \text{ cm}$ .